

AS-Level
Normal Distribution
May : 2013- May : 2025
Questions

Question 1

Buildings in a certain city centre are classified by height as tall, medium or short. The heights can be modelled by a normal distribution with mean 50 metres and standard deviation 16 metres. Buildings with a height of more than 70 metres are classified as tall.

- (i) Find the probability that a building chosen at random is classified as tall. [2]
- (ii) The rest of the buildings are classified as medium and short in such a way that there are twice as many medium buildings as there are short ones. Find the height below which buildings are classified as short. [5]

Question 2

Cans of lemon juice are supposed to contain 440 ml of juice. It is found that the actual volume of juice in a can is normally distributed with mean 445 ml and standard deviation 3.6 ml.

- (i) Find the probability that a randomly chosen can contains less than 440 ml of juice. [3]

It is found that 94% of the cans contain between $(445 - c)$ ml and $(445 + c)$ ml of juice.

- (ii) Find the value of c . [3]

Question 3

The random variable Y is normally distributed with mean equal to five times the standard deviation. It is given that $P(Y > 20) = 0.0732$. Find the mean. [3]

Question 4

- (a) The random variable Y is normally distributed with positive mean μ and standard deviation $\frac{1}{2}\mu$. Find the probability that a randomly chosen value of Y is negative. [3]
- (b) The weights of bags of rice are normally distributed with mean 2.04 kg and standard deviation σ kg. In a random sample of 8000 such bags, 253 weighed over 2.1 kg. Find the value of σ . [4]

Question 5

Assume that, for a randomly chosen person, their next birthday is equally likely to occur on any day of the week, independently of any other person's birthday. Find the probability that, out of 350 randomly chosen people, at least 47 will have their next birthday on a Monday. [5]

Question 6

- (a) The random variable X is normally distributed with mean 82 and standard deviation 7.4. Find the value of q such that $P(82 - q < X < 82 + q) = 0.44$. [3]
- (b) The random variable Y is normally distributed with mean μ and standard deviation σ . It is given that $5\mu = 2\sigma^2$ and that $P(Y < \frac{1}{2}\mu) = 0.281$. Find the values of μ and σ . [4]

Question 7

A factory produces flower pots. The base diameters have a normal distribution with mean 14 cm and standard deviation 0.52 cm. Find the probability that the base diameters of exactly 8 out of 10 randomly chosen flower pots are between 13.6 cm and 14.8 cm. [5]

Question 8

On trains in the morning rush hour, each person is either a student with probability 0.36, or an office worker with probability 0.22, or a shop assistant with probability 0.29 or none of these.

- (i) 8 people on a morning rush hour train are chosen at random. Find the probability that between 4 and 6 inclusive are office workers. [3]
- (ii) 300 people on a morning rush hour train are chosen at random. Find the probability that between 31 and 49 inclusive are neither students nor office workers nor shop assistants. [6]

Question 9

The amount of fibre in a packet of a certain brand of cereal is normally distributed with mean 160 grams. 19% of packets of cereal contain more than 190 grams of fibre.

- (i) Find the standard deviation of the amount of fibre in a packet. [3]
- (ii) Kate buys 12 packets of cereal. Find the probability that at least 1 of the packets contains more than 190 grams of fibre. [2]

Question 10

It is given that $X \sim N(1.5, 3.2^2)$. Find the probability that a randomly chosen value of X is less than -2.4 . [3]

Question 11

Lengths of a certain type of carrot have a normal distribution with mean 14.2 cm and standard deviation 3.6 cm.

- (i) 8% of carrots are shorter than c cm. Find the value of c . [3]
- (ii) Rebekah picks 7 carrots at random. Find the probability that at least 2 of them have lengths between 15 and 16 cm. [6]

Question 12

It is given that $X \sim N(30, 49)$, $Y \sim N(30, 16)$ and $Z \sim N(50, 16)$. On a single diagram, with the horizontal axis going from 0 to 70, sketch three curves to represent the distributions of X , Y and Z . [3]

Question 13

When Moses makes a phone call, the amount of time that the call takes has a normal distribution with mean 6.5 minutes and standard deviation 1.76 minutes.

- (i) 90% of Moses's phone calls take longer than t minutes. Find the value of t . [3]
- (ii) Find the probability that, in a random sample of 9 phone calls made by Moses, more than 7 take a time which is within 1 standard deviation of the mean. [5]

Question 14

There is a probability of $\frac{1}{7}$ that Wenjie goes out with her friends on any particular day. 252 days are chosen at random.

- (i) Use a normal approximation to find the probability that the number of days on which Wenjie goes out with her friends is less than 30 or more than 44. [5]
- (ii) Give a reason why the use of a normal approximation is justified. [1]

Question 15

The time Rafa spends on his homework each day in term-time has a normal distribution with mean 1.9 hours and standard deviation σ hours. On 80% of these days he spends more than 1.35 hours on his homework.

- (i) Find the value of σ . [3]
- (ii) Find the probability that, on a randomly chosen day in term-time, Rafa spends less than 2 hours on his homework. [2]
- (iii) A random sample of 200 days in term-time is taken. Use an approximation to find the probability that the number of days on which Rafa spends more than 1.35 hours on his homework is between 163 and 173 inclusive. [6]

Question 16

Lengths of a certain type of white radish are normally distributed with mean μ cm and standard deviation σ cm. 4% of these radishes are longer than 12 cm and 32% are longer than 9 cm. Find μ and σ . [5]

Question 17

The petrol consumption of a certain type of car has a normal distribution with mean 24 kilometres per litre and standard deviation 4.7 kilometres per litre. Find the probability that the petrol consumption of a randomly chosen car of this type is between 21.6 kilometres per litre and 28.7 kilometres per litre. [4]

Question 18

Gem stones from a certain mine have weights, X grams, which are normally distributed with mean 1.9 g and standard deviation 0.55 g. These gem stones are sorted into three categories for sale depending on their weights, as follows.

Small: under 1.2 g Medium: between 1.2 g and 2.5 g Large: over 2.5 g

- (i) Find the proportion of gem stones in each of these three categories. [5]
- (ii) Find the value of k such that $P(k < X < 2.5) = 0.8$. [4]

Question 19

Packets of tea are labelled as containing 250 g. The actual weight of tea in a packet has a normal distribution with mean 260 g and standard deviation σ g. Any packet with a weight less than 250 g is classed as 'underweight'. Given that 1% of packets of tea are underweight, find the value of σ . [3]

Question 20

In Marumbo, three quarters of the adults own a cell phone.

