

SATPREP

Assignment- Differentiation

Differentiate each function with respect to x .

$$1) \ y = \sin^{-1} 3x^4$$

$$2) \ y = \tan^{-1} -4x^4$$

$$3) \ y = \cos^{-1} 5x^5$$

$$4) \ y = (2x^2 + 1)\sin 5x^3$$

$$5) \ y = (2x^5 - 3)\sin 2x^2$$

$$6) \ y = \frac{-3x^4 - 2}{\tan 2x^2}$$

$$7) \ y = e^{4x^5}(3x^2 + 1)$$

$$8) \ y = (2x^3 + 5) \cdot e^{3x^5}$$

$$9) \ y = (2x^2 + 1)\ln 4x^4$$

$$10) \ y = (x^3 + 2)\log_3 2x^5$$

Answers to Assignment- Differentiation

- 1) $\frac{dy}{dx} = \frac{1}{\sqrt{1 - (3x^4)^2}} \cdot 12x^3$
- $$= \frac{12x^3}{\sqrt{1 - 9x^8}}$$
- 2) $\frac{dy}{dx} = \frac{1}{(-4x^4)^2 + 1} \cdot -16x^3$
- $$= -\frac{16x^3}{16x^8 + 1}$$
- 3) $\frac{dy}{dx} = -\frac{1}{\sqrt{1 - (5x^5)^2}} \cdot 25x^4$
- $$= -\frac{25x^4}{\sqrt{1 - 25x^{10}}}$$
- 4) $\frac{dy}{dx} = (2x^2 + 1) \cdot \cos 5x^3 \cdot 15x^2 + \sin 5x^3 \cdot 4x$
- $$= x(30x^3 \cos 5x^3 + 15x \cos 5x^3 + 4 \sin 5x^3)$$
- 5) $\frac{dy}{dx} = (2x^5 - 3) \cdot \cos 2x^2 \cdot 4x + \sin 2x^2 \cdot 10x^4$
- $$= 2x(4x^5 \cos 2x^2 - 6 \cos 2x^2 + 5x^3 \sin 2x^2)$$
- 6) $\frac{dy}{dx} = \frac{\tan 2x^2 \cdot -12x^3 - (-3x^4 - 2) \cdot \sec^2 2x^2 \cdot 4x}{\tan^2 2x^2}$
- $$= \frac{4x(-3x^2 \tan 2x^2 + 3x^4 \sec^2 2x^2 + 2 \sec^2 2x^2)}{\tan^2 2x^2}$$
- 7) $\frac{dy}{dx} = e^{4x^5} \cdot 6x + (3x^2 + 1) \cdot e^{4x^5} \cdot 20x^4$
- $$= 2xe^{4x^5}(3 + 30x^5 + 10x^3)$$
- 8) $\frac{dy}{dx} = (2x^3 + 5) \cdot e^{3x^5} \cdot 15x^4 + e^{3x^5} \cdot 6x^2$
- $$= 3x^2 e^{3x^5}(10x^5 + 25x^2 + 2)$$
- 9) $\frac{dy}{dx} = (2x^2 + 1) \cdot \frac{1}{4x^4} \cdot 16x^3 + \ln 4x^4 \cdot 4x$
- $$= \frac{4(x^2 \ln 4x^4 + 2x^2 + 1)}{x}$$
- 10) $\frac{dy}{dx} = (x^3 + 2) \cdot \frac{1}{2x^5 \ln 3} \cdot 10x^4 + \log_3 2x^5 \cdot 3x^2$
- $$= \frac{3x^3 \log_3 2x^5 \cdot \ln 3 + 5x^3 + 10}{x \ln 3}$$