

SATPREP**Assignment - Limits - Algebraic**

1. Evaluate each of the following limits :

$$(a) \lim_{x \rightarrow 2} [2(x+3)+7] \quad (b) \lim_{x \rightarrow 0} (x^2 + 3x + 7) \quad (c) \lim_{x \rightarrow 1} [(x+3)^2 - 16]$$
$$(d) \lim_{x \rightarrow 1} [(x+1)^2 + 2] \quad (e) \lim_{x \rightarrow 0} [(2x+1)^3 - 5] \quad (f) \lim_{x \rightarrow 1} (3x+1)(x+1)$$

2. Find the limits of each of the following functions :

$$(a) \lim_{x \rightarrow 5} \frac{x-5}{x+2} \quad (b) \lim_{x \rightarrow 1} \frac{x+2}{x+1} \quad (c) \lim_{x \rightarrow 1} \frac{3x+5}{x-10}$$
$$(d) \lim_{x \rightarrow 0} \frac{px+q}{ax+b} \quad (e) \lim_{x \rightarrow 3} \frac{x^2-9}{x-3} \quad (f) \lim_{x \rightarrow 5} \frac{x^2-25}{x+5}$$
$$(g) \lim_{x \rightarrow 2} \frac{x^2-x-2}{x^2-3x+2} \quad (h) \lim_{x \rightarrow \frac{1}{3}} \frac{9x^2-1}{3x-1}$$

3. Evaluate each of the following limits:

$$(a) \lim_{x \rightarrow 1} \frac{x^3-1}{x-1} \quad (b) \lim_{x \rightarrow 0} \frac{x^3+7x}{x^2+2x} \quad (c) \lim_{x \rightarrow 1} \frac{x^4-1}{x-1}$$
$$(d) \lim_{x \rightarrow 1} \left[\frac{1}{x-1} - \frac{2}{x^2-1} \right]$$

4. Evaluate each of the following limits :

$$(a) \lim_{x \rightarrow 0} \frac{\sqrt{4+x} - \sqrt{4-x}}{x} \quad (b) \lim_{x \rightarrow 0} \frac{\sqrt{2+x} - \sqrt{2}}{x} \quad (c) \lim_{x \rightarrow 3} \frac{\sqrt{3+x} - \sqrt{6}}{x-3}$$

$$(d) \lim_{x \rightarrow 0} \frac{x}{\sqrt{1+x} - 1} \quad (e) \lim_{x \rightarrow 2} \frac{\sqrt{3x-2} - x}{2 - \sqrt{6-x}}$$

5. (a) Find $\lim_{x \rightarrow 0} \frac{2}{x}$, if it exists. (b) Find $\lim_{x \rightarrow 2} \frac{1}{x-2}$, if it exists.

6. Find the values of the limits given below :

$$(a) \lim_{x \rightarrow 0} \frac{x}{5-|x|} \quad (b) \lim_{x \rightarrow 2} \frac{1}{|x+2|} \quad (c) \lim_{x \rightarrow 2} \frac{1}{|x-2|}$$

(d) Show that $\lim_{x \rightarrow 5} \frac{|x-5|}{x-5}$ does not exist.

7. (a) Find the left hand and right hand limits of the function

$$f(x) = \begin{cases} -2x + 3, & x \leq 1 \\ 3x - 5, & x > 1 \end{cases} \text{ as } x \rightarrow 1$$

(b) If $f(x) = \begin{cases} x^2, & x \leq 1 \\ 1, & x > 1 \end{cases}$, find $\lim_{x \rightarrow 1} f(x)$

(c) Find $\lim_{x \rightarrow 4} f(x)$ if it exists, given that $f(x) = \begin{cases} 4x + 3, & x < 4 \\ 3x + 7, & x \geq 4 \end{cases}$

8. Find the value of 'a' such that $\lim_{x \rightarrow 2} f(x)$ exists, where $f(x) = \begin{cases} ax + 5, & x < 2 \\ x - 1, & x \geq 2 \end{cases}$

9. Let $f(x) = \begin{cases} x, & x < 1 \\ 1, & x = 1 \\ x^2, & x > 1 \end{cases}$

Establish the existence of $\lim_{x \rightarrow 1} f(x)$.

10. Find $\lim_{x \rightarrow 2} f(x)$ if it exists, where

$$f(x) = \begin{cases} x - 1, & x < 2 \\ 1, & x = 2 \\ x + 1, & x > 2 \end{cases}$$