- (i) A random sample of 8 adults from Marumbo is taken. Find the probability that the number of adults who own a cell phone is between 4 and 6 inclusive. [3]
- (ii) A random sample of 160 adults from Marumbo is taken. Use an approximation to find the probability that more than 114 of them own a cell phone. [5]
- (iii) Justify the use of your approximation in part (ii). [1]

Question 21

- (a) The time, X hours, for which people sleep in one night has a normal distribution with mean 7.15 hours and standard deviation 0.88 hours.
 - (i) Find the probability that a randomly chosen person sleeps for less than 8 hours in a night. [2]
 - (ii) Find the value of q such that $P(X < q) = 0.75$. [3]
- (b) The random variable Y has the distribution $N(\mu, \sigma^2)$, where $2\sigma = 3\mu$ and $\mu \neq 0$. Find $P(Y > 4\mu)$. [3]

Question 22

A farmer finds that the weights of sheep on his farm have a normal distribution with mean 66.4 kg and standard deviation 5.6 kg.

- (i) 250 sheep are chosen at random. Estimate the number of sheep which have a weight of between 70 kg and 72.5 kg. [5]
- (ii) The proportion of sheep weighing less than 59.2 kg is equal to the proportion weighing more than y kg. Find the value of y . [2]

Another farmer finds that the weights of sheep on his farm have a normal distribution with mean μ kg and standard deviation 4.92 kg. 25% of these sheep weigh more than 67.5 kg.

- (iii) Find the value of μ . [3]

Question 23

The heights of books in a library, in cm, have a normal distribution with mean 21.7 and standard deviation 6.5. A book with a height of more than 29 cm is classified as 'large'.

- (i) Find the probability that, of 8 books chosen at random, fewer than 2 books are classified as large. [6]
- (ii) n books are chosen at random. The probability of there being at least 1 large book is more than 0.98. Find the least possible value of n . [3]

Question 24

On a production line making cameras, the probability of a randomly chosen camera being substandard is 0.072. A random sample of 300 cameras is checked. Find the probability that there are fewer than 18 cameras which are substandard. [5]

Question 25

The weights, in grams, of onions in a supermarket have a normal distribution with mean μ and standard deviation 22. The probability that a randomly chosen onion weighs more than 195 grams is 0.128. Find the value of μ . [3]

Question 26

- (a) Once a week Zak goes for a run. The time he takes, in minutes, has a normal distribution with mean 35.2 and standard deviation 4.7.
- (i) Find the expected number of days during a year (52 weeks) for which Zak takes less than 30 minutes for his run. [4]
- (ii) The probability that Zak's time is between 35.2 minutes and t minutes, where $t > 35.2$, is 0.148. Find the value of t . [3]
- (b) The random variable X has the distribution $N(\mu, \sigma^2)$. It is given that $P(X < 7) = 0.2119$ and $P(X < 10) = 0.6700$. Find the values of μ and σ . [5]

Question 27

- (i) In a certain country, 68% of households have a printer. Find the probability that, in a random sample of 8 households, 5, 6 or 7 households have a printer. [4]
- (ii) Use an approximation to find the probability that, in a random sample of 500 households, more than 337 households have a printer. [5]
- (iii) Justify your use of the approximation in part (ii). [1]

Question 28

The lengths, in metres, of cars in a city are normally distributed with mean μ and standard deviation 0.714. The probability that a randomly chosen car has a length more than 3.2 metres and less than μ metres is 0.475. Find μ . [4]

Question 29

A factory makes water pistols, 8% of which do not work properly.

- (i) A random sample of 19 water pistols is taken. Find the probability that at most 2 do not work properly. [3]
- (ii) In a random sample of n water pistols, the probability that at least one does not work properly is greater than 0.9. Find the smallest possible value of n . [3]
- (iii) A random sample of 1800 water pistols is taken. Use an approximation to find the probability that there are at least 152 that do not work properly. [5]
- (iv) Justify the use of your approximation in part (iii). [1]

Question 30

The time taken for cucumber seeds to germinate under certain conditions has a normal distribution with mean 125 hours and standard deviation σ hours.

- (i) It is found that 13% of seeds take longer than 136 hours to germinate. Find the value of σ . [3]
- (ii) 170 seeds are sown. Find the expected number of seeds which take between 131 and 141 hours to germinate. [4]

Question 31

- (a) A petrol station finds that its daily sales, in litres, are normally distributed with mean 4520 and standard deviation 560.

- (i) Find on how many days of the year (365 days) the daily sales can be expected to exceed 3900 litres. [4]

The daily sales at another petrol station are X litres, where X is normally distributed with mean m and standard deviation 560. It is given that $P(X > 8000) = 0.122$.

- (ii) Find the value of m . [3]
 - (iii) Find the probability that daily sales at this petrol station exceed 8000 litres on fewer than 2 of 6 randomly chosen days. [3]
- (b) The random variable Y is normally distributed with mean μ and standard deviation σ . Given that $\sigma = \frac{2}{3}\mu$, find the probability that a random value of Y is less than 2μ . [3]

Question 32

The faces of a biased die are numbered 1, 2, 3, 4, 5 and 6. The probabilities of throwing odd numbers are all the same. The probabilities of throwing even numbers are all the same. The probability of throwing an odd number is twice the probability of throwing an even number.

- (i) Find the probability of throwing a 3. [3]
- (ii) The die is thrown three times. Find the probability of throwing two 5s and one 4. [3]
- (iii) The die is thrown 100 times. Use an approximation to find the probability that an even number is thrown at most 37 times. [5]

Question 33

- (a) Amy measured her pulse rate while resting, x beats per minute, at the same time each day on 30 days. The results are summarised below.

$$\Sigma(x - 80) = -147 \quad \Sigma(x - 80)^2 = 952$$

Find the mean and standard deviation of Amy's pulse rate. [4]

- (b) Amy's friend Marok measured her pulse rate every day after running for half an hour. Marok's pulse rate, in beats per minute, was found to have a mean of 148.6 and a standard deviation of 18.5. Assuming that pulse rates have a normal distribution, find what proportion of Marok's pulse rates, after running for half an hour, were above 160 beats per minute. [3]

Question 34

The random variable X has the distribution $N(\mu, \sigma^2)$. It is given that $P(X < 54.1) = 0.5$ and $P(X > 50.9) = 0.8665$. Find the values of μ and σ . [4]

Question 35

The times taken by a garage to fit a tow bar onto a car have a normal distribution with mean m hours and standard deviation 0.35 hours. It is found that 95% of times taken are longer than 0.9 hours.

- (i) Find the value of m . [3]
- (ii) On one day 4 cars have a tow bar fitted. Find the probability that none of them takes more than 2 hours to fit. [5]

The times in hours taken by another garage to fit a tow bar onto a car have the distribution $N(\mu, \sigma^2)$ where $\mu = 3\sigma$.

- (iii) Find the probability that it takes more than 0.6μ hours to fit a tow bar onto a randomly chosen car at this garage. [3]

Question 36

Passengers are travelling to Picton by minibus. The probability that each passenger carries a backpack is 0.65, independently of other passengers. Each minibus has seats for 12 passengers.

