

AS-Level
Topic : Normal Distribution
May : 2013-May :2023
Answers

Question 1

| | | |
|---|--------------|---|
| <p>(i) $P(\text{tall}) = P\left(z > \frac{70-50}{16}\right) = P(z > 1.25)$ $= 1 - 0.8944$ $= 0.106$</p> | <p>M1</p> | <p>+ve/-ve Standardising no cc no sq rt no sq</p> |
| | <p>A1</p> | <p>[2] Correct answer</p> |
| <p>(ii) $P(\text{short}) = (1 - 0.1056)/3$</p> <p>$= 0.2981$</p> <p>$z = -0.53$</p> <p>$-0.53 = \frac{x-50}{16}$</p> <p>$x = 41.5$</p> | <p>M1</p> | <p>Subt their (i) from 1 or their (i) and multiplying by $\frac{1}{3}$ or $\frac{2}{3}$</p> |
| | <p>A1 ft</p> | <p>Rounding to 0.298, only ft for $\frac{(1-(i))}{3}$</p> |
| | <p>A1</p> | <p>\pm z-value rounding to 0.53, condone ± 0.24</p> |
| | <p>M1</p> | <p>Standardising with their z value (not a probability), no cc sq rt etc.</p> |
| | <p>A1</p> | <p>[5] Correct answer</p> |

Question 2

| | | |
|---|-------------------|--|
| <p>(i) $P(x < 440)$ $= P\left(z < \frac{440-445}{3.6}\right) = 1 - \Phi(1.389)$ $= 1 - 0.9176$</p> <p>Ans = 0.0824</p> | <p>M1</p> | <p>Standardising no cc no sq or sq rt</p> |
| | <p>M1</p> | <p>Correct area $(1 - \Phi)$ oe (indep)</p> |
| | <p>A1</p> | <p>Rounding to correct answer accept 0.0825</p> |
| | <p>[3]</p> | |
| <p>(ii) $z = 1.881$</p> <p>$\frac{c}{3.6} = 1.881$</p> <p>$c = 6.77$</p> | <p>M1</p> | <p>± 1.88 or 1.881 or 1.882 or 1.555 seen\pm</p> |
| | <p>M1</p> | <p>Equation with $\pm c/3.6$ or $2c/3.6$ only = z or prob (can be implied)</p> |
| | <p>A1</p> | <p>[3] Correct answer accept 6.78</p> |

Question 3

| | | |
|---|-----------|--|
| <p>$z = 1.452$</p> <p>$1.452 = \frac{20 - \mu}{\mu/5}$</p> <p>$\mu = 15.5$</p> | <p>B1</p> | <p>Rounding to ± 1.45</p> |
| | <p>B1</p> | <p>$\frac{20 - \mu}{\mu/5}$ or $\frac{20 - 5\sigma}{\sigma}$ seen oe</p> |
| | <p>B1</p> | <p>[3] rounding to correct answer</p> |

Question 4

| | | | | |
|-------|--|----------------------|-----|---|
| 4 (a) | $P(y < 0) = P\left(z < \frac{0 - \mu}{\mu/2}\right)$ $= P(z < -2)$ $= 1 - 0.9772 = 0.0228$ | M1 A1 A1 | [3] | Standardising containing 0 (can be implied) and μ only $z < -2$ seen Correct answer |
| (b) | $P(x > 2.1) = 253/8000 = 0.031625$ $P(x < 2.1) = 0.968375 = \Phi(z)$ $z = 1.857 \text{ or } 1.858 \text{ or } 1.859 = \frac{2.1 - 2.04}{\sigma}$ $\sigma = 0.0323$ | M1 A1 M1 A1 | [4] | 1 - their 253/8000 used to obtain a z-value Rounded to 1.86 seen Solving for σ using their z val must be a z val Correct answer |

Question 5

| | | | |
|---|----------|---|----------------|
| $np = 350 \times 1/7 (= 50)$ $npq = 350 \times 1/7 \times 6/7 (= 42.857)$ | B1 M1 | Correct unsimplified np and npq standardising, with or without cc, must have sq rt | |
| $P(x = 47) = P\left(z > \frac{46.5 - 50}{\sqrt{42.857}}\right) =$ | M1 M1 | continuity correction 46.5 or 47.5 correct area ie > 0.5 must be a Φ | |
| $P(z > -0.5346)$ $= 0.704$ | A1 | [5] | correct answer |

Question 6

| | | |
|---|----------------------|---|
| <p>(a) $P(X < q + 82) = 0.72$ $z = 0.583$ $\frac{\pm q}{7.4} \text{ or } \frac{\pm 2q}{7.4} = z \text{ or probability (o.e.)}$ $q = 4.31$</p> | M1 M1 A1 | Rounding to ± 0.58 or ± 0.15 seen Standardising, no cc, no sq, no sq rt 3 correct answer |
| <p>(b) $\frac{0.5\mu - \mu}{\sigma} = \frac{\pm 0.5\mu}{\sigma}$ $\frac{0.2\sigma^2}{\sigma} = -0.2\sigma = -0.580$ $\sigma = 2.90$ $\mu = 3.36$</p> | M1 B1 M1 A1 | Standardising attempt some μ/σ allow cc, sq rt, sq Can be implied ± 0.580 seen (accept ± 0.58) substituting to eliminate μ or σ , arriving at numerical solution, any z value or probability – not dependent 4 both answers correct, accept 2.9 |

Question 7

2

$$P(13.6 < X < 14.8) = P\left(\frac{13.6-14}{0.52} < z < \frac{14.8-14}{0.52}\right)$$

$$\begin{aligned} &= P(-0.7692 < z < 1.538) \\ &= \Phi(1.538) - [1 - \Phi(0.7692)] \\ &= 0.9380 - [1 - 0.7791] \\ &= 0.7171 \end{aligned}$$

$$P(8) = (0.7171)^8 (0.2829)^2 {}_{10}C_8$$

$$= 0.252$$

| | |
|----|---|
| M1 | Standardising 1 expression, no cc, no sq rt, no sq, ±, mean on num. |
| M1 | $\Phi_1 + \Phi_2 - 1$ (indep) oe ($\Phi_2 - \Phi_1$ if cc used) |
| A1 | Correct probability rounding to 0.72 here |
| M1 | Binomial expression ${}_{10}C_8 p^8 q^2$, $\Sigma p + q = 1$, any p |
| A1 | 5 Correct answer (rounding to 0.252) |

Question 8

(i) $P(4, 5, 6) = (0.22)^4 (0.78)^4 {}_8C_4 + (0.22)^5 (0.78)^3 {}_8C_5 + (0.22)^6 (0.78)^2 {}_8C_6$

$$= 0.0763$$

(ii) prob = 0.13
mean = $300 \times 0.13 = 39$
var = $300 \times 0.13 \times 0.87 = 33.93$

$$P(30 < x < 50) = P\left(\frac{30.5 - 39}{\sqrt{33.93}} < z < \frac{49.5 - 39}{\sqrt{33.93}}\right)$$

$$\begin{aligned} &= P(-1.4592 < z < 1.8026) \\ &= \Phi(1.8026) + \Phi(1.4592) - 1 \\ &= 0.9643 + 0.9278 - 1 = 0.892 \end{aligned}$$

| | |
|------------|---|
| M1 | Bin term with ${}_8C_r p^r (1-p)^{8-r}$ |
| M1 | seen $r \neq 0$ any $p < 1$ |
| A1 | Summing 2 or 3 bin probs $p = 0.22$, $n = 8$ |
| [3] | Correct answer |
| B1 | Correct prob can be implied |
| B1ft | Correct unsimplified np and npq ft wrong 0.13 |
| M1 | Standardising a value need sq rt |
| M1 | Cont correction 30.5 / 31.5 or 48.5/49.5 only |
| M1 | Correct area $\Phi_1 + \Phi_2 - 1$ oe |
| A1 | Rounding to correct answer SC $P(31, \dots, 49) = {}_{300}C_{31} (0.13)^{31} (0.87)^{269} + \dots + {}_{300}C_{49}$ etc.) B1B1 |
| [6] | |

Question 9

(i) $z = 0.878$
 $\frac{190 - 160}{\sigma} = 0.878$
 $\sigma = 34.2$

(ii) $P(\text{at least } 1) = 1 - P(0)$

$$= 1 - (0.81)^{12} = 0.920$$

| | |
|----|---|
| B1 | $\pm 0.878, 0.88$, rounding to 0.88 seen |
| M1 | $(190 - 160)/\sigma = \text{something}$ |
| A1 | [3] Correct answer |
| M1 | Using $1 - P(0)$, $1 - P(0, 1)$, $P(1, 2 \dots 12)$ or $P(2, \dots 12)$ with $p = 0.19$ or 0.81 , terms must be evaluated to get the M1 |
| A1 | [2] Correct answer accept 0.92 |

Question 10

$$P(x < -2.4) = P\left(z < \frac{-2.4 - 1.5}{3.2}\right)$$

$$= P(z < -1.219)$$

$$= 1 - 0.8886$$

$$= 0.111$$

M1

Standardising no cc can have sq

M1

Correct area, i.e. < 0.5

A1

[3] Correct answer rounding to 0.111

Question 11

(i) $z = -1.406$

$$\frac{c - 14.2}{3.6} = -1.406$$

$$c = 9.14$$

B1

Rounding to ± 1.41 seen

M1

Standardising allow sq rt no cc

A1

3 Correct answer

(ii) $P\left(\frac{15 - 14.2}{3.6} < z < \frac{16 - 14.2}{3.6}\right)$

$$= \Phi(0.5) - \Phi(0.222)$$

$$= 0.6915 - 0.5879$$

$$= 0.1036$$

M1

2 attempts at standardising no cc no sq rt

M1

Subt two Φ s (indep mark)

A1

Needn't be entirely accurate, rounding to 0.10

$$P(\text{at least } 2) = 1 - P(0, 1)$$

$$= 1 - (0.8964)^7 - (0.8964)^6(0.1036)$$

$$= 1 - 0.8413$$

M1

Binomial term with ${}^7C_r p^r (1-p)^{7-r}$ seen $r \neq 0$ any $p < 1$

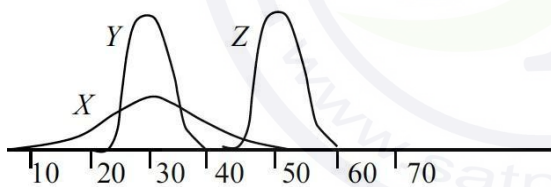
M1

$1 - P(0), 1 - P(1), 1 - P(0, 1)$ seen their p

A1

6 Correct answer accept 3sf rounding to 0.16

Question 12



B1

X mean at 30, roughly from 10 to 50 or 15 - 45

B1

Y same mean as X but higher and thinner

B1ft

3

Z same shape as Y but mean at 50 ft wrong Y

Question 13

(i) $z = -1.282$

B1

Rounding to ± 1.28 seen

$$-1.282 = \frac{t - 6.5}{1.76}$$

M1

Standardising, no cc, no sq or sq rt, $z \neq \pm 0.9, \pm 0.1$

$$t = 4.24$$

A1

3

Correct answer, accept 4.25

(ii) $P(z < 1) = 0.8413$

M1

$z = 1$ used to find a probability

$$P(\text{within 1sd of mean}) = 2\Phi - 1$$

$$= 0.6826$$

B1

correct prob, accept answer rounding to 0.66, 0.67, 0.68, not from wrong working. If quoted, then implies first M1.

$$P(8, 9)$$

$$= {}^9C_8 (0.6826)^8 (0.3174) + (0.6826)^9$$

M1

Binomial term $p^r (1-p)^{9-r} C_r$, 9C_r must be seen Binomial expression for $P(8) + P(9)$, any p

M1

$$= 0.167$$

A1

5

Correct ans

Question 14

| | | | |
|---|----------|----------|--|
| (i) $np = 252 \times 1/7 = 36,$ $npq = 252 \times 1/7 \times 6/7 = 30.857$ | B1 | | Unsimplified 36 and 30.857 seen, oe |
| $P\left(z < \left(\frac{29.5 - 36}{\sqrt{30.857}}\right)\right) + P\left(z > \left(\frac{44.5 - 36}{\sqrt{30.857}}\right)\right)$ | M1 M1 | | any standardising, sq rt needed any continuity correction either 29.5, 30.5, 43.5, 44.5 |
| $= P(z < -1.170) + P(z > 1.530)$ | | | |
| $= 1 - 0.8790 + 1 - 0.9370$ | M1 | | correct area $2 - (\Phi_1 + \Phi_2)$ |
| $= 0.184$ | A1 | 5 | correct answer |
| <hr/> | | | |
| (ii) np and nq are both > 5 | B1 | 1 | must have both |

Question 15

| | | | |
|---|----|----------|---|
| (i) $z = -0.842$ | B1 | | \pm rounding to 0.84 seen |
| $P(x > 1.35) = P\left(z > \frac{1.35 - 1.9}{\sigma}\right)$ | M1 | | $\pm \frac{1.35 - 1.9}{\sigma} =$ a prob or a z-value NOT 0.8 or 0.2 allow a 1-... |
| $-0.842 = -0.55/\sigma$ | | | |
| $\sigma = 0.653$ | A1 | 3 | Correct answer from correct working |
| <hr/> | | | |
| (ii) $P(x < 2) = P\left(z < \frac{2 - 1.9}{0.6532}\right)$ | M1 | | \pm standardising no continuity correction their σ |
| $= P(z < 0.1531)$ | | | |
| $= 0.561$ | A1 | 2 | Correct answer |
| <hr/> | | | |
| (iii) $X \sim N(160, 32)$ | B1 | | Unsimplified 160 and 32 seen |
| $P(162.5 < x < 173.5) =$ | | | |
| $P\left(\frac{162.5 - 160}{\sqrt{32}} < z < \frac{173.5 - 160}{\sqrt{32}}\right)$ | M1 | | Standardising need sq rt |
| $P(0.442 < z < 2.386)$ | M1 | | Any of 162.5, 163.5, 172.5, 173.5 seen |
| $= \Phi(2.386) - \Phi(0.442)$ | M1 | | $\Phi_2 - \Phi_1$ oe |
| $= 0.9915 - 0.6707$ | A1 | | One correct Φ to 3sf |
| $= 0.321$ | A1 | 6 | Correct answer accept 0.320 |

Question 17

$$1.751 = \frac{12 - \mu}{\sigma}$$

$$0.468 = \frac{9 - \mu}{\sigma}$$

$$\sigma = 2.34$$

$$\mu = 7.91$$

B1

Rounding to ± 1.75 seen

B1

± 0.468 seen

M1

An eqn with a z-value, μ and σ no $\sqrt{\sigma}$, no σ^2

M1

Sensible attempt to eliminate μ or σ by substitution or subtraction, need a value

A1

5

correct answers

Question 18

$$P(21.6 < x < 28.7)$$

$$= P\left(\left(\frac{21.6 - 24}{4.7}\right) < z < \left(\frac{28.7 - 24}{4.7}\right)\right)$$

$$= P(-0.5106 < z < 1) = \Phi(1) - \Phi(-0.5106)$$

$$= 0.8413 - (1 - 0.6953)$$

$$= 0.537 \text{ (0.5366)}$$

M1

Standardising; no cc, no sq rt

A1

One rounding to $\Phi(0.841$ or $0.695)$

M1

$\Phi_1 + \Phi_2 - 1$

A1

4

Correct answer

Question 19

(i) $P(< 1.2) = P\left(z < \frac{1.2 - 1.9}{0.55}\right) = P(z < -1.2727)$

$$= 1 - \Phi(1.273) = 1 - 0.8986$$

$$= 0.1014$$

$$P(> 2.5) = P\left(z < \frac{2.5 - 1.9}{0.55}\right) = P(z > 1.0909)$$

$$= 1 - \Phi(1.0909) = 1 - 0.8623$$

$$= 0.138$$

$$P(1.2 < wt < 2.5) = 1 - 0.101 - 0.138$$

$$= 0.761$$

M1

Standardising for wt 1.2 or 2.5, no cc, sq, sq rt
May be awarded in (ii) if not attempted in (i)
Accept 0.102

A1

First correct proportion seen

A1

Second correct proportion seen

M1

Third proportion 1 - their previous 2 proportions or correct attempt for remaining proportion

A1 \checkmark **5**

Correct answer or 1 - their 2 previous correct proportions

(ii) $P(x > k) = 0.8 + 0.1377 = 0.9377$

$$z = -1.536$$

$$-1.536 = \frac{k - 1.9}{0.55}$$

$$k = 1.06$$

M1

Valid method to obtain $P(x > k)$ or $P(x < k)$

A1

± 1.536 seen accept 3sf rounding to 1.53 or 1.54

M1

Attempt to solve equation with their 'correct' area z value, k, 1.9 and 0.55

A1

4

Correct answer or rounding to 1.05

Question 19

$$\frac{z = -2.326}{\frac{250 - 260}{\sigma} = -2.326}$$

$$\sigma = 4.30$$

| | |
|----|--|
| B1 | ± 2.325 to ± 2.33 seen |
| M1 | Standardising and = or < their z, no cc, sq, sq rt |
| A1 | 3 Correct ans |

Question 20

(i) $P(4, 5, 6) = (0.75)^4(0.25)^4 \times {}^8C_4 + (0.75)^5(0.25)^3 \times {}^8C_5 + (0.75)^6(0.25)^2 \times {}^8C_6$

$$= 0.606$$

| | |
|----|---|
| M1 | Bin term $p^r(1-p)^{8-r} \times {}^8C_r$ seen any p |
| M1 | Correct unsimplified answer |
| A1 | 3 Correct ans |

(ii) $np = 160 \times 0.75 = 120$ $npq = 30$

$$P(> 114) = P\left(z > \left(\frac{114.5 - 120}{\sqrt{30}}\right)\right)$$

$$= P(z > -1.004)$$

$$= \Phi(1.004) = 0.842$$

| | |
|----|--|
| B1 | Unsimplified mean and var correct |
| M1 | Standardising, need sq rt |
| M1 | Cont correction either 114.5 or 113.5 |
| M1 | Correct area consistent with their working |

