

Cambridge IGCSE™

ADDITIONAL MATHEMATICS**0606/11**

Paper 1

October/November 2024

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2024 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

This document consists of **8** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics-Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfww	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$\pm 3(x+4)(2x-1)(x-2)$	3	B1 for \pm B1 for 3, may be implied by a linear factor B1 for $(x+4)(2x-1)(x-2)$ and no extra terms; may be implied if 3 is included
2(a)	$2^{8(x+y)} \times 2^{4(-2x)} = 2^{3(-x+3y)}$	M1	For attempt at a common factor, must have at least one correct
	$y = 3x$	A1	Must show sufficient detail
2(b)	$x^2 + 3(9x^2) = 56$ or $\frac{y^2}{9} + 3y^2 = 56$	M1	For obtaining an equation in terms of one variable using <i>their</i> $y = 3x$ with attempt to solve to obtain $x =$, or $y =$
	$x = \sqrt{2}, y = 3\sqrt{2}$ or exact equivalent $x = -\sqrt{2}, y = -3\sqrt{2}$ or exact equivalent	2	A1 for a correct pair
3	$b = \frac{3}{8}$	B1	
	$6 = a + c$ or $0 = -\frac{a}{2} + c$	M1	For using either intercept with <i>their</i> b
	$c = 2$	A1	
	$a = 4$	A1	
4	$\ln(4x+3)$	B1	
	$2\ln(8a+7) - 2\ln(3)$ ($= \ln 16$)	M1	Dep for correct application of limits in <i>their</i> $k \ln(4x+3)$
	$(2)\ln \frac{8a+7}{3}$ oe	M1	Dep for use of division rule
	$\ln 16 = 2\ln 4$ oe	B1	
	$a = \frac{5}{8}$ only	A1	
5(a)	${}^{15}C_3 k^3 = -29120$ oe	M1	
	$k = -4$	A1	

Question	Answer	Marks	Guidance
5(b)	${}^{12}C_8(8y^2)^4\left(-\frac{1}{2y}\right)^8$ or ${}^{12}C_4(8y^2)^4\left(-\frac{1}{2y}\right)^8$	M1	
	7920	A1	
6	$b = 12$	2	M1 for attempt at differentiation
	$-27a + 99 - 3b + c = 0$ $a + 11 + b + c = 16$	2	M1 for attempt at $p(-3) = 0$ or $p(1) = 16$
	$a = 2$ $c = -9$	2	M1 for attempt to solve <i>their</i> equations
7(a)	$e^{5y} = mx^3 + c$ soi	B1	
	$4.38 = -2.56m + c$ $9.84 = 6.54m + c$	M1	Must be using the coordinates correctly
	$m = 0.6, c = 5.92$	2	M1 dep for solution of <i>their</i> equations
	$y = \frac{1}{5} \ln(0.6x^3 + 5.92)$	A1	
	Alternative		
	$e^{5y} = mx^3 + c$ soi	B1	
	Gradient = $\frac{5.46}{9.1} (=m)$	M1	Must be using the coordinates correctly
	$4.38 = -2.56m + c$ or $9.84 = 6.54m + c$	M1	Must be using the coordinates correctly
	$m = 0.6, c = 5.92$	A1	
	$y = \frac{1}{5} \ln(0.6x^3 + 5.92)$	A1	
7(b)	$0.6x^3 + 5.92 > 0$	M1	Allow use of <i>their</i> $\frac{1}{5} \ln(0.6x^3 + 5.916)$
	$x > -2.14$	2	M1 dep for a correct method of solution to obtain $x > \dots$

Question	Answer	Marks	Guidance
8	$(f'(x) =) k(3x+5)^{\frac{1}{3}} (+c)$	M1	
	$(f'(x) =) (3x+5)^{\frac{1}{3}} (+c)$	A1	Allow unsimplified
	$(f'(1) =) 6 = (3+5)^{\frac{1}{3}} + c$	M1	Dep M1 for use of given condition
	$f'(x) = (3x+5)^{\frac{1}{3}} + 4$ soi	A1	
	$m(3x+5)^{\frac{4}{3}}$	M1	
	$(f(x) =) m(3x+5)^{\frac{4}{3}} + cx + d$	M1	Dep M1, FT on <i>their c</i>
	$(f(1) =) 20 = m(8)^{\frac{4}{3}} + c + d$	M1	Dep M1, FT on <i>their c</i>
	$(f(x) =) \frac{1}{4}(3x+5)^{\frac{4}{3}} + 4x + 12$	A1	
9(a)	$\frac{dy}{dx} = \frac{(x+1)(-3e^{-3x+2}) - e^{-3x+2}}{(x+1)^2}$	3	B1 for $-3e^{-3x+2}$ M1 for correct attempt at differentiation of a quotient A1 all terms apart from $-3e^{-3x+2}$ correct
	$\frac{e^{-3x+2}(-3x-4)}{(x+1)^2}$	2	M1 dep for attempt to obtain the given form, allow sign errors
9(b)	$e^{-3x+2} \neq 0$	B1	
	$x = -\frac{4}{3}$	B1	FT on <i>their</i> $-3x-4$ $\frac{dy}{dx}$ must be in the correct form
	$y = -3e^6$	B1	
10(a)	$ar^2 = 6$ $ar^7 = 1458$ soi	B1	
	$r^5 = 243$	B1	
	$r = 3$	B1	
	$a = \frac{2}{3}$	B1	

Question	Answer	Marks	Guidance
10(b)	$r = 2\cos\theta$	B1	
	$-\frac{1}{2} < \cos\theta < \frac{1}{2}$ $-1 < 2\cos\theta < 1$ $ 2\cos\theta < 1$	B1	
	$-90^\circ < \theta < -60^\circ$	B1	
	$60^\circ < \theta < 90^\circ$	B1	
11	$4x + k\cos 3x$	M1	
	$4x - \frac{2}{3}\cos 3x$	A1	
	$\left(\frac{4\pi}{3} - k\cos\pi\right) - \left(\frac{4\pi}{18} - k\cos\frac{\pi}{6}\right)$	M1	M1 dep for correct application of limits
	Area under the curve $\frac{10\pi}{9} + \frac{2}{3} + \frac{\sqrt{3}}{3}$	A2	A1 for one correct term
	When $x = \frac{\pi}{18}$, $y = 5$	B1	May be seen on the diagram
	When $x = \frac{\pi}{3}$, $y = 4$	B1	May be seen on the diagram
	Area of trapezium $= \frac{5\pi}{4}$	B1	For area of trapezium
	Shaded area $= \frac{2}{3} + \frac{\sqrt{3}}{3} - \frac{5\pi}{36}$	A1	

Question	Answer	Marks	Guidance
12(a)	$2(\cot^2 \theta + 1) - 5 = 5 \cot \theta$ soi	B1	
	$2 \cot^2 \theta - 5 \cot \theta - 3 = 0$	M1	For attempt to obtain a 3-term quadratic in terms of $\cot \theta$, equated to zero
	$(2 \cot \theta + 1)(\cot \theta - 3) = 0$	M1	M1 dep for attempt to factorise, or use of quadratic formula oe
	$\tan \theta = -2, \tan \theta = \frac{1}{3}$	M1	M1 dep for obtaining in terms of $\tan \theta$, using <i>their</i> factors
	$-161.6^\circ, -63.4^\circ, 18.4^\circ, 116.6^\circ$	3	M1 for a correct solution A1 for another correct solution A1 for a further 2 correct solutions and no extras in the range
	Alternative		
	$2(\cot^2 \theta + 1) - 5 = 5 \cot \theta$ soi	B1	
	$2 \cot^2 \theta - 5 \cot \theta - 3 = 0$	M1	For attempt to obtain a 3-term quadratic in terms of $\cot \theta$, equated to zero
	$3 \tan^2 \theta + 5 \tan \theta - 2 = 0$	M1	M1 dep for attempt to obtain a 3-term quadratic in terms of $\tan \theta$, equated to zero
	$(3 \tan \theta - 1)(\tan \theta + 2) = 0$ $\tan \theta = -2, \tan \theta = \frac{1}{3}$	M1	M1 dep for attempt to factorise, or use of quadratic formula oe and obtaining $\tan \theta = \dots$
	$-161.6^\circ, -63.4^\circ, 18.4^\circ, 116.6^\circ$	3	M1 for a correct solution A1 for another correct solution A1 for a further 2 correct solutions and no extras in the range
10(b)	$\sin(2\phi + 1.5) = \frac{2}{3}$ $2\phi + 1.5 = 0.7297\dots$ soi	M1	
	$2\phi + 1.5 = 2.4119$ or 7.0129 or 8.6591	A1	
	$0.456, 2.76, 3.6[0]$	3	M1 for correct order of operations A1 for one correct solution A1 for a further 2 correct solutions and no extras in the range.

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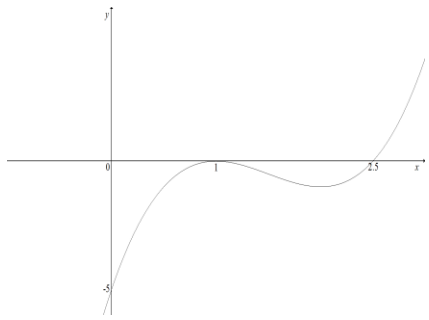
Types of mark

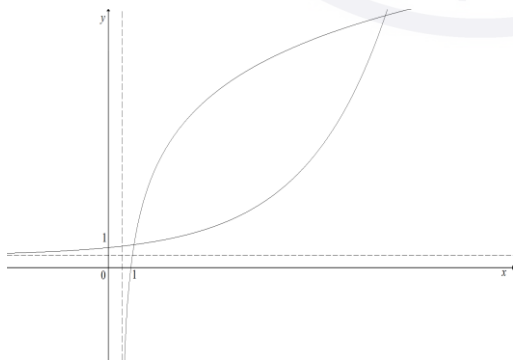
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Abbreviations

awrt	answers which round to
cao	correct answer only
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isw	ignore subsequent working
nfwf	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(a)	$b = 3$	B1	
	Use of $y = a \cos bx + c$, with <i>their</i> b and either set of given coordinates	M1	<i>their</i> $b \neq \frac{2\pi}{3}$
	$c = -2$	A1	
	$a = 5$	A1	
1(b)	Minimum when $\cos bx = -1$ so	B1	Allow for <i>their</i> b , $b \neq \frac{2\pi}{3}$
	$x = \frac{\pi}{3}$	B1	Allow if b is correct
	$y = -7$	B1	FT on <i>their</i> c – <i>their</i> a
	Alternative		
	$\frac{dy}{dx} = -15 \sin 3x$	(B1)	FT on <i>their</i> a , b and c , $b \neq \frac{2\pi}{3}$
	When $\frac{dy}{dx} = 0$, $x = \frac{\pi}{3}$	(B1)	Allow if b is correct
	$y = -7$	(B1)	FT on <i>their</i> c – <i>their</i> a
2(a)	$(f'(x)) = 2(x-1)(2x-5) + 2(x-1)^2$ oe or $6x^2 - 18x + 12$	M1	For use of product rule or expansion and differentiation
	$2(x+1)(2x-5) + 2(x-1)^2 = 0$ oe or $6x^2 - 18x + 12 = 0$ oe	M1	Dep for equating <i>their</i> quadratic $f'(x)$ to zero and attempt to solve to obtain $x = \dots$
	$x=1, y=0$ $x=2, y=-1$	2	A1 for any correct pair, must be from correct working only
2(b)		3	B1 for a correct cubic shape B1 for a correct cubic shape in the correct position, touching the x -axis once in the 4th quadrant and intersecting once with the positive x -axis B1 for all intercepts and no extras
2(c)	$k < -1$	B1	
	$k > 0$	B1	

Question	Answer	Marks	Guidance
3(a)	$ACB = 2 \tan^{-1} \left(\frac{12}{5} \right)$ oe	M1	
	$ACB = (2 \times 1.176...)$ $= 2.35$ to 2 dp	A1	Must see justification to 2 dp
3(b)	Arc length $= 5 \times ACB$	B1	
	Perimeter $= 35.8$	B1	Allow awrt 35.8
3(c)	Area $= (12 \times 5) - \left(\frac{1}{2} \times 5^2 \times 2.35 \right)$	M2	M1 for area of kite or area of sector M1 dep for kite area – sector area
	30.6	A1	Allow greater accuracy Any use of fractions gets A0
4(a)(i)	$\frac{2}{3}$	B1	Allow $x > \frac{2}{3}$, $a = \frac{2}{3}$, but not $x = \frac{2}{3}$ unless it is replaced with a correct answer
4(a)(ii)	\mathbb{R} oe	B1	Must be using correct notation
4(a)(iii)	$3y - 2 = e^{\frac{x}{4}}$ or $3x - 2 = e^{\frac{y}{4}}$	M1	For valid attempt to reach this stage
	$f^{-1}(x) = \frac{1}{3} \left(e^{\frac{x}{4}} + 2 \right)$	A1	Must be using correct notation
	Domain $x \in \mathbb{R}$ Range $f^{-1} > \frac{2}{3}$	B2	B1 for each, must be using the correct notation.
4(a)(iv)		4	B1 for the shape of $y = f(x)$ in the first and fourth quadrants only B1 dep on previous B1 for (1, 0) B1 for a correct shape for $f^{-1}(x)$, or FT on <i>their</i> $y = f(x)$ with correct shape in first quadrant for symmetry about $y = x$ soi B1 dep on previous B1 , for (0, 1) and at least one point of intersection with $y = f(x)$ correct in the first quadrant

Question	Answer	Marks	Guidance
4(b)	$\left(2\left((2x+1)^{\frac{1}{2}}+4\right)+1\right)^{\frac{1}{2}}+4$	B1	
	$(2x+1)^{\frac{1}{2}}=8$	B1	Dep
	$x=31.5$ oe	B1	Dep on both previous B marks
	Alternative		
	$g(x)=9, x=12$	(B1)	
	$g(x)=12$	(B1)	Dep
	$x=31.5$ oe	(B1)	Dep on both previous B marks
5(a)	$\frac{\operatorname{cosec}^2 \theta}{\cot^2 \theta} = \frac{1}{\sin^2 \theta} \times \frac{\sin^2 \theta}{\cos^2 \theta}$ $= \frac{1}{\cos^2 \theta} = \sec^2 \theta$	B1	Sufficient detail is needed Do not award if θ is consistently omitted
	Alternative 1		
	$\frac{\frac{\sin^2 \theta + \cos^2 \theta}{\sin^2 \theta}}{\frac{\cos^2 \theta}{\sin^2 \theta}}$ $= \frac{1}{\cos^2 \theta} = \sec^2 \theta$	(B1)	Sufficient detail is needed Do not award if θ is consistently omitted
	Alternative 2		
	$\frac{1}{\cot^2 \theta} + 1$ $\tan^2 \theta + 1$	(B1)	Sufficient detail is needed Do not award if θ is consistently omitted
5(b)	$\sec^2 \theta$	B1	
5(c)	$\int (\sec^2 \theta - \sin \theta) d\theta$ soi	B1	
	$\tan \theta + \cos \theta$	B2	B1 for each
	$\sqrt{3} - \frac{1}{2}$ or exact equivalent	B1	Dep on 3 previous B marks
6(a)	$x^{10} + 20x^7 + 180x^4$	3	B1 for each correct term