- (i) Find the probability that, in a full minibus travelling to Picton, between 8 passengers and 10 passengers inclusive carry a backpack. [3]
- (ii) Passengers get on to an empty minibus. Find the probability that the fourth passenger who gets on to the minibus will be the first to be carrying a backpack. [2]
- (iii) Find the probability that, of a random sample of 250 full minibuses travelling to Picton, more than 54 will contain exactly 7 passengers carrying backpacks. [6]

Question 37

The heights of school desks have a normal distribution with mean 69 cm and standard deviation σ cm. It is known that 15.5% of these desks have a height greater than 70 cm.

- (i) Find the value of σ . [3]

When Jodu sits at a desk, his knees are at a height of 58 cm above the floor. A desk is comfortable for Jodu if his knees are at least 9 cm below the top of the desk. Jodu's school has 300 desks.

- (ii) Calculate an estimate of the number of these desks that are comfortable for Jodu. [5]

Question 38

The time in minutes taken by Peter to walk to the shop and buy a newspaper is normally distributed with mean 9.5 and standard deviation 1.3.

- (i) Find the probability that on a randomly chosen day Peter takes longer than 10.2 minutes. [3]
- (ii) On 90% of days he takes longer than t minutes. Find the value of t . [3]
- (iii) Calculate an estimate of the number of days in a year (365 days) on which Peter takes less than 8.8 minutes to walk to the shop and buy a newspaper. [3]

Question 39

When visiting the dentist the probability of waiting less than 5 minutes is 0.16, and the probability of waiting less than 10 minutes is 0.88.

- (i) Find the probability of waiting between 5 and 10 minutes. [1]

A random sample of 180 people who visit the dentist is chosen.

- (ii) Use a suitable approximation to find the probability that more than 115 of these people wait between 5 and 10 minutes. [5]

Question 40

Plastic drinking straws are manufactured to fit into drinks cartons which have a hole in the top. A straw fits into the hole if the diameter of the straw is less than 3 mm. The diameters of the straws have a normal distribution with mean 2.6 mm and standard deviation 0.25 mm.

- (i) A straw is chosen at random. Find the probability that it fits into the hole in a drinks carton. [3]
- (ii) 500 straws are chosen at random. Use a suitable approximation to find the probability that at least 480 straws fit into the holes in drinks cartons. [5]
- (iii) Justify the use of your approximation. [1]

Question 41

The height of maize plants in Mpapwa is normally distributed with mean 1.62 m and standard deviation σ m. The probability that a randomly chosen plant has a height greater than 1.8 m is 0.15. Find the value of σ . [3]

Question 42

Each day Annabel eats rice, potato or pasta. Independently of each other, the probability that she eats rice is 0.75, the probability that she eats potato is 0.15 and the probability that she eats pasta is 0.1.

- (i) Find the probability that, in any week of 7 days, Annabel eats pasta on exactly 2 days. [2]
- (ii) Find the probability that, in a period of 5 days, Annabel eats rice on 2 days, potato on 1 day and pasta on 2 days. [3]
- (iii) Find the probability that Annabel eats potato on more than 44 days in a year of 365 days. [5]

Question 43

The weights of bananas in a fruit shop have a normal distribution with mean 150 grams and standard deviation 50 grams. Three sizes of banana are sold.

Small: under 95 grams

Medium: between 95 grams and 205 grams

Large: over 205 grams

- (i) Find the proportion of bananas that are small. [3]
- (ii) Find the weight exceeded by 10% of bananas. [3]

The prices of bananas are 10 cents for a small banana, 20 cents for a medium banana and 25 cents for a large banana.

- (iii) (a) Show that the probability that a randomly chosen banana costs 20 cents is 0.7286. [1]
- (b) Calculate the expected total cost of 100 randomly chosen bananas. [3]

Question 44

The time taken to cook an egg by people living in a certain town has a normal distribution with mean 4.2 minutes and standard deviation 0.6 minutes.

- (i) Find the probability that a person chosen at random takes between 3.5 and 4.5 minutes to cook an egg. [3]

12% of people take more than t minutes to cook an egg.

- (ii) Find the value of t . [3]

- (iii) A random sample of n people is taken. Find the smallest possible value of n if the probability that none of these people takes more than t minutes to cook an egg is less than 0.003. [3]

Question 45

On any day at noon, the probabilities that Kersley is asleep or studying are 0.2 and 0.6 respectively.

- (i) Find the probability that, in any 7-day period, Kersley is either asleep or studying at noon on at least 6 days. [3]

- (ii) Use an approximation to find the probability that, in any period of 100 days, Kersley is asleep at noon on at most 30 days. [5]

Question 46

Packets of rice are filled by a machine and have weights which are normally distributed with mean 1.04 kg and standard deviation 0.017 kg.

- (i) Find the probability that a randomly chosen packet weighs less than 1 kg. [3]

- (ii) How many packets of rice, on average, would the machine fill from 1000 kg of rice? [1]

The factory manager wants to produce more packets of rice. He changes the settings on the machine so that the standard deviation is the same but the mean is reduced to μ kg. With this mean the probability that a packet weighs less than 1 kg is 0.0388.

- (iii) Find the value of μ . [3]

- (iv) How many packets of rice, on average, would the machine now fill from 1000 kg of rice? [1]

Question 47

The random variable X is such that $X \sim N(20, 49)$. Given that $P(X > k) = 0.25$, find the value of k . [3]

Question 48

- (a) The lengths, in centimetres, of middle fingers of women in Raneland have a normal distribution with mean μ and standard deviation σ . It is found that 25% of these women have fingers longer than 8.8 cm and 17.5% have fingers shorter than 7.7 cm.

- (i) Find the values of μ and σ . [5]

The lengths, in centimetres, of middle fingers of women in Snoland have a normal distribution with mean 7.9 and standard deviation 0.44. A random sample of 5 women from Snoland is chosen.

- (ii) Find the probability that exactly 3 of these women have middle fingers shorter than 8.2 cm. [5]

- (b) The random variable X has a normal distribution with mean equal to the standard deviation. Find the probability that a particular value of X is less than 1.5 times the mean. [3]

Question 49

It is found that 10% of the population enjoy watching Historical Drama on television. Use an appropriate approximation to find the probability that, out of 160 people chosen randomly, more than 17 people enjoy watching Historical Drama on television. [5]

Question 50

- (a) The random variable X has the distribution $N(\mu, \sigma^2)$, where $\mu = 1.5\sigma$. A random value of X is chosen. Find the probability that this value of X is greater than 0. [3]
- (b) The life of a particular type of torch battery is normally distributed with mean 120 hours and standard deviation s hours. It is known that 87.5% of these batteries last longer than 70 hours. Find the value of s . [3]

Question 51

The probability that George goes swimming on any day is $\frac{1}{3}$. Use an approximation to calculate the probability that in 270 days George goes swimming at least 100 times. [5]

Question 52

The lengths of videos of a certain popular song have a normal distribution with mean 3.9 minutes. 18% of these videos last for longer than 4.2 minutes.

- (i) Find the standard deviation of the lengths of these videos. [3]
- (ii) Find the probability that the length of a randomly chosen video differs from the mean by less than half a minute. [4]

The lengths of videos of another popular song have a normal distribution with the same mean of 3.9 minutes but the standard deviation is twice the standard deviation in part (i). The probability that the length of a randomly chosen video of this song differs from the mean by less than half a minute is denoted by p .