(iii) np and nq both > 5

| | |
|----|----------------------|
| A1 | 5 Correct ans |
| B1 | 1 Need both |

Question 21

(a) (i) $P(x < 8) = P\left(z < \frac{8 - 7.15}{0.88}\right)$

$$= \Phi(0.9659)$$

$$= 0.833$$

| | |
|----|--|
| M1 | Standardising \pm , no cc no sq rt no sq |
| A1 | 2 Correct answer |

(ii) $z = 0.674$

$$\frac{q - 7.15}{0.88} = 0.674$$

$$q = 7.74$$

| | |
|----|---|
| B1 | Accept ± 0.674 or 0.675 only |
| M1 | Standardised eqn = \pm their z-value, allow sq or sq rt if already penalised in (i) |
| A1 | 3 Correct answer |

(b) $P(Y > 4\mu) = P\left(z > \left(\frac{4\mu - \mu}{(3\mu/2)}\right)\right) = P(z > 2)$

$$= 1 - 0.9772$$

$$= 0.0228$$

| | |
|----|---|
| M1 | Standardising no sq rt, no cc, no sq, one variable |
| A1 | $z = \pm 2$ seen |
| A1 | 3 correct ans SR B1 if made-up values used and 0.0228 obtained |

Question 22

| | | | | |
|-------|---|------|---|---|
| (i) | $z_1 = \frac{70 - 66.4}{5.6} = 0.6429$ | M1 | | Standardising one variable, no cc, no sq rt |
| | $z_2 = \frac{72.5 - 66.4}{5.6} = 1.089$ | M1 | | Correct area $\Phi_2 - \Phi_1$ |
| | $\Phi(1.089) - \Phi(0.643) = 0.8620 - 0.7399$ $= 0.1221$ | A1 | | Correct answer rounding to 0.12 |
| | $0.1221 \times 250 = 30.5$ | M1 | | Mult by 250 |
| | 30 or 31 sheep | A1ft | 5 | Correct answer ft their 0.1221 |
| (ii) | $66.4 - 59.2 = 7.2$ | M1 | | Subt from 66.4 |
| | $66.4 + 7.2 = 73.6$ | A1 | 2 | Correct answer |
| (iii) | $z = 0.674$ | B1 | | ± 0.674 or 0.675 seen |
| | $\frac{67.5 - \mu}{4.92} = 0.674$ | M1 | | Standardising with a z-value no cc no sq rt |
| | $\mu = 64.2$ | A1 | 3 | Correct answer |

Question 23

| | | | | |
|------|--|----------------|-----|---|
| (i) | $P(\text{large}) = 1 - \Phi\left(\frac{29 - 21.7}{6.5}\right)$ $= 1 - \Phi(1.123) = 1 - 0.8692$ $= 0.1308$ | M1 M1 A1 | | Standardising no cc no sq rt Correct area $1 - \Phi$ Rounding to 0.13 |
| | $P(0,1) = (0.8692)^8 + {}^8C_1(0.1308)(0.8692)^7$ | M1 M1 | | Any bin term with ${}^8C_x p^x (1-p)^{8-x}$ $0 < p < 1$ Summing bin $P(0) + P(1)$ only with $n = 8$, oe |
| | $= 0.718$ | A1 | [6] | Correct ans |
| (ii) | $= 1 - (0.8692)^n > 0.98$ | M1 | | eq/ineq involving their $(0.8692)^n$ or $(0.1308)^n$, 0.02 or 0.98 oe with or without a 1 |
| | $(0.8692)^n < 0.02$ | M1 | | solving attempt (could be trial and error) – may be implied by their answer |
| | Least number = 28 | A1 | [3] | correct answer |

Question 24

| | | | |
|--|----|-----|--|
| $\mu = 300 \times 0.072 = 21.6, \sigma^2 = 20.0448$ | B1 | | 300 \times 0.072 seen and |
| $P(x < 18) = P\left(z < \frac{17.5 - 21.6}{\sqrt{20.0448}}\right)$ | M1 | | 300 \times 0.072 \times 0.928 seen or implied ($\sigma = 4.4771, \sigma^2 = 20(.0)$) oe |
| $= P(z < -0.9157)$ | M1 | | \pm Standardising, their mean/var, with sq root |
| $= 1 - 0.8201$ | M1 | | Cont corr 17.5 or 18.5 |
| $= 0.180$ | A1 | [5] | Correct area $1 - \Phi$ Answer wrt 0.180, nfw |

Question 25

| | | |
|--|----------------|---|
| $z = 1.136$ $1.136 = \frac{195 - \mu}{22}$ $\mu = 170$ | B1 M1 A1 | ± 1.136 seen, not ± 1.14 , Standardising, no cc no sq rt, equated to their z not 0.128 or 0.872 Correct answer, nfw |
| [3] | | |

Question 26

| | | |
|--|------------------------------------|---|
| <p>(a) (i)</p> $\text{prob} = P\left(z < \frac{30 - 35.2}{4.7}\right)$ $= P(z < -1.106)$ $= 1 - 0.8655 = 0.1345$ $0.1345 \times 52 = 6.99$ | M1 M1 A1 A1 | Standardising no sq rt no cc no sq $1 - \Phi$ Correct ans rounding to 0.13 Correct final answer accept 6 or 7 if 6.99 not seen but previous prob 0.1345 correct |
| <p>(ii)</p> $\Phi(t) = 0.648 \quad z = 0.380$ $0.380 = \frac{t - 35.2}{4.7}$ $t = 37.0$ | B1 M1 A1 | 0.648 seen standardising allow cc, sq rt, sq, need use of tables not 0.148, 0.648, 0.352, 0.852 correct answer rounding to 37.0 |
| <p>(b)</p> $\frac{7 - \mu}{\sigma} = -0.8 \quad \text{so} \quad 7 - \mu = -0.8\sigma$ $\frac{10 - \mu}{\sigma} = 0.44 \quad \text{so} \quad 10 - \mu = 0.44\sigma$ $\mu = 8.94 \quad \sigma = 2.42$ | B1 B1 M1 M1 A1 | ± 0.8 seen ± 0.44 seen An eqn with z -value, μ and σ no sq rt no cc no sq Sensible attempt to eliminate μ or σ by subst or subtraction, need at least one value Correct answers |
| [5] | | |

Question 27

| | | |
|---|--|---|
| <p>(i)</p> $P(5, 6, 7) = {}^8C_5(0.68)^5(0.32)^3 + {}^8C_6(0.68)^6(0.32)^2 + {}^8C_7(0.68)^7(0.32)$ $= 0.722$ | M1 M1 A1 A1 | Binomial term ${}^8C_x p^x(1-p)^{8-x}$ seen $0 < p < 1$ Summing 3 binomial terms Correct unsimplified answer Correct answer |
| <p>(ii)</p> $np = 340, npq = 108.8$ $P(x > 337) = P\left(z > \frac{337.5 - 340}{\sqrt{108.8}}\right)$ $= P(z > -0.2396)$ $= 0.595$ | B1 M1 M1 M1 A1 | Correct (unsimplified) mean and var standardising with sq rt must have used 500 cc either 337.5 or 336.5 correct area (> 0.5) must have used 500 correct answer |
| [5] | | |
| <p>(iii)</p> $np(340) > 5 \text{ and } nq(160) > 5$ | B1 | [1] must have both or at least the smaller, need numerical justification |

Question 28

| | |
|--|---|
| $P(x < 3.273) = 0.5 - 0.475 = 0.025$ $z = -1.96$ $\frac{3.2 - \mu}{0.714} = -1.96$ $\mu = 4.60s$ | <p>M1 Attempt to find z-value using tables in reverse</p> <p>A1 ± 1.96 seen</p> <p>M1 Solving their standardised equation z-value not nec</p> <p>A1 [4] Correct ans accept 4.6</p> |
|--|---|

Question 29

| | |
|---|---|
| <p>(i) $P(0, 1, 2) =$ $(0.92)^{19} + {}^{19}C_1(0.08)(0.92)^{18} + {}^{19}C_2(0.08)^2(0.92)^{17}$ $= 0.809$</p> | <p>M1 Binomial term ${}^{19}C_x p^x (1-p)^{19-x}$ seen $0 < p < 1$</p> <p>M1 Correct unsimplified expression</p> <p>A1 3 Correct answer (no working SC B2)</p> |
| <p>(ii) $P(\text{at least } 1) = 1 - P(0)$ $= 1 - P(0.92)^n > 0.90$ $0.1 > (0.92)^n$ $n > 27.6$</p> <p>Ans 28</p> | <p>M1 Eqn with their 0.92^n, 0.9 or 0.1, 1 not nec</p> <p>M1 Solving attempt by logs or trial and error, power eqn with one unknown power</p> <p>A1 3 Correct answer, not approx., \approx, \geq, $>$, \leq, $<$</p> |
| <p>(iii) $np = 1800 \times 0.08 = 144$ $npq = 132.48$</p> $P(\text{at least } 152) = P\left(z > \left(\frac{151.5 - 144}{\sqrt{132.48}}\right)\right)$ $= P(z > 0.6516)$ $= 1 - 0.7429$ $= 0.257$ | <p>B1 correct unsimplified np and npq seen accept 132.5, 132, 11.5, awrt 11.51</p> <p>M1 standardising, with $\sqrt{\quad}$</p> <p>M1 cont correction 151.5 or 152.5 seen</p> <p>M1 correct area $1 - \Phi$ (probability)</p> <p>A1 5 correct answer</p> |
| <p>(iv) Use because 1800×0.08 (and 1800×0.92 are both) > 5</p> | <p>B1 1 $1800 \times 0.08 > 5$ is sufficient $np > 5$ is sufficient if clearly evaluated in (iii)</p> <p>If $npq > 5$ stated then award B0</p> |

Question 30

| | |
|--|---|
| <p>(i) $z = 1.127$ $1.127 = \frac{136-125}{\sigma}$ $\sigma = 9.76$</p> | <p>B1 ± 1.127 seen accept rounding to ± 1.13 M1 Standardising no cc no sq rt, with attempt at z A1 3 (not $\pm 0.8078, \pm 0.5517, \pm 0.13, \pm 0.87$) Correct ans</p> |
| <p>(ii) $P(131 < x < 141) = P\left(\frac{131-125}{9.76} < z < \frac{141-125}{9.76}\right)$ $= \Phi(1.639) - \Phi(0.6147)$ $= 0.9493 - 0.7307$ $= 0.2186$ Number = $0.2186 \times 170 = 37$ or 38 or awrt 37.2</p> | <p>M1 Standardising once with their sd, no $\sqrt{\quad}$, allow cc M1 Correct area $\Phi 2 - \Phi 1$ M1 Mult by 170, $P < 1$ A1 4 Correct answer, nfw</p> |

Question 31

| | |
|--|--|
| <p>(a) (i) $P(x > 3900) = P\left(z > \frac{3900 - 4520}{560}\right)$ $= P(z > -1.107) = \Phi(1.107)$ $= 0.8657$ Number of days = 365×0.8657 $= 315$ or 316 (315.98)</p> | <p>M1 Standardising no cc no sq rt no sq M1 Correct area Φ ie > 0.5 A1 Prob rounding to 0.866 B1 4 Correct answer ft their wrong prob if previous A0, $p < 1$, ft must be accurate to 3sf</p> |
| <p>(ii) $z = 1.165$ $1.165 = \frac{8000 - m}{560}$ $m = 7350$ (7347.6)</p> | <p>B1 ± 1.165 seen M1 Standardising eqn allow sq, sq rt, cc, must have z-value eg not 0.122, 0.878, 0.549, 0.810. A1 3 Correct answer rounding to 7350</p> |
| <p>(iii) $P(0, 1) = (0.878)^6 + {}^6C_1(0.122)^1(0.878)^5$ $= 0.840$ accept 0.84 Normal approx. to Binomial. M0, M0, A0</p> | <p>M1 Binomial term ${}^6C_x p^x (1-p)^{6-x}$ $0 < p < 1$ seen M1 Correct unsimplified expression A1 3 Correct answer</p> |
| <p>(b) $P(< 2\mu) = P\left(z > \frac{2\mu - \mu}{\sigma}\right) = P(z < 1.5)$ $= 0.933$</p> | <p>M1 Standardising with μ and σ M1 Attempt at one variable and cancel A1 3 Correct answer</p> |

Question 32

| | | | |
|-------|--|---|--|
| (i) | let $P(2, 4, 6) \text{ all} = p$ then $P(1, 3, 5) \text{ all} = 2p$ $3p + 6p = 1$ $p = 1/9$ so prob (3) = $2/9$ (0.222) | M1 M1 A1 [3] | Using $P(\text{even}) = 2P(\text{odd})$ or vice versa oe Summing $P(\text{odd} + \text{even})$ or $P(1, 2, 3, 4, 5, 6) = 1$ Correct answer |
| (ii) | $P(5, 5, 6) = 2/9 \times 2/9 \times 1/9 \times {}^3C_2$ $= 4/243$ (0.0165) | M1 M1 A1 [3] | Mult three probs together Mult by 3 oe ie summing 3 options Correct answer |
| (iii) | $\mu = 100 \times 1/3 = 33.3$, $\sigma = 100 \times 1/3 \times 2/3 = 22.2$ $P(x \leq 37) = P\left(z \leq \frac{37.5 - \frac{100}{3}}{\sqrt{\frac{200}{9}}}\right) = P(z \leq 0.8839)$ $= 0.812$ | B1 M1 M1 M1 A1 [5] | Unsimplified $100/3$ and $200/9$ seen Standardising need sq rt 36.5 or 37.5 seen correct area using their mean Correct answer |

Question 33

| | | | |
|------|---|--|---|
| (i) | $\bar{x} = 80 - 147/30 = 80 - 4.9$ $= 75.1$ $sd = \sqrt{\left(\frac{952}{30} - \left(\frac{147}{30}\right)^2\right)} = \sqrt{7.72\dots}$ $sd = 2.78$ | M1 A1 M1 A1 [4] | For $-147/30$ oe seen Correct answer $952/30 - (\pm \text{their coded mean})^2$ Correct answer |
| (ii) | $P(x > 160) = P\left(z > \frac{160 - 148.6}{18.5}\right)$ $= P(z > 0.616)$ $= 1 - 0.7310$ $= 0.269$ | M1 M1 A1 [3] | Standardising no cc no sq rt $1 - \Phi$ Correct answer |

Question 34

| | | |
|--|--|---|
| $\mu = 54.1$ $z = -1.11$ $-1.11 = \frac{50.9 - 54.1}{\sigma}$ $\sigma = 2.88$ | B1 B1 M1 A1 [4] | Stated or evaluated Accept rounding to ± 1.1 Standardising no cc no sq rt Correct answer |
|--|--|---|

Question 35

| | | |
|---|--|--|
| <p>(i) $z = -1.645$ $-1.645 = \frac{0.9 - m}{0.35}$ $m = 1.48$</p> | <p>B1 M1 A1</p> | <p>± 1.64 to 1.65 seen Standardising with a z-value accept $(0.35)^2$ Correct answer</p> |
| <p>(ii) $P(< 2) = P\left(z < \frac{2 - 1.476}{0.35}\right)$ $= P(z < 1.50)$ $= 0.933$ Prob $= (0.9332)^4$ $= 0.758$</p> | <p>M1 M1 A1 M1 A1</p> | <p>Standardising no sq, FT <i>their m</i>, no cc Correct area i.e. F Accept correct to 2sf here Power of 4, from attempt at $P(z)$ Correct answer</p> |
| <p>(iii) $P(t > 0.6\mu) = P\left(z > \frac{0.6\mu - \mu}{\mu/3}\right)$ $= P(z > -1.2)$ $= 0.885$</p> | <p>M1 M1 A1</p> | <p>Standardising attempt with 1 or 2 variables Eliminating μ or σ Correct final answer</p> |

Question 36

| | | |
|--|---|--|
| <p>(i) ${}^{12}C_8 (0.65)^8 (0.35)^4 + {}^{12}C_9 (0.65)^9 (0.35)^3 + {}^{12}C_{10} (0.65)^{10} (0.35)^2$ $= 0.541$</p> | <p>M1 M1 A1</p> | <p>Bin term with ${}^{12}C_r p^r (1-p)^{12-r}$ seen $r \neq 0$ any $p < 1$ Summing 2 or 3 bin probs $p = 0.65$ or 0.35, $n = 12$</p> |
| <p>(ii) $P(\overline{RRRR}) = 0.35 \times 0.35 \times 0.35 \times 0.65$ $= 0.0279$</p> | <p>M1 A1</p> | <p>Mult 4 probs either $(0.35)^3 (0.65)$ or $(0.65)^3 (0.35)$</p> |
| <p>(iii) $P(7) = 0.2039$ (unsimplified) Mean $= 250 \times 0.2039$ ($= 50.9798$) Var $= 250 \times 0.2039 \times (1 - 0.2039)$ ($= 40.5851$) $P(> 54) = P\left(\frac{54.5 - 50.9798}{\sqrt{40.5851}}\right)$ $= P(z > 0.5526)$ $= 1 - \Phi(0.5526) = 1 - 0.7098$ $= 0.290$</p> | <p>B1 B1 M1 M1 M1 A1</p> | <p>${}^{12}C_7 (0.65)^7 (0.35)^5$ Correct unsimplified np and npq using 'their 0.2039' but not 0.65 or 0.35 Standardising need sq rt – must be from working with 54 cc either 53.5 or 54.5 correct area < 0.5 i.e. $1 - \Phi$ - must be from working with 54</p> |