Question	Answer	Marks	Guidance
6(b)	${}^8C_4(4x^2)^4\left(\frac{1}{2x^2}\right)^4$	M1	May be implied by working to obtain $r = 4$
	1120	A1	From correct working
7	$\left(\frac{dy}{dx} = \frac{(x+2)\left(\frac{6x}{3x^2-1}\right) - \ln(3x^2-1)}{(x+2)^2}\right)$ or $\frac{6x}{(3x^2-1)}(x+2)^{-1} - (x+2)^{-2}\ln(3x^2-1)$ oe	3	B1 for $\frac{6x}{3x^2-1}$ M1 for correct attempt at differentiation of a quotient or a correct product A1 for all terms apart from $\frac{6x}{3x^2-1}$ correct.
	When $x = 1$, $\frac{dy}{dx} = \frac{9 - \ln 2}{9}$	M1	For use of $x = 1$ in <i>their</i> $\frac{dy}{dx}$, must see a substitution if in decimal form unless 0.923 obtained from a correct derivative
	$\frac{dx}{dt} = \frac{9h}{9 - \ln 2}$ or exact equivalent	2	M1 for $\frac{h}{\text{their}\left(\frac{9 - \ln 2}{9}\right)}$, with $x = 1$ substituted in A0 if using small changes
8	$\frac{dy}{dx} = e^x k(2x+5)^{-\frac{1}{2}} + e^x(2x+5)^{\frac{1}{2}}$	M1	
	$\frac{dy}{dx} = e^x(2x+5)^{-\frac{1}{2}} + e^x(2x+5)^{\frac{1}{2}}$	A1	
	When $x = 2$, $\frac{dy}{dx} = \frac{10e^2}{3}$	M1	Dep allow unsimplified Allow for using <i>their</i> $\frac{dy}{dx}$
	When $x = 2$, $y = 3e^2$	B1	
	Tangent: $y - 3e^2 = \frac{10e^2}{3}(x - 2)$	M1	Allow for using <i>their</i> $\frac{dy}{dx}$ and <i>their</i> y
	When $y = 0$, $x = \frac{11}{10}$	A1	Must be simplified Must be from correct work
	When $x = 0$, $y = -\frac{11e^2}{3}$	A1	
	$\left(\frac{11}{20}, -\frac{11e^2}{6}\right)$	A1	FT on <i>their</i> coordinates for x and y , but must be exact and simplified

Question	Answer	Marks	Guidance
9	$\frac{8}{2x+1} = 6x+1$ $12x^2 + 8x - 7 = 0$	M1	Attempt to obtain a 3-term quadratic in one variable equated to zero.
	$x = \frac{1}{2}$	2	M1 dep for solution, see guidance
	$k \ln(2x+1)$	M1	
	Area under curve = $[k \ln(2x+1)]_0^{\text{their } \frac{1}{2}}$ $= k \ln(2(\text{their } x) + 1) (-0)$	M1	Dep on previous M1 for correct application of limits using <i>their</i> x , k and zero Allow unsimplified
	Area under curve = $2 \ln 2$	A1	Not from incorrect work
	Area under straight line = $\frac{5}{8}$ or 0.625 oe	B1	
	Shaded area = $\ln 4 - \frac{5}{8}$	A1	Not from incorrect work

Question	Answer	Marks	Guidance
9	Alternative		
	Either $\frac{8}{2x+1} = 6x+1$ $12x^2 + 8x - 7 = 0$	(M1)	Attempt to obtain a 3-term quadratic in one variable equated to zero.
	$x = \frac{1}{2}$	(2)	M1 dep for solution, see guidance
	$y = 2$	(A1)	Award only if attempt at integration with respect to y is subsequently seen
	Or $x = \frac{2}{y} - \frac{1}{2}$ and $x = \frac{2y-1}{6}$ oe	(M1)	For rearranging both equations to obtain x or $2x$ in terms of y
	$2y^2 + 2y - 12 = 0$	(M1)	Dep for attempt to obtain a 3-term quadratic in one variable equated to zero.
	$y = 2$	(2)	M1 dep for solution, see guidance
	Then area enclosed between curve, y -axis and the line $y = 2 = \left[k \ln y - \frac{1}{2} y \right]_{\text{their } 2}^4$ $= k \ln 4 - 2 - k \ln 2 + 1$	(M1)	For correct application of limits using <i>their</i> $y = 2$, k and 4 Allow unsimplified
	$2 \ln 2 - 1$	(A1)	Not from incorrect work
	Area enclosed by straight line, the y axis and the line $y = 2$, $= \frac{3}{8}$	(B1)	
	Shaded area $= \ln 4 - \frac{5}{8}$	(A1)	Not from incorrect work
10(a)	$\frac{30}{2}(4 \tan 2x + (29 \times 3 \tan 2x)) = 455\sqrt{3}$	M1	For attempt to use sum formula with correct a and d
	$\tan 2x = \frac{\sqrt{3}}{3}, \frac{455\sqrt{3}}{1365}$	A1	
	$x = -165^\circ, -75^\circ, 15^\circ, 105^\circ$	3	M1 for 1 correct solution (allow if in radians or from use of $\tan 2x = 0.577$ or $\tan 2x = 0.58$ e.g. $14.99^\circ, 15.06^\circ$) A1 for a second correct solution A1 for 2 further correct solutions and no extras in the range

Question	Answer	Marks	Guidance
10(b)	$r = 4 \cos^2 \left(\theta - \frac{\pi}{2} \right)$	B1	
	$4 \cos^2 \left(\theta - \frac{\pi}{2} \right) < 1$ or $-1 < 4 \cos^2 \left(\theta - \frac{\pi}{2} \right) < 1$ or $0 \leq 4 \cos^2 \left(\theta - \frac{\pi}{2} \right) < 1$	M1	For use of sum to infinity condition
	$\theta = -\frac{\pi}{6}, \frac{\pi}{6}, \frac{5\pi}{6}, \frac{7\pi}{6}$	2	M1 dep for one correct critical value A1 for all critical values and no extras in the range $-\frac{\pi}{6} \leq \theta \leq \frac{7\pi}{6}$
	$-\frac{\pi}{6} < \theta < \frac{\pi}{6}$ (excluding 0) $\frac{5\pi}{6} < \theta < \frac{7\pi}{6}$ (excluding π)	2	A1 for each correct set of values

Cambridge IGCSE™

ADDITIONAL MATHEMATICS**0606/13**

Paper 1

October/November 2024

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2024 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

This document consists of **8** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics-Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

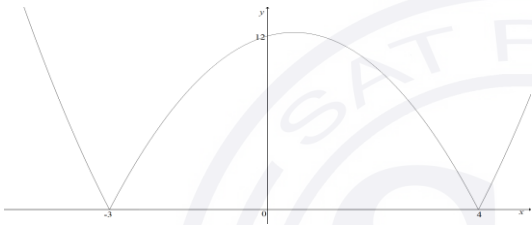
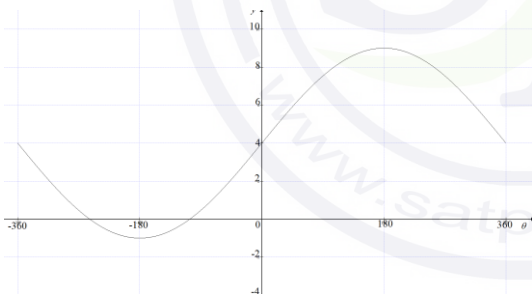
Types of mark

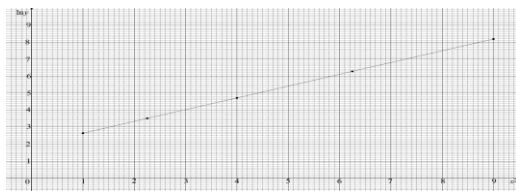
- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(a)	$y = x^2 - x - 12$ $\frac{dy}{dx} = 2x - 1$ or $(x + 3) + (x - 4)$ or $y = \left(x - \frac{1}{2}\right)^2 - \frac{49}{4}$ or using symmetry $x = \frac{4-3}{2}$	M1	For expanding the brackets and differentiate with at least one correct term or for using the product rule or for completing the square or for using symmetry
	$x = \frac{1}{2}$	A1	
	$y = -\frac{49}{4}$ oe	A1	
1(b)		2	B1 for the correct shape. Must have the parabola part of the curve with maximum in the first quadrant and cusps on the x-axis. Ignore labelling of their maximum point if incorrect coordinates B1 for correct intercepts. Must be correct shape
1(c)	$k > \frac{49}{4}$ oe	B1	FT on $\left \text{their } -\frac{49}{4} \right $ excluding $k > 12$
2		4	B1 for correct shape must be a curve with one min in 3 rd quadrant and one max in first quadrant and correct endpoints $(-360, 4)$ and $(360, 4)$ Ignore labelling of their maximum point if incorrect coordinates. depB1 for intercept of 4 on y-axis. Must have the correct shape depB1 for max in correct position of $(180^\circ, 9)$. Must have the correct shape depB1 for min in correct position of $(-180^\circ, -1)$. Must have the correct shape
3	$4x^2 - 4kx - k + 2 = 0$	B1	soi
	$k^2 + k - 2$ Critical values $-2, 1$	2	M1 for use of discriminant on <i>their</i> three-term quadratic equation to obtain two critical values
	$-2 < k < 1$	A1	Strict inequality

Question	Answer	Marks	Guidance												
4(a)	$3 = \log_2 8$	B1													
	$\log_2 \frac{8a^4}{b}$	2	M1 for correct use of two operations from multiplication, division or power rule for logs to the base of 2. A1 for log to the base of 2 only												
4(b)	$\lg x = \frac{4}{\lg x}$ or $\frac{1}{\log_x 10} = 4\log_x 10$	B1	Change of base												
	$(\lg x)^2 = 4$ or $(\log_x 10)^2 = \frac{1}{4}$	B1	Dep on correct change of base Must work with $(\lg x)^2$ or $(\log_x 10)^2$ not $\log x^2$ or $(\log_x 100)$												
	$x = 100$	B1	Dep on correct change of base												
	$x = \frac{1}{100}$ or 0.01	B1	Dep on correct change of base												
5(a)	$p(-2): -8a + 4b + 38 + c = 0$	M1	For substitution of -2 in $p(x)$ and equating to zero. Allow one sign error in evaluating												
	$p(-1): -a + b + 19 + c = 20$	M1	For substitution of -1 in $p(x)$ and equating to 20. Allow one sign error in evaluating												
	$7a - 3b = 39$	A1	AG – must be from correct work												
5(b)	$p'(1): 3a + 2b - 19 = 1$	M1	For substitution of 1 in $p'(x)$ and equating to 1 Allow one sign error in evaluating. Can be unsimplified												
	$a = 6, b = 1, c = 6$	2	M1 dep for solution of <i>their</i> equation with that from (a) to find at least one unknown.												
6(a)	<table><tr><td>x^2</td><td>1</td><td>2.25</td><td>4</td><td>6.25</td><td>9</td></tr><tr><td>$\ln y$</td><td>2.64</td><td>3.51</td><td>4.72</td><td>6.28</td><td>8.18</td></tr></table> 	x^2	1	2.25	4	6.25	9	$\ln y$	2.64	3.51	4.72	6.28	8.18	2	M1 for plotting points with one error
x^2	1	2.25	4	6.25	9										
$\ln y$	2.64	3.51	4.72	6.28	8.18										

Question	Answer	Marks	Guidance
6(b)	$\ln y = x^2 \ln b + \ln A$	B1	May be seen in part (a)
	Gradient = $\ln b$ ($\ln b = 0.7$) $b = 2$	2	M1 for attempt to find the gradient and equate to $\ln b$ Gradient must be from linear graph of $\ln y$ vs x^2
	Intercept = $\ln A$ ($\ln A = 1.95$) $A = 7$	2	M1 for attempt to use intercept
6(c)	When $y = 200$, $\ln y = 5.3$ $x^2 = 4.85$ $x = 2.2$ (allow 2.1 or 2.3)	2	M1 for using <i>their</i> linear graph with $\ln y = 5.3$ to obtain a value for x^2 A0 for $x = \pm 2.2$ if -2.2 is not rejected
7(a)	$x^2 + 3x^2 \ln x$	2	M1 for attempt to differentiate a product Allow unsimplified for 2 marks
7(b)	$\int 3x^2 \ln x \, dx = x^3 \ln x - \int x^2 \, dx$	B1	
	$\left[x^3 \ln x - \frac{x^3}{3} \right]_1^2$ $8 \ln 2 - \frac{8}{3} + \frac{1}{3}$	M1	Dep on B1 M1 for correct use of limits
	$\ln 256 - \frac{7}{3}$	2	A1 for one correct term
8(a)	$5x^2 + 3x - 14 = 0$ or $5y^2 - 4y - 57 = 0$	M1	soi
	$x = \frac{7}{5}$, $y = \frac{19}{5}$ $x = -2$, $y = -3$	3	M1 for attempt to solve <i>their</i> quadratic to obtain either $x = \dots$ or $y = \dots$ A1 for one correct pair both x or both y or one correct (x, y) point
	Midpoint $\left(-\frac{3}{10}, \frac{2}{5} \right)$	B1	Must be correct midpoint
	Gradient of perpendicular $-\frac{1}{2}$	B1	Must be correct
	Perp bisector: $y - \frac{2}{5} = -\frac{1}{2} \left(x + \frac{3}{10} \right)$	M1	Must be using <i>their</i> midpoint and a gradient $= -\frac{1}{2}$
	$k = -\frac{4}{5}$	A1	

Question	Answer	Marks	Guidance
8(b)	$\left(\frac{9}{2}, -2\right)$	2	B1 for one correct FT on $2 \times (\text{their } k) - \text{their } \frac{2}{5}$
	$\left(-\frac{51}{10}, \frac{14}{5}\right)$	2	B1 for one correct FT on $\left[\left(3 \times \text{their } \frac{2}{5}\right) - (2 \times \text{their } k) \right]$
9(a)	$\mathbf{c} - 2\mathbf{a}$	B1	
9(b)	$4\mathbf{a} + \frac{2}{3}(\text{their } (\mathbf{c} - 2\mathbf{a}))$ oe	M1	Alternative route: $OC + CB + BD = \mathbf{c} + 2\mathbf{a} - \frac{1}{3} \text{their } AB$
	$\frac{8}{3}\mathbf{a} + \frac{2}{3}\mathbf{c}$	A1	Allow unsimplified
9(c)	$\mu \left(\text{their } \left(\frac{8}{3}\mathbf{a} + \frac{2}{3}\mathbf{c} \right) \right)$	B1	Must be in terms of \mathbf{a} and \mathbf{c} in a valid vector form. Allow unsimplified
9(d)	$\overrightarrow{AC} = \mathbf{c} - 4\mathbf{a}$	B1	
	$\lambda(\text{their } (\mathbf{c} - 4\mathbf{a}))$	B1	Must be in terms of \mathbf{a} and \mathbf{c} in a valid vector form
9(e)	$4\mathbf{a} = \text{their } (\mathbf{c}) - \text{their } (\mathbf{d})$ oe	M1	Must be in terms of \mathbf{a} and \mathbf{c} in a valid vector form
	$\lambda = \frac{1}{2}, \mu = \frac{3}{4}$	3	M1 dep on first M1 for equating like vectors once M1 dep on first M1 for attempt to solve 2 simultaneous equations in λ and μ . leading to $\lambda = \dots$ or $\mu = \dots$ A1 for both
10(a)	$\tan \theta = \frac{2}{7}, \tan \theta = -1$	2	M1 for attempt to factorise or use formula to obtain $\tan \theta = \dots$
	$15.9^\circ, -164.1^\circ, -45^\circ, 135^\circ$	2	A1 for two correct solutions A1 for a further 2 correct solutions and no extras in the range