- (iii) Without any further calculation, determine whether p is more than, equal to, or less than your answer to part (ii). You must explain your reasoning. [2]

Question 53

- (a) The random variable X has a normal distribution with mean μ and standard deviation σ . You are given that $\sigma = 0.25\mu$ and $P(X < 6.8) = 0.75$.
- (i) Find the value of μ . [4]
- (ii) Find $P(X < 4.7)$. [3]
- (b) The lengths of metal rods have a normal distribution with mean 16 cm and standard deviation 0.2 cm. Rods which are shorter than 15.75 cm or longer than 16.25 cm are not usable. Find the expected number of usable rods in a batch of 1000 rods. [4]

Question 54

Josie aims to catch a bus which departs at a fixed time every day. Josie arrives at the bus stop T minutes before the bus departs, where $T \sim N(5.3, 2.1^2)$.

- (i) Find the probability that Josie has to wait longer than 6 minutes at the bus stop. [3]
- On 5% of days Josie has to wait longer than x minutes at the bus stop.
- (ii) Find the value of x . [3]
- (iii) Find the probability that Josie waits longer than x minutes on fewer than 3 days in 10 days. [3]
- (iv) Find the probability that Josie misses the bus. [3]

Question 55

In Jimpuri the weights, in kilograms, of boys aged 16 years have a normal distribution with mean 61.4 and standard deviation 12.3.

- (i) Find the probability that a randomly chosen boy aged 16 years in Jimpuri weighs more than 65 kilograms. [3]
- (ii) For boys aged 16 years in Jimpuri, 25% have a weight between 65 kilograms and k kilograms, where k is greater than 65. Find k . [4]

In Brigville the weights, in kilograms, of boys aged 16 years have a normal distribution. 99% of the boys weigh less than 97.2 kilograms and 33% of the boys weigh less than 55.2 kilograms.

- (iii) Find the mean and standard deviation of the weights of boys aged 16 years in Brigville. [5]

Question 56

Blank CDs are packed in boxes of 30. The probability that a blank CD is faulty is 0.04. A box is rejected if more than 2 of the blank CDs are faulty.

- (i) Find the probability that a box is rejected. [3]
- (ii) 280 boxes are chosen randomly. Use an approximation to find the probability that at least 30 of these boxes are rejected. [5]

Question 57

The weight, in grams, of pineapples is denoted by the random variable X which has a normal distribution with mean 500 and standard deviation 91.5. Pineapples weighing over 570 grams are classified as 'large'. Those weighing under 390 grams are classified as 'small' and the rest are classified as 'medium'.

- (i) Find the proportions of large, small and medium pineapples. [5]
- (ii) Find the weight exceeded by the heaviest 5% of pineapples. [3]
- (iii) Find the value of k such that $P(k < X < 610) = 0.3$. [5]

Question 58

The results of a survey at a certain large college show that the proportion of students who own a car is $\frac{1}{4}$.

- (i) Five students at the college are chosen at random. Find the probability that at least four of these students own a car. [3]
- (ii) For a random sample of n students at the college, the probability that at least one of the students owns a car is greater than 0.995. Find the least possible value of n . [3]
- (iii) For a random sample of 160 students at the college, use a suitable approximate distribution to find the probability that fewer than 50 own a car. [4]

Question 59

The weights of packets of a certain type of biscuit are normally distributed with mean 400 grams and standard deviation σ grams.

- (i) In a random sample of 6000 packets of this type of biscuit, 225 packets weighed more than 410 grams. Find the value of σ . [4]
- (ii) In a random sample of 500 packets of this type of biscuit, how many packets would you expect to find with weights that are more than 1.5 standard deviations from the mean? [4]

Question 60

The diameters of apples in an orchard have a normal distribution with mean 5.7 cm and standard deviation 0.8 cm. Apples with diameters between 4.1 cm and 5 cm can be used as toffee apples.

- (i) Find the probability that an apple selected at random can be used as a toffee apple. [3]
- (ii) 250 apples are chosen at random. Use a suitable approximation to find the probability that fewer than 50 can be used as toffee apples. [5]

Question 61

The random variable X has the distribution $N(-3, \sigma^2)$. The probability that a randomly chosen value of X is positive is 0.25.

- (i) Find the value of σ . [3]
- (ii) Find the probability that, of 8 random values of X , fewer than 2 will be positive. [3]

Question 62

In a certain country, 60% of mobile phones sold are made by Company A, 35% are made by Company B and 5% are made by other companies.

- (i) Find the probability that, out of a random sample of 13 people who buy a mobile phone, fewer than 11 choose a mobile phone made by Company A. [3]
- (ii) Use a suitable approximation to find the probability that, out of a random sample of 130 people who buy a mobile phone, at least 50 choose a mobile phone made by Company B. [5]
- (iii) A random sample of n mobile phones sold is chosen. The probability that at least one of these phones is made by Company B is more than 0.98. Find the least possible value of n . [3]

Question 63

- (i) The volume of soup in Super Soup cartons has a normal distribution with mean μ millilitres and standard deviation 9 millilitres. Tests have shown that 10% of cartons contain less than 440 millilitres of soup. Find the value of μ . [3]
- (ii) A food retailer orders 150 Super Soup cartons. Calculate the number of these cartons for which you would expect the volume of soup to be more than 1.8 standard deviations above the mean. [3]

Question 64

In Pelmerdon 22% of families own a dishwasher.

- (i) Find the probability that, of 15 families chosen at random from Pelmerdon, between 4 and 6 inclusive own a dishwasher. [3]
- (ii) A random sample of 145 families from Pelmerdon is chosen. Use a suitable approximation to find the probability that more than 26 families own a dishwasher. [5]

Question 65

- (a) The distance that car tyres of a certain make can travel before they need to be replaced has a normal distribution. A survey of a large number of these tyres found that the probability of this distance being more than 36 800 km is 0.0082 and the probability of this distance being more than 31 000 km is 0.6915. Find the mean and standard deviation of the distribution. [5]
- (b) The random variable X has the distribution $N(\mu, \sigma^2)$, where $3\sigma = 4\mu$ and $\mu \neq 0$. Find $P(X < 3\mu)$. [3]

Question 66

The weights of apples sold by a store can be modelled by a normal distribution with mean 120 grams and standard deviation 24 grams. Apples weighing less than 90 grams are graded as 'small'; apples weighing more than 140 grams are graded as 'large'; the remainder are graded as 'medium'.

- (i) Show that the probability that an apple chosen at random is graded as medium is 0.692, correct to 3 significant figures. [4]
- (ii) Four apples are chosen at random. Find the probability that at least two are graded as medium. [4]

Question 67

The lifetimes, in hours, of a particular type of light bulb are normally distributed with mean 2000 hours and standard deviation σ hours. The probability that a randomly chosen light bulb of this type has a lifetime of more than 1800 hours is 0.96.