Question 37

| | | | |
|------|--|-----------|---|
| (i) | $z = 1.015$ $1.015 = \frac{70 - 69}{\sigma}$ $\sigma = 0.985 \text{ (200/203)}$ | B1 | Accept z between ± 1.01 and 1.02 |
| | | M1 | Standardising |
| | | A1 | [3] |
| (ii) | $58 + 9 = 67$ $P(> 67) = P\left(z > \frac{67 - 69}{0.9852}\right)$ $= P(z > -2.03)$ $= 0.9788$ 300×0.9788 $= 293.6 \text{ so } 293$ | M1 | 58 + 9 seen or implied (or 69-58 or 69-9) |
| | | M1 | Standardising $\pm z$ no cc allow their sd (must be +ve) |
| | | | Alt. 1 69-58 = 11, $P(>9) = P\left(z > \frac{9-11}{0.9852}\right)$ |
| | | | Alt. 2 69-9 = 60, $P(>58) = P\left(z > \frac{58-60}{0.9852}\right)$ |
| | | M1 | Correct prob area |
| | | M1 | Multiply their prob (from use of tables) by 300 |
| | | A1 | [5] – accept 293 or 294 from fully correct working |

Question 38

| | | | |
|-------|--|-----------|---|
| (i) | $P(x > 10.2) = P\left(z > \frac{10.2 - 9.5}{1.3}\right)$ $= P(z > 0.53846)$ $= 1 - 0.7046$ $= 0.295$ | M1 | Standardising allow cc, sq rt, sq |
| | | M1 | 1 – Φ final solution attempt |
| | | A1 | [3] |
| (ii) | $z = -1.282$ $-1.282 = \frac{t - 9.5}{1.3}$ $t = 7.83$ | B1 | \pm rounding to 1.28 seen |
| | | M1 | Standardising correctly can be $\pm z$ value here |
| | | A1 | [3] Correct answer from $z = -1.282$ only |
| (iii) | $P(x < 8.8) = 0.2954 \text{ by symmetry}$ $\text{Days} = 365 \times 0.2954$ $= 107 \text{ or } 108$ | B1 | oe method, FT <i>their 0.2954 from (i)</i> |
| | | M1 | Mult a probability <1 by 365 |
| | | A1 | [3] Correct answer (no decimals) |

Question 39

| | | | |
|------|--|--|---|
| (i) | 0.72 | B1 [1] | |
| (ii) | $np = 180 \times 0.72, npq = 180 \times 0.72 \times 0.28$ $X \sim N(129.6, 36.288)$ $P(x > 115) = P\left(z > \frac{115.5 - 129.6}{\sqrt{36.288}}\right)$ $= P(z > -2.341)$ $= 0.990$ | B1 [✓] M1 M1 M1 A1 [5] | $180 \times 0.72, 180 \times 0.72 \times 0.28$ seen, their values or correct Standardising (\pm) must have sq rt cc either 115.5 or 114.5 seen Correct area, Φ from final answer attempt fully correct method |

Question 40

| | | | |
|-------|---|---|---|
| (i) | $P(x < 3.0) = P\left(z < \frac{3.0 - 2.6}{0.25}\right)$ $+ P(z < 1.6) = 0.945$ | M1 M1 A1 [3] | Standardising no sq rt no cc Correct area i.e. prob > 0.5 legit |
| (ii) | $X \sim B(500, 0.9452) \sim N(472.6, 25.898)$ $P\left(z > \frac{479.5 - 472.6}{\sqrt{25.89848}}\right) = P(z > 1.3558)$ $= 1 - 0.9125 = 0.0875$ | M1 M1 M1 M1 A1 [5] | $500 \times '0.9452'$ and $500 \times '0.9452' \times ('1 - 0.9452')$ seen oe Standardising must have sq rt. All M marks indep cc either 479.5 or 480.5 seen correct area i.e. < 0.5 |
| (iii) | 500×0.9452 and $500 \times (1 - 0.9452)$ are both > 5 | B1 [✓] [1] | must see at least $500 \times 0.0548 > 5$ oe ft their (i) accept $np > 5, nq > 5$ if both not $npq > 5$ |

Question 42

| | | | | |
|-------|---|------------------------------------|-----|---|
| (i) | $P(2) = {}^7C_2(0.1)^2(0.9)^5$ $= 0.124$ | M1 A1 | [2] | Bin term ${}^7C_2p^2(1-p)^5$ $0 < p < 1$ |
| (ii) | $(0.15)^1(0.1)^2(0.75)^2 \times 5!/2!2!$ $= 0.0253$ or $81/3200$ | M1 M1 A1 | [3] | Mult probs for options, $(0.15)^a(0.1)^b(0.75)^c$ where $a + b + c$ sum to 5 Mult by $5!/2!2!$ oe |
| (iii) | mean = 365×0.15 (= 54.75 or 219/4) Var = $365 \times 0.15 \times 0.85$ (= 46.5375 or 3723/80) $P(x > 44) = P\left(z > \frac{44.5 - 54.75}{\sqrt{46.5375}}\right)$ $= P(z > -1.5025)$ $= 0.933$ | B1 M1 M1 M1 A1 | [5] | Correct unsimplified mean and var, oe \pm Standardising need sq rt cc either 44.5 (or 43.5) Φ Correct answer accept 0.934 |

Question 43

| | | | | |
|-------|--|----------------------|-----|---|
| (i) | $P(\text{small}) = P\left(z < \frac{95 - 150}{50}\right)$ $= P(z < -1.1)$ $= 1 - 0.8643$ $= 0.136$ | M1 M1 A1 | [3] | \pm standardising using 95, no cc, no sq, no sq rt $1 - \Phi$ (in final answer) |
| (ii) | $z = 1.282$ $1.282 = \frac{x - 150}{50}$ $x = 214$ g | B1 M1 A1 | [3] | \pm rounding to 1.28 Standardised eqn in their z allow cc |
| (iii) | $P(\text{small}) = 0.1357$, $P(\text{large}) = 0.1357$ symmetry $P(\text{medium}) = 1 - 0.1357 \times 2 = 0.7286$ AG | B1 | [1] | Correct answer legit obtained |
| (b) | Expected cost per banana = $0.1357 \times 10 + 0.1357 \times 25 + 0.7286 \times 20 = 19.3215$ cents Total cost of 100 bananas $= 1930$ (cents) (\$19.30) | *M1 DM1 A1 | [3] | Attempt at multiplying each 'prob' by a price and summing Mult by 100 |

Question
44

| | | | |
|-------|--|----|---|
| (i) | $P(< 4.5) = P\left(z < \frac{4.5 - 4.2}{0.6}\right) = P(z < 0.5)$ | M1 | Standardising once no cc no sq no sq rt |
| | $= 0.6915$ | | |
| | $P(< 3.5) = P\left(z < \frac{3.5 - 4.2}{0.6}\right) = P(z < -1.167)$ | M1 | |
| | $= 1 - 0.8784 = 0.1216$ | | $\Phi_1 - (1 - \Phi_2)$ [$P_1 - P_2$, $1 > P_1 > 0.5$, $0.5 > P_2 > 0$] oe |
| | $0.6915 - 0.1216 = 0.570$ | A1 | [3] |
| (ii) | $z = 1.175$ | B1 | ± 1.17 to 1.18 seen |
| | $1.175 = \frac{t - 4.2}{0.6}$ | M1 | Standardising no cc, allow sq, sq rt with z - value (not ± 0.8106 , 0.5478 , 0.4522 , 0.1894 , 0.175 etc.) |
| | $t = 4.91$ | A1 | [3] Correct answer from $z = 1.175$ seen (4sf) |
| (iii) | $(0.88)^n < 0.003$ | M1 | Inequality or eqn in 0.88 , power correctly placed using n or $(n \pm 1)$, 0.003 or $(1 - 0.003)$ oe |
| | $n > \lg(0.003)/\lg(0.88)$ | M1 | Attempt to solve by logs or trial and error (may be implied by answer) |
| | $n > 45.4$ | A1 | Correct integer answer |
| | $n = 46$ | | [3] |

Question 45

| | | | |
|------|---|----|---|
| (i) | Bin (7, 0.8) | M1 | ${}^7C_n p^n (1-p)^{7-n}$ seen |
| | $P(6, 7) = {}^7C_6 (0.8)^6 (0.2)^1 + (0.8)^7$ | M1 | |
| | $= 0.577$ | A1 | |
| | | | [3] Correct unsimplified expression for $P(6, 7)$ |
| (ii) | mean = $100 \times 0.2 = 20$ | B1 | Correct unsimplified mean and var |
| | Var = $100 \times 0.2 \times 0.8 = 16$ | | |
| | $P(\text{at most } 30) = P\left(z < \frac{30.5 - 20}{\sqrt{16}}\right)$ | M1 | Standardising must have sq rt, their μ , variance cc either 29.5 or 30.5 |
| | $= P(z < 2.625)$ | M1 | Correct area Φ , from final process |
| | $= 0.996$ | A1 | [5] |

Question 46

| | | | |
|-------|---|-----------------|---|
| (i) | $P(< 1) = P\left(z < \frac{1 - 1.04}{0.017}\right) = P(z < -2.353)$ | M1 | Standardising no cc, no \sqrt or sq |
| | $= 1 - 0.9907$ | M1 | |
| | $= 0.0093$ | A1 | |
| | | | [3] $1 - \Phi$ (final process) |
| (ii) | expected number $1000 \div 1.04 = 961$ or 962 | B1 | [1] Or anything in between |
| (iii) | $z = -1.765$ | B1 | ± 1.76 to 1.77 |
| | $-1.765 = \frac{1 - \mu}{0.017}$ | M1 | Standardising must have a z - value, allow \sqrt or sq |
| | $= 1.03$ | A1 | [3] |
| (iv) | expected number = $1000 \div 1.03 = 971$ or 970 | B1 [✓] | [1] Or anything in between, ft their (iii) |

Question

47

| | | |
|----------------------------|-----------|--------------------------------------|
| $z = 0.674$ | M1 | ± 0.674 seen |
| $0.674 = \frac{k - 20}{7}$ | M1 | Standardising no cc, no sq, no sq rt |
| $k = 24.7$ | A1 | [3] |

Question 48

| | | | |
|---------|--|------------|--|
| (a)(i) | $0.674 = \frac{8.8 - \mu}{\sigma} \Rightarrow 0.674\sigma = 8.8 - \mu$ | B1 | ± 0.674 seen |
| | $-0.935 = \frac{7.7 - \mu}{\sigma} \Rightarrow -0.935\sigma = 7.7 - \mu$ | B1 | ± 0.935 seen (condone ± 0.934) |
| | | M1 | An eqn with a z -value, μ and σ allow sq rt, sq cc |
| | | M1 | sensible attempt to eliminate μ or σ by substitution or subtraction |
| | $\sigma = 0.684$ $\mu = 8.34$ | A1 | correct answers (from -0.935) |
| | Total: | 5 | |
| (a)(ii) | $P(< 8.2) = P\left(z < \frac{8.2 - 7.9}{0.44}\right)$ | M1 | Standardising no cc no sq rt no sq |
| | | M1 | Correct area ie Φ , final solution |
| | $= P(z < 0.6818) = 0.7524$ | A1 | Correct prob rounding to 0.752 |
| | $P(3) = {}^5C_3 (0.7524)^3 (0.2476)^2$ | M1 | Binomial 5C_3 , powers summing to 5, any p , $\Sigma p = 1$ |
| | $= 0.261$ | A1 | |
| | Total: | 5 | |
| (b) | $P(< 1.5\mu) = P\left(z < \frac{1.5\mu - \mu}{\mu}\right) = P(z < 0.5)$ | *M1 | standardising with μ and σ (σ may be replaced by μ) |
| | | DM1 | just one variable |
| | $= 0.692$ | A1 | |
| | Total: | 3 | |

Question 49

| | | |
|---|-----------|---|
| $np = 160 \times 0.1$ (16) $npq = 160 \times 0.1 \times 0.9$ (14.4) | B1 | Correct unsimplified np and npq |
| $P(> 17) = P\left(z > \frac{17.5 - 16}{\sqrt{14.4}}\right) = P(z > 0.3953)$ | M1 | Standardising need $\sqrt{\quad}$ |
| | M1 | 16.5 or 17.5 seen in standardised eqn for continuity correction |
| $= 1 - 0.6536$ | M1 | Correct area from their mean ($1 - \Phi$), final solution |
| $= 0.346$ | A1 | |
| Total: | 5 | |

Question 50

| | | | |
|------|---|-----------|--|
| l(a) | $P(x > 0) = P\left(z > \pm \frac{0 - \mu}{\sigma}\right)$ $= P\left(z > \frac{-\mu}{\mu/1.5}\right) \text{ or } P\left(z > \frac{-1.5\sigma}{\sigma}\right)$ | M1 | \pm Standardising, in terms of μ and/or σ with 0 - in numerator, no continuity correction, no $\sqrt{\quad}$ |
| | $= P(z > -1.5)$ | A1 | Obtaining z value of ± 1.5 by eliminating μ and σ , SOI |
| | $= 0.933$ | A1 | |
| | Total: | 3 | |
| l(b) | $z = -1.151$ | B1 | $\pm z$ value rounding to 1.1 or 1.2 |
| | $-1.151 = \frac{70 - 120}{s}$ | M1 | \pm Standardising (using 70) equated to a z-value, no cc, no squaring, no $\sqrt{\quad}$ |
| | $\sigma = 43.4 \text{ or } 43.5$ | A1 | |
| | Totals: | 3 | |

Question 51

| | | |
|--|------------------------|---|
| $np = 270 \times 1/3 = 90, npq = 270 \times 1/3 \times 2/3 = 60$ | B1 | Correct unsimplified np and npq , SOI |
| $P(x > 100) = P\left(z > \frac{99.5 - 90}{\sqrt{60}}\right) = P(z > 1.2264)$ | M1 M1 | \pm Standardising using 100 need sq rt Continuity correction, 99.5 or 100.5 used |
| $= 1 - 0.8899$ | M1 | Correct area $1 - \Phi$ implied by final prob. < 0.5 |
| $= 0.110$ | A1 | |
| Total: | 5 | |

Question 52

| | | | |
|---------------|---|------------|--|
| i(i) | $(z =) \frac{4.2 - 3.9}{\sigma}$ | M1 | Standardising, not square root of σ , not σ^2 |
| | $z = 0.916 \text{ or } 0.915$ | B1 | Accept $0.915 \leq z \leq 0.916$ seen |
| | $\sigma = 0.328$ | A1 | Correct final answer (allow 20/61 or 75/229) |
| | Total: | 3 | |
| ii) | $z = 4.4 - 3.9/\text{their } 0.328 \text{ or } z = 3.4 - 3.9/\text{their } 0.328$ $= 1.5267 \quad = -1.5267$ | M1 | Standardising attempt with 3.4 or 4.4 only, allow square root of σ , or σ^2 |
| | $\Phi = 0.9364$ | A1 | $0.936 \leq \Phi \leq 0.937$ or $0.063 \leq \Phi \leq 0.064$ seen |
| | Prob = $2\Phi - 1 = 2(0.9364) - 1$ | M1 | Correct area $2\Phi - 1$ OE i.e. $\Phi = -(1 - \Phi)$, linked to final solution |
| | $= 0.873$ | A1 | Correct final answer from $0.9363 \leq \Phi \leq 0.9365$ |
| | Total: | 4 | |
| iii) | dividing (0.5) by a larger number gives a smaller z-value or more spread out as sd larger or use of diagrams | *B1 | No calculations or calculated values present e.g. $(\sigma =) 0.656$ seen Reference to spread or z value required |
| | Prob is less than that in (ii) | DB1 | Dependent upon first B1 |
| Total: | | 2 | |

Question 53

| | | | |
|----------|---|------------|--|
| (a)(i) | $z = 0.674$ | B1 | rounding to ± 0.674 or 0.675 |
| | $0.674 = \frac{6.8 - \mu}{0.25\mu}$ | M1 | standardising, no cc, no sq rt, no sq. σ may still be present on RHS |
| | | M1 | subst and sensible solving for μ must collect terms, no z -value needed can be 0.75 or 0.7734 need a value for μ |
| | $\mu = 5.82$ | A1 | |
| | Total: | 4 | |
| i(a)(ii) | $P(X < 4.7) = P\left(z < \frac{4.7 - 5.819}{1.4548}\right)$ | M1 | \pm standardising no cc, no sq rt, no sq unless penalised in (a)(i) |
| | $= \Phi(-0.769) = 1 - 0.7791$ | M1 | correct side for their mean i.e. $1 - \Phi$ (final solution) |
| | $= 0.221$ | A1 | |
| | Total: | 3 | |
| 6(b) | $P(< 15.75) = P\left(z < \frac{15.75 - 16}{0.2}\right) = 1 - P(z < 1.25) = 1 - 0.8944 = 0.1056$ and $P(> 16.25) = 0.1056$ by sym | *M1 | Standardising for 15.75 or 16.25 no cc no sq no sq rt unless penalised in (a)(i) or (a)(ii) |
| | $P(\text{usable}) = 1 - 0.2112 = 0.7888$ | B1 | $2\Phi - 1$ OE for required prob. (final solution) |
| | Usable rods = $1000 \times 0.7888 =$ | DM1 | Mult their prob by 1000 dep on recognisable attempt to standardise |
| | 788 or 789 | A1 | |
| | Total: | 4 | |

Question 54

| | | | |
|-------|--|------------|---|
| i(i) | $P(t > 6) = P\left(z > \frac{6 - 5.3}{2.1}\right) = P(z > 0.333)$ | M1 | Standardising, no continuity correction, no sq, no sq rt |
| | $= 1 - 0.6304$ | M1 | Correct area $1 - \Phi (< 0.5)$, final solution |
| | $= 0.370$ or 0.369 | A1 | |
| | 3 | | |
| (ii) | $z = 1.645$ | B1 | ± 1.645 |
| | $1.645 = \frac{x - 5.3}{2.1}$ | M1 | Standardising, no continuity correction, allow sq, sq rt. Must be equated to a z -value |
| | $x = 8.75$ or 8.755 or 8.7545 | A1 | |
| | 3 | | |
| (iii) | $n = 10, p = 0.05$ | M1 | Bin term ${}^{10}C_x p^x (1-p)^{10-x}$ |
| | $P(0, 1, 2) = (0.95)^{10} + {}^{10}C_1(0.05)(0.95)^9 + {}^{10}C_2(0.05)^2(0.95)^8$ | M1 | Correct unsimplified answer |
| | $= 0.988$ (0.9885 to 4 sf) | A1 | |
| | 3 | | |
| (iv) | $P(\text{misses bus}) = P(t < 0)$ | *M1 | Seeing t linked to zero |
| | $= P\left(z < \frac{0 - 5.3}{2.1}\right) = P(z < -2.524) = 1 - \Phi(2.524)$ | DM1 | Standardising with $t = 0$, no continuity correction, no sq, no sq rt |
| | $= 1 - 0.9942$ | | |
| | $= 0.0058$ | A1 | |
| | 3 | | |