Question	Answer	Marks	Guidance
10(b)	$\sin(3\phi - 1.5) = \frac{2}{3}$ $3\phi - 1.5 = 0.7297$	M1	Correct order of the operation Do not accept in degrees
	$3\phi - 1.5 = 2.41[12], 7.01[3]$	A1	soi by correct answers with no extras within the range
	0.743, 1.30, 2.84	3	M1 dep on first M1 for correct order of operations or one correct solution A1 for one solution A1 for a further 2 correct solutions and no extras in the range Do not accept in degrees
11(a)	$d = 3\log_x 3$ or $\log_x 3^3$ nfw	B1	Must be exact Allow $d = \log_x 27$ nfw
	$\frac{n}{2}(2\log_x 3 + 3(n-1)\log_x 3)$ nfw	M1	For use of sum formula with <i>their</i> d must be in the form of $\log_x 3$
	$\frac{n}{2}(3n-1)\log_x 3$ or $\left(\frac{3n^2}{2} - \frac{n}{2}\right)\log_x 3$	A1	Must be in the form of $k\log_x 3$
11(b)	$r = 3\tan^2 \theta$	B1	soi
	$ 3\tan^2 \theta < 1$ or $[-1 <] 3\tan^2 \theta < 1$ or $\left[-\frac{1}{3} < \right] \tan^2 \theta < \frac{1}{3}$ or $[0 <] \tan^2 \theta < \frac{1}{3}$	B1	
	$\tan \theta < \frac{1}{\sqrt{3}}$ or $0 < \tan \theta < \frac{1}{\sqrt{3}}$	B1	
	$0 < \theta < \frac{\pi}{6}$	B1	



CANDIDATE
NAME

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CENTRE
NUMBER

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CANDIDATE
NUMBER

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0606/11

May/June 2024

2 hours

No additional materials are needed.

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages.

Mathematical Formulae**1. ALGEBRA***Quadratic Equation*

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a + b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series

$$u_n = a + (n-1)d$$

$$S_n = \frac{1}{2}n(a + l) = \frac{1}{2}n\{2a + (n-1)d\}$$

Geometric series

$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \quad (r \neq 1)$$

$$S_\infty = \frac{a}{1-r} \quad (|r| < 1)$$

2. TRIGONOMETRY*Identities*

$$\begin{aligned}\sin^2 A + \cos^2 A &= 1 \\ \sec^2 A &= 1 + \tan^2 A \\ \operatorname{cosec}^2 A &= 1 + \cot^2 A\end{aligned}$$

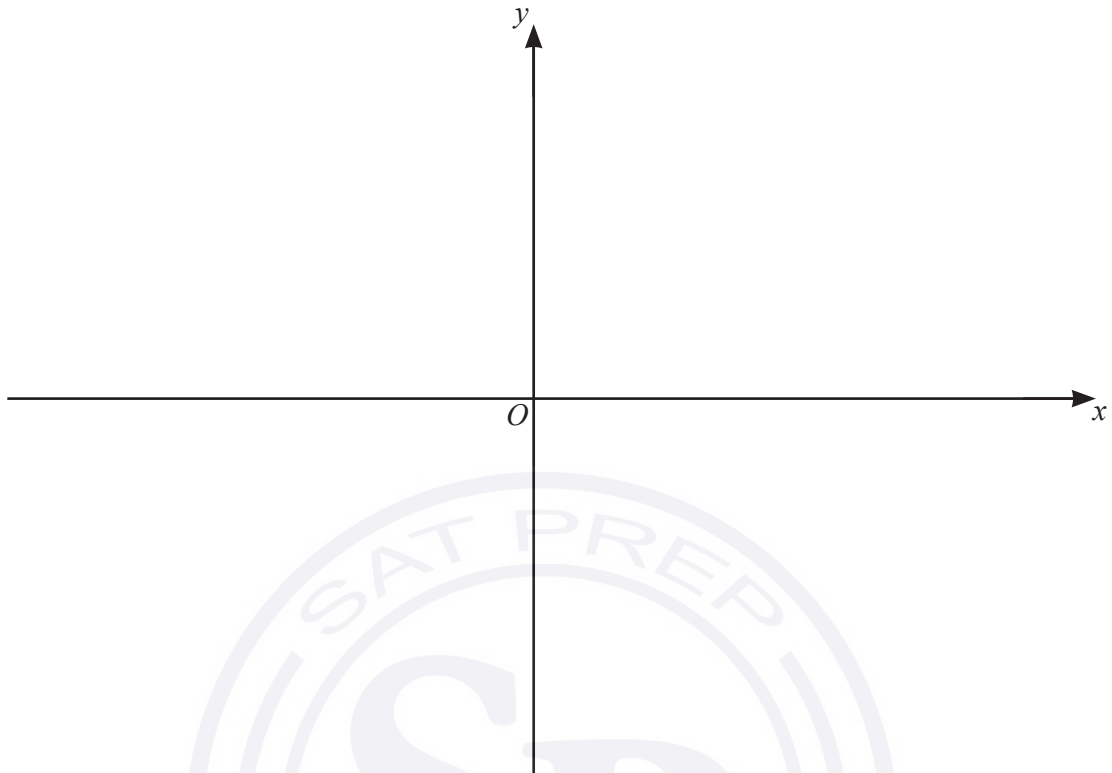
Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2}bc \sin A$$

- 1 (a) On the axes, sketch the graph of $y = -\frac{1}{5}(x+2)(2x-1)(x+5)$, stating the intercepts with the axes. [3]



- (b) Hence solve the inequality $-\frac{1}{5}(x+2)(2x-1)(x+5) \geq 0$. [2]

2 DO NOT USE A CALCULATOR IN THIS QUESTION.

The polynomial p is such that $p(x) = 6x^3 - 35x^2 + 34x + 45$.

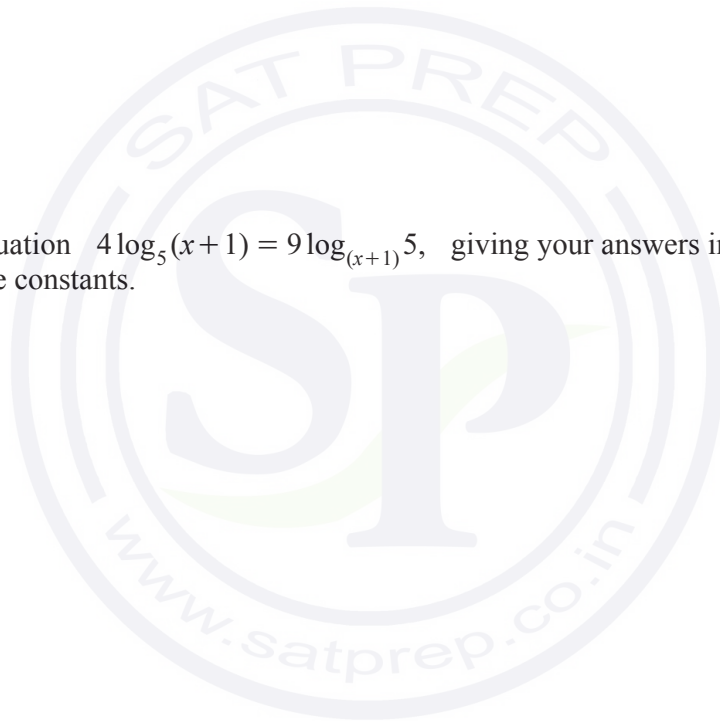
(a) Find $p(x)$ in the form $(2x - 5)q(x) + r$, where $q(x)$ is a polynomial and r is a constant. [3]

(b) Hence write the expression $p(x) - 5$ as a product of linear factors. [2]

(c) Hence write down the solutions of the equation $p(x) = 5$. [1]

- 3 (a) Write $1 + \lg(x^2 - 1) - 2 \lg(x - 1)$, where $x > 1$, as a single logarithm to base 10. Give your answer in its simplest form. [4]

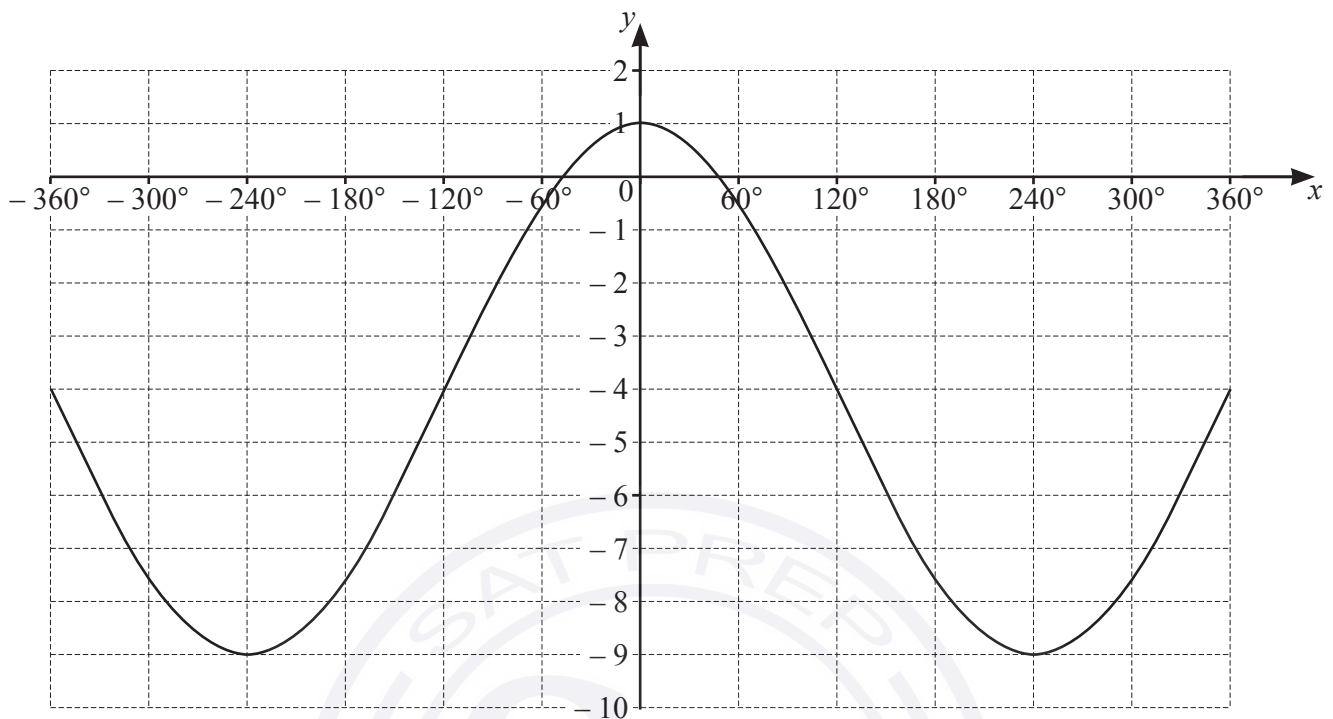
- (b) Solve the equation $4 \log_5(x + 1) = 9 \log_{(x+1)} 5$, giving your answers in the form $a + b\sqrt{c}$, where a, b and c are constants. [5]



- 4 (a) The first three terms, in ascending powers of x , in the expansion of $(3+px)^n$ are $243 + 810x + qx^2$, where n , p and q are constants. Find the values of n , p and q . [5]

- (b) Find the term independent of y in the expansion of $\left(2y - \frac{1}{3y^2}\right)^6$. Give your answer in exact form. [2]

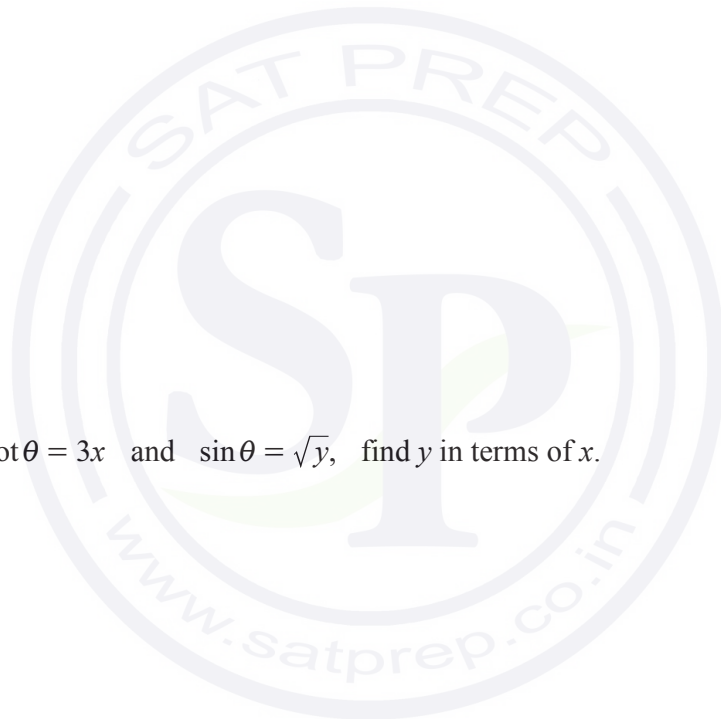
- 5 (a) The diagram shows the graph of $y = a \cos bx + c$, for $-360^\circ \leq x \leq 360^\circ$, where a , b and c are constants. Find the values of a , b and c . [3]



- (b) The line $y = p$ is a tangent to the curve $y = 3 - 2 \sin 6\theta$. Write down the possible values of p . [2]

6 Find $\int_2^4 \left(\frac{2}{2x-3} - \frac{3}{(3x-5)^2} \right) dx$, giving your answer in exact form. [4]

7 Given that $2 + \cot \theta = 3x$ and $\sin \theta = \sqrt{y}$, find y in terms of x . [3]



- 8 Solve the equation $4 \sin^2\left(2\alpha - \frac{\pi}{3}\right) = 1$ for $-\frac{\pi}{2} \leq \alpha \leq \frac{\pi}{2}$. Give your answers in terms of π . [5]



- 9 (a) Solve the following simultaneous equations.

$$e^{x+y} \times e^{3x-2y} = 1$$

$$x^2y = 256$$

[5]



- (b) Solve the equation $10e^{(2x-1)} - 11 = 6e^{(1-2x)}$, giving your answer in exact form. [4]



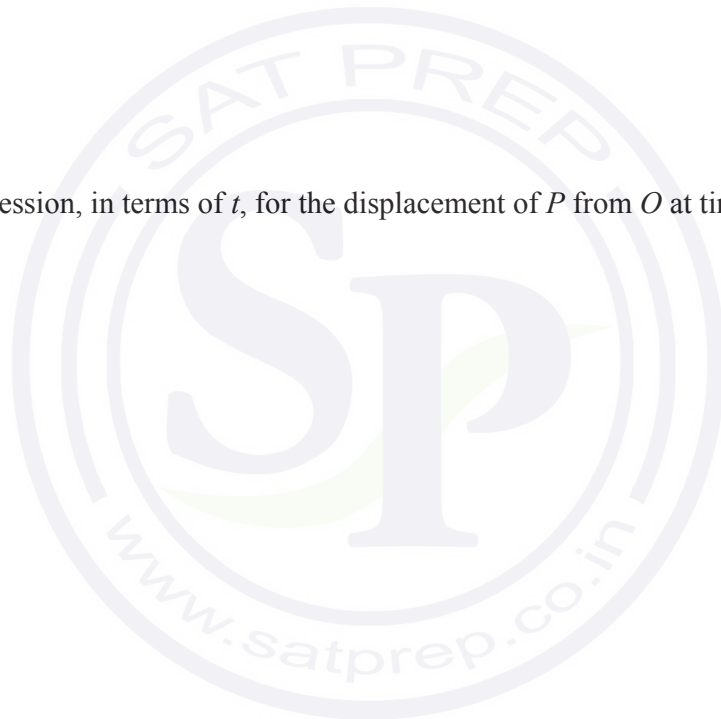
10 In this question, all distances are in metres and time, t , is in seconds.