- (i) Find the value of σ . [3]

New technology has resulted in a new type of light bulb. It is found that on average one in five of these new light bulbs has a lifetime of more than 2500 hours.

- (ii) For a random selection of 300 of these new light bulbs, use a suitable approximate distribution to find the probability that fewer than 70 have a lifetime of more than 2500 hours. [4]
- (iii) Justify the use of your approximate distribution in part (ii). [1]

Question 68

(a) The time, X hours, for which students use a games machine in any given day has a normal distribution with mean 3.24 hours and standard deviation 0.96 hours.

- (i) On how many days of the year (365 days) would you expect a randomly chosen student to use a games machine for less than 4 hours? [3]
- (ii) Find the value of k such that $P(X > k) = 0.2$. [3]
- (iii) Find the probability that the number of hours for which a randomly chosen student uses a games machine in a day is within 1.5 standard deviations of the mean. [3]

(b) The variable Y is normally distributed with mean μ and standard deviation σ , where $4\sigma = 3\mu$ and $\mu \neq 0$. Find the probability that a randomly chosen value of Y is positive. [3]

Question 69

(a) It is given that $X \sim N(31.4, 3.6)$. Find the probability that a randomly chosen value of X is less than 29.4. [3]

(b) The lengths of fish of a particular species are modelled by a normal distribution. A scientist measures the lengths of 400 randomly chosen fish of this species. He finds that 42 fish are less than 12 cm long and 58 are more than 19 cm long. Find estimates for the mean and standard deviation of the lengths of fish of this species. [5]

Question 70

At the Nonland Business College, all students sit an accountancy examination at the end of their first year of study. On average, 80% of the students pass this examination.

- (i) A random sample of 9 students who will take this examination is chosen. Find the probability that at most 6 of these students will pass the examination. [3]
- (ii) A random sample of 200 students who will take this examination is chosen. Use a suitable approximate distribution to find the probability that more than 166 of them will pass the examination. [5]
- (iii) Justify the use of your approximate distribution in part (ii). [1]

Question 71

The times taken, in minutes, for trains to travel between Alphaton and Beeton are normally distributed with mean 140 and standard deviation 12.

- (i) Find the probability that a randomly chosen train will take less than 132 minutes to travel between Alphaton and Beeton. [3]
- (ii) The probability that a randomly chosen train takes more than k minutes to travel between Alphaton and Beeton is 0.675. Find the value of k . [3]

Question 72

The time taken, in minutes, by a ferry to cross a lake has a normal distribution with mean 85 and standard deviation 6.8.

- (i) Find the probability that, on a randomly chosen occasion, the time taken by the ferry to cross the lake is between 79 and 91 minutes. [3]
- (ii) Over a long period it is found that 96% of ferry crossings take longer than a certain time t minutes. Find the value of t . [3]

Question 73

The weight of adult female giraffes has a normal distribution with mean 830 kg and standard deviation 120 kg.

- (i) There are 430 adult female giraffes in a particular game reserve. Find the number of these adult female giraffes which can be expected to weigh less than 700 kg. [4]
- (ii) Given that 90% of adult female giraffes weigh between $(830 - w)$ kg and $(830 + w)$ kg, find the value of w . [3]

The weight of adult male giraffes has a normal distribution with mean 1190 kg and standard deviation σ kg.

- (iii) Given that 83.4% of adult male giraffes weigh more than 950 kg, find the value of σ . [3]

Question 74

The heights of students at the Mainland college are normally distributed with mean 148 cm and standard deviation 8 cm.

- (i) The probability that a Mainland student chosen at random has a height less than h cm is 0.67. Find the value of h . [3]

120 Mainland students are chosen at random.

- (ii) Find the number of these students that would be expected to have a height within half a standard deviation of the mean. [4]

Question 75

A competition is taking place between two choirs, the Notes and the Classics. There is a large audience for the competition.

- 30% of the audience are Notes supporters.
 - 45% of the audience are Classics supporters.
 - The rest of the audience are not supporters of either of these choirs.
 - No one in the audience supports both of these choirs.
- (i) A random sample of 6 people is chosen from the audience.
- (a) Find the probability that no more than 2 of the 6 people are Notes supporters. [3]
- (b) Find the probability that none of the 6 people support either of these choirs. [2]
- (ii) A random sample of 240 people is chosen from the audience. Use a suitable approximation to find the probability that fewer than 50 do not support either of the choirs. [5]

Question 76

The heights, in metres, of fir trees in a large forest have a normal distribution with mean 40 and standard deviation 8.

- (i) Find the probability that a fir tree chosen at random in this forest has a height less than 45 metres. [2]
- (ii) Find the probability that a fir tree chosen at random in this forest has a height within 5 metres of the mean. [2]
- In another forest, the heights of another type of fir tree are modelled by a normal distribution. A scientist measures the heights of 500 randomly chosen trees of this type. He finds that 48 trees are less than 10 m high and 76 trees are more than 24 m high.
- (iii) Find the mean and standard deviation of the heights of trees of this type. [5]

Question 77

In Quarendon, 66% of households are satisfied with the speed of their wifi connection.

- (i) Find the probability that, out of 10 households chosen at random in Quarendon, at least 8 are satisfied with the speed of their wifi connection. [3]
- (ii) A random sample of 150 households in Quarendon is chosen. Use a suitable approximation to find the probability that more than 84 are satisfied with the speed of their wifi connection. [5]

Question 78

The shortest time recorded by an athlete in a 400 m race is called their personal best (PB). The PBs of the athletes in a large athletics club are normally distributed with mean 49.2 seconds and standard deviation 2.8 seconds.

- (i) Find the probability that a randomly chosen athlete from this club has a PB between 46 and 53 seconds. [4]
- (ii) It is found that 92% of athletes from this club have PBs of more than t seconds. Find the value of t . [3]
- Three athletes from the club are chosen at random.
- (iii) Find the probability that exactly 2 have PBs of less than 46 seconds. [3]

Question 79

The weights of apples of a certain variety are normally distributed with mean 82 grams. 22% of these apples have a weight greater than 87 grams.

- (a) Find the standard deviation of the weights of these apples. [3]
- (b) Find the probability that the weight of a randomly chosen apple of this variety differs from the mean weight by less than 4 grams. [4]

Question 80

In Greenton, 70% of the adults own a car. A random sample of 8 adults from Greenton is chosen.

- (a) Find the probability that the number of adults in this sample who own a car is less than 6. [3]

A random sample of 120 adults from Greenton is now chosen.

- (b) Use an approximation to find the probability that more than 75 of them own a car. [5]

Question 81

In a certain town, the time, X hours, for which people watch television in a week has a normal distribution with mean 15.8 hours and standard deviation 4.2 hours.

- (a) Find the probability that a randomly chosen person from this town watches television for less than 21 hours in a week. [2]
- (b) Find the value of k such that $P(X < k) = 0.75$. [3]

Question 82

A pair of fair coins is thrown repeatedly until a pair of tails is obtained. The random variable X denotes the number of throws required to obtain a pair of tails.