Question 55

| | | | |
|-------|--|-----------|--|
| (i) | $P(> 65) = P\left(z > \frac{65 - 61.4}{12.3}\right) = P(z > 0.2927)$ | M1 | Standardising no continuity correction, no square or square root, condone \pm standardisation formula |
| | $= 1 - 0.6153 = 0.385$ | M1 | Correct area (< 0.5) |
| | | A1 | |
| (ii) | $P(< 65) = 0.6153$ so $P(< k) = 0.25 + 0.6153 = 0.8653$ | 3 | |
| | $z = 1.105$ | B1 | $z = \pm 1.105$ seen or rounding to 1.1 |
| | $1.105 = \frac{k - 61.4}{12.3}$ | B1 | standardising allow \pm , cc, sq rt, sq. Need to see use of tables backwards so must be a z -value, not $1 - z$ value. |
| | $k = 75.0$ | M1 | Answers which round to 75.0. Condone 75 if supported. |
| | | A1 | |
| (iii) | $2.326 = \frac{97.2 - \mu}{\sigma}$ | 4 | |
| | $-0.44 = \frac{55.2 - \mu}{\sigma}$ | B1 | ± 2.326 seen (Use of critical value) |
| | | B1 | ± 0.44 seen |
| | | M1 | An equation with a z -value, μ , σ and 97.2 or 55.2, allow $\sqrt{\sigma}$ or σ^2 |
| | | M1 | Algebraic elimination μ or σ from <i>their</i> two simultaneous equations |
| | $\mu = 61.9$ $\sigma = 15.2$ | A1 | both correct answers |
| | 5 | | |

Question 56

| | | | |
|-------|--|--------------|--|
| 5(i) | <i>EITHER:</i> $P(> 2) = 1 - P(0, 1, 2)$ | (M1) | Binomial term of form ${}^{30}C_x p^x (1-p)^{30-x}$, $0 < p < 1$ any p |
| | $= 1 - (0.96)^{30} - {}^{30}C_1(0.04)(0.96)^{29} - {}^{30}C_2(0.04)^2(0.96)^{28}$ ($= 1 - 0.2938\dots - 0.3673\dots - 0.2219\dots$) | A1 | Correct unsimplified answer |
| | $= 1 - 0.883103 = 0.117$ (0.116896) | A1) | |
| | <i>OR:</i> $P(> 2) = P(3, 4, 5, \dots, 30)$ | (M1) | Binomial term of form ${}^{30}C_x p^x (1-p)^{30-x}$, $0 < p < 1$ any p |
| | $= {}^{30}C_3(0.04)^3(0.96)^{27} + {}^{30}C_4(0.04)^4(0.96)^{26} + \dots + (0.04)^{30}$ | A1 | Correct unsimplified answer |
| | $= 0.117$ | A1) | |
| 5(ii) | $np = 280 \times 0.1169 = 32.73$, $npq = 280 \times 0.1169 \times 0.8831 = 28.9$ | 3 | |
| | $P(\geq 30) = P\left(z > \frac{29.5 - 32.73}{\sqrt{28.9}}\right) = P(z > -0.6008)$ | M1 FT | Correct unsimplified np and npq , FT their p from (i), |
| | | M1 | Substituting <i>their</i> μ and σ (\sqrt{npq} only) into the Standardisation Formula |
| | | M1 | Using continuity correction of 29.5 or 30.5 |
| | $= 0.726$ | M1 | Appropriate area Φ from standardisation formula $P(z > \dots)$ in final solution |
| | A1 | | |
| | 5 | | |

Question 57

| | | | |
|-------|---|-------------|--|
| (i) | $P(< 570) = P\left(z < \frac{570 - 500}{91.5}\right) = P(z < 0.7650)$ $= 0.7779$ | M1 | Standardising for either 570 or 390, no cc, no sq, no $\sqrt{\quad}$ |
| | $P(< 390) = P\left(z < \frac{390 - 500}{91.5}\right) = P(z < -1.202)$ | A1 | One correct z value |
| | $= 1 - 0.8853 = 0.1147$ | A1 | One correct Φ , final solution |
| | Large: 0.222 (0.2221) Small: 0.115 (0.1147) | A1 | Correct small and large |
| | Medium: 0.663 (0.6632) | A1FT | Correct Medium rounding to 0.66 or ft 1 - (their small + their large) |
| | | 5 | |
| (ii) | $1.645 = \left(\frac{x - 500}{91.5}\right)$ | B1 | ± 1.645 seen (critical value) |
| | | M1 | Standardising accept cc, sq, sq rt |
| | $x = 651$ | A1 | $650 \leq \text{Ans} \leq 651$ |
| | | 3 | |
| (iii) | $P(x > 610) = 0.1147$ (symmetry) | M1 | Attempt to find upper end prob $x > 610$ or $\Phi(x)$, ft their $P(< 390)$ from (i) |
| | $0.3 + 0.1147 = 0.4147 \Rightarrow \Phi(x) = 0.5853$ | M1 | Adding 0.3 to <i>their</i> $P(x > 610)$ or sub 0.5 from $\Phi(x)$ or $0.8853 - 0.3$ |
| | $z = 0.215$ or 0.216 | M1 | Finding $z = \Phi^{-1}(0.5853)$ |
| | $0.215 = \frac{k - 500}{91.5}$ | M1 | Standardising and solving, accept cc, sq, sq rt |
| | $k = 520$ | A1 | |
| | | 5 | |

Question 58

| | | | |
|-------|---|-----------|---|
| (i) | $P(4) + P(5) = {}^5C_4 \left(\frac{1}{4}\right)^4 \left(\frac{3}{4}\right)^1 + {}^5C_5 \left(\frac{1}{4}\right)^5 \left(\frac{3}{4}\right)^0$ | M1 | One binomial term, with $p < 1$, $n=5$, $p+q=1$ |
| | $= 0.014648.. + 0.00097656..$ | M1 | Add 2 correct unsimplified binomial terms |
| | $= 0.0156$ or $\frac{1}{64}$ | A1 | |
| | | 3 | |
| (ii) | $1 - P(0) > 0.995: 0.75^n < 0.005$ | M1 | Equation or inequality involving 0.75^n and 0.005 or 0.25^n and 0.995 |
| | $n \log 0.75 < \log 0.005$ $n > 18.4:$ | M1 | Attempt to solve <i>their</i> exponential equation using logs, or trial and error May be implied by their answer |
| | $n = 19$ | A1 | |
| | | 3 | |
| (iii) | $p = 0.25, n = 160$: mean = $160 \times 0.25 (= 40)$ variance = $160 \times 0.25 \times 0.75 (= 30)$ | B1 | Correct unsimplified mean and variance |
| | $P(X < 50) = P\left(Z < \frac{49.5 - 40}{\sqrt{30}}\right)$ | M1 | Use standardisation formulae must include square root. |
| | | M1 | Use continuity correction ± 0.5 (49.5 or 50.5) |
| | $= P(Z < 1.734) = 0.959$ | A1 | Correct final answer |
| | | 4 | |

Question 59

| | | | |
|------|---|-------------|--|
| (i) | $P(X > 410) = 225/6000 = 0.0375$ $P\left(Z > \frac{410 - 400}{\sigma}\right) = 0.0375: 0.9625$ | M1 | Use $1 - 225/6000 = 0.9625$ to find z value |
| | z value = ± 1.78 | A1 | z value: ± 1.78 |
| | $\frac{10}{\sigma} = 1.78$ | M1 | $(410 - 400)/\sigma = \text{their } z$ (must be a z value) |
| | $\sigma = 5.62$ | A1 | |
| | | 4 | |
| (ii) | We need $P(Z < -1.5)$ and $P(Z > 1.5)$ | M1 | Attempt at $P(Z < -1.5)$ or $P(Z > 1.5)$ $1 - \Phi(1.5)$ seen |
| | $\Phi(-1.5) + 1 - \Phi(1.5)$ $= 2 - 2\Phi(1.5)$ | M1 | Or equivalent expression with values |
| | $= 2 - 2 \times 0.9332 = 0.1336$ (0.134) | A1 | Correct to 3sf |
| | Number expected = 500×0.1336 $= 66.8$: 66 or 67 packets | B1ft | 0.1336 used or FT their 4sf probability times 500, (not 0.9625 or 0.0375) rounded or truncated |
| | | 4 | |

Question 60

| | | | |
|------|---|-------------|--|
| (i) | $z_1 = \pm \frac{4.1 - 5.7}{0.8} = -2$ $z_2 = \pm \frac{5 - 5.7}{0.8} = -0.875$ | M1 | At least one standardising no cc no sq rt no sq using 5.7 and 0.8 and either 4.1 or 5 |
| | $P(\text{Toffee Apple}) = P(d < 5.0) - P(d < 4.1)$ $= P(z < -0.875) - P(z < -2)$ $= \Phi(-0.875) - \Phi(-2)$ $= \Phi(2) - \Phi(0.875)$ | M1 | Correct area $\Phi - \Phi$ legitimately obtained – need 2 negative z -values or 2 positives – not one of each |
| | $= 0.9772 - 0.8092 = 0.168$ (or $0.1908 - 0.0228$) | A1 | Correct final answer |
| | Total: | 3 | |
| (ii) | $np = 250 \times 0.168 = 42$, $npq = 34.944$ | B1ft | Correct unsimplified mean and var – ft their prob for (i) providing ($0 < p < 1$) Implied by $\sigma = \sqrt{34.944} = 5.911$ |
| | $P(< 50) = P\left(z < \frac{49.5 - 42}{\sqrt{34.944}}\right) = P(z < 1.2687)$ | M1 | \pm Standardising using 50, their mean and sd; must have sq rt. |
| | $= \Phi(1.2687)$ | M1 | 49.5 or 50.5 seen as a cc |
| | $= 0.898$ | M1 | Correct area $\Phi(> 0.5$ for $+z$ and < 0.5 for $-z$) in their final answer |
| | | A1 | Correct final answer |
| | Total: | 5 | |

Question 61

| | | | |
|------|---|-----------|---|
| (i) | $z = 0.674$ | B1 | z value ± 0.674 |
| | $0.674 = \frac{0 - -3}{\sigma}$ | M1 | \pm Standardising with 0 and equating to a z-value |
| | $\sigma = 4.45$ | A1 | Correct answer www ie not ignoring a minus sign |
| | Total: | 3 | |
| (ii) | $P(0, 1)$ | M1 | Any bin of form ${}^8C_x(0.75)^x(0.25)^{8-x}$ any x |
| | $= (0.75)^8 + {}^8C_1(0.25)(0.75)^7$ | M1 | Correct unsimplified answer, may be implied by numerical values |
| | $0.1001 + 0.2670 = 0.367$ | A1 | Correct answer |
| | Method 2 | M1 | Any bin of form ${}^8C_x(0.75)^x(0.25)^{8-x}$ any x |
| | $1 - P(8, 7, 6, 5, 4, 3, 2) = 1 - (0.25)^8 - {}^8C_1(0.75)(0.25)^7 - \dots$ | M1 | Correct unsimplified answer |
| | $- {}^8C_2(0.75)^6(0.25)^2$ | A1 | Correct answer |
| | $= 0.367$ | | |
| | Total: | 3 | |

Question 62

| | | | |
|-------|---|-----------|--|
| (i) | Method 1 | M1 | Binomial expression of form ${}^{13}C_x(p)^x(1-p)^{13-x}$, $0 < x < 13$, $0 < p < 1$ |
| | $P(< 11) = 1 - P(11, 12, 13)$ | | |
| | $= 1 - {}^{13}C_{11}(0.6)^{11}(0.4)^2 - {}^{13}C_{12}(0.6)^{12}(0.4) - (0.6)^{13}$ | M1 | Correct unsimplified answer |
| | $= 0.942$ | A1 | CAO |
| | Method 2 | M1 | Binomial expression of form ${}^{13}C_x(p)^x(1-p)^{13-x}$, $0 < x < 13$, $0 < p < 1$ |
| | $P(< 11) = P(0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10)$ | | |
| | $= (0.4)^{13} + {}^{13}C_1(0.4)^{12}(0.6) + \dots + {}^{13}C_{10}(0.4)^3(0.6)^{10}$ | M1 | Correct unsimplified answer |
| | $= 0.942$ | A1 | CAO |
| | | 3 | |
| (ii) | $\mu = 130 \times 0.35 = 45.5$ var = $130 \times 0.35 \times 0.65 = 29.575$ | B1 | Correct unsimplified mean and var (condone $\sigma^2 = 29.6$, $\sigma = 5.438$) |
| | $P(\geq 50) = P\left(z > \frac{49.5 - 45.5}{\sqrt{29.575}}\right) = P(z > 0.7355)$ | M1 | Standardising, using $\pm \left(\frac{x - \text{their mean}}{\text{their } \sigma}\right)$, $x =$ value to standardise 49.5 or 50.5 seen in \pm standardisation equation |
| | $= 1 - \Phi(0.7355)$ | M1 | Correct final area |
| | $= 1 - 0.7691$ | M1 | |
| | $= 0.231$ | A1 | Correct final answer |
| (iii) | | 5 | |
| | $1 - (0.65)^n > 0.98$ or $0.02 > (0.65)^n$ | M1 | Eqn or inequality involving, 0.65^n and 0.02 or 0.35^n and 0.98 |
| | $n > 9.08$ | M1 | Attempt to solve their eqn or inequality by logs or trial and error |
| | $n = 10$ | A1 | CAO |
| | | 3 | |

Question 63

| | | | |
|------|---|-------------|---|
| (i) | $z = -1.282$ | B1 | ± 1.282 seen |
| | $-1.282 = \frac{440 - \mu}{9}$ | M1 | \pm Standardisation equation with 440, 9 and μ , equated to a z -value, (not $1 - z$ -value or probability e.g. 0.1841, 0.5398, 0.6202, 0.8159) |
| | $\mu = 452$ | A1 | Correct answer rounding to 452, not dependent on B1 |
| | | 3 | |
| (ii) | $P(z > 1.8) = 1 - 0.9641 = 0.0359$ | B1 | |
| | Number = 0.0359×150 $= 5.385$ | M1 | $p \times 150, 0 < p < 1$ |
| | (Number of cartons =) 5 | A1FT | Accept either 5 or 6, not indicated as an approximation, e.g. \sim , about FT their $p \times 150$, answer as an integer |
| | | 3 | |

Question 64

| | | | |
|------|--|-----------|---|
| (i) | $P(4, 5, 6) = {}^{15}C_4(0.22)^4(0.78)^{11} + {}^{15}C_5(0.22)^5(0.78)^{10} +$ | M1 | One binomial term ${}^{15}C_x p^x (1-p)^{15-x} \quad 0 < p < 1$ |
| | ${}^{15}C_6(0.22)^6(0.78)^9$ | A1 | Correct unsimplified expression |
| | $= 0.398$ | A1 | Correct answer |
| | | 3 | |
| (ii) | $\mu = 145 \times 0.22 = 31.9 \quad \sigma^2 = 145 \times 0.22 \times 0.78 = 24.882$ | B1 | Correct unsimplified mean and variance |
| | $P(x > 26) = P\left(z > \frac{26.5 - 31.9}{\sqrt{24.882}}\right) = P(z > -1.08255)$ | M1 | Standardising must have sq rt |
| | | M1 | 25.5 or 26.5 seen as a cc |
| | $= \Phi(1.08255)$ | M1 | Correct area Φ , must agree with their μ |
| | $= 0.861$ | A1 | Correct final answer accept 0.861, or 0.860 from 0.8604 not from 0.8599 |
| | 5 | | |

Question 65

| | | | |
|-----|---|-----------|--|
| (a) | $z_1 = 2.4$ | B1 | ± 2.4 seen accept 2.396 |
| | $z_2 = -0.5$ | B1 | ± 0.5 seen |
| | $2.4 = \frac{36800 - \mu}{\sigma}$ | M1 | Either standardisation eqn with z value, not 0.5082, 0.7565, 0.0082, 0.6915, 0.3085, 0.6209, 0.0032 or any other probability |
| | $-0.5 = \frac{31000 - \mu}{\sigma}$ | M1 | Sensible attempt to eliminate μ or σ by substitution or subtraction from their 2 equations (z -value not required), need at least 1 value stated |
| | $\sigma = 2000$ $\mu = 32000$ | A1 | Both correct answers |
| | 5 | | |
| (b) | $P(X < 3\mu) = P\left(z < \frac{3\mu - \mu}{(4\mu/3)}\right)$ or $P = \left(z < \frac{(9\sigma/4) - (3\sigma/4)}{\sigma}\right)$ | M1 | Standardise, in terms of one variable, accept σ^2 or $\sqrt{\sigma}$ |
| | $P\left(z < \frac{6}{4}\right)$ | M1 | $\frac{6}{4}$ or $\frac{6}{4\sigma}$ seen |
| | $= 0.933$ | A1 | Correct final answer |
| | | 3 | |