A particle P is at a fixed point O at time $t = 0$.

The velocity, v , of P is given by $v = 3 \sin 2t$ for $t \geq 0$.

(a) Find the exact value of t for which the velocity is zero for the first time after P leaves O . [2]

(b) Find an expression, in terms of t , for the displacement of P from O at time t . [4]



(c) Find the distance travelled by P for $0 \leq t \leq \pi$.

[3]



- 11 The tangent to the curve $y = (3x - 1)^{\frac{1}{3}}$ at the point where $x = 3$ meets the coordinate axes at the points A and B . The point with coordinates (a, a) lies on the perpendicular bisector of the line AB . Find the exact value of a . [10]



Continuation of working space for Question 11.



Question 12 is printed on the next page.

12 (a) It is given that $y = \frac{\ln 3x}{x^2}$ for $x > 0$.

Find $\frac{dy}{dx}$. Give your answer in the form $\frac{A+B\ln 3x}{x^3}$, where A and B are integers. [4]

(b) Hence find $\int \frac{\ln 3x}{x^3} dx$. [4]



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ADDITIONAL MATHEMATICS

0606/12

Paper 1

May/June 2024

2 hours

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
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- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
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INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

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Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series

$$u_n = a + (n-1)d$$

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$$

Geometric series

$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \quad (r \neq 1)$$

$$S_\infty = \frac{a}{1-r} \quad (|r| < 1)$$

2. TRIGONOMETRY

Identities

$$\begin{aligned}\sin^2 A + \cos^2 A &= 1 \\ \sec^2 A &= 1 + \tan^2 A \\ \operatorname{cosec}^2 A &= 1 + \cot^2 A\end{aligned}$$

Formulae for $\triangle ABC$

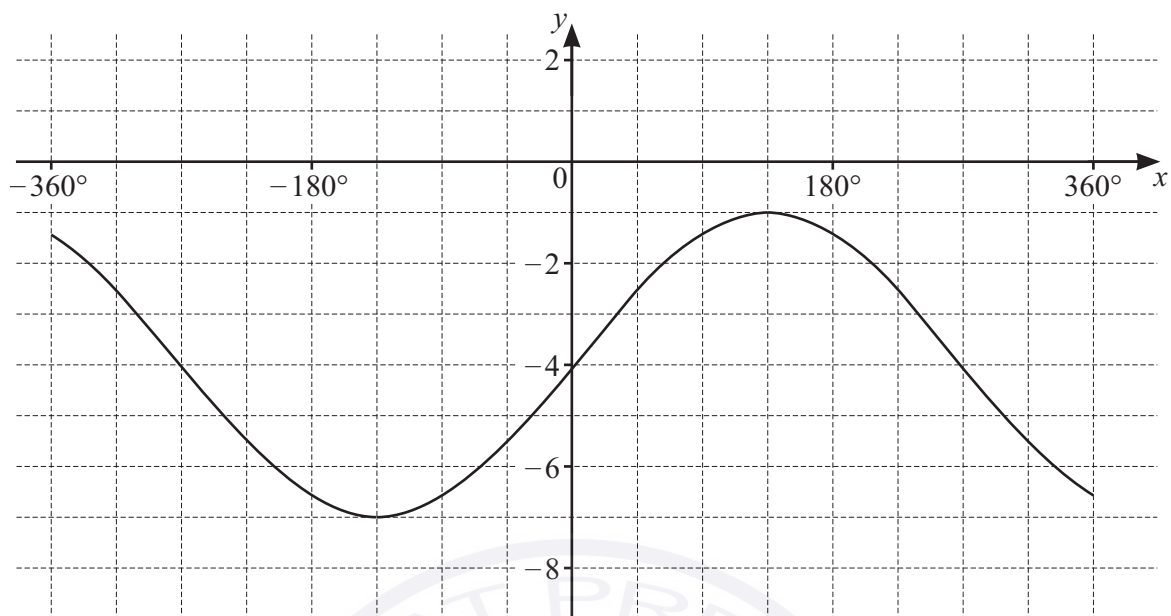
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

$$\Delta = \frac{1}{2}bc \sin A$$



1



The diagram shows the graph of $y = a \sin bx + c$ for $-360^\circ \leq x \leq 360^\circ$, where a , b and c are constants. Find the values of a , b and c . [3]

- 2 Given that $\log_3 r + 2 \log_9 s = 8$, find the value of rs . [3]





- 3 Given that $y = \tan \frac{x}{2}$, find the exact value of $\frac{dy}{dx}$ when $x = \frac{\pi}{3}$.

[4]





4 A team of 8 people is to be formed from 6 teachers, 5 doctors and 4 police officers.

(a) Find the number of teams that can be formed. [1]

(b) Find the number of teams that can be formed without any teachers. [1]

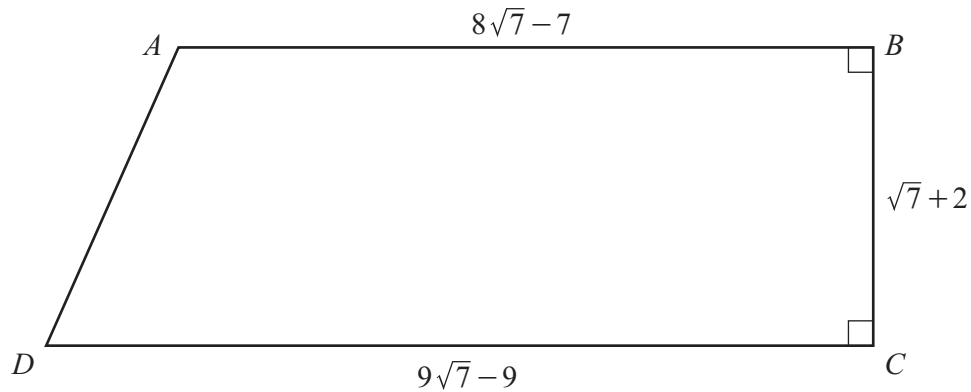
(c) Find the number of teams that can be formed with the same number of doctors as teachers. [4]





5 DO NOT USE A CALCULATOR IN THIS QUESTION.

In this question, all lengths are in centimetres.



The diagram shows the trapezium $ABCD$. The lengths of AB , BC and CD are $8\sqrt{7} - 7$, $\sqrt{7} + 2$ and $9\sqrt{7} - 9$ respectively. The line BC is perpendicular to the lines AB and CD .

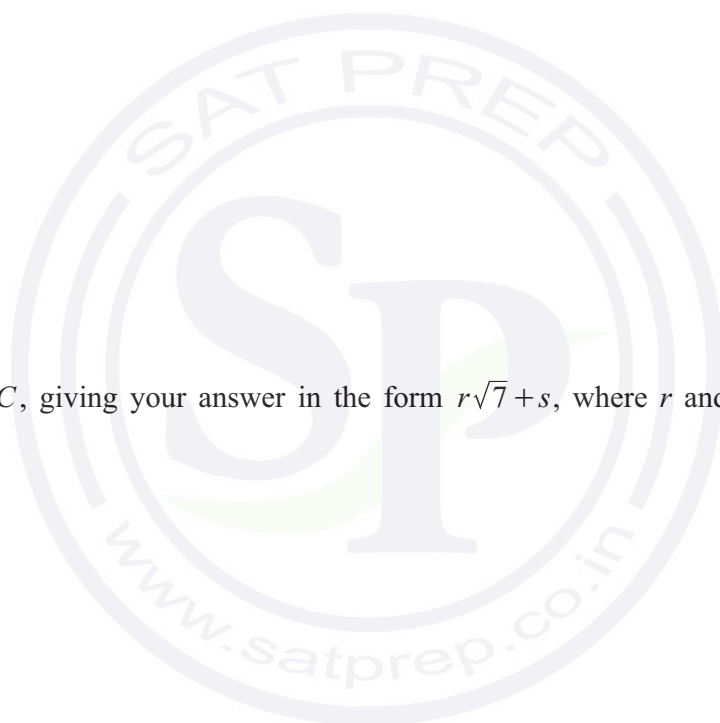
- (a) Find the perimeter of the trapezium, giving your answer in its simplest form. [3]

- (b) Find the area of the trapezium, giving your answer in the form $p\sqrt{7} + q$, where p and q are rational numbers. [3]

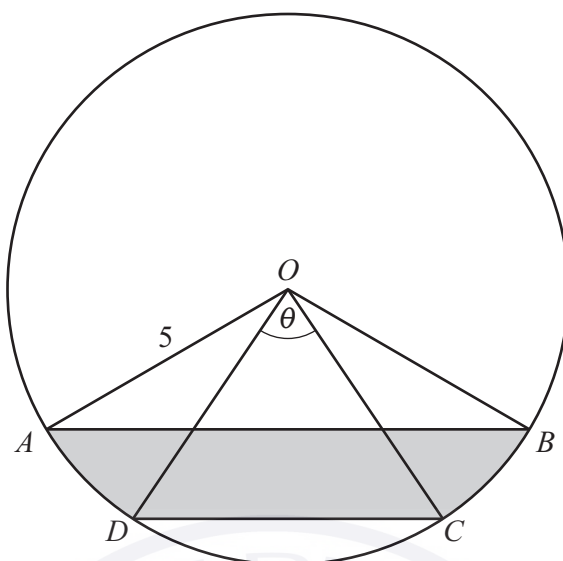




- (c) Find $\cot DBC$, giving your answer in the form $r\sqrt{7} + s$, where r and s are simplified rational numbers. [3]



- 6 In this question, all lengths are in metres and all angles are in radians.



The diagram shows a circle with centre O and radius 5. The points A , B , C and D lie on the circumference of the circle. Angle $DOC = \theta$. Angle $AOD = \text{angle } COB = 0.5$. The length of the minor arc DC is 3.75.

- (a) Show that $\theta = 0.75$. [1]

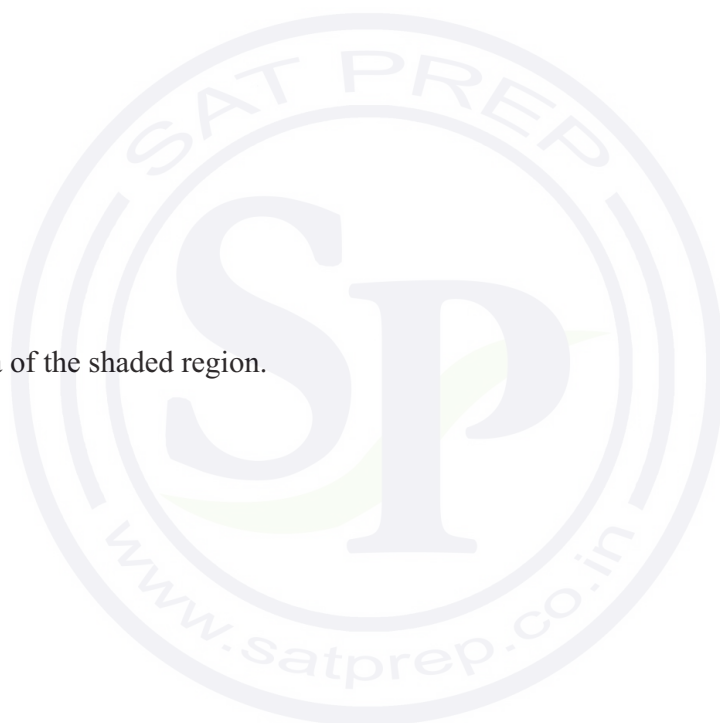
- (b) Find the perimeter of the shaded region. [5]





(c) Find the area of the shaded region.

