

Assignment : Power rule and Chain Rule

Differentiate each function with respect to x .

1) $y = -5\sqrt[4]{x} - 4x^{\frac{1}{5}}$

2) $y = -\frac{4}{x} + 4x^{-3}$

3) $y = -\frac{3}{x} + 3x^{-4}$

4) $y = 3x^{\frac{2}{5}} + \frac{3}{x^2}$

5) $y = (3x^4 + 5)^{-5}$

6) $y = (2x^3 + 1)^4$

7) $y = \sqrt[3]{3x^4 + 1}$

8) $y = (5x^2 + 2)^{-3}$

9) $y = \sqrt[4]{x^3 + 4}$

10) $y = (x^2 + 2)^{-5}$

Answers to Assignment : Power rule and Chain Rule

1)
$$\frac{dy}{dx} = -\frac{5}{4x^{\frac{3}{4}}} - \frac{4}{5x^{\frac{5}{4}}}$$

2)
$$\frac{dy}{dx} = \frac{4}{x^2} - \frac{12}{x^4}$$

3)
$$\frac{dy}{dx} = \frac{3}{x^2} - \frac{12}{x^5}$$

4)
$$\frac{dy}{dx} = \frac{6}{5x^{\frac{3}{5}}} - \frac{6}{x^3}$$

5)
$$\begin{aligned}\frac{dy}{dx} &= -5(3x^4 + 5)^{-6} \cdot 12x^3 \\ &= -\frac{60x^3}{(3x^4 + 5)^6}\end{aligned}$$

6)
$$\begin{aligned}\frac{dy}{dx} &= 4(2x^3 + 1)^3 \cdot 6x^2 \\ &= 24x^2(2x^3 + 1)^3\end{aligned}$$

7)
$$\begin{aligned}\frac{dy}{dx} &= \frac{1}{3}(3x^4 + 1)^{-\frac{2}{3}} \cdot 12x^3 \\ &= \frac{4x^3}{(3x^4 + 1)^{\frac{2}{3}}}\end{aligned}$$

8)
$$\begin{aligned}\frac{dy}{dx} &= -3(5x^2 + 2)^{-4} \cdot 10x \\ &= -\frac{30x}{(5x^2 + 2)^4}\end{aligned}$$

9)
$$\begin{aligned}\frac{dy}{dx} &= \frac{1}{4}(x^3 + 4)^{-\frac{3}{4}} \cdot 3x^2 \\ &= \frac{3x^2}{4(x^3 + 4)^{\frac{3}{4}}}\end{aligned}$$

10)
$$\begin{aligned}\frac{dy}{dx} &= -5(x^2 + 2)^{-6} \cdot 2x \\ &= -\frac{10x}{(x^2 + 2)^6}\end{aligned}$$