Question 66

| | | | |
|------|---|-----------|--|
| (i) | $z_1 = \pm \frac{90-120}{24} = -\frac{5}{4}, z_2 = \pm \frac{140-120}{24} = \frac{5}{6}$ | M1 | At least one standardisation, no cc, no sq rt, no sq using 120 and 24 and either 90 or 140 |
| | $= \Phi\left(\frac{20}{24}\right) - \Phi\left(-\frac{30}{24}\right)$ | A1 | -5/4 and 5/6 unsimplified |
| | $= \Phi(0.8333) - (1 - \Phi(1.25))$ $= 0.7975 - (1 - 0.8944)$ or $0.8944 - 0.2025 = 0.6919$ | M1 | Correct area $\Phi - \Phi$ legitimately obtained and evaluated from phi(their z_2) - phi (their z_1) |
| | $= 0.692$ AG | A1 | Correct answer obtained from 0.7975 and 0.1056 oe to 4sf or 0.6919 seen www |
| | | 4 | |
| (ii) | Method 1 | | |
| | Probability = $P(2, 3, 4)$ $= 0.692^2(1 - 0.692)^2 \times {}^4C_2 + 0.692^3(1 - 0.692) \times {}^4C_3 + 0.692^4$ | M1 | Any binomial term of form $4C_x p^x (1-p)^{4-x}, x \neq 0$ or 4 |
| | | B1 | One correct bin term with $n = 4$ and $p = 0.692$, |
| | $= 0.27256 + 0.40825 + 0.22931$ | M1 | Correct unsimplified expression using 0.692 or better |
| | $= 0.910$ | A1 | Correct answer |
| | Method 2: | | |
| | $1 - P(0, 1) =$ | M1 | Any binomial term of form $4C_x p^x (1-p)^{4-x}, x \neq 0$ or 4 |
| | $1 - 0.692^0(1 - 0.692)^4 \times {}^4C_0 - 0.692^1(1 - 0.692)^3 \times {}^4C_1$ | B1 | One correct bin term with $n = 4$ and $p = 0.692$ |
| | $= 1 - 0.00899 - 0.0808757$ | M1 | Correct unsimplified expression using 0.692 or better |
| | $= 0.910$ | A1 | Correct answer |
| | | 4 | |

Question 67

| | | | |
|-------|--|-----------|---|
| (i) | $P(X > 1800) = 0.96$, so $P(Z > \frac{1800-2000}{\sigma}) = 0.96$ | B1 | ± 1.75 seen |
| | $\Phi\left(\frac{200}{\sigma}\right) = 0.96$ $\frac{200}{\sigma} = 1.751$ | M1 | $z = \pm \frac{1800-2000}{\sigma}$, allow cc, allow sq rt, allow sq equated to a z-value |
| | $\sigma = 114$ | A1 | Correct final answer www |
| | | 3 | |
| (ii) | Mean = $300 \times 0.2 = 60$ and variance = $300 \times 0.2 \times 0.8 = 48$ | B1 | Correct unsimplified mean and variance |
| | $P(X < 70) = P(Z > \frac{69.5-60}{\sqrt{48}})$ | M1 | $Z = \pm \frac{x-their 60}{\sqrt{their 48}}$ |
| | $= \Phi(1.371)$ | M1 | 69.5 or 70.5 seen in an attempted standardisation expression as cc |
| | $= 0.915$ | A1 | Correct final answer |
| | | 4 | |
| (iii) | $np = 60, nq = 240$: both > 5 , (so normal approximation holds) | B1 | Both parts evaluated are required |
| | | 1 | |

Question 68

| | | | |
|----------|---|-------------|---|
| (a)(i) | $P(X < 4) = P\left(Z < \frac{4 - 3.24}{0.96}\right)$ | M1 | \pm Standardisation formula, no cc, no sq rt, no square |
| | $= P(Z < 0.7917) = 0.7858$ | A1 | $0.7855 < p \leq 0.7858$ or $p = 0.786$ Cao (implies M1A1 awarded), may be seen used in calculation |
| | <i>their</i> $0.7858 \times 365 = 286$ (or 287) | B1ft | <i>Their</i> probability $\times 365$ provided 4sf probability seen . FT answer rounded or truncated to nearest integer. No approximation notation used. |
| | | 3 | |
| (a)(ii) | $P(X < k) = P\left(Z < \frac{k - 3.24}{0.96}\right) = 0.8$ | B1 | $(z=) \pm 0.842$ seen |
| | $\frac{k - 3.24}{0.96} = 0.842$ | M1 | $z = \pm \frac{k - 3.24}{0.96}$, allow cc, sq rt or square equated to a z-value (0.7881, 0.2119, 0.158, 0.8, 0.2 etc. are not acceptable) |
| | $k = 4.05$ | A1 | Correct final answer, www |
| | | 3 | |
| (a)(iii) | $P(-1.5 < Z < 1.5) =$ | M1 | $\Phi(z = 1.5)$ or $\Phi(z = -1.5)$ seen used or $p = 0.9332$ seen |
| | $\Phi(1.5) - \Phi(-1.5) = 2\Phi(1.5) - 1$ $= 2 \times 0.9332 - 1$ oe | M1 | Correct final area expression using <i>their</i> probabilities |
| | $= 0.866$ | A1 | Correct final answer |
| | | 3 | |
| (b) | $P(Y > 0) = P\left(Z > \frac{0 - \mu}{\sigma}\right) \equiv P\left(Z > \frac{0 - \mu}{3\mu/4}\right)$ or $P\left(Z > \frac{0 - \left(\frac{4\sigma}{3}\right)}{\sigma}\right)$ | M1 | \pm Standardisation attempt in terms of one variable no sq rt or square, condone ± 0.5 as cc |
| | $= P(Z > -4/3)$ | A1 | Correct unsimplified standardisation, no variables |
| | $= 0.909$ | A1 | Correct final answer |
| | | 3 | |

Question 69

| | | | |
|-----|---|-----------|---|
| (a) | $P(X < 29.4) = P\left(Z < \frac{29.4 - 31.4}{\sqrt{3.6}}\right)$ | M1 | Standardise, no cc, must have sq rt. |
| | $= P(Z < -1.0541)$ | M1 | Obtain $1 - \text{prob}$ |
| | $= 1 - 0.8540$ | A1 | Correct final answer |
| | $= 0.146$ | 3 | |
| (b) | $P(X < 12) = \frac{42}{400} = 0.105$ and $P(X > 19) = \frac{58}{400} = 0.145$ | M1 | Eqn with μ, σ and a z-value. Allow cc, wrong sign, but not $\sqrt{\sigma}$ or σ^2 |
| | $\frac{12 - \mu}{\sigma} = -1.253$ | B1 | Any form with z value rounding to ± 1.25 |
| | $\frac{19 - \mu}{\sigma} = 1.058$ | B1 | Any form with z value rounding to ± 1.06 |
| | $12 - \mu = -1.253\sigma$ $19 - \mu = 1.058\sigma$ | M1 | Solve 2 equations in μ, σ eliminating to 1 unknown |
| | $7 = 2.307\sigma$ or $36.455 + 2.307\mu = 0$ oe | | |
| | $\mu = 15.8, \sigma = 3.03$ | A1 | Correct answers |
| | 5 | | |

Question 70

| | | | |
|-------|--|-----------|---|
| (i) | $1 - (P(7) + P(8) + P(9))$ $= 1 - ({}^9C_7 0.8^7 \times 0.2^2 + {}^9C_8 0.8^8 \times 0.2^1 + {}^9C_9 0.8^9 \times 0.2^0)$ | M1 | Any binomial term of form ${}^9C_x p^x (1-p)^{9-x}$, $x \neq 0$ |
| | | M1 | Correct unsimplified expression |
| | $= 1 - (0.3019899 + 0.3019899 + 0.1342177)$ $= 0.262$ | A1 | Correct answer |
| | | 3 | |
| (ii) | Mean = $200 \times 0.8 = 160$: var = $200 \times 0.8 \times 0.2 = 32$ | B1 | Both unsimplified |
| | $P(X > 166) = P\left(Z > \frac{166.5 - 160}{\sqrt{32}}\right)$ | M1 | Standardise, $z = \pm \frac{x - \text{their } 160}{\sqrt{\text{their } 32}}$ with square root |
| | | M1 | 166.5 or 165.5 seen in attempted standardisation expression |
| | $= P(Z > 1.149) = 1 - 0.8747$ | M1 | 1 - a Φ -value, correct area expression, linked to final answer |
| | $= 0.125$ | A1 | Correct final answer |
| | | 5 | |
| (iii) | $np = 160$, $nq = 40$: both > 5 (so normal approx. holds) | B1 | Both parts required |
| | | 1 | |

Question 71

| | | | |
|------|--|-----------|--|
| (i) | $P(X < 132) = P\left(Z < \frac{132 - 140}{12}\right) = P(Z < -0.6667)$ | M1 | Using \pm standardisation formula, no continuity correction, not σ^2 or $\sqrt{\sigma}$ |
| | $= 1 - 0.7477$ | M1 | Appropriate area Φ from standardisation formula $P(z < \dots)$ in final solution |
| | $= 0.252$ awrt | A1 | Condone linear interpolation = 0.25243 |
| | | 3 | |
| (ii) | $P(\text{time} > k) = 0.675$, $z = -0.454$ | B1 | ± 0.454 seen |
| | $\frac{k - 140}{12} = -0.454$ | M1 | An equation using the standardisation formula with a z-value (not $1 - z$), condone σ^2 or $\sqrt{\sigma}$ |
| | $k = 135, 134.6, 134.55$ | A1 | B0M1A1 max from -0.45 |
| | | 3 | |

Question 72

| | | | |
|------|---|-----------|---|
| (i) | $P(79 < X < 91) = P\left(\frac{79 - 85}{6.8} < Z < \frac{91 - 85}{6.8}\right)$ $= P(-0.8824 < Z < 0.8824)$ | M1 | Using \pm standardisation formula for either 79 or 91, no continuity correction |
| | $= \Phi(0.8824) - \Phi(-0.8824)$ $= 0.8111 - (1 - 0.8111)$ | M1 | Correct area ($\Phi - \Phi$) with one +ve and one -ve z-value or $2\Phi - 1$ or $2(\Phi - 0.5)$ |
| | $= 0.622$ | A1 | Correct answer |
| | | 3 | |
| (ii) | $z = -1.751$ | B1 | ± 1.751 seen |
| | $-1.751 = \frac{t - 85}{6.8}$ | M1 | An equation using \pm standardisation formula with a z-value, condone σ^2 or $\sqrt{\sigma}$ |
| | $t = 73.1$ | A1 | Correct answer |
| | | 3 | |

Question 73

| | | | |
|-------|--|-----------|---|
| (i) | $P(< 700) = P\left(z < \frac{700 - 830}{120}\right) = P(z < -1.083)$ | M1 | Using \pm standardisation formula, no continuity correction, not σ^2 or $\sqrt{\sigma}$ |
| | $= 1 - 0.8606$ | M1 | Appropriate area Φ from standardisation formula $P(z < \dots)$ in final probability solution. (<0.5 if z is $-ve$, >0.5 if z is $+ve$) |
| | $= 0.1394$ | A1 | Correct final probability rounding to 0.139 |
| | Expected number of female adults = $430 \times$ their 0.1394 $= 59.9$ So 59 or 60 | B1 | FT their 3 or 4 SF probability, rounded or truncated to integer |
| | | 4 | |
| (ii) | $P(\text{giraffe} < 830+w) = 95\%$ so $z = 1.645$ | B1 | ± 1.645 seen (critical value) |
| | $\frac{(830+w) - 830}{120} = \frac{w}{120} = 1.645$ | M1 | An equation using the standardisation formula with a z -value (not $1 - z$), condone σ^2 or $\sqrt{\sigma}$ not 0.8519, 0.8289 |
| | $w = 197$ | A1 | Correct answer |
| | | 3 | |
| (iii) | $P(\text{male} > 950) = 0.834$, so $z = -0.97$ | B1 | ± 0.97 seen |
| | $\frac{950 - 1190}{\sigma} = -0.97$ | M1 | Using \pm standardisation formula, condone continuity correction, σ^2 or $\sqrt{\sigma}$, condone equating with non z -value not 0.834, 0.166 |
| | $\sigma = 247$ | A1 | Condone $-\sigma = -247$. www. |
| | | 3 | |

Question 74

| | | | |
|------|--|-------------|---|
| (i) | $P(h < 148) = 0.67$ | B1 | $z = \pm 0.44$ seen |
| | $\frac{h - 148}{8} = 0.44$ | M1 | $z\text{-value} = \pm \frac{(h - 148)}{8}$ |
| | $151.52 \approx 152$ | A1 | CAO |
| | | 3 | |
| (ii) | $P(144 < X < 152) = P\left(\frac{144 - 148}{8} < Z < \frac{152 - 148}{8}\right)$ | M1 | Using \pm standardisation formula for either 144 or 152, $\mu = 148$, $\sigma = 8$ and no continuity correction, allow σ^2 or $\sqrt{\sigma}$ |
| | $= P\left(-\frac{1}{2} < Z < \frac{1}{2}\right) = 0.6915 - (1 - 0.6915) = 2 \times 0.6915 - 1$ | M1 | Correct final area legitimately obtained from $\text{phi}(\text{their } z_2) - \text{phi}(\text{their } z_1)$ |
| | $= 0.383$ | A1 | Final probability answer |
| | $0.383 \times 120 = 45.96$ Accept 45 or 46 only | B1FT | Their prob (to 3 or 4 sf) $\times 120$, rounded to a whole number or truncated |
| | | 4 | |

Question 75

| | | | |
|--------|---|-------------|--|
| (i)(a) | $P(0, 1, 2) = {}^6C_0 0.3^0 0.7^6 + {}^6C_1 0.3^1 0.7^5 + {}^6C_2 0.3^2 0.7^4$ | M1 | Binomial term of form ${}^6C_x p^x (1-p)^{6-x}$ $0 < p < 1$ any $p, x \neq 6, 0$ |
| | 0.1176 ... + 0.3025 ... + 0.3241 ... | A1 | Correct unsimplified answer |
| | 0.744 | A1 | Correct final answer |
| | | 3 | |
| (i)(b) | $P(\text{support neither choir}) = 1 - (0.3 + 0.45) = 0.25$ | M1 | 0.25^n seen alone, $1 < n \leq 6$ |
| | $P(6 \text{ support neither choir}) = 0.25^6$ $= 0.000244$ or $\frac{1}{4096}$ | A1 | Correct final answer |
| | | 2 | |
| 7(ii) | Mean = $240 \times 0.25 = 60$ Variance = $240 \times 0.25 \times 0.75 = 45$ | B1FT | Correct unsimplified $240p$ and $240pq$ where $p = \text{their } P(\text{support neither choir})$ or 0.25 |
| | $P(X < 50) = P\left(Z < \frac{49.5 - 60}{\sqrt{45}}\right) = P(Z < -1.565)$ | M1 | Substituting <i>their</i> μ and σ (condone σ^2) into the \pm Standardisation Formula with a numerical value for '49.5'. |
| | | M1 | Using continuity correction 49.5 or 50.5 within a standardisation expression |
| | $1 - 0.9412$ | M1 | Appropriate area Φ from standardisation formula $P(z < \dots)$ in final solution, (< 0.5 if z is -ve, > 0.5 if z is +ve) |
| | 0.0588 | A1 | Correct final answer |
| | | 5 | |

Question 76

| | | | |
|-------|---|-------------|---|
| (i) | $P(X < 45) = P\left(Z < \frac{45 - 40}{8}\right)$ $= P(Z < 0.625)$ | M1 | \pm Standardise, no continuity correction, σ^2 or $\sqrt{\sigma}$, formula must be seen |
| | 0.734(0) | A1 | CAO |
| | | 2 | |
| (ii) | $1 - 2(1 - (i)) = 2(i) - 1 = 2((i) - 0.5)$ | M1 | Use result of part (i) or recalculated to find area OE |
| | 0.468 | A1ft | $0 < \text{FT from (i)} < 1$ or correct. |
| | | 2 | |
| (iii) | $P(X < 10) = 48/500 = 0.096$ $z = -1.305$ | B1 | $z = \pm 1.305$ |
| | $P(X > 24) = 76/500 = 0.152$ $z = 1.028$ | B1 | $z = \pm 1.028$ |
| | $10 - \mu = -1.305\sigma$ $24 - \mu = 1.028\sigma$ | M1 | Form 1 equation using 10 or 24 with μ, σ, z -value. Allow continuity correction, not $\sigma^2, \sqrt{\sigma}$ |
| | $14 = 2.333\sigma$ | M1 | OE Solve two equations in σ and μ to form equation in one variable |
| | $\sigma = 6.[00], \mu = 17.8[3]$ | A1 | CAO, WWW |
| | | 5 | |

Question 77

| | | | |
|------|--|-----------|---|
| (i) | $P(8, 9, 10) = {}^{10}C_8 0.66^8 0.34^2 + {}^{10}C_9 0.66^9 0.34^1 + 0.66^{10}$ | M1 | Correct binomial term, ${}^{10}C_a 0.66^a (1-0.66)^b$ $a+b = 10, 0 < a, b < 10$ |
| | | A1 | Correct unsimplified expression |
| | 0.284 | B1 | CAO |
| | | 3 | |
| (ii) | $np = 0.66 \times 150 = 99$ $npq = 0.66 \times (1 - 0.66) \times 150 = 33.66$ | B1 | Accept evaluated or unsimplified μ, σ^2 numerical expressions, condone $\sigma = \sqrt{33.66} = 5.8017$ or 5.802 CAO |
| | $P(X > 84) = P\left(Z > \frac{84.5 - 99}{\sqrt{33.66}}\right)$ | M1 | \pm Standardise, $\frac{x - \text{their } 99}{\sqrt{\text{their } 33.66}}$, condone σ^2, x a value |
| | | M1 | 84.5 or 83.5 used in <i>their</i> standardisation formula |
| | $(= P(Z > -2.499))$ | M1 | Correct final area |
| | 0.994 | A1 | Final answer (accept 0.9938) SC if no standardisation formula seen, B2 $P(Z > -2.499) = 0.994$ |
| | | 5 | |