- (a) Find the expected value of X . [1]
- (b) Find the probability that exactly 3 throws are required to obtain a pair of tails. [1]
- (c) Find the probability that fewer than 6 throws are required to obtain a pair of tails. [2]

On a different occasion, a pair of fair coins is thrown 80 times.

- (d) Use an approximation to find the probability that a pair of tails is obtained more than 25 times. [5]

Question 83

Trees in the Redian forest are classified as tall, medium or short, according to their height. The heights can be modelled by a normal distribution with mean 40 m and standard deviation 12 m. Trees with a height of less than 25 m are classified as short.

- (a) Find the probability that a randomly chosen tree is classified as short. [3]

Of the trees that are classified as tall or medium, one third are tall and two thirds are medium.

- (b) Show that the probability that a randomly chosen tree is classified as tall is 0.298, correct to 3 decimal places. [2]
- (c) Find the height above which trees are classified as tall. [3]

Question 84

On any given day, the probability that Moena messages her friend Pasha is 0.72.

- (a) Find the probability that for a random sample of 12 days Moena messages Pasha on no more than 9 days. [3]
- (b) Moena messages Pasha on 1 January. Find the probability that the next day on which she messages Pasha is 5 January. [1]
- (c) Use an approximation to find the probability that in any period of 100 days Moena messages Pasha on fewer than 64 days. [5]

Question 85

The times taken to swim 100 metres by members of a large swimming club have a normal distribution with mean 62 seconds and standard deviation 5 seconds.

- (a) Find the probability that a randomly chosen member of the club takes between 56 and 66 seconds to swim 100 metres. [3]
- (b) 13% of the members of the club take more than t minutes to swim 100 metres. Find the value of t . [3]

Question 86

Pia runs 2 km every day and her times in minutes are normally distributed with mean 10.1 and standard deviation 1.3.

- (a) Find the probability that on a randomly chosen day Pia takes longer than 11.3 minutes to run 2 km. [3]
- (b) On 75% of days, Pia takes longer than t minutes to run 2 km. Find the value of t . [3]
- (c) On how many days in a period of 90 days would you expect Pia to take between 8.9 and 11.3 minutes to run 2 km? [3]

Question 87

The time in hours that Davin plays on his games machine each day is normally distributed with mean 3.5 and standard deviation 0.9.

- (a) Find the probability that on a randomly chosen day Davin plays on his games machine for more than 4.2 hours. [3]
- (b) On 90% of days Davin plays on his games machine for more than t hours. Find the value of t . [3]
- (c) Calculate an estimate for the number of days in a year (365 days) on which Davin plays on his games machine for between 2.8 and 4.2 hours. [3]

Question 88

The time spent by shoppers in a large shopping centre has a normal distribution with mean 96 minutes and standard deviation 18 minutes.

- (a) Find the probability that a shopper chosen at random spends between 85 and 100 minutes in the shopping centre. [3]

88% of shoppers spend more than t minutes in the shopping centre.

- (b) Find the value of t . [3]

Question 89

The lengths of the leaves of a particular type of tree are modelled by a normal distribution. A scientist measures the lengths of a random sample of 500 leaves from this type of tree and finds that 42 are less than 4 cm long and 100 are more than 10 cm long.

- (a) Find estimates for the mean and standard deviation of the lengths of leaves from this type of tree. [5]

The lengths, in cm, of the leaves of a different type of tree have the distribution $N(\mu, \sigma^2)$. The scientist takes a random sample of 800 leaves from this type of tree.

- (b) Find how many of these leaves the scientist would expect to have lengths, in cm, between $\mu - 2\sigma$ and $\mu + 2\sigma$. [4]

Question 90

The weights of bags of sugar are normally distributed with mean 1.04 kg and standard deviation σ kg. In a random sample of 2000 bags of sugar, 72 weighed more than 1.10 kg.

Find the value of σ . [4]

Question 91

A company produces a particular type of metal rod. The lengths of these rods are normally distributed with mean 25.2 cm and standard deviation 0.4 cm. A random sample of 500 of these rods is chosen.

How many rods in this sample would you expect to have a length that is within 0.5 cm of the mean length? [5]

Question 92

Raj wants to improve his fitness, so every day he goes for a run. The times, in minutes, of his runs have a normal distribution with mean 41.2 and standard deviation 3.6.

- (a) Find the probability that on a randomly chosen day Raj runs for more than 43.2 minutes. [3]
- (b) Find an estimate for the number of days in a year (365 days) on which Raj runs for less than 43.2 minutes. [2]
- (c) On 95% of days, Raj runs for more than t minutes.

Find the value of t . [3]

Question 93

The times taken, in minutes, to complete a particular task by employees at a large company are normally distributed with mean 32.2 and standard deviation 9.6.

- (a) Find the probability that a randomly chosen employee takes more than 28.6 minutes to complete the task. [3]

- (b) 20% of employees take longer than t minutes to complete the task.

Find the value of t . [3]

- (c) Find the probability that the time taken to complete the task by a randomly chosen employee differs from the mean by less than 15.0 minutes. [4]

Question 94

The times, in minutes, that Karli spends each day on social media are normally distributed with mean 125 and standard deviation 24.

- (a) (i) On how many days of the year (365 days) would you expect Karli to spend more than 142 minutes on social media? [5]

- (ii) Find the probability that Karli spends more than 142 minutes on social media on fewer than 2 of 10 randomly chosen days. [3]

- (b) On 90% of days, Karli spends more than t minutes on social media.

Find the value of t . [3]

Question 95

The weights of male leopards in a particular region are normally distributed with mean 55 kg and standard deviation 6 kg.

- (a) Find the probability that a randomly chosen male leopard from this region weighs between 46 and 62 kg. [4]

The weights of female leopards in this region are normally distributed with mean 42 kg and standard deviation σ kg. It is known that 25% of female leopards in the region weigh less than 36 kg.

- (b) Find the value of σ . [3]

The distributions of the weights of male and female leopards are independent of each other. A male leopard and a female leopard are each chosen at random.

- (c) Find the probability that both the weights of these leopards are less than 46 kg. [4]

Question 96

Farmer Jones grows apples. The weights, in grams, of the apples grown this year are normally distributed with mean 170 and standard deviation 25. Apples that weigh between 142 grams and 205 grams are sold to a supermarket.

- (a) Find the probability that a randomly chosen apple grown by Farmer Jones this year is sold to the supermarket. [4]

Farmer Jones sells the apples to the supermarket at \$0.24 each. He sells apples that weigh more than 205 grams to a local shop at \$0.30 each. He does not sell apples that weigh less than 142 grams.

The total number of apples grown by Farmer Jones this year is 20 000.

- (b) Calculate an estimate for his total income from this year's apples. [3]

Farmer Tan also grows apples. The weights, in grams, of the apples grown this year follow the distribution $N(182, 20^2)$. 72% of these apples have a weight more than w grams.

