

**Assignment : Derivative**

For each problem, find the derivative of the function at the given value.

1)  $y = -2x^2 - 16x - 26$  at  $x = -2$

2)  $y = -x^2 + 4x - 5$  at  $x = 2$

3)  $y = -x^2 - 4x + 1$  at  $x = -3$

4)  $y = 2x^2 + 12x + 19$  at  $x = -2$

For each problem, find the points where gradient of the tangent is zero

5)  $y = x^3 - 4x^2 + 6$

6)  $y = x^3 - 2x^2 + 4$

7)  $y = -x^3 + 3x^2 - 4$

8)  $y = -x^3 + x^2 - 1$

For each problem, find all points of relative minima and maxima.

9)  $y = x^3 - x^2 + 1$

10)  $y = x^2 - 6x + 11$

11)  $y = -x^3 + 8x^2 - 20x + 13$

12)  $y = x^3 - 3x^2 - 1$

## Answers to Assignment : Derivative

$$1) \left. \frac{dy}{dx} \right|_{x=-2} = -8$$

$$2) \left. \frac{dy}{dx} \right|_{x=2} = 0$$

$$3) \left. \frac{dy}{dx} \right|_{x=-3} = 2$$

$$4) \left. \frac{dy}{dx} \right|_{x=-2} = 4$$

$$5) (0, 6), \left(\frac{8}{3}, -\frac{94}{27}\right)$$

$$6) (0, 4), \left(\frac{4}{3}, \frac{76}{27}\right)$$

$$7) (0, -4), (2, 0)$$

$$8) (0, -1), \left(\frac{2}{3}, -\frac{23}{27}\right)$$

$$9) \text{Relative minimum: } \left(\frac{2}{3}, \frac{23}{27}\right)$$

$$10) \text{Relative minimum: } (3, 2)$$

No relative maxima.

$$\text{Relative maximum: } (0, 1)$$

$$11) \text{Relative minimum: } (2, -3)$$

$$\text{Relative maximum: } \left(\frac{10}{3}, -\frac{49}{27}\right)$$

$$12) \text{Relative minimum: } (2, -5)$$

$$\text{Relative maximum: } (0, -1)$$