Question 78

| | | | |
|-------|--|-----------|---|
| (i) | $P(46 < X < 53) = P\left(\frac{46 - 49.2}{2.8} < Z < \frac{53 - 49.2}{2.8}\right)$ | M1 | Using \pm standardisation formula for either 46 or 53, no continuity correction, σ^2 or $\sqrt{\sigma}$ |
| | $P(-1.143 < Z < 1.357)$ | A1 | Both standardisations correct unsimplified |
| | $\Phi(1.357) + \Phi(1.143) - 1$ $= 0.9126 + 0.8735 - 1$ | M1 | Correct final area |
| | 0.786 | A1 | Final answer |
| | | 4 | |
| (ii) | $\frac{t - 49.2}{2.8} = -1.406$ | B1 | ± 1.406 seen |
| | | M1 | An equation using \pm standardisation formula with a z -value, condone σ^2 or $\sqrt{\sigma}$ |
| | 45.3 | A1 | |
| | | 3 | |
| (iii) | $P(X < 46) = 0.1265$ | M1 | Calculated or ft from (i) |
| | $P(2PB < 46) = 3(1 - 0.1265)0.1265^2$ | M1 | $3(1-p)p^2, 0 < p < 1$ |
| | 0.0419 | A1 | |
| | | 3 | |

Question 79

| | | | |
|-----|---|-----------|---|
| (a) | $P(X > 87) = P\left(Z > \frac{87-82}{\sigma}\right) = 0.22$ | M1 | Using \pm standardisation formula, not σ^2 , not $\sqrt{\sigma}$, no continuity correction |
| | $P\left(Z < \frac{5}{\sigma}\right) = 0.78$ $\left(\frac{5}{\sigma} = \right) 0.772$ | B1 | AWRT ± 0.772 seen B0 for ± 0.228 |
| | $\sigma = 6.48$ | A1 | |
| | | 3 | |
| (b) | $P\left(-\frac{4}{\sigma} < Z < \frac{4}{\sigma}\right) = P(-0.6176 < Z < 0.6176)$ | M1 | Using ± 4 used within a standardisation formula (SOI), allow σ^2 , $\sqrt{\sigma}$ and continuity correction |
| | | M1 | Standardisation formula applied to both <i>their</i> ± 4 |
| | $\Phi = 0.7317$ Prob = $2\Phi - 1 = 2(0.7317) - 1$ | M1 | Correct area $2\Phi - 1$ oe linked to final solution |
| | $= 0.463$ | A1 | |
| | | 4 | |

Question 80

| | | | |
|-----|--|--|--|
| (a) | $1 - P(6, 7, 8)$ $= 1 - ({}^8C_6 0.7^6 0.3^2 + {}^8C_7 0.7^7 0.3^1 + 0.7^8)$ | M1 | One term ${}^8C_x p^x (1-p)^{8-x}$, $0 < p < 1$, $x \neq 0$ |
| | $= 1 - 0.55177$ | A1 | Correct unsimplified expression, or better |
| | $= 0.448$ | A1 | |
| | Alternative method for question 5(a) | | |
| | $P(0, 1, 2, 3, 4, 5)$ $= 0.3^8 + {}^8C_1 0.7^1 0.3^7 + {}^8C_2 0.7^2 0.3^6 + {}^8C_3 0.7^3 0.3^5 + {}^8C_4 0.7^4 0.3^4 + {}^8C_5 0.7^5 0.3^3$ | M1 | One term ${}^8C_x p^x (1-p)^{8-x}$, $0 < p < 1$, $x \neq 0$ |
| | A1 | Correct unsimplified expression, or better | |
| | $= 0.448$ | A1 | |
| | | 3 | |
| (b) | Mean = $120 \times 0.7 = 84$ Var = $120 \times 0.7 \times 0.3 = 25.2$ | B1 | Correct mean and variance, allow unsimplified |
| | $P(\text{more than } 75) = P\left(z > \frac{75.5 - 84}{\sqrt{25.2}}\right)$ | M1 | Substituting <i>their</i> μ and σ into the \pm standardising formula (any number), not σ^2 , not $\sqrt{\sigma}$ |
| | | M1 | Using continuity correction 75.5 or 74.5 |
| | $P(z > -1.693)$ | M1 | Appropriate area Φ , from final process, must be a probability |
| | $= 0.955$ | A1 | Allow $0.9545 < p \leq 0.955$ |
| | 5 | | |

Question 81

| | | |
|-----|---|----|
| (a) | $P(X < 21) = P\left(z < \frac{21 - 15.8}{4.2}\right) = \Phi(1.238)$ | M1 |
| | 0.892 | A1 |
| | | 2 |
| (b) | $z = \pm 0.674$ | B1 |
| | $\frac{k - 15.8}{4.2} = 0.674$ | M1 |
| | 18.6 | A1 |
| | | 3 |

Question 82

| | | |
|-----|--|----|
| (a) | $\frac{1}{\frac{1}{4}} = 4$ | B1 |
| | | 1 |
| (b) | $\frac{9}{64} (= 0.141)$ | B1 |
| | | 1 |
| (c) | $P(X < 6) = 1 - \left(\frac{3}{4}\right)^5$ (FT their probability/mean from part (a)) | M1 |
| | 0.763 | A1 |
| | | 2 |
| (d) | Mean = $80 \times 0.25 = 20$ Var = $80 \times 0.25 \times 0.75 = 15$ | M1 |
| | $P(\text{more than } 25) = P\left(z > \frac{25.5 - 20}{\sqrt{15}}\right)$ | M1 |
| | $P(z > 1.42)$ | M1 |
| | $1 - 0.9222$ | M1 |
| | 0.0778 | A1 |
| | | 5 |

Question 83

| | | |
|-----|---|----|
| (a) | $P(X < 25) = P\left(z < \frac{25-40}{12}\right) = P(z < -1.25)P(X < 25) = P(z < -)$ | M1 |
| | 1 - 0.8944 | M1 |
| | 0.106 | A1 |
| | | 3 |
| (b) | 0.8944 divided by 3 (M1 for 1 - their (a) divided by 3) | M1 |
| | 0.298 AG | A1 |
| | | 2 |
| (c) | 0.2981 gives $z = 0.53$ | B1 |
| | $\frac{h-40}{12} = 0.53$ | M1 |
| | $h = 46.4$ | A1 |
| | | 3 |

Question 84

| | | |
|-----|---|----|
| (a) | $1 - P(10, 11, 12)$ $= 1 - [{}^{12}C_{10}0.72^{10}0.28^2 + {}^{12}C_{11}0.72^{11}0.28^1 + 0.72^{12}]$ | M1 |
| | $1 - (0.19372 + 0.09057 + 0.01941)$ | A1 |
| | 0.696 | A1 |
| | | 3 |
| (b) | $0.28^3 \times 0.72 = 0.0158$ | B1 |
| | | 1 |
| (c) | Mean = $100 \times 0.72 = 72$ Var = $100 \times 0.72 \times 0.28 = 20.16$ | M1 |
| | $P(\text{less than } 64) = P\left(z < \frac{63.5-72}{\sqrt{20.16}}\right)$ (M1 for substituting their μ and σ into \pm standardisation formula with a numerical value for '63.5') | M1 |
| | Using either 63.5 or 64.5 within a \pm standardisation formula | M1 |
| | Appropriate area Φ , from standardisation formula $P(z < \dots)$ in final solution $= P(z < -1.893)$ | M1 |
| | 0.0292 | A1 |
| | | 5 |

Question 85

| | | | |
|-----|--|-----------|--|
| (a) | $P(56 < X < 66) = P\left(\frac{56-62}{5} < z < \frac{66-62}{5}\right)$ $= P(-1.2 < z < 0.8)$ | M1 | Using \pm standardisation formula at least once, no $\sqrt{\sigma}$ or σ^2 , allow continuity correction |
| | $\Phi(0.8) + \Phi(1.2) - 1$ $= 0.7881 + 0.8849 - 1$ | M1 | Appropriate area Φ , from standardisation formula in final solution |
| | 0.673 | A1 | |
| | | 3 | |
| (b) | $z = 1.127$ | B1 | $\pm(1.126 - 1.127)$ seen, 4 sf or more |
| | $\frac{60t - 62}{5} = 1.127$ $60t = 5.635 + 62 = 67.635$ | M1 | z-value = $\pm \frac{(60t - 62)}{5}$ condone z-value = $\pm \frac{(t - 62)}{5}$ no continuity correction, condone $\sqrt{\sigma}$ or σ^2 |
| | $t = 1.13$ | A1 | CAO |
| | | 3 | |

Question 86

| | | | |
|-----|--|--------------|--|
| (a) | $P(X > 11.3) = P\left(z > \frac{11.3 - 10.1}{1.3}\right) = P(z > 0.9231)$ | M1 | Using \pm standardisation formula, no $\sqrt{\sigma}$ or σ^2 , continuity correction |
| | $1 - 0.822$ | M1 | Appropriate area Φ , from standardisation formula $P(z > \dots)$ in final solution |
| | 0.178 | A1 | 0.1779... |
| | | 3 | |
| (b) | $z = -0.674$ | B1 | ± 0.674 seen (critical value) |
| | $\frac{t - 10.1}{1.3} = -0.674$ | M1 | An equation using \pm standardisation formula with a z-value, condone $\sqrt{\sigma}$ or σ^2 , continuity correction. |
| | $t = 9.22$ | A1 | AWRT. Only dependent on M1 |
| | | 3 | |
| (c) | $P(8.9 < X < 11.3) = 1 - 2 \times \text{their 3(a)}$ $\equiv 2(1 - \text{their 3(a)}) - 1$ $\equiv 2(0.5 - \text{their 3(a)})$ $= 0.644$ | B1 FT | FT from <i>their 3(a)</i> < 0.5 or correct, accept unevaluated probability OE |
| | Number of days = 90×0.644 $= 57.96$ | M1 | $90 \times \text{their } p$ seen, $0 < p < 1$ |
| | So 57 (days) | A1 FT | Accept 57 or 58, not 57.0 or 58.0, no approximation/rounding stated FT must be an integer value |

Question 87

| | | | |
|------|---|--------------|---|
| (a) | $P(X > 4.2) = P\left(z > \frac{4.2 - 3.5}{0.9}\right)$ $= P(z > 0.7778)$ | M1 | Using \pm standardisation formula, no $\sqrt{\sigma}$ or σ^2 , continuity correction |
| | $1 - 0.7818$ | M1 | Appropriate area Φ , from standardisation formula $P(z > \dots)$ in final solution |
| | 0.218 | A1 | |
| | | 3 | |
| (b) | $z = -1.282$ | B1 | ± 1.282 seen (critical value) |
| | $\frac{t - 3.5}{0.9} = -1.282$ | M1 | An equation using \pm standardisation formula with a z -value, condone $\sqrt{\sigma}$, σ^2 and continuity correction |
| | $t = 2.35$ | A1 | AWRT, only dependent on M mark |
| | | 3 | |
| i(c) | $P(2.8 < X < 4.2) = 1 - 2 \times \text{their 5(a)}$ $\equiv 2(1 - \text{their 5(a)}) - 1$ $\equiv 2(0.5 - \text{their 5(a)})$ $= 0.5636$ | B1 FT | FT from <i>their 5(a)</i> < 0.5 or correct Accept unevaluated probability OE Accept 0.564 |
| | Number of days = $365 \times 0.5636 = 205.7$ | M1 | $365 \times \text{their } p$ |
| | So, 205 (days) | A1 FT | Accept 205 or 206, not 205.0 or 206.0 no approximation/rounding stated FT must be an integer value |

Question 88

| | | | |
|------|---|-----------|---|
| i(a) | $P\left(\left(\frac{85 - 96}{18}\right) < z < \left(\frac{100 - 96}{18}\right)\right)$ | M1 | Use of \pm standardisation formula once with appropriate values substituted, no continuity correction, not σ^2 or $\sqrt{\sigma}$. |
| | $P(-0.6111 < z < 0.2222)$ $= \Phi(0.2222) + \Phi(0.6111) - 1$ $= 0.5879 + 0.7294 - 1$ | M1 | Appropriate area Φ , from final process, must be probability. Use of $(1 - z)$ implies M0. |
| | 0.317 | A1 | Final answer which rounds to 0.317. |
| | | 3 | |
| i(b) | $z = \pm 1.175$ | B1 | $1.17 \leq z \leq 1.18$ or $-1.18 \leq z \leq -1.17$ |
| | $-1.175 = \frac{t - 96}{18}$ | M1 | An equation using \pm standardisation formula with a z -value, condone σ^2 , $\sqrt{\sigma}$ or continuity correction. E.g. equating to 0.88, 0.12, 0.8106, 0.1894, 0.5478, 0.4522, ± 0.175 or ± 2.175 implies M0. |
| | 74.85 or 74.9 | A1 | $74.85 \leq t \leq 74.9$ |
| | | 3 | |

Question 89

| | | | |
|-----|---|--------------|--|
| (a) | $z_1 = \frac{4 - \mu}{\sigma} = -1.378$ | B1 | $1.378 \leq z_1 \leq 1.379$ or $-1.379 \leq z_1 \leq -1.378$ |
| | $z_2 = \frac{10 - \mu}{\sigma} = 0.842$ | B1 | $0.841 \leq z_2 \leq 0.842$ or $-0.842 \leq z_2 \leq -0.841$ |
| | Solve to find at least one unknown: $\frac{4 - \mu}{\sigma} = -1.378$ $\frac{10 - \mu}{\sigma} = 0.842$ | M1 | Use of \pm standardisation formula once with μ , σ , a z -value and 4 or 10, allow continuity correction, not σ^2 or $\sqrt{\sigma}$ |
| | | M1 | Use either the elimination method or the substitution method to solve two equations in μ and σ . |
| | $\sigma = 2.70$ $\mu = 7.72$ | A1 | $2.70 \leq \sigma \leq 2.71$ $7.72 \leq \mu \leq 7.73$ |
| | | 5 | |
| (b) | $\Phi(2) - \Phi(-2) = 2\Phi(2) - 1$ | M1 | Identifying 2 and -2 as the appropriate z -values |
| | $2 \times \text{their } 0.9772 - 1$ | B1 | Calculating the appropriate area from stated phis of z -values which must be \pm the same number |
| | 0.9544 or 0.9545 | A1 | Accept AWRT 0.954 |
| | $0.9544 \times 800 = 763.52$ 763 or 764 | B1 FT | FT <i>their</i> 4SF (or better) probability, final answer must be positive integer |
| | | 4 | |

Question 90

| | | |
|---|-----------|---|
| $\left[P(X > 1.1) = \frac{72}{2000} (= 0.036) \right]$ $z = \pm 1.798$ | B1 | $1.79 < z \leq 1.80$, $-1.80 \leq z < -1.79$ seen |
| $\frac{1.1 - 1.04}{\sigma} = 1.798$ $\left[\frac{0.06}{\sigma} = 1.798 \right]$ | B1 | 1.1 and 1.04 substituted in \pm standardisation formula, allow continuity correction, not σ^2 or $\sqrt{\sigma}$ |
| | M1 | Equate <i>their</i> \pm standardisation formula to a z -value and to solve for the appropriate area leading to final answer (expect $\sigma < 0.5$). $\left(\text{Accept } \pm \frac{0.06}{\sigma} = z - \text{value} \right)$ |
| $\sigma = 0.0334$ | A1 | $0.03335 \leq \sigma \leq 0.0334$. At least 3 3s.f. |
| | 4 | |

Question 91

| | | |
|--|--------------|--|
| $\left[P\left(\left(\frac{25.2 - (25.5 + 0.50)}{0.4} \right) < z < \left(\frac{25.2 - (25.2 - 0.50)}{0.4} \right) \right) \right]$ $= P\left(-\frac{0.5}{0.4} < z < \frac{0.5}{0.4} \right)$ | M1 | Use of \pm Standardisation formula once; no continuity correction, σ^2 , $\sqrt{\sigma}$ |
| $[= 2\Phi(1.25) - 1]$ $= 2 \times 0.8944 - 1$ | A1 | For AWRT 0.8944 SOI |
| | M1 | Appropriate area $2\Phi - 1$ OE, from final process, must be probability |
| 0.7888 | A1 | Accept AWRT 0.789 |
| Number of rods = 0.7888×500 $= 394$ or 395 | B1 FT | Correct or FT <i>their</i> 4SF (or better) probability, final answer must be positive integer, not 394.0 or 395.0, no approximation/rounding stated, only 1 answer |
| | 5 | |

Question 92

| | | | |
|-----|---|-------------|--|
| (a) | $P(X > 43.2) = P\left(Z > \frac{43.2 - 41.2}{3.6}\right) = P(Z > 0.5556)$ | M1 | Use of \pm Standardisation formula once, allow continuity correction, not σ^2 , $\sqrt{\sigma}$. |
| | $1 - \Phi(0.5556) = 1 - 0.7108$ | M1 | Appropriate area Φ , from final process, must be probability. |
| | 0.289 | A1 | AWRT |
| | | 3 | |
| (b) | Probability = $1 - \text{their (a)} = 1 - 0.2892 = 0.7108$ | B1FT | $1 - \text{their (a)}$ or correct. |
| | $0.7108 \times 365 = 259.4$ 259, 260 | B1FT | FT <i>their</i> 4SF (or better) probability, final answer must be positive integer. |
| | | 2 | |
| (c) | $z = \pm 1.645$ | B1 | CAO, critical z value. |
| | $\frac{t - 41.2}{3.6} = -1.645$ | M1 | Use of \pm standardisation formula with μ , σ equated to a z -value, no continuity correction, allow σ^2 , $\sqrt{\sigma}$. |
| | $t = 35.3$ | A1 | |
| | | 3 | |