[3]



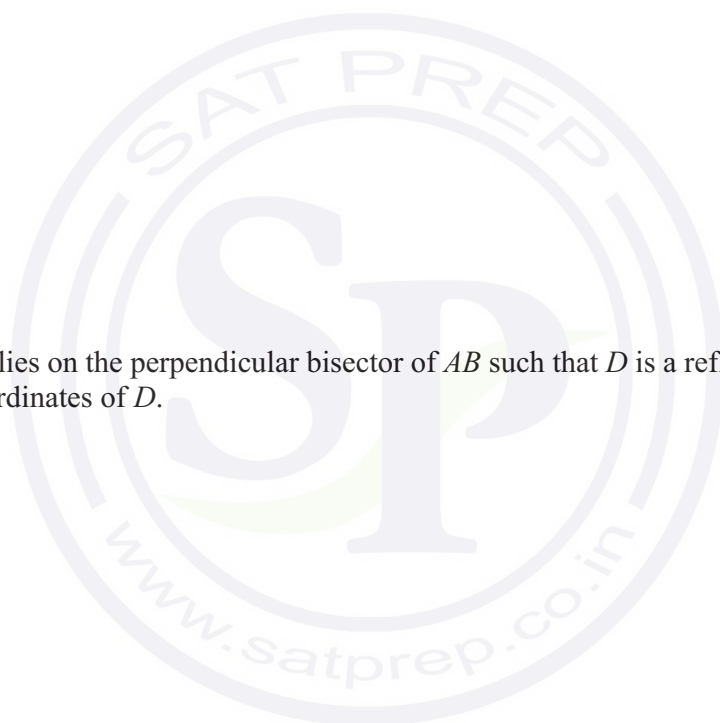


- 7 (a) The line $y = 3x - 2$ intersects the curve $2x^2 - xy + y^2 = 2$ at the points A and B . The point C with coordinates $\left(k, \frac{7}{8}\right)$ lies on the perpendicular bisector of the line AB . Find the exact value of k . [9]





- (b) The point D lies on the perpendicular bisector of AB such that D is a reflection of C in the line AB . Find the coordinates of D . [2]

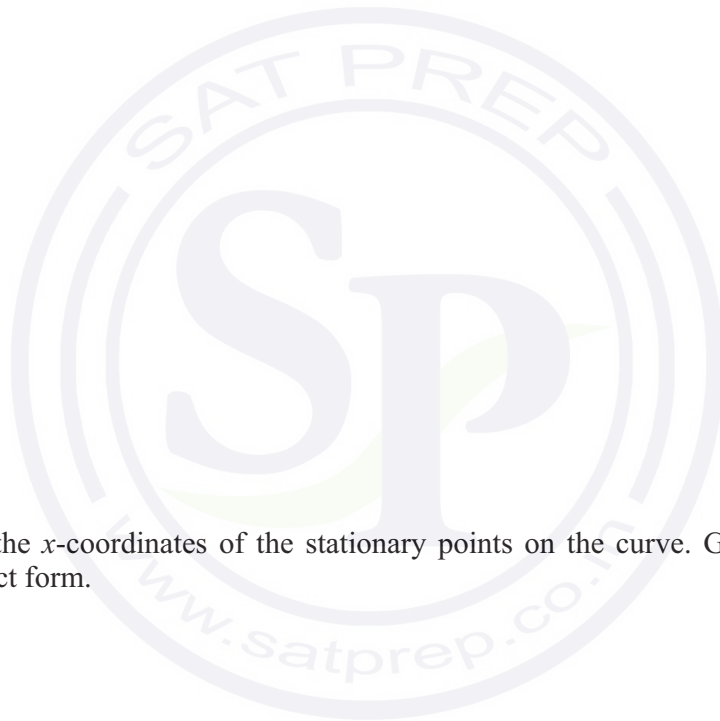




8 A curve has equation $y = \frac{(3x^2 - 5)^{\frac{1}{3}}}{x + 4}$.

(a) Show that $\frac{dy}{dx}$ can be written in the form $\frac{Ax^2 + Bx + C}{(3x^2 - 5)^{\frac{2}{3}}(x + 4)^2}$, where A , B and C are integers. [5]

(b) Hence find the x -coordinates of the stationary points on the curve. Give your answers in their simplest exact form. [3]



9 In this question, all distances are in metres and time, t , is in seconds.

A particle P moves with a speed of 14.5 parallel to the vector $\begin{pmatrix} -20 \\ 21 \end{pmatrix}$.

(a) Find the velocity vector of P .

[2]

Initially, P has position vector $\begin{pmatrix} 3 \\ 5 \end{pmatrix}$.

(b) Write down the position vector of P at time t .

[2]

A second particle Q has position vector $\begin{pmatrix} -1 \\ 3 \end{pmatrix} + \begin{pmatrix} -5 \\ 7.5 \end{pmatrix} t$ at time t .

(c) Find, in terms of t , the distance between P and Q at time t . Simplify your answer.

[4]

(d) Hence show that P and Q never collide.

[2]

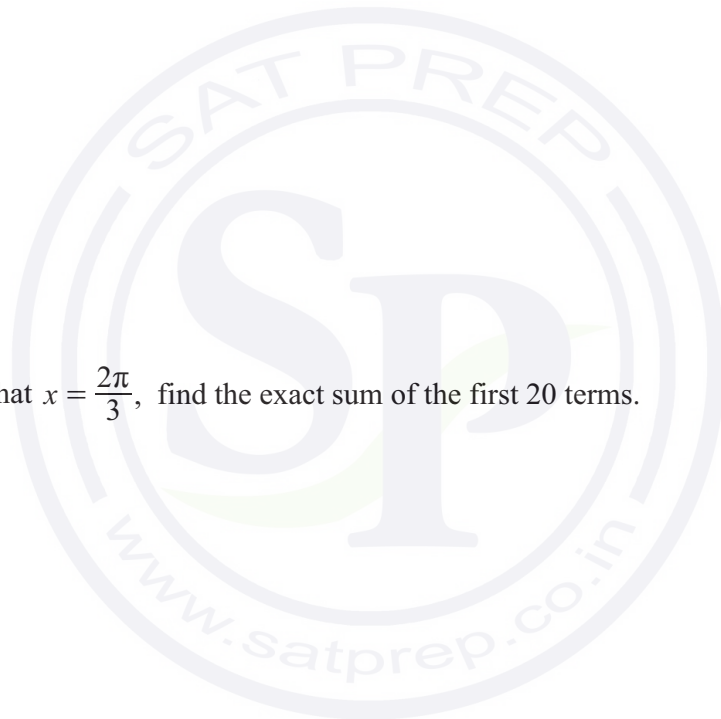




10 (a) The first 3 terms of an arithmetic progression are $3 \sin 2x$, $5 \sin 2x$, $7 \sin 2x$.

- (i) Show that the sum to n terms of this arithmetic progression can be written in the form $n(n+a)\sin 2x$, where a is a constant. [3]

- (ii) Given that $x = \frac{2\pi}{3}$, find the exact sum of the first 20 terms. [2]



(b) The first 3 terms of a geometric progression are $\ln 2y$, $\ln 4y^2$, $\ln 16y^4$.

(i) Find the n th term of this geometric progression.

[2]

(ii) Find the sum to n terms of this geometric progression, giving your answer in its simplest form.

[2]

(c) The first 3 terms of a different geometric progression are $\left(2w - \frac{1}{4}\right)$, $\left(2w - \frac{1}{4}\right)^2$, $\left(2w - \frac{1}{4}\right)^3$.

Find the values of w for which this geometric progression has a sum to infinity.

[3]





11 (a) Given that $y = x^2 \ln x$, find $\frac{dy}{dx}$.

[2]

(b) Hence find $\int x \ln x \, dx$.

[3]



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Mathematical Formulae**1. ALGEBRA***Quadratic Equation*

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a + b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series

$$u_n = a + (n-1)d$$

$$S_n = \frac{1}{2}n(a + l) = \frac{1}{2}n\{2a + (n-1)d\}$$

Geometric series

$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \quad (r \neq 1)$$

$$S_\infty = \frac{a}{1-r} \quad (|r| < 1)$$

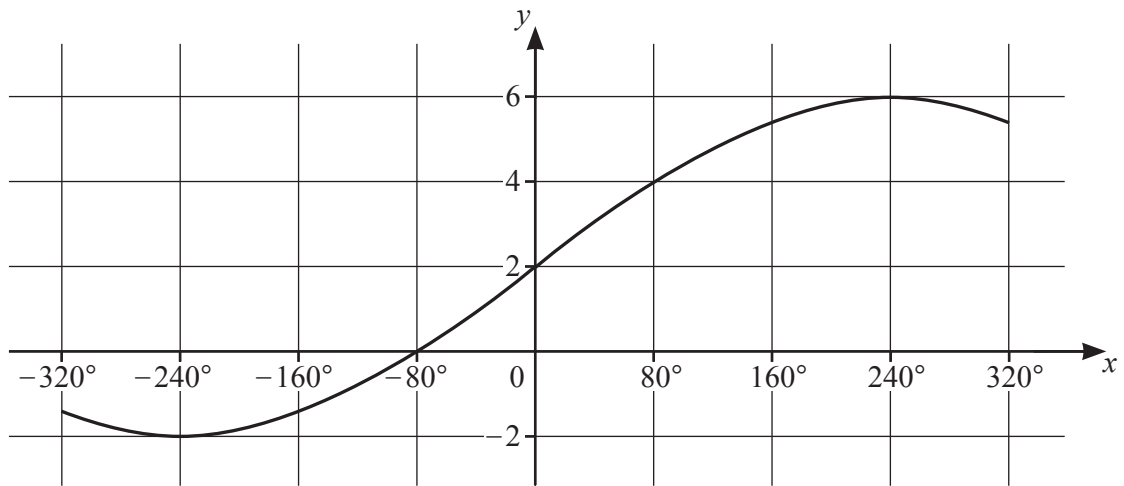
2. TRIGONOMETRY*Identities*

$$\begin{aligned}\sin^2 A + \cos^2 A &= 1 \\ \sec^2 A &= 1 + \tan^2 A \\ \operatorname{cosec}^2 A &= 1 + \cot^2 A\end{aligned}$$

Formulae for $\triangle ABC$

$$\begin{aligned}\frac{a}{\sin A} &= \frac{b}{\sin B} = \frac{c}{\sin C} \\ a^2 &= b^2 + c^2 - 2bc \cos A \\ \Delta &= \frac{1}{2}bc \sin A\end{aligned}$$

1

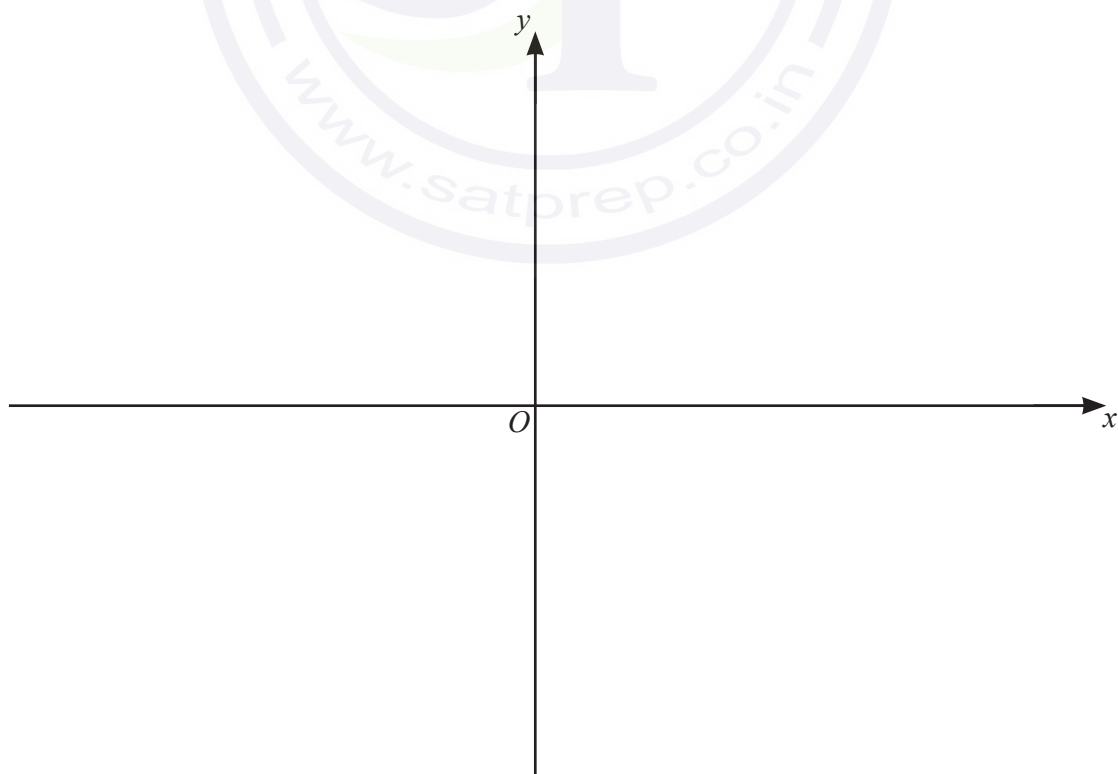


The diagram shows the graph of $y = a \sin bx + c$, for $-320^\circ \leq x \leq 320^\circ$, where a , b and c are constants. Find the values of a , b and c . [3]

- 2 Solve the equation $3(2^{2x+1}) - 11(2^x) + 3 = 0$, giving your answers correct to 2 decimal places. [4]

- 3 (a) Find the coordinates of the stationary points on the curve $y = (2x + 1)^2(x - 3)$. [4]

- (b) On the axes, sketch the graph of $y = (2x + 1)^2(x - 3)$, stating the intercepts with the axes. [3]



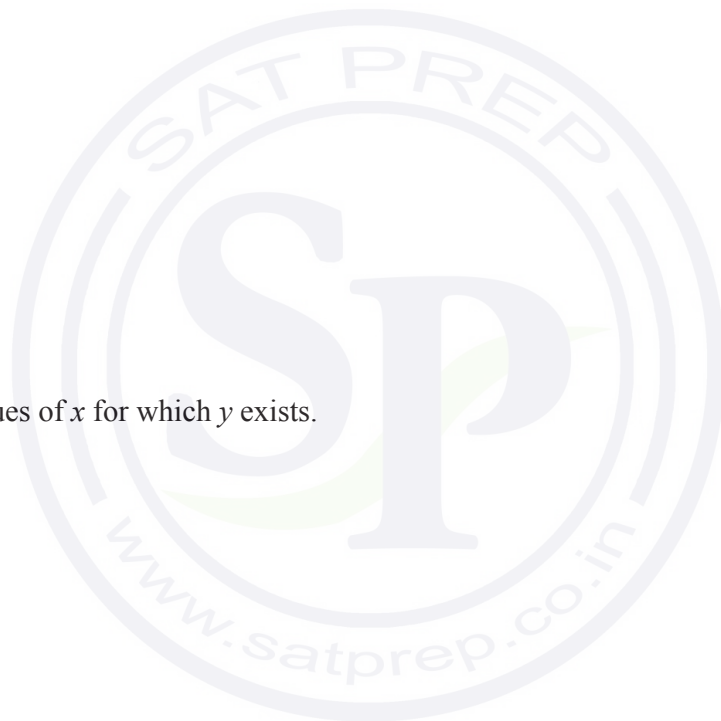
- (c) Write down the values of k for which the equation $(2x+1)^2(x-3) = k$ has exactly one solution. [2]

- 4 Find $\int_0^2 (1 + e^{2x})^2 dx$, giving your answer in exact form. [5]



- 5 When e^{2y} is plotted against x^3 , a straight line graph that passes through the points (2, 5) and (6.4, 7.2) is obtained.
- (a) Find y in terms of x . [4]

- (b) Find the values of x for which y exists. [2]



6 It is given that $y = \frac{\ln(2x^2 + 1)}{x + 2}$, $x \neq -2$.

(a) Find $\frac{dy}{dx}$. [3]

(b) Given that x increases from 1 to $1 + h$, where h is small, find the approximate corresponding change in y . [2]

(c) When $x = 1$, the rate of change in y is 3 units per second. Find the corresponding rate of change in x . [2]

- 7 (a) A 6-digit number is to be formed using the digits 0, 1, 2, 3, 4, 5, 6, 7, 8, 9. The 6-digit number cannot start with 0. Each digit can be used at most once in any 6-digit number. Find how many of these 6-digit numbers are divisible by 5. [3]

- (b) The number of combinations of $(n + 1)$ objects taken 13 at a time is equal to 16 times the number of combinations of n objects taken 12 at a time. Find the value of n . [3]

- 8 The line L is the normal to the curve $y = 3(5x+6)^{\frac{1}{2}}$ at the point where $x = 2$. The point $(-2, k)$, where k is a constant, lies on L . Find the exact value of k . [7]



- 9 In this question, all lengths are in metres, and time, t , is in seconds.