- (c) Find the value of w . [3]

Question 97

In a large college, 28% of the students do not play any musical instrument, 52% play exactly one musical instrument and the remainder play two or more musical instruments.

A random sample of 12 students from the college is chosen.

- (a) Find the probability that more than 9 of these students play at least one musical instrument. [3]

A random sample of 90 students from the college is now chosen.

- (b) Use an approximation to find the probability that fewer than 40 of these students play exactly one musical instrument. [5]

Question 98

The weights, in kg, of bags of rice produced by Anders have the distribution $N(2.02, 0.03^2)$.

- (a) Find the probability that a randomly chosen bag of rice produced by Anders weighs between 1.98 and 2.03 kg. [3]

The weights of bags of rice produced by Binders are normally distributed with mean 2.55 kg and standard deviation σ kg. In a random sample of 5000 of these bags, 134 weighed more than 2.6 kg.

- (b) Find the value of σ . [4]

Question 99

The lengths, in cm, of the leaves of a particular type are modelled by the distribution $N(5.2, 1.5^2)$.

- (a) Find the probability that a randomly chosen leaf of this type has length less than 6 cm. [2]

The lengths of the leaves of another type are also modelled by a normal distribution. A scientist measures the lengths of a random sample of 500 leaves of this type and finds that 46 are less than 3 cm long and 95 are more than 8 cm long.

- (b) Find estimates for the mean and standard deviation of the lengths of leaves of this type. [5]

- (c) In a random sample of 2000 leaves of this second type, how many would the scientist expect to find with lengths more than 1 standard deviation from the mean? [4]

Question 100

In a large college, 32% of the students have blue eyes. A random sample of 80 students is chosen.

Use an approximation to find the probability that fewer than 20 of these students have blue eyes. [5]

Question 101

The weights of the bags of sugar produced by company B are normally distributed with mean 1.04 kg and standard deviation 0.06 kg.

Find the probability that a randomly chosen bag produced by company B weighs more than 1.11 kg. [3]

Question 102

81% of the bags of sugar produced by company B weigh less than w kg.

Find the value of w . [3]

Question 103

The lengths of the rods produced by a company are normally distributed with mean 55.6 mm and standard deviation 1.2 mm.

(a) In a random sample of 400 of these rods, how many would you expect to have length less than 54.8 mm? [4]

(b) Find the probability that a randomly chosen rod produced by this company has a length that is within half a standard deviation of the mean. [3]

Question 104

At a company's call centre, 90% of callers are connected immediately to a representative.

A random sample of 12 callers is chosen.

(a) Find the probability that fewer than 10 of these callers are connected immediately. [3]

A random sample of 80 callers is chosen.

(b) Use an approximation to find the probability that more than 69 of these callers are connected immediately. [5]

(c) Justify the use of your approximation in part (b). [1]

Question 105

The residents of Persham were surveyed about the reliability of their internet service. 12% rated the service as 'poor', 36% rated it as 'satisfactory' and 52% rated it as 'good'.

A random sample of 8 residents of Persham is chosen.

(a) Find the probability that more than 2 and fewer than 8 of them rate their internet service as poor or satisfactory. [3]

A random sample of 125 residents of Persham is now chosen.

(b) Use an approximation to find the probability that more than 72 of these residents rate their internet service as good. [5]

Question 106

In a large population, the systolic blood pressure (SBP) of adults is normally distributed with mean 125.4 and standard deviation 18.6.

(a) Find the probability that the SBP of a randomly chosen adult is less than 132. [2]

The SBP of 12-year-old children in the same population is normally distributed with mean 117. Of these children 88% have SBP more than 108.

(b) Find the standard deviation of this distribution. [3]

Three adults are chosen at random from this population.

(c) Find the probability that each of these three adults has SBP within 1.5 standard deviations of the mean. [4]

Question 107

In a cycling event the times taken to complete a course are modelled by a normal distribution with mean 62.3 minutes and standard deviation 8.4 minutes.

- (a) Find the probability that a randomly chosen cyclist has a time less than 74 minutes. [2]
- (b) Find the probability that 4 randomly chosen cyclists all have times between 50 and 74 minutes. [4]

In a different cycling event, the times can also be modelled by a normal distribution. 23% of the cyclists have times less than 36 minutes and 10% of the cyclists have times greater than 54 minutes.

- (c) Find estimates for the mean and standard deviation of this distribution. [5]

Question 108

Anil is a candidate in an election. He received 40% of the votes. A random sample of 120 voters is chosen.

Use an approximation to find the probability that, of the 120 voters, between 36 and 54 inclusive voted for Anil. [5]

Question 109

The mass of grapes sold per day by a large shop can be modelled by a normal distribution with mean 28 kg. On 10% of days less than 16 kg of grapes are sold.

- (a) Find the standard deviation of the mass of grapes sold per day. [3]

The mass of grapes sold on any day is independent of the mass sold on any other day.

- (b) 12 days are chosen at random.

Find the probability that less than 16 kg of grapes are sold on more than 2 of these 12 days. [3]

- (c) In a random sample of 365 days, on how many days would you expect the mass of grapes sold to be within 1.3 standard deviations of the mean? [4]

Question 110

The lengths of Western bluebirds are normally distributed with mean 16.5 cm and standard deviation 0.6 cm.

A random sample of 150 of these birds is selected.

- (a) How many of these 150 birds would you expect to have length between 15.4 cm and 16.8 cm? [4]

The lengths of Eastern bluebirds are normally distributed with mean 18.4 cm and standard deviation σ cm. It is known that 72% of Eastern bluebirds have length greater than 17.1 cm.

- (b) Find the value of σ . [3]

A random sample of 120 Eastern bluebirds is chosen.

- (c) Use an approximation to find the probability that fewer than 80 of these 120 bluebirds have length greater than 17.1 cm. [5]

Question 111

A mathematical puzzle is given to a large number of students. The times taken to complete the puzzle are normally distributed with mean 14.6 minutes and standard deviation 5.2 minutes.

- (a) In a random sample of 250 of the students, how many would you expect to have taken more than 20 minutes to complete the puzzle? [4]

All the students are given a second puzzle to complete. Their times, in minutes, are normally distributed with mean μ and standard deviation σ . It is found that 20% of the students have times less than 14.5 minutes and 67% of the students have times greater than 18.5 minutes.

- (b) Find the value of μ and the value of σ . [5]

Question 112

The weights of large bags of pasta produced by a company are normally distributed with mean 1.5 kg and standard deviation 0.05 kg.

- (a) Find the probability that a randomly chosen large bag of pasta weighs between 1.42 kg and 1.52 kg. [3]

The weights of small bags of pasta produced by the company are normally distributed with mean 0.75 kg and standard deviation σ kg. It is found that 68% of these small bags have weight less than 0.9 kg.

- (b) Find the value of σ . [3]

Question 113

- (a) The heights of the members of a club are normally distributed with mean 166 cm and standard deviation 10 cm.