Question 93

| | | | |
|-----|--|-----------|--|
| (a) | $[P(X > 28.6) =] P\left(Z > \frac{28.6 - 32.2}{9.6}\right)$ $[= P(Z > -0.375)]$ | M1 | 28.6, 32.2 and 9.6 substituted appropriately in \pm Standardisation formula once, allow continuity correction of ± 0.05 , no σ^2 , $\sqrt{\sigma}$. |
| | $[\Phi(\text{their } 0.375) =] \text{their } 0.6462$ | M1 | Appropriate numerical area, from final process, must be probability, expect > 0.5 . |
| | 0.646 | A1 | AWRT |
| | | 3 | |
| (b) | $z = \pm 0.842$ | B1 | $0.841 < z \leq 0.842$ or $-0.842 \leq z < -0.841$ seen. |
| | $\frac{t - 32.2}{9.6} = 0.842$ | M1 | Substituting 32.2 and 9.6 into \pm standardisation formula, no continuity correction, allow σ^2 , $\sqrt{\sigma}$, must be equated to a z -value. |
| | $t = 40.3$ | A1 | $40.28 \leq t < 40.3$ WWW |
| | | 3 | |
| (c) | $P\left(-\frac{15}{9.6} < Z < \frac{15}{9.6}\right)$ $P(-1.5625 < Z < 1.5625)$ | M1 | Identifying at least one of $\frac{15}{9.6}$ and $-\frac{15}{9.6}$ as the appropriate z -values or substituting <i>their</i> (32.2 ± 15) into \pm Standardisation formula once, no continuity correction, σ^2 nor $\sqrt{\sigma}$. Condone ± 1.563 for M1 . |
| | $[2 \Phi\left(\frac{15}{9.6}\right) - 1]$ $= 2 \times 0.9409 - 1$ | A1 | $p = 0.941$ AWRT SOI |
| | | M1 | Appropriate area $2\Phi - 1$ oe, (eg $1 - 2 \times 0.0591$, $2 \times (0.9409 - 0.5)$ or $0.9409 - 0.0591$), from final process, must be probability > 0.5 . |
| | 0.882 | A1 | |
| | | 4 | |

Question 94

| | | | |
|---------|--|--------------|--|
| (a)(i) | $P(X > 142) = P\left(Z > \frac{142-125}{24}\right)$ | M1 | Substitution of correct values into the \pm Standardisation formula, allow continuity correction, not σ^2 , $\sqrt{\sigma}$. |
| | $[= P(Z > 0.7083)] = 1 - 0.7604$ | M1 | Appropriate numerical area Φ , from final process, must be probability, expect $p < 0.5$. |
| | 0.2396 | A1 | $0.239 \leq p \leq 0.240$ to at least 3sf. |
| | <i>Their</i> 0.2396×365 [= 87.454] | M1 | FT <i>their</i> 4sf (or better) probability. |
| | 87 or 88 | A1 FT | Final answer must be positive integer, no indication of approximation/rounding, only dependent on previous M mark. SC B1 FT for <i>their</i> 3sf probability $\times 365 =$ integer value, condone 0.24 used. |
| | | 5 | |
| (a)(ii) | $P(0, 1) = 0.7604^{10} + {}^{10}C_1 \times 0.2396^1 \times 0.7604^9$ [= 0.064628 + 0.20364] | M1 | One term: ${}^{10}C_x p^x (1-p)^{10-x}$ for $0 < x < 10$, any p . |
| | | A1 FT | Correct unsimplified expression using <i>their</i> probability to at least 3sf from (a)(i) or correct. |
| | 0.268 | A1 | AWRT, WWW. |
| | | 3 | |
| (b) | $z = \pm 1.282$ | B1 | Correct value only, critical value. |
| | $\frac{t-125}{24} = -1.282$ | M1 | Use of \pm Standardisation formula with correct values substituted, allow continuity correction, σ^2 , $\sqrt{\sigma}$, to form an equation with a z -value and not probability. |
| | $t = 94.2$ | A1 | AWRT, condone AWRT 94.3. Not dependent on B mark. |
| | | 3 | |

Question 95

| | | | |
|-----|--|-----------|---|
| (a) | $P(46 < X < 62) = P\left(\frac{46-55}{6} < Z < \frac{62-55}{6}\right)$ | M1 | 46 or 62, 55 and 6 substituted into \pm standardisation formula once. Condone 6^2 and continuity correction ± 0.5 |
| | $= P\left(-1.5 < Z < \frac{7}{6}\right)$ | B1 | Both standardisation values correct, accept unsimplified |
| | $\left[-\Phi\left(\frac{7}{6}\right) - (1 - \Phi(1.5))\right]$ $= 0.8784 + (0.9332 - 1)$ | M1 | Calculating the appropriate area from stated Φ s of z -values, must be probabilities. |
| | 0.812 | A1 | $0.8115 < p \leq 0.812$ |
| | | 4 | |
| (b) | $z = \pm 0.674$ | B1 | CAO, critical z -value |
| | $\frac{36-42}{\sigma} = -0.674$ | M1 | 36 and 42 substituted in \pm standardisation formula, no continuity correction, not σ^2 , $\sqrt{\sigma}$, equated to a z -value |
| | $\sigma = 8.9[0]$ | A1 | WWW. Only dependent on M. |
| | | 3 | |
| (c) | $P(\text{male} < 46) = 1 - \text{their } 0.9332 = 0.0668$ | M1 | FT value from part (a) or Correct: $1 - \Phi\left(\frac{46-55}{6}\right)$, condone continuity correction, σ^2 , $\sqrt{\sigma}$, and probability found. Condone unsupported correct value stated. |
| | $P(\text{female} < 46) = P\left(Z < \frac{46-42}{\text{their } 8.90}\right) [= \Phi(0.449)]$ $= 0.6732$ | M1 | 46, 42 and <i>their</i> 4(b) σ (or correct σ) substituted in \pm standardisation formula, condone continuity correction, σ^2 , $\sqrt{\sigma}$, and probability found Condone $\frac{4}{\text{their } 8.90}$. |
| | $P(\text{both}) = 0.0668 \times 0.6732$ | M1 | Product of <i>their</i> 2 probabilities ($0 < \text{both} < 1$) Not 0.25 or <i>their</i> final answer to 4(a) used. |
| | 0.0450 or 0.0449 | A1 | $0.0449 \leq p \leq 0.0450$ |
| | | 4 | |

Question 96

| | | | |
|-----|--|--------------|--|
| (a) | $P(142 < X < 205) = P\left(\frac{142-170}{25} < z < \frac{205-170}{25}\right)$ | M1 | Use of \pm standardisation formula once substituting 170, 25 and either 142 or 205 appropriately.. Condone 25^2 and continuity correction ± 0.5 . |
| | $P(-1.12 < z < 1.4)$ | A1 | Both correct. Accept unsimplified. |
| | $\Phi(1.4) - (1 - \Phi(1.12)) = 0.9192 + 0.8686 - 1$ | M1 | Calculating the appropriate area from stated phis of z -values. |
| | 0.788 | A1 | AWRT, not from wrong working |
| | | 4 | |
| (b) | $P(X > 205) = 1 - 0.9192 = 0.0808$ | B1 FT | Correct or FT from part 5(a). |
| | $(0.0808 \times 0.30 + \text{their } 0.788 \times 0.24) \times 20000$ | M1 | Correct or <i>their</i> $0.0808 \times 0.30 \times k + \text{their } 0.788 \times 0.24 \times k$, k positive integer. |
| | [\$]4266.24 | A1 | $4265 < \text{income} \leq 4270$, not from wrong working |
| | | 3 | |
| (c) | $P\left(Z > \frac{w-182}{20}\right) = 0.72$ | B1 | $0.5828 \leq z \leq 0.583$ or $-0.583 \leq z \leq -0.5828$ seen. |
| | $\frac{w-182}{20} = -0.583$ | M1 | 182 and 20 substituted in \pm standardisation formula, no continuity correction, not σ^2 , $\sqrt{\sigma}$, equated to a z -value. |
| | $w = 170$ | A1 | $170 \leq w < 170.35$ |
| | | | 3 |

Question 97

| | | | |
|-----|--|-----------|---|
| (a) | $P(10, 11, 12) =$ ${}^{12}C_{10}0.72^{10}0.28^2 + {}^{12}C_{11}0.72^{11}0.28^1 + {}^{12}C_{12}0.72^{12}0.28^0$ | M1 | One term ${}^{12}C_x p^x (1-p)^{12-x}$, for $0 < x < 12$, $0 < p < 1$. |
| | $= 0.193725 + 0.0905726 + 0.0194084$ | A1 | Correct expression, accept unsimplified, no terms omitted, leading to final answer. |
| | 0.304 | B1 | Final answer $0.3036 < p \leq 0.304$. |
| | Alternative method for question 5(a) | | |
| | $[1 - P(0, 1, 2, 3, 4, 5, 6, 7, 8, 9) =]$ $1 - ({}^{12}C_0 0.72^0 0.28^{12} + {}^{12}C_1 0.72^1 0.28^{11} + {}^{12}C_2 0.72^2 0.28^{10} +$ ${}^{12}C_3 0.72^3 0.28^9 + {}^{12}C_4 0.72^4 0.28^8 + {}^{12}C_5 0.72^5 0.28^7 +$ ${}^{12}C_6 0.72^6 0.28^6 + {}^{12}C_7 0.72^7 0.28^5 + {}^{12}C_8 0.72^8 0.28^4 +$ ${}^{12}C_9 0.72^9 0.28^3)$ | M1 | One term ${}^{12}C_x p^x (1-p)^{12-x}$, for $0 < x < 12$, $0 < p < 1$. |
| | | A1 | Correct expression, accept unsimplified, no terms omitted, leading to final answer. |
| | 0.304 | B1 | Final answer $0.3036 < p \leq 0.304$. |
| | | 3 | |
| (b) | Mean = $[0.52 \times 90] = 46.8$, var = $[0.52 \times 0.48 \times 90] = 22.464$ | B1 | 46.8 and 22.464 or 22.46 seen, allow unsimplified, $(4.739 < \sigma \leq 4.740$ imply correct variance). |
| | $P(X < 40) = P\left(z < \frac{39.5 - 46.8}{\sqrt{22.464}}\right)$ | M1 | Substituting <i>their</i> mean and <i>their</i> variance into \pm standardisation formula (any number for 39.5), not σ^2 , $\sqrt{\sigma}$. |
| | | M1 | Using continuity correction 39.5 or 40.5 in <i>their</i> standardisation formula. |
| | $= [P(Z < -1.540)] = 1 - 0.9382$ | M1 | Appropriate area Φ , from final process, must be probability. |
| | 0.0618 | A1 | $0.06175 \leq p \leq 0.0618$ |
| | | 5 | |

Question 98

| | | | |
|-----|---|-----------|--|
| (a) | $P(1.98 < X < 2.03) = P\left(\frac{1.98-2.02}{0.03} < z < \frac{2.03-2.02}{0.03}\right)$ $[= P(-1.333 < z < 0.333)]$ | M1 | Use of \pm standardisation formula once with 2.02, 0.03 and either 1.98 or 2.03 substituted appropriately. Condone 0.03^2 and continuity correction ± 0.005 , not $\sqrt{0.03}$. |
| | $[= \Phi(0.333) - (1 - \Phi(1.333))]$ $= 0.6304 + 0.9087 - 1$ | M1 | Calculating the appropriate probability area from <i>their</i> z-values. (or $0.6304 - 0.09121$ or $(0.9087 - 0.5) + (0.6304 - 0.5)$ etc) |
| | 0.539 | A1 | $0.539 \leq z < 0.5395$ Only dependent upon 2nd M mark. If M0 scored SC B1 for $0.539 \leq z < 0.5395$. |
| | | 3 | |
| (b) | $P(X > 2.6) = \frac{134}{5000} = 0.0268]$ $P(X < 2.6) = 1 - 0.0268 = 0.9732$ | B1 | 0.9732 or $\frac{4866}{5000}$ or $\frac{2433}{2500}$ seen. |
| | $\frac{2.6 - 2.55}{\sigma} = 1.93$ | M1 | Use of \pm standardisation formula with 2.6 and 2.55 substituted, no σ^2 , $\sqrt{\sigma}$ or continuity correction. |
| | | M1 | <i>Their</i> standardisation formula with values substituted equated to z-value which rounds to ± 1.93 . |
| | $\sigma = 0.0259$ | A1 | AWRT 0.0259 or $\frac{5}{193}$. If M0 earned, SC B1 for correct final answer. |
| | | 4 | |

Question 99

| | | | |
|-----|--|--------------|--|
| (a) | $P(X < 6) = P\left(Z < \frac{6-5.2}{1.5}\right) = P(Z < 0.5333)$ | M1 | 6, 5.2, 1.5 substituted into \pm standardisation formula, condone 1.5^2 , continuity correction ± 0.5 |
| | 0.703 | A1 | |
| | | 2 | |
| (b) | $z_1 = \frac{3-\mu}{\sigma} = -1.329$ $z_2 = \frac{8-\mu}{\sigma} = 0.878$ | B1 | $1.328 < z_1 < 1.329$ or $-1.329 \leq z_1 < -1.328$ |
| | | B1 | $0.877 < z_2 \leq 0.878$ or $-0.878 \leq z_2 < -0.877$ |
| | Solve to find at least one unknown: $\frac{3-\mu}{\sigma} = -1.329$ $\frac{8-\mu}{\sigma} = 0.878$ | M1 | Use of the \pm standardisation formula once with μ , σ , a z-value (not 0.8179, 0.7910, 0.5367, 0.5753, 0.19, 0.092 etc.) and 3 or 8, condone continuity correction but not σ^2 or $\sqrt{\sigma}$ |
| | | M1 | Use either the elimination method or the substitution method to solve their two equations in μ and σ |
| | $\sigma = 2.27, \mu = 6.01$ | A1 | $2.26 \leq \sigma \leq 2.27, 6.01 \leq \mu \leq 6.02$ |
| | | 5 | |
| (c) | $[P(Z < -1) + P(Z > 1)] \Phi(1) - \Phi(-1) =$ $= 2 - 2 \Phi(1)$ $= 2 - 2 \times 0.8413$ | M1 | Identify 1 and -1 as the appropriate z-values. |
| | | M1 | Calculating the appropriate area from stated phis of z-values which must be \pm the same number |
| | 0.3174 | A1 | Accept AWRT 0.317 |
| | Number of leaves: $2000 \times 0.3174 = 634.8$ so 634 or 635 | B1 FT | FT <i>their</i> 4 s.f. (or better) probability, final answer must be positive integer no approximation or rounding stated |
| | | 4 | |

Question 100

| | | |
|---|-----------|---|
| Mean = $80 \times 0.32 = 25.6$ var = $80 \times 0.32 \times 0.68 = 17.408$ | B1 | 25.6 and 17.4[08] seen, allow unsimplified. 4.172... implies correct variance. |
| $P(X < 20) = P\left(Z < \frac{19.5 - 25.6}{\sqrt{17.408}}\right) = P(Z < -1.462)$ | M1 | Substituting <i>their</i> 25.6 and 17.408 into \pm standardisation formula (any number for 19.5), not σ^2 , $\sqrt{\sigma}$. |
| | M1 | Using continuity correction 19.5 or 20.5 in <i>their</i> standardisation formula. |
| $= [1 - \Phi(1.462)] = 1 - 0.9282$ | M1 | Appropriate area Φ , from final process, must be probability. (Expect final ans < 0.5). Note: the correct final answer may imply M1 from use of calculator. |
| 0.0718 | A1 | $0.0718 \leq p \leq 0.0719$ |
| | 5 | |

Question 101

| | | |
|--|-----------|--|
| $[P(X > 1.11) =]P(Z > \frac{1.11-1.04}{0.06}) = P(Z > 1.167)$ | M1 | 1.11, 1.04 and 0.06 substituted into \pm Standardisation formula, no continuity correction not 0.06^2 or $\sqrt{0.06}$ |
| $= 1 - 0.8784$ | M1 | 1 - <i>their</i> 0.8784 as final answer, must be probability. (Expect final ans < 0.5). |
| 0.122 | A1 | $0.1216 \leq p \leq 0.122$ SC M0 M1 B1 for 0.122 with no standardisation formula. |
| | 3 | |

Question 102

| | | |
|--|-----------|--|
| $[P(X < w) = P(Z < \frac{w-1.04}{0.06}) = 0.81]$ | B1 | $0.8775 < z \leq 0.878$ or $-0.878 \leq z < -0.8775$ seen. |
| $\frac{w-1.04}{0.06} = 0.878$ | M1 | 1.04 and 0.06 substituted in \pm standardisation formula, no continuity correction, not σ^2 , $\sqrt{\sigma}$, equated to a z-value. |
| $w = 1.09$ | A1 | $1.09 \leq w \leq 1.093$ |
| | 3 | |

Question 103

| | | |
|--|--------------|--|
| (a) $[P(X < 54.8) = P(Z < \frac{54.8-55.6}{1.2})$ | M1 | Use of \pm standardisation formula, with 54.8, 55.6 and 1.2 substituted. condone 1.2^2 , $\sqrt{1.2}$ or continuity correction of 54.75 or 54.85 |
| $[= P(Z < -0.6667)] = 1 - 0.7477$ | M1 | Appropriate area Φ , from final process, must be probability. |
| $= 0.2523$ | A1 | $0.252 \leq p \leq 0.2525$ If A0 scored S CB1 for $0.252 \leq p \leq 0.2525$ |
| [Expected number =] $400 \times 0.2523 = 100.92$ 100 or 101 | B1 FT | FT <i>their</i> 4SF (or better) probability from a normal calculation. Must be a single integer answer. |
| | 4 | |
| (b) $[P(-\frac{1}{2} < Z < \frac{1}{2}) = \Phi(\frac{1}{2}) - \Phi(-\frac{1}{2}) =]$ $2\Phi(\frac{1}{2}) - 1$ $= 2 \times \text{their } 0.6915 - 1$ or <i>their</i> $0.6915 - (1 - \text{their } 0.6915)$ or $2 \times (0.6915 - 0.5)$ | M1 | {Both $\frac{1}{2}$ and $-\frac{1}{2}$ seen as z-values or appropriate use of $+\frac{1}{2}$ or $-\frac{1}{2}$ } and {no other z-values in part}. Condone $\frac{56.2-55.6}{1.2}$ and $\frac{55[.0]-55.6}{1.2}$ seen as z-values. |
| 0.383 | A1 | Calculating the appropriate area from stated phis of z-values which must be \pm the same number. $0.3829 \leq z \leq 0.383$ If A0 scored SC B1 for $0.3829 \leq z \leq 0.383$ |
| | 3 | |