A particle P moves in a straight line such that, t seconds after leaving a fixed point O , its displacement, s , is given by $s = 4t - 4\cos 2t + 4$.

- (a) Find the velocity, v , of P at time t . [2]

- (b) On the axes, sketch the velocity–time graph for P for $0 \leq t \leq \pi$, stating the intercepts with the axes in exact form. [5]



(c) Find the acceleration of P at time t .

[1]

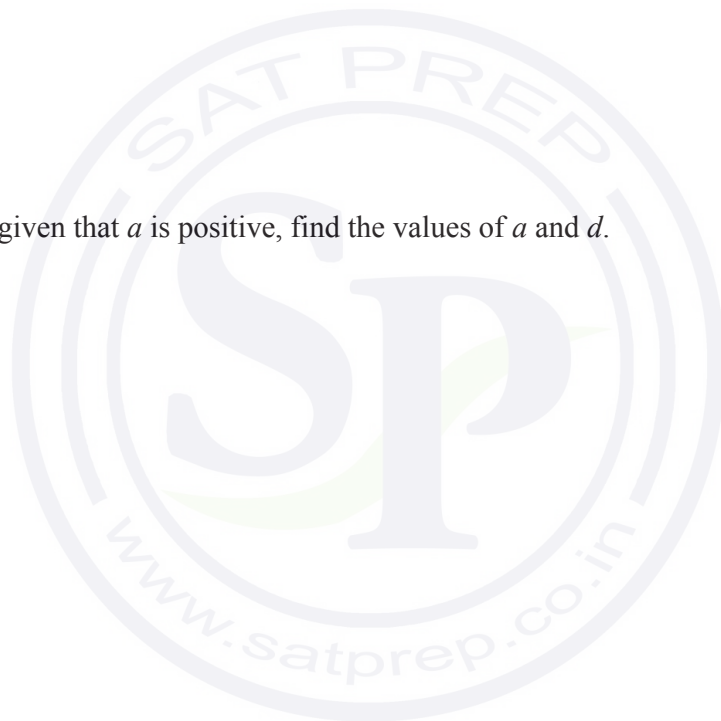
(d) Find the times when the acceleration of P is zero for $0 \leq t \leq \pi$. Give your answers in terms of π .
[2]



- 10 (a) In an arithmetic progression, the first term is a and the common difference is d . The sum of the first three terms of this arithmetic progression is 42. The product of the first three terms of this arithmetic progression is -6720 .

(i) Show that $a(a+2d) = -480$. [3]

(ii) Hence, given that a is positive, find the values of a and d . [4]



- (b) In a geometric progression, the 3rd term is $\frac{e^{4x}}{4}$ and the 10th term is $\frac{e^{11x}}{512}$. Find the first term and the common ratio. [5]



- 11 Solve the following simultaneous equations, giving your answers in exact form.

$$8 \log_3 x + 12 \log_{81} y = 5$$

$$4 \log_9 x + 3 \log_3 y = 2$$

[6]



- 12 Solve the equation $\sec\left(3\theta - \frac{\pi}{2}\right) = 2$ for $-\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$. Give your answers in exact form. [5]



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Cambridge IGCSE™

ADDITIONAL MATHEMATICS**0606/12**

Paper 1

February/March 2024

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the February/March 2024 series for most Cambridge IGCSE, Cambridge International A and AS Level components, and some Cambridge O Level components.

This document consists of **8** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptions for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics-Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

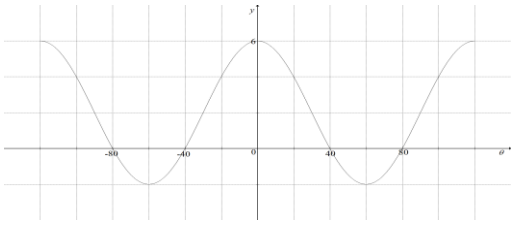
Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(a)	4	B1	
1(b)	120°	B1	
1(c)		3	To score marks, must have minimum points in the correct quadrants and symmetry about the y-axis. B1 for correct θ intercepts $\pm 40^\circ$, $\pm 80^\circ$ and no others B1 for y-intercept of 6 B1 for a completely correct shape with no errors.
2(a)	$\log_p \frac{12a}{6} = \log_p 4^3$ soi	2	B1 for correct use of addition and subtraction rule B1 for correct use of power rule
	$a = 32$	B1	
2(b)	$4\log_3 x = \frac{9}{\log_3 x}$ or $\frac{4}{\log_x 3} = 9\log_x 3$ soi	B1	For change of base
	$(\log_3 x)^2 = \frac{9}{4}$ or $(\log_x 3)^2 = \frac{4}{9}$ soi	B1	
	$x = 3^{\pm 1.5}$ or exact equivalents	2	B1 for each solution
3	$\frac{3x^2}{x^3 + 3}$	B1	
	When $x = 1$, $\frac{dy}{dx} = \frac{3}{4}$ oe	M1	For finding the value of <i>their</i> $\frac{dy}{dx}$
	$y = \ln 4$	B1	
	$y - \ln 4 = -\frac{4}{3}(x - 1)$	2	M1 for attempt at normal equation using <i>their</i> $\frac{dy}{dx}$ and <i>their</i> y Allow A1 if $c = \frac{4}{3} + \ln 4$ seen
	$\left(\frac{4 + 3\ln 4}{7}, \frac{4 + 3\ln 4}{7} \right)$	2	M1 dep for attempt to use $y = x$ and obtain at least one solution
4(a)	$f > 2$	B1	
4(b)	$f^{-1}(x) = -\frac{1}{3}\ln(x - 2)$ or $\frac{1}{3}\ln\left(\frac{1}{x - 2}\right)$ isw	2	M1 for a complete attempt at inverse, allow sign slip but brackets must be used correctly.

Question	Answer	Marks	Guidance
4(c)		4	B1 for correct $y = f(x)$ with y -intercept of 3. Must have correct asymptotic behaviour and be in the first and second quadrant. B1dep for correct reflection of $y = f(x)$ to obtain $y = f^{-1}(x)$ with x -intercept of 3. Must have correct asymptotic behaviour and be in the first and fourth quadrant. B1 for asymptote of $y = 2$ stated or drawn through $y = 2$, must have a correctly shaped $y = f(x)$ B1 for asymptote of $x = 2$ stated or drawn or drawn through $x = 2$, must have a correctly shaped $y = f^{-1}(x)$
4(d)	$(2 + e^{-3x})^{\frac{3}{2}} + 4$ soi	B1	For correct order
	$2 + e^{-3x} = 4$	M1	For forming an equation, must be correct order
	$x = -\frac{1}{3} \ln 2$	2	M1 dep for correct attempt to solve for x .
5(a)	$p'(x) = 15x^2 + 2ax + 39$ soi	B1	
	$p'(-3): 135 - 6a + 39 = 0$ oe	B1	
	$p(-3): -135 + 9a - 117 + b = 0$ oe	B1	
	$a = 29$	B1	
	$b = -9$	B1	
5(b)	$[(x+3)](5x^2 + 14x - 3)$	2	M1 for attempt by any valid method, to obtain a quadratic with 2 correct terms or correct follow through on <i>their a and b</i> .
	$x = -3, \frac{1}{5}$	A1	For both

Question	Answer	Marks	Guidance
5(c)	$\operatorname{cosec} 2\theta = -3$ soi	B1	
	$\sin 2\theta = -\frac{1}{3}$ $2\theta = -19.47^\circ, 199.47^\circ, 340.53^\circ, 559.47^\circ,$ 700.53° $\theta = 99.7^\circ, 170.3^\circ, 279.7^\circ, 350.3^\circ$	4	M1 a correct double angle M1 for correct order of operations to obtain one correct solution. May be implied by e.g. a correct solution or $\theta = -9.7^\circ$ or a correct angle in radians A1 for 2 correct solutions A1 for a further 2 correct solutions and no extra solutions within the range
6(a)(i)	$300 + \frac{1}{2}(10 + V)40 + \frac{1}{2}50V = 2750$ or $700 + \frac{1}{2}(40 \times (V - 10)) + \frac{1}{2}50V = 2750$ oe	M1	Allow one slip, but must be considering complete area
	$V = 50$	A1	
6(a)(ii)	-1 nfww	2	M1 FT <i>their</i> V for a correct gradient calculation
6(b)(i)	$\left(\frac{dv}{dt} =\right) t\left(\frac{1}{2} \times 2t \times (t^2 + 5)^{-\frac{1}{2}}\right) + (t^2 + 5)^{\frac{1}{2}}$ soi	3	B1 for $\frac{1}{2} \times 2t \times (t^2 + 5)^{-\frac{1}{2}}$ M1 for a correct attempt at a product A1 for all correct apart from $\frac{1}{2} \times 2t \times (t^2 + 5)^{-\frac{1}{2}}$
	$\frac{13}{3}$	A1	
6(b)(ii)	There is no change of sign for v as v is always positive, so no change in direction. oe	B1	
7(a)	$a(5x - 2)^{\frac{1}{3}}$	M1	
	$\frac{3}{5}(5x - 2)^{\frac{1}{3}}$ oe	A1	
	$\frac{3}{5}\left(18^{\frac{1}{3}} - 2\right)$ or exact equivalent	2	Dependent M1 for correct use of limits

Question	Answer	Marks	Guidance
7(b)	$2\ln(2x+1)$ oe	B1	
	$-\frac{4}{2x+1}$ oe	B1	
	$\left(2\ln 2 - \frac{4}{2}\right) - (-4)$	M1	For correct substitution of limits, must be using the form $a\ln(2x+1) + \frac{b}{2x+1}$
	$\ln 4 + 2$	2	A1 for each term
8(a)(i)	15 120	B1	
8(a)(ii)	Total: 3780	3	B1 : Starts with 5, 7 or 9: 2520 soi B1 : Starts with 6 or 8: 1260 soi
	Alternative		
	Total: 3780	(3)	B1 : Ends with 2 or 4: 2100 soi B1 : Ends with 6 or 8: 1680 soi
8(b)	2 nurses, 2 dentists, 5 doctors = 36 2 nurses, 3 dentists, 4 doctors = 60 2 nurses, 4 dentists, 3 doctors = 20	2	M1 for two correct cases
	Total = 116	A1	
	Alternative		
	1 dentist only = 4 No nurses = 10 1 nurse only = 90	(M1)	
	Total = 116	(2)	M1 for attempt to subtract at least 2 correct cases from 220
9(a)(i)	$d = 3\lg \theta$	B1	
	$\frac{n}{2}(2(2\lg \theta) + (n-1)3\lg \theta) = 4732\lg \theta$	M1	For use of the sum formula to obtain an equation in $\lg \theta$ only, using <i>their</i> a and d and $4732\lg \theta$
	$3n^2 + n - 9464 = 0$	A1	
	$n = 56$ only	2	M1 for attempt to solve <i>their</i> quadratic equation in n
9(a)(ii)	0.001 oe	B1	

Question	Answer	Marks	Guidance
9(b)(i)	$r = \frac{1}{3}$ so i	B1	
	$ r < 1$ oe, so has a sum to infinity	B1	Dep on previous B1
9(b)(ii)	n th term $(\lg \phi^3) \left(\frac{1}{3}\right)^{n-1}$	B1	
	$3^{2-n} \lg \phi$	2	B1 for $(3 \lg \phi) 3^{1-n}$ or $\frac{3 \lg \phi}{3^{n-1}}$
9(b)(iii)	10	B1	





Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/11

Paper 1

October/November 2023

MARK SCHEME

Maximum Mark: 80

Published

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- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Mathematics-Specific Marking Principles

- 1 Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
- 2 Unless specified in the question, non-integer answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
- 4 Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

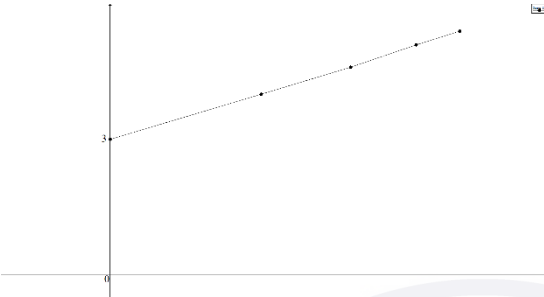
- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

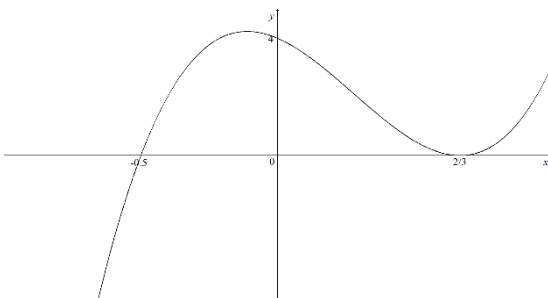
When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfwf	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$a = 4$	B1	
	$b = 3$	B1	
	$c = -5$	B1	
2(a)	$c = 0$	B1	
	$P\left(-\frac{1}{2}\right): a + 4b = -34$ oe	B1	Allow multiples but must be in terms of a , b and one numeric term.
	$P'(x) = 3ax^2 - 22x + b$ $P'(2) = 12a - 44 + b$ soi	M1	For attempt to differentiate and substitute in $x = 2$
	$12a + b = 62$	A1	Allow multiples but must be in terms of a , b and one numeric term.
	$a = 6, b = -10$	2	M1 dep for attempt to solve <i>their</i> simultaneous equations. A1 for both
2(b)	$x(6x^2 - 11x - 10)$	M1	For $x((\text{their } a)x^2 - 11x + \text{their } b)$
	$x(3x + 2)(2x - 5)$	A1	
3(a)	$\pm \begin{pmatrix} -5 \\ 12 \end{pmatrix}$	B1	
	$\begin{pmatrix} -5 \\ 12 \end{pmatrix}$	B1	
3(b)	13	B1	FT on <i>their</i> (a)
3(c)	$3(\text{their } \overrightarrow{AB}) = 2\overrightarrow{OX} - 2\begin{pmatrix} 2 \\ -6 \end{pmatrix}$	M1	Condone $3(\text{their } \overrightarrow{AB}) = 2\begin{pmatrix} 2 \\ -6 \end{pmatrix} - 2\overrightarrow{OX}$
	$\begin{pmatrix} -\frac{11}{2} \\ 12 \end{pmatrix}$	A1	