(i) Find the probability that a randomly chosen member of the club has height less than 170 cm. [2]

(ii) Given that 40% of the members have heights greater than h cm, find the value of h correct to 2 decimal places. [3]

- (b) The random variable X is normally distributed with mean μ and standard deviation σ .

Given that $\sigma = \frac{2}{3}\mu$, find the probability that a randomly chosen value of X is positive. [3]

Question 114

A factory produces a certain type of electrical component. It is known that 15% of the components produced are faulty. A random sample of 200 components is chosen.

Use an approximation to find the probability that more than 40 of these components are faulty. [5]

Question 115

A farmer sells eggs. The weights, in grams, of the eggs can be modelled by a normal distribution with mean 80.5 and standard deviation 6.6. Eggs are classified as small, medium or large according to their weight. A small egg weighs less than 76 grams and 40% of the eggs are classified as medium.

- (a) Find the percentage of eggs that are classified as small. [3]

- (b) Find the least possible weight of an egg classified as large. [3]

150 of the eggs for sale last week were weighed.

- (c) Use an approximation to find the probability that more than 68 of these eggs were classified as medium. [5]

Question 116

A company sells small and large bags of rice. The masses of the small bags of rice are normally distributed with mean 1.20 kg and standard deviation 0.16 kg.

- (a) In a random sample of 500 of these small bags of rice, how many would you expect to have a mass greater than 1.26 kg? [4]

The masses of the large bags of rice are normally distributed with mean 2.50 kg and standard deviation σ kg. 20% of these large bags of rice have a mass less than 2.40 kg.

- (b) Find the value of σ . [3]

A random sample of 80 large bags of rice is chosen.

- (c) Use a suitable approximation to find the probability that fewer than 22 of these large bags of rice have a mass less than 2.40 kg. [5]

Question 117

In a certain country, the heights of the adult population are normally distributed with mean 1.64 m and standard deviation 0.25 m.

- (a) Find the probability that an adult chosen at random from this country will have height greater than 1.93 m. [3]

In another country, the heights of the adult population are also normally distributed. 33% of the adult population have height less than 1.56 m. 25% of the adult population have height greater than 1.86 m.

- (b) Find the mean and the standard deviation of this distribution. [5]

Question 118

The weights of oranges can be modelled by a normal distribution with mean 131 grams and standard deviation 54 grams. Oranges are classified as small, medium or large. A large orange weighs at least 184 grams and 20% of oranges are classified as small.

- (a) Find the percentage of oranges that are classified as large. [3]
(b) Find the greatest possible weight of a small orange. [3]

Question 119

The lengths of the tails of adult raccoons of a certain species are normally distributed with mean 28 cm and standard deviation 3.3 cm.

- (a) Find the probability that a randomly chosen adult raccoon of this species has a tail length between 23 cm and 35 cm. [4]

The masses of adult raccoons of this species are normally distributed with mean 8.5 kg and standard deviation σ kg. 75% of adult raccoons of this species have mass greater than 7.6 kg.

- (b) Find the value of σ . [3]

Question 120

In Molimba, the heights, in cm, of adult males are normally distributed with mean 176 cm and standard deviation 4.8 cm.

- (a) Find the probability that a randomly chosen adult male in Molimba has a height greater than 170 cm. [3]

60% of adult males in Molimba have a height between 170 cm and k cm, where k is greater than 170.

- (b) Find the value of k , giving your answer correct to 1 decimal place. [4]

Question 121

The heights, in metres, of white pine trees are normally distributed with mean 19.8 and standard deviation 2.4 .

In a certain forest there are 450 white pine trees.

- (a) How many of these trees would you expect to have height less than 18.2 metres? [4]

The heights, in metres, of red pine trees are normally distributed with mean 23.4 and standard deviation σ . It is known that 26% of red pine trees have height greater than 25.5 metres.

- (b) Find the value of σ . [3]

Question 122

The heights of the female students at Breven college are normally distributed:

- 90% of the female students have heights less than 182.7 cm.
- 40% of the female students have heights less than 162.5 cm.

- (a) Find the mean and the standard deviation of the heights of the female students at Breven college. [5]

Ten female students are chosen at random from those at Breven college.

- (b) Find the probability that fewer than 8 of these 10 students have heights more than 162.5 cm. [3]

Question 123

The weights of the green apples sold by a shop are normally distributed with mean 90 grams and standard deviation 8 grams.

- (a) Find the probability that a randomly chosen green apple weighs between 83 grams and 95 grams. [4]
- (b) The shop also sells red apples. 60% of the red apples sold by the shop weigh more than 80 grams. 160 red apples are chosen at random from the shop.

Use a suitable approximation to find the probability that fewer than 105 of the chosen red apples weigh more than 80 grams. [5]

Question 124

The mass of peaches sold per day in a supermarket is normally distributed with mean 65.8 kg and standard deviation 9.6 kg.

- (a) Find the probability that the mass of peaches sold on any given day is between 56 kg and 75 kg. [3]

The mass of cherries sold per day in a supermarket is normally distributed with mean 72.4 kg and standard deviation σ kg. It is known that on 10% of days less than 59.1 kg of cherries are sold.

- (b) Find the value of σ . [3]

The supermarket is open 7 days a week.

- (c) Find the probability that, in a randomly chosen week, the first day on which less than 59.1 kg of cherries are sold is the fifth day of the week. [1]
- (d) Find the probability that, in a randomly chosen week, the first day on which less than 59.1 kg of cherries are sold is before the fifth day of the week. [2]

Question 125

A company sells bags of pasta. The masses of large bags of pasta are normally distributed with mean 2.50 kg and standard deviation 0.12 kg.

- (a) Find the probability that the mass of pasta in a randomly chosen large bag is less than 2.65 kg. [2]

A restaurant manager buys 160 of these large bags of pasta.

- (b) Find the number of bags for which you would expect the mass of pasta to be more than 1.65 standard deviations above the mean. [3]

The masses of small bags of pasta sold by the company are normally distributed with mean μ kg and standard deviation σ kg. Tests show that 77% of these bags have masses greater than 1.26 kg, and 44% have masses less than 1.35 kg.

- (c) Find, in either order, the value of μ and the value of σ . [5]

Question 126

Kestrels are birds whose adult wingspans are normally distributed with mean 74.8 cm and standard deviation 3.2 cm. A random sample of 120 adult kestrels is selected.

- (a) How many of these 120 adult kestrels would you expect to have wingspan between 72.4 cm and 76.3 cm? [4]

The masses of adult kestrels are normally distributed with mean μ kg and standard deviation σ kg. It is known that 20% of adult kestrels have mass greater than 0.202 kg and 28% have mass less than 0.185 kg.

- (b) Find the value of μ and the value of σ . [5]

Question 127

The masses of the bags of rice made by a company are normally distributed with mean μ kg and standard deviation 0.14 kg. The probability that the mass of a randomly chosen bag of this rice is less than 1.48 kg is 0.22.

- Find the value of μ . [3]