Question 104

| | | | |
|-----|---|-----------|--|
| (a) | $[1 - P(10, 11, 12) =]$ $1 - ({}^{12}C_{10} 0.9^{10} 0.1^2 + {}^{12}C_{11} 0.9^{11} 0.1^1 + {}^{12}C_{12} 0.9^{12} 0.1^0)$ $= 1 - (0.230128 + 0.376573 + 0.282430)$ | M1 | One term ${}^{12}C_x p^x (1-p)^{12-x}$, for $0 < x < 12$, $0 < p < 1$ |
| | 0.111 | A1 | Correct expression, accept unsimplified, no terms omitted, leading to final answer. |
| (b) | [Mean = $80 \times 0.9 =$] 72, [Variance = $80 \times 0.9 \times 0.1 =$] 7.2 | B1 | 72 and 7.2 seen, allow unsimplified. May be seen in standardisation formula. ($2.683 \leq \sigma < 2.684$ imply correct variance). |
| | $P(X > 69) = P(Z > \frac{69.5 - 72}{\sqrt{7.2}})$ | M1 | Substituting <i>their</i> mean and $\sqrt{\text{their variance}}$ into \pm standardisation formula (any number for 69.5), not <i>their</i> 7.2, not $\sqrt{\text{their } 2.683}$ |
| | [= $P(Z > -0.9317) =$] $\Phi(0.9317)$ | M1 | Using continuity correction 69.5 or 68.5 in <i>their</i> standardisation formula. |
| | $\Phi(0.9317)$ | M1 | Appropriate area Φ , from final process, must be probability. |
| | 0.824 | A1 | $0.8239 \leq p \leq 0.8243$ WWW. |
| (c) | $np = 72$, $nq = 8$ Both greater than 5, [so approximation is valid] | 5 | |
| | | B1 | np , nq evaluated accurately. both np & nq referenced correctly. > 5 or greater than 5 seen. |
| | | 1 | |

Question 105

| | | | |
|-----|---|-----------|--|
| (a) | $[P(3, 4, \dots, 7) = 1 - P(0, 1, 2, 8)]$ $= 1 - ({}^8C_0 0.48^0 0.52^8 + {}^8C_1 0.48^1 0.52^7$ $+ {}^8C_2 0.48^2 0.52^6 + {}^8C_8 0.48^8 0.52^0)$ | M1 | One term ${}^8C_x p^x (1-p)^{8-x}$, for $0 < x < 8$, $0 < p < 1$ |
| | $= 1 - (0.00534597 + 0.039478 + 0.127544 + 0.0028179)$ | A1 | Correct expression, accept unsimplified, no terms omitted, leading to final answer. |
| | 0.825 | B1 | Mark the final answer at the most accurate value. $0.8248 < p \leq 0.825$ WWW. |
| (b) | [Mean = $0.52 \times 125 =$] 65, [var = $0.52 \times 0.48 \times 125 =$] 31.2 | B1 | 65 and 31.2 seen, allow unsimplified. May be seen in standardisation formula. ($5.585 < \sigma \leq 5.586$ imply correct variance). |
| | $P(X > 72) = P(Z > \frac{72.5 - 65}{\sqrt{31.2}})$ [= $P(Z > 1.343)$] | M1 | Substituting <i>their</i> 65 and $\sqrt{\text{their } 31.2}$ into \pm standardisation formula (any number for 72.5), not <i>their</i> 31.2, $\sqrt{\text{their } 5.586}$. |
| | | M1 | Using continuity correction 72.5 or 71.5 in <i>their</i> standardisation formula. Note $\frac{\pm 7.5}{\sqrt{31.2}}$ or $\frac{\pm 7.5}{5.586}$ seen gains M2 BOD |
| | $= 1 - 0.9104$ | M1 | Appropriate area Φ , from final process, must be probability. |
| | 0.0896 | A1 | $0.0896 \leq p \leq 0.0897$ WWW. |
| | | 5 | |

Question 106

| | | | |
|-----|--|--------------|--|
| (a) | $P(X < 132) = P\left(Z < \frac{132 - 125.4}{18.6}\right) = P(Z < 0.3548)$ | M1 | Use of \pm standardisation formula with 132 and 125.4 substituted, condone continuity correction 132 ± 0.5 and use of 18.6^2 , $\sqrt{18.6}$ |
| | 0.639 | A1 | $0.6385 < p \leq 0.639$ If M0 scored, SC B1 for $0.6385 < p \leq 0.639$ |
| | | 2 | |
| (b) | $\frac{108 - 117}{\sigma} = -1.175$ | B1 | $1.1749 < z \leq 1.175$ or $-1.175 \leq z < -1.1749$ |
| | $\sigma = 7.66$ | A1 | $7.659 \leq \sigma \leq 7.66$ If M0 scored, SC B1 for $7.659 \leq \sigma \leq 7.66$ |
| | | 3 | |
| (c) | $P(-1.5 < Z < 1.5)$ $[\Phi(1.5) - \Phi(-1.5)]$ $[= 2\Phi(1.5) - 1]$ $= 2 \times \text{their } 0.9332 - 1$ or $\text{their } 0.9332 - (1 - \text{their } 0.9332)$ or $2 \times (\text{their } 0.9332 - 0.5)$ | M1 | {Both 1.5 and -1.5 seen as z-values or appropriate use of 1.5 or -1.5 and {no other z-values in part}. |
| | 0.8664 | A1 | Accept answers wrt 0.866 If A0 scored SC B1 for answers wrt 0.866 |
| | $0.8664^3 = 0.650[36\dots]$ | B1 FT | FT <i>their</i> 4SF (or better) probability, accept final answers to 3SF. |
| | | 4 | |

Question 107

| | | | |
|-----|---|--------------|--|
| (a) | $[P(X < 74) = P\left(Z < \frac{74 - 62.3}{8.4}\right)] = P(Z < 1.393)$ | M1 | Use of \pm standardisation formula with 74, 62.3 and 8.4 substituted appropriately, not 8.4^2 , not $\sqrt{8.4}$, no continuity correction. |
| | = 0.918 | A1 | $0.918 \leq p < 0.9185$. |
| | | 2 | |
| (b) | $[P(50 < X < 74) = P\left(\frac{50 - 62.3}{8.4} < Z < \frac{74 - 62.3}{8.4}\right)]$ $[P(-1.464 < Z < 1.393)]$ | M1 | Use of \pm standardisation formula with both 74 (may be seen in 6(a) if <i>their</i> value seen) & 50, 62.3 and 8.4 substituted appropriately. Condone use of 8.4^2 , $\sqrt{8.4}$ and continuity correction ± 0.5 (73.5 or 74.5 and 49.5 or 50.5). |
| | $[\Phi(1.464) + \Phi(1.393) - 1]$ $0.9285 + 0.9182 - 1$ | M1 | Calculating the appropriate probability area from stated Φ of z-values (leading to <i>their</i> final answer > 0.5) but not symmetrical values. |
| | = 0.847 | A1 | $0.8465 \leq p < 0.8475$. SC B1 for $0.8465 \leq p < 0.8475$ if M0A0 awarded. |
| | $(0.8467)^4 = 0.514$ | B1 FT | Accept $0.513 \leq p < 0.514$. FT (<i>their</i> 4-figure p) ⁴ , $0 < p < 1$. |
| | | 4 | |
| (c) | $z_1 = \frac{36 - \mu}{\sigma} = -0.739$ $z_2 = \frac{54 - \mu}{\sigma} = 1.282$ | B1 | $-0.740 < z_1 < -0.738$ or $0.738 < z_1 < 0.740$. |
| | | B1 | $z_2 = \pm 1.282$ (critical value). |
| | | M1 | Use of the \pm standardisation formula once with μ , σ and a z-value (not 0.23, 0.77, 0.90, 0.10, ± 0.261 , $\pm 0.282\dots$). Condone continuity correction ± 0.5 , not σ^2 , $\sqrt{\sigma}$. |
| | Solve, obtaining values for μ and σ $\mu = 42.6$, $\sigma = 8.91$ | M1 | Solve using the elimination method, substitution method or other appropriate approach to obtain values for both μ and σ . |
| | | A1 | $42.58 \leq \mu < 42.6$, $8.90 \leq \sigma < 8.91$. |
| | | 5 | |

Question 108

Mean = $120 \times 0.4 = 48$
 Var = $120 \times 0.4 \times 0.6 = 28.8$

| | | |
|--|-----------|--|
| | B1 | 48 and $28\frac{4}{5}$, 28.8 seen, allow unsimplified. ($5.366 \leq \sigma \leq 5.367$ or $\frac{12\sqrt{5}}{5}$ implies correct variance). |
| $P(36 \leq X \leq 54) = P\left(\frac{35.5 - 48}{\sqrt{28.8}} < Z < \frac{54.5 - 48}{\sqrt{28.8}}\right)$ | M1 | Substituting <i>their</i> μ and σ into one \pm standardisation formula (any number for 35.5 or 54.5), condone σ^2 and $\sqrt{\sigma}$. |
| | M1 | Using continuity correction 35.5, 36.5 or 53.5, 54.5 once in <i>their</i> standardisation formula. Note: $\frac{\pm 12.5}{\sqrt{28.8}}$ or $\frac{\pm 6.5}{\sqrt{28.8}}$ seen gains M2 BOD. |
| $[= P(-2.3292 < Z < 1.211) =] 0.8871 + 0.9900 - 1$ | M1 | Appropriate area Φ , from final process. Must be a probability. Expect final answer > 0.5 . Note: correct final answer implies this M1. |
| $= 0.877$ | A1 | $0.877 \leq p < 0.8772$. |
| | 5 | |

Question 109

| | | | |
|---|--|--------------|--|
| (a) | $\left[P(X < 16) = P\left(Z < \frac{16 - 28}{\sigma}\right) = 0.1 \right]$ $\frac{16 - 28}{\sigma} = -1.282$ | B1 | ± 1.282 seen, cao – critical value. |
| | | M1 | Use of the \pm standardisation formula with 16, 28, σ and a z -value (not 0.1, 0.9, 0.282, 0.5398, 0.8159) equated to a z -value. Condone continuity correct ± 0.5 , not $\sigma^2, \sqrt{\sigma}$. Condone $\pm \frac{12}{\sigma} = -1.282$. |
| | $\sigma = 9.36$ | A1 | |
| | | 3 | |
| (b) | $[1 - P(0, 1, 2) =] 1 - ({}^{12}C_0(0.1)^0(0.9)^{12} + {}^{12}C_1(0.1)^1(0.9)^{11} + {}^{12}C_2(0.1)^2(0.9)^{10})$ $[1 - (0.2824 + 0.3766 + 0.2301)]$ | M1 | One term ${}^{12}C_x (p)^x (1-p)^{12-x}$, $0 < p < 1$. $x \neq 0, 1, 2$. |
| | | A1 | Correct expression, accept unsimplified, no terms omitted leading to final answer. |
| | 0.111 | B1 | 0.1108699... rounded to at least 3SF. |
| Alternative Method for Question 6(b) | | | |
| | $P(3, 4, 5, 6, 7, 8, 9, 10, 11, 12) = {}^{12}C_3(0.1)^3(0.9)^9 + {}^{12}C_4(0.1)^4(0.9)^8 + \dots + {}^{12}C_{11}(0.1)^{11}(0.9)^1 + {}^{12}C_{12}(0.1)^{12}(0.9)^0$ $[0.08523 + 0.02131 + \dots + 1.08 \times 10^{-10} + 1 \times 10^{-12}]$ | M1 | One term ${}^{12}C_x (p)^x (1-p)^{12-x}$, $0 < p < 1$. $x \neq 0, 1, 2$. |
| | | A1 | Correct expression, accept unsimplified, no terms omitted leading to final answer. |
| | 0.111 | B1 | 0.1108699... rounded to at least 3SF. |
| | | 3 | |
| (c) | $[P(-1.3 < Z < 1.3)$ $= 2\Phi(1.3) - 1]$ $= 2 \times 0.9032 - 1$ | B1 | Identifying at least one of -1.3 or 1.3 as the appropriate z -values. |
| | | M1 | Calculating the appropriate probability area from 2 symmetrical z -values (leading to their final answer, expect > 0.5). |
| | $= 0.806, \frac{504}{625}$ | A1 | $0.8064, 0.806 \leq p < 0.8065$. |
| | $[In 365 \text{ days } 0.8064 \times 365]$ $= 294 \text{ or } 295$ | B1 FT | Strict FT <i>their</i> at least 4-figure probability (not z -value). Final answer must be positive integer, no approximation or rounding stated. |
| | | 4 | |

Question 110

| | | | |
|-----|---|--------------|--|
| (a) | $[P(15.4 < X < 16.8) =] P\left(\frac{15.4-16.5}{0.6} < Z < \frac{16.8-16.5}{0.6}\right)$ $[= P(-1.833 < Z < 0.5)]$ | M1 | Use of \pm standardisation formula once with 16.5, 0.6 and either 15.4 or 16.8 substituted. |
| | $[= \Phi(0.5) + \Phi(1.833) - 1 =]$ $0.6915 + 0.9666 - 1$ | M1 | Calculating the appropriate probability area (leading to their final answer, expect > 0.5). $0.6915 - (1 - 0.9666)$ or $(0.6915 - 0.5) + (0.9666 - 0.5)$ OE are alternatives. |
| | $= 0.658$ | A1 | $0.658 \leq p < 0.6585$. If A0 scored, SC B1 for $0.658 \leq p < 0.6585$. |
| | [Expected number =] 0.6581×150 $= 98, 99$ | B1 FT | FT <i>their</i> 4SF (or better) probability from a normal calculation. Must be a positive single integer answer. No approximation notation. |
| | | 4 | |
| (b) | $\left[P\left(Z > \frac{17.1-18.4}{\sigma} \right) = 0.72 \right]$ $\frac{17.1-18.4}{\sigma} = -0.583$ | B1 | $0.5825 < z \leq 0.583$ or $-0.583 \leq z < -0.5825$ seen. |
| | $\sigma = 2.23$ | M1 | Use of the \pm standardisation formula with 17.1, 18.4, σ and a z-value (not 0.28, 0.72, 0.4175, 0.2358, 0.7642, 0.6103, 0.3897, ...). Condone continuity correct ± 0.05 , not $\sigma^2, \sqrt{\sigma}$. |
| | | A1 | AWRT |
| | | 3 | |
| (c) | [Mean = $120 \times 0.72 =$] 86.4 [Var = $120 \times 0.72 \times 0.28 =$] 24.192 | B1 | 86.4, $84\frac{2}{5}$ and $24\frac{24}{125}$, 24.192 to at least 3SF seen, allow unsimplified. May be seen in standardisation formula. $(4.918 \leq \sigma \leq 4.919)$ implies correct variance) Incorrect notation is penalised. |
| | $P(X < 80) = P\left(Z < \frac{79.5-86.4}{\sqrt{24.192}} \right)$ | M1 | Substituting <i>their</i> mean (not 18.4) and <i>their positive</i> 4.9185 into \pm standardisation formula (any number for 79.5), condone <i>their</i> 4.918 ² and $\sqrt{\textit{their}}$ 4.918 . |
| | | M1 | Using continuity correction 79.5 or 80.5 in <i>their</i> standardisation formula. |
| | $[P(Z < -1.4029) = 1 - \Phi(1.403)]$ $1 - 0.9196$ | M1 | Appropriate area Φ , from final process, must be a probability. Expect final answer < 0.5 . Note: correct final answer implies this M1. |
| | 0.0804 | A1 | $0.0803 \leq p \leq 0.0804$ |
| | | 5 | |

Question 111

| | | | |
|-----|--|--------------|---|
| (a) | $P(Z > \frac{20-14.6}{5.2}) = P(Z > 1.03846)$ | M1 | Use of \pm standardisation formula with 20, 14.6 and 5.2 not σ^2 , not $\sqrt{\sigma}$, no continuity correction. |
| | 1 - 0.8504 | M1 | Calculating the appropriate probability area (leading to their final answer). |
| | 0.150 | A1 | 0.1496, $0.149 < p \leq 0.15[0]$. Only dependent on the 2 nd M mark so M0M1A1 possible. SC B1 for $0.149 < p \leq 0.15[0]$ if M0M0A0 awarded. |
| | [250 \times their 0.1496 =] 37, 38 | B1 FT | Strict FT <i>their</i> at least 4-figure probability seen anywhere (give BOD if they go on to use 0.150). Final answer must be positive integer, no approximation or rounding stated. |
| | | 4 | |
| (b) | $z_1 = \frac{14.5 - \mu}{\sigma} = -0.842$ | B1 | $-0.843 < z_1 < -0.841$ or $0.841 < z_1 < 0.843$. |
| | $z_2 = \frac{18.5 - \mu}{\sigma} = -0.44$ | B1 | $-0.441 < z_2 < -0.439$ or $0.439 < z_2 < 0.441$. |
| | | M1 | Use of the \pm standardisation formula once with μ , σ and a z -value (not 0.20, 0.80, 0.67, 0.23, 0.5793, 0.7881, 0.7486, 0.591 or $1-z$ i.e. 0.158 etc.). Condone continuity correction ± 0.05 , not $\sigma^2, \sqrt{\sigma}$. |
| | Solve, obtaining values for μ and σ . | M1 | Solve using the elimination method, substitution method or other appropriate approach to obtain values for both μ and σ . |
| | $\mu = 22.9, \sigma = 9.95$ | A1 | AWRT 22.9, 9.95. |
| | 5 | | |