Question	Answer	Marks	Guidance												
4(a)	$\ln y = \ln A + b \ln x$ soi	B1	May be implied by parts (b) and (c)												
	<table><tr><td>$\ln x$</td><td>0</td><td>0.69</td><td>1.1</td><td>1.4</td><td>1.6</td></tr><tr><td>$\ln y$</td><td>3</td><td>4</td><td>4.6</td><td>5.1</td><td>5.4</td></tr></table> 	$\ln x$	0	0.69	1.1	1.4	1.6	$\ln y$	3	4	4.6	5.1	5.4	2	M1 for attempt to plot a correct graph, allow one point error on the graph. A1 All points correct on the graph.
	$\ln x$	0	0.69	1.1	1.4	1.6									
$\ln y$	3	4	4.6	5.1	5.4										
4(b)	Vertical intercept = $\ln A$ (= 3)	M1	Dep on a straight line graph												
	20	A1													
	Gradient = b	M1	Dep on a straight line graph												
	$b = 1.5$ (allow 1.4 to 1.6)	A1													
4(c)	Reading off graph for $\ln x = 1.25$ to obtain $\ln y$ or use of <i>their</i> equation	M1	Dep on a straight line graph												
	$120 \leq y \leq 150$	A1													
5(a)(i)	5040	B1													
5(a)(ii)	2520	B1													
5(a)(iii)	There are 504 codes less than 1000 $5040 - 504 = 4536$	2	M1 for <i>their</i> (i) -504 or $9 \times$ (a product of 3 relevant numbers)												
5(b)	With family: 462	B1													
	Without family: 55	B1													
	Total: 517	B1													
6(a)	$\lg 50x^3$	3	B1 for $\lg x^3$ or $\lg 2$ or $\lg 100$ B1 for $\lg \frac{x^3}{2}$												

Question	Answer	Marks	Guidance
6(b)	$\log_4 a = \frac{1}{\log_a 4}$	B1	
	$2(\log_a 4)^2 - 5\log_a 4 - 3 = 0$	M1	For attempt to obtain a 3-term quadratic equation in $\log_a 4$ and an attempt to solve to obtain $\log_a 4 = \dots$
	$\log_a 4 = -\frac{1}{2}, \log_a 4 = 3$ $a = \frac{1}{16}, a = 4^{\frac{1}{3}}$ oe	3	M1 Dep for dealing with logarithms correctly at least once, to obtain $a = \dots$ A1 for each correct solution nfww.
	Alternative:		
	$\log_a 4 = \frac{1}{\log_4 a}$	(B1)	
	$3(\log_4 a)^2 + 5\log_4 a - 2 = 0$	(M1)	For attempt to obtain a 3-term quadratic equation in $\log_a 4$ and an attempt to solve to obtain $\log_a 4 = \dots$
	$\log_4 a = -2, 3\log_4 a = 1$ $a = \frac{1}{16}, a = 4^{\frac{1}{3}}$ oe	(3)	M1 Dep for dealing with logarithms correctly at least once, to obtain $a = \dots$ A1 for each correct solution nfww.
7(a)	$\frac{dy}{dx} = 2 \times 3 \times (2x+1)(3x-2) + 2(3x-2)^2$	2	M1 for attempt at differentiation of a product, allow one arithmetic error. A1 all correct, allow unsimplified.
	$2(3x-2)(9x+1)$	A1	
7(b)	$\left(\frac{2}{3}, 0\right)$	B1	Must be from a correct derivative
	$\left(-\frac{1}{9}, \frac{343}{81}\right)$ or $\left(-\frac{1}{9}, 4.23\right)$	B1	
7(c)		3	B1 for a correct cubic shape with a maximum in the second quadrant. B1 for $-\frac{1}{2}$ and $\frac{2}{3}$, must have a cubic shape B1 for 4 must have a cubic shape

Question	Answer	Marks	Guidance
7(d)	$0 < k < \frac{343}{81}$ or $0 < k < 4.23$	2	B1 for critical values 0 and <i>their</i> 4.23 or $\frac{343}{81}$
8	$4x^2 - 6x - 5 = 1 - 4x$ oe $2x^2 - x - 3 = 0$ oe	2	M1 for attempt to eliminate y and simplify to a 3-term quadratic equation = 0. A1 for a correct equation.
	Correct attempt to solve <i>their</i> quadratic equation to obtain 2 values for x or for y	M1	
	$x = -1, \frac{3}{2}$	A1	
	$y = 5, -5$	A1	
	$\frac{dy}{dx} = 8x - 6$ When $x = \frac{3}{2}, \frac{dy}{dx} = 6$	M1	For finding the value of $\frac{dy}{dx}$ using <i>their</i> $x = \frac{3}{2}$
	Equation of tangent: $y = 6x - 14$	2	Dep M1 for attempt to find the equation of the tangent using <i>their</i> $x = \frac{3}{2}$ and <i>their</i> $y = -5$. A1 allow unsimplified.
	$5 = 6x - 14$ oe	M1	For use of <i>their</i> $y = 5$ in <i>their</i> tangent equation
	$x = 3.17$	A1	
9(a)(i)	$-3 \tan \frac{\theta}{2} + 11 \left(2 \tan \frac{\theta}{2} \right) = \frac{19\sqrt{3}}{3}$	2	M1 for use of 12th term with <i>their</i> common difference. A1 allow unsimplified.
	$\tan \frac{\theta}{2} = \frac{\sqrt{3}}{3}$ $\theta = \frac{\pi}{3}$	2	Dep M1 for correct attempt to solve <i>their</i> $\tan \frac{\theta}{2} = \frac{\sqrt{3}}{3}$
9(a)(ii)	$\frac{10}{2} \left(2 \left(-3 \times \frac{\sqrt{3}}{3} \right) + 9 \left(2 \times \frac{\sqrt{3}}{3} \right) \right)$ oe	M1	For the use of the sum to 10 terms using <i>their</i> $\tan \frac{\theta}{2} = \frac{\sqrt{3}}{3}$
	$20\sqrt{3}$	A1	

Question	Answer	Marks	Guidance
9(b)(i)	Common ratio = $4 \sin^2 \phi$	B1	
	$1 + 4 \sin^2 \phi = 4$	M1	For use of $1 + \text{their } r = 4$
	$\sin \phi = \pm \frac{\sqrt{3}}{2}$ $\phi = \pm \frac{\pi}{3}$	2	M1 for a correct attempt to solve <i>their</i> $\sin \phi = \pm \frac{\sqrt{3}}{2}$ to obtain at least one solution.
9(b)(ii)	Common ratio = 3 soi	M1	For attempt to find numerical value of <i>their</i> common ratio.
	$3 > 1$ so no sum to infinity [as $-1 < r < 1$ to have a sum to infinity.] oe	A1	Must have correct common ratio.
10(a)	$\frac{(x-4) \left(\frac{1}{2} \times 6x(3x^2-2)^{-\frac{1}{2}} \right) - (3x^2-2)^{\frac{1}{2}}}{(x-4)^2}$	3	B1 for $\frac{1}{2} \times 6x(3x^2-2)^{-\frac{1}{2}}$, allow unsimplified. M1 for a correct attempt to differentiate a quotient. A1 for all other terms correct.
	$\frac{(3x^2-2)^{-\frac{1}{2}}}{(x-4)^2} (3x(x-4) - (3x^2-2))$	M1	For a correct attempt to simplify to obtain the given form.
	$\frac{-12x+2}{\sqrt{3x^2-2}(x-4)^2}$	A1	
10(b)	When $x=3$, $\frac{dy}{dx} = \frac{-36+2}{5}$	M1	For attempt using <i>their</i> $\frac{dy}{dx}$
	$-6.8h$	2	Dep M1 for attempt at small changes using their -6.8 . A1 cao



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

October/November 2023

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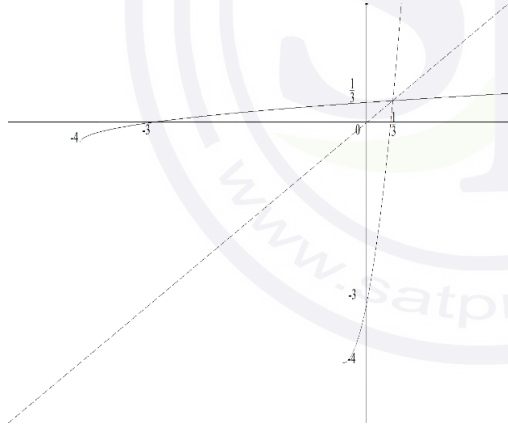
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rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(a)	$(f(x) \text{ or } y =) -3(3x+1)(x-1)(2x-5)$	3	B1 for $k\left(x+\frac{1}{3}\right)(x-1)\left(x-\frac{5}{2}\right)$ and no other work that would gain marks. B2 for $m(3x+1)(x-1)(2x-5)$ and no other work that would gain marks.
1(b)	$-\frac{1}{3} < x < 1$	B1	Must be in terms of x
	$x > \frac{5}{2}$	B1	Must be in terms of x
2(a)	5	B1	
2(b)	480°	B1	
2(c)		3	<p>To obtain any marks the graph must be a curve with one min in the third quadrant and one max in the first quadrant.</p> <p>B1 for the shape, starting in the 3rd quadrant and ending in the 1st quadrant. Must cross the x-axis only once, between 0° and 60°. Must extend for the complete domain starting with $-6 < y < -5$ and ending with $1 < y < 2$</p> <p>B1 for passing through $(0, -2)$</p> <p>B1 for passing through $(120^\circ, 3)$ and $(-120^\circ, -7)$ soi</p>
3	$\ln(y+2) = mx^2 + c$ soi	B1	
	Either of: $9.37 = 2.25m + c$ $3.92 = 4.75m + c$	M1	For at least one correct equation involving m and c
	$m = -2.18, -\frac{109}{50}$ oe $c = 14.3, 14.28, 14.275, \frac{571}{40}$	2	Dep M1 for attempt to solve for at least one unknown. A1 for both.
	$y = e^{(14.3-2.18x^2)} - 2$ oe	A1	FT on the first M1 for <i>their</i> m and c

Question	Answer	Marks	Guidance
3	Alternative		
	$\ln(y+2) = mx^2 + c$ soi	(B1)	
	Gradient = -2.18 , $-\frac{109}{50}$ oe	(B1)	
	$9.37 = 2.25m + c$ $3.92 = 4.75m + c$	(M1)	Use of a correct equation with <i>their</i> gradient and c
	$c = 14.3, 14.28, 14.275, \frac{571}{40}$	(A1)	
	$y = e^{(14.3-2.18x^2)} - 2$ oe	(A1)	FT on <i>their</i> m and c
4(a)	$n = 16$	B1	
	$+\frac{n(n-1)}{2!}\left((-)\frac{x}{2}\right)^2, {}^nC_2\left((-)\frac{x}{2}\right)^2$ oe $\frac{n(n-1)}{8} = p, p = 30$	2	M1 for attempt at third term allow unsimplified in terms of n or <i>their</i> n , but not just as part of an expansion unless used to find p A1 for p .
	$+\frac{n(n-1)(n-2)}{3!}\left((-)\frac{x}{2}\right)^3, {}^nC_3\left((-)\frac{x}{2}\right)^3$ $\frac{n(n-1)(n-2)}{48} = q, q = -70$	2	M1 for attempt at fourth term, allow unsimplified in terms of n or <i>their</i> n , but not just as part of an expansion unless used to find q A1 for q .
4(b)	${}^6C_4\left(\frac{2}{x^2}\right)^2\left(\frac{x}{3}\right)^4$	B1	For identifying the correct term and attempting to evaluate.
	$\frac{20}{27}$	B1	
5	$\cos\left(2\theta + \frac{\pi}{6}\right) = (\pm)\frac{\sqrt{3}}{2}$ oe or $\tan\left(2\theta + \frac{\pi}{6}\right) = (\pm)\frac{1}{\sqrt{3}}$ oe	B1	
	$\theta = -\frac{\pi}{6}, 0, \frac{\pi}{3}$ oe	4	M1 for a correct order of operations, may be implied by one correct solution. A1 for 1 correct solution. A1 for a 2nd correct solution A1 for a 3rd correct solution with no extra solutions in the range. All solutions must be from correct working.

Question	Answer	Marks	Guidance
6(a)	$c = 12$	B1	
	$p\left(\frac{1}{3}\right): \frac{a}{27} + \frac{b}{9} + \frac{c}{3} - 5 = 0$ soi	M1	Allow one arithmetic or sign error, may substitute in their c .
	$p(2): 8a + 4b + 2c - 5 = 95$	M1	Allow one arithmetic or sign error, may substitute in their c .
	$a + 3b = 27$ or $\frac{a}{27} + \frac{b}{9} = 1$ oe	A1	Allow multiples but c needs to have been eliminated and terms with powers evaluated.
	$2a + b = 19$ oe	A1	Allow multiples but c needs to have been eliminated
	$a = 6, b = 7$	2	M1, dep on at least one previous M1 , for attempt to solve <i>their</i> equations in a and b only, to find a or b . A1 for both a and b .
6(b)	$(3x - 1)(2x^2 + 3x + 5)$ cao	2	M1 for attempt at 2 terms in <i>their</i> quadratic factor. A1 for both factors.
	For $2x^2 + 3x + 5 = 0$, discriminant is less than zero, so no solutions. [Only solution is $x = \frac{1}{3}$.]	B1	Allow other valid arguments, but must be using a correct quadratic factor and an attempt to evaluate the discriminant
7(a)(i)	136 080	B1	
7(a)(ii)	(End in 0) $15\,120$ or 9P_5 or $9 \times 8 \times 7 \times 6 \times 5$	B1	
	(End in 5) $13\,440$ or $8 \times {}^8P_4$ or $8 \times 8 \times 7 \times 6 \times 5$	B1	
	Total: 28 560	B1	
	Alternative 1		
	(Does not start with 5:) $26\,880$ or $16 \times {}^8P_4$	(B1)	
	(Starts with 5:) $1\,680$ or 8P_4	(B1)	
	Total: 28 560	(B1)	

Question	Answer	Marks	Guidance
7(a)(ii)	Alternative 2		
	(Number not divisible by 5): $107\,520$ or $8 \times 8 \times {}^8P_4$	(B1)	
	$136\,080 - 107\,520$	(B1)	FT on <i>their</i> 136080
	Total: 28560	(B1)	
7(b)(i)	346104	B1	
7(b)(ii)	18	B1	Do not isw subsequent work
7(b)(iii)	the number of committees with no dentists: 11 440	M1	Allow attempts at 7 options, but must have all of them: 8, 448, 6720, 39 200, 101 920, 122 304 and 64 064
	334664	A1	May come from ${}^{24}C_7 - {}^{16}C_7$
8(a)(i)	$a = -\frac{1}{3}$ or $x \geq -\frac{1}{3}$	B1	Allow -0.333 or better Allow a correct recurring decimal
8(a)(ii)	$f \geq -4$	B1	
8(a)(iii)		4	B1 for $y = f(x)$, must have a correct shape (right hand side from the vertex of a quadratic curve), must be a 1:1 function, intersecting each of the x and y axes once, in quadrants 1, 3 and 4. B1, dependent on previous B for passing through $(0, -3)$ and $(\frac{1}{3}, 0)$. B1 dependent on first B1 for $y = f^{-1}(x)$, being a correct reflection of <i>their</i> $y = f(x)$, intersecting each of the x and y axes and $y = f(x)$ once. B1 dependent on previous B for passing through $(-3, 0)$ and $(0, \frac{1}{3})$.
8(b)	$3(\ln(2x^2 + 5)) - 2 (= 4)$	M1	For correct order
	$x = \sqrt{\frac{e^2 - 5}{2}}$ or exact equivalent	2	M1 dep for a correct attempt to deal with logarithms and obtain $x = \dots$ Allow one arithmetic or sign slip.

Question	Answer	Marks	Guidance
9	$12\left(x^{\frac{2}{3}}\right)^2 - 11\left(x^{\frac{2}{3}}\right) - 5 = 0$	B1	For recognition of a 3-term quadratic equation in terms of $x^{\frac{2}{3}}$ or a suitable substitution
	$\left(3x^{\frac{2}{3}} + 1\right)\left(4x^{\frac{2}{3}} - 5\right) = 0$ $x^{\frac{2}{3}} = -\frac{1}{3}, x^{\frac{2}{3}} = \frac{5}{4}$	2	M1 for attempt to solve a 3-term quadratic equation in the form $12u^2 \pm 11u \pm 5 = 0$ to obtain at least one solution in the form $x^{\frac{2}{3}} = \dots$ or 'u' = ... A1 for at least one correct solution.
	$x = 1.4$ only	A1	
10(a)	$27 = 12\theta$ $\theta = \frac{9}{4}$ oe	B1	$\angle AOB = \theta$
	Either $\tan(\pi - \theta) = \frac{CB}{12}$ soi Or $\frac{CB}{\sin(\pi - \theta)} = \frac{12}{\sin\left(\theta - \frac{\pi}{2}\right)}$	M1	Allow with <i>their</i> θ .
	Perimeter = $24 + 27 + 2(14.86\dots)$	M1	Allow with <i>their</i> CB .
	Perimeter = awrt 80.7	A1	From correct working only
10(b)	$\left(\frac{1}{2} \times 12^2 \times \text{their } \theta\right) + (12 \times \text{their } CB)$ 340 oe or 341 oe	3	M1 for each area A1 for awrt 340 or 341
11(a)	$\overrightarrow{AX} = \frac{\mathbf{b}}{2} - \mathbf{a}$	B1	Allow unsimplified
	$\overrightarrow{OZ} = \mathbf{a} + \lambda\left(\frac{\mathbf{b}}{2} - \mathbf{a}\right)$	2	M1 for $\overrightarrow{OZ} = \mathbf{a} + \lambda \times \text{their}\left(\frac{\mathbf{b}}{2} - \mathbf{a}\right)$ Allow unsimplified Mark final answer
11(b)	$\overrightarrow{OY} = \frac{1}{2}(\mathbf{a} + \mathbf{b})$ oe	B1	Allow unsimplified
	$\overrightarrow{OZ} = \frac{\mu}{2}(\mathbf{a} + \mathbf{b})$	B1	FT on <i>their</i> \overrightarrow{OY} , allow unsimplified Mark final answer

Question	Answer	Marks	Guidance
11(c)	$\mathbf{a} + \lambda \left(\frac{\mathbf{b}}{2} - \mathbf{a} \right) = \frac{\mu}{2} (\mathbf{a} + \mathbf{b})$	M1	For equating <i>their</i> final answer for (a) and <i>their</i> final answer for (b) and attempt to equate like vectors at least once to obtain a scalar equation
	$\lambda = \mu = \frac{2}{3}$	2	M1 dep for solving <i>their</i> simultaneous equations to obtain at least one unknown. Each equation must be in terms of λ and μ A1 for both.
11(d)	$\overrightarrow{OZ} = \frac{1}{3}(\mathbf{a} + \mathbf{b})$ oe	B1	Must be from correct work
12(a)	Cannot have the square root of a negative number. oe	B1	Must be a correct statement related to the question. Allow a numerical argument.
12(b)	$\frac{(x-3) \left(\frac{5}{2} \times (5x-2)^{-\frac{1}{2}} \right) - (5x-2)^{\frac{1}{2}}}{(x-3)^2}$ or $(x-3)^{-1} \frac{5}{2} (5x-2)^{-\frac{1}{2}} + \left(-(x-3)^{-2} \right) (5x-2)^{\frac{1}{2}}$	3	B1 for $\frac{5}{2} \times (5x-2)^{-\frac{1}{2}}$ seen M1 for an attempt to differentiate a quotient or correct product A1 for all other terms correct.
	$\frac{(5x-2)^{-\frac{1}{2}}}{2(x-3)^2} (5(x-3) - 2(5x-2))$ oe	M1	Dep for an attempt to simplify to the given form, allow a sign error and an arithmetic error (e.g. Omission of a factor of 2 in the linear term).
	$\frac{-(5x+11)}{2(x-3)^2 \sqrt{5x-2}}$ cao	A1	



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/13

Paper 1

October/November 2023

MARK SCHEME

Maximum Mark: 80

Published

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- the standard of response required by a candidate as exemplified by the standardisation scripts.

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- 3 Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
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- 5 Where a candidate has misread a number or sign in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 A or B mark for the misread.
- 6 Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

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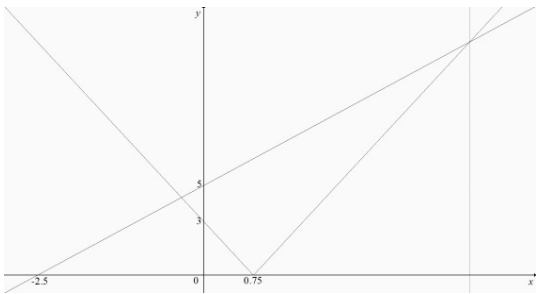
Types of mark

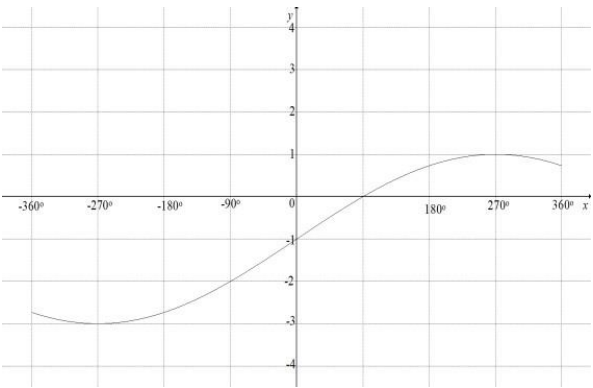
- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

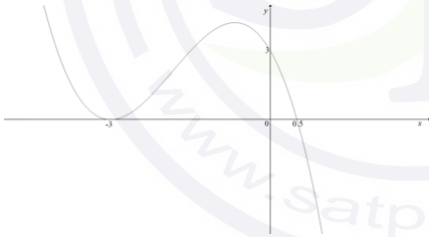
When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

- | | |
|------|----------------------------|
| awrt | answers which round to |
| cao | correct answer only |
| dep | dependent |
| FT | follow through after error |
| isw | ignore subsequent working |
| nfww | not from wrong working |
| oe | or equivalent |
| rot | rounded or truncated |
| SC | Special Case |
| soi | seen or implied |

Question	Answer	Marks	Guidance
1(a)		3	B1 for a V shaped graph with a vertex on the positive x -axis. B1 for 0.75 and 3 marked correctly and dependent on first B1 B1 for a straight line passing through -2.5 and 5 marked correctly, axis with a gradient such that there are two points of intersection. The second point of intersection may be implied.
1(b)	$4x - 3 < 2x + 5$ so $x < 4$	B1	
	$2x + 5 > -4x + 3$ so $x > -\frac{1}{3}$	B1	nfww
	$-\frac{1}{3} < x < 4$	B1	Dependent on both B1 SC2 for the values $-\frac{1}{3}$ and 4 without any or with wrong inequality signs nfww
	Alternative		
	$3x^2 - 11x - 4 < 0$ or $= 0$	(M1)	For squaring each side of the inequality and forming a 3-term quadratic. Allow multiples.
	$-\frac{1}{3}, 4$	(A1)	Critical values
	$-\frac{1}{3} < x < 4$	(A1)	
2	Mid-point $\left(\frac{3}{2}, -\frac{5}{6}\right)$	B1	Do not allow if unsimplified
	Gradient $= -\frac{1}{3}$	B1	Allow unsimplified
	$k + \frac{5}{6} = 3 \times \left(2 - \frac{3}{2}\right)$ oe	M1	For attempt at perpendicular bisector Must be with <i>their</i> perpendicular gradient and <i>their</i> mid-point
	$k = \frac{2}{3}$	A1	

Question	Answer	Marks	Guidance
3		4	B1 for a correct shape, starting in approximately correct places between -2 and -3 and finishing in approximately correct places between 0 and 1 , having an amplitude of 2 and crossing the x -axis only once, on the positive x -axis. B1 for a correct shape and $(0, -1)$ B1 for a correct shape and a max and a min in approximately correct places. $(270^\circ, 1)$ and $(-270^\circ, -3)$ B1 for a correct shape crosses at $(90^\circ, 0)$
4(a)	$P\left(-\frac{1}{2}\right): -\frac{a}{8} + \frac{b}{4} - \frac{3}{2} + 2 = 0$	M1	Allow one arithmetic error. Must be equated to 0 soi Allow unsimplified
	$P(-1): -a + b - 3 + 2 = -6$	M1	Allow unsimplified Must be equated to -6 soi
	$-a + 2b + 4 = 0$ oe $-a + b + 5 = 0$ oe	A1	For both allow unsimplified
	$a = 6, b = 1$	2	M1 dep on at least one previous M1 for attempt to solve <i>their</i> simultaneous equations to find at least one of <i>their</i> unknowns. A1 for both.
4(b)	$(2x+1)(3x^2 - x + 2)$	2	M1 for correct attempt to obtain 2 terms of the quadratic for <i>their</i> $P(x)$. Must divide by $(2x + 1)$ A1 for correct quadratic $(3x^2 - x + 2)$
	For $3x^2 - x + 2$, the discriminant is < 0 so only one real root of $-\frac{1}{2}$ oe	B1	Must have a valid attempt to evaluate the discriminant.
5(a)(i)	30 240	B1	
5(a)(ii)	720	B1	the number of passwords with no symbols. Not part of a product
	29 520	B1	
5(a)(iii)	$(6 \times 5) \times 6 \times (4 \times 3) = 2160$ oe	2	B1 for (6×5) and (4×3) soi

Question	Answer	Marks	Guidance
5(b)	1 of each and 6 police officers = 20	B1	For ${}^4C_1 \times {}^5C_1 \times {}^6C_6$ must be evaluated, could be implied by a correct total
	2 of each and 4 police officers = 900	B1	For ${}^4C_2 \times {}^5C_2 \times {}^6C_4$ must be evaluated, could be implied by a correct total
	3 of each and 2 police officers = 600	B1	For ${}^4C_3 \times {}^5C_3 \times {}^6C_2$ must be evaluated, could be implied by a correct total
	4 of each and no police officers = 5	B1	For ${}^4C_4 \times {}^5C_4$ must be evaluated, could be implied by a correct total
	Total = 1525	B1	
6(a)	$q'(x) = -\frac{1}{3}(2(2x-1)(x+3) + 2(x+3)^2)$ oe	2	M1 for attempt to differentiate, allow one arithmetic slip. A1 – allow unsimplified.
	$\left[q'(x) = -\frac{2}{3} \right] (3x^2 + 11x + 6) = 0$ $x = -3$ and $x = -\frac{2}{3}$	2	Dep M1 for equating <i>their</i> $q'(x)$ to zero and attempt to solve <i>their</i> 3-term quadratic to get two solutions for $x = \dots$ A1 for both x values correct nfww
6(b)		3	B1 for correct cubic shape with maximum point in correct quadrant. B1 for correct cubic shape touching at $(-3, 0)$ and passing through $(0.5, 0)$, intercepts must be marked. B1 for correct cubic shape passing through $(0, 3)$ intercept must be marked.
6(c)	$k < 0$	B1	Condone $y < 0$
	$x = -\frac{2}{3}, y = \frac{343}{81}$ or $y = 4.23$	M1	For finding the value of y at <i>their</i> max point. If incorrect must see substitution of <i>their</i> $x = -\frac{2}{3}$ nfww
	$k > \frac{343}{81}$ or $k > 4.23$	A1	Condone $y > \frac{343}{81}$ or $y > 4.23$

Question	Answer	Marks	Guidance
7	$6\left(x^{\frac{1}{3}}\right)^2 - x^{\frac{1}{3}} - 2 = 0$ <p>or $6m^2 - m - 2 = 0$ where $m = x^{\frac{1}{3}}$ oe</p>	B1	
	$x^{\frac{1}{3}} = \frac{2}{3}, x^{\frac{1}{3}} = -\frac{1}{2} \text{ oe}$	M1	For attempt to solve 3-term quadratic equation in the form $6m^2 \pm m \pm 2 = 0$ and obtain $x^{\frac{1}{3}} = \dots$ or $m = \dots$ from correct work only
	$x = \frac{8}{27}, x = -\frac{1}{8}$	2	Dep M1 for dealing with the power of $\frac{1}{3}$ correctly at least once. A1 for both
8	$(2x)^2 = 256x^{16} \text{ soi } n = 8$	B1	
	$\binom{8}{1}(2x^2)^7 \times \left(-\frac{1}{4x}\right) = ax^{13} \text{ oe}$ <p>leading to $a = -256$</p>	2	M1 for attempt at 2nd term with <i>their</i> n to find a , need to see one step to evaluate. Allow a sign error in simplifying but not missing in $-\frac{1}{4x}$
	$\binom{8}{2}(2x^2)^6 \left(-\frac{1}{4x}\right)^2 = bx^c$ <p>leading to $b = 112$</p>	2	M1 for attempt at 3rd term with <i>their</i> n to find b , need to see one step to evaluate. Allow a sign error but not missing in $\left(-\frac{1}{4x}\right)^2$
	$c = 10$	B1	Can be seen by observation.

Question	Answer	Marks	Guidance
9	$\left[\frac{dy}{dx} = \frac{\frac{5}{3}(5x+2)^{-\frac{2}{3}} \times (x-1)^2 - 2(5x+2)^{\frac{1}{3}}(x-1)}{(x-1)^4} \right]$ or $\left[\frac{dy}{dx} = \frac{5}{3}(5x+2)^{-\frac{2}{3}} \times (x-1)^{-2} + (5x+2)^{\frac{1}{3}} \times -2 \times (x-1)^{-3} \right]$	3	B1 for $\frac{5}{3}(5x+2)^{-\frac{2}{3}}$ M1 for attempt at differentiation of a quotient or product. A1 all other terms correct.
	$\frac{(5x+2)^{\frac{2}{3}}}{3(x-1)^3} (5x-5-30x-12)$	M1	Dep M1 for attempt to simplify by factorising $(5x+2)^{-\frac{2}{3}}$ or $(x-1)$ nfw to the given form, allow one arithmetic slip and/or one sign slip.
	$\frac{-(25x+17)}{3(x-1)^3(5x+2)^{\frac{2}{3}}}$	A1	Must be in correct form.

Question	Answer	Marks	Guidance
10	$40 + 20\theta = 65$	*M1	
	$\theta = 1.25$	A1	
	$\sin\left(\frac{\text{their } \theta}{2}\right) = \frac{\frac{1}{2}AB}{20}$ $AB = 23.4 \text{ or } \frac{1}{2}AB = 11.7$	2	Dep M1 for an attempt to find AB or $\frac{1}{2}AB$
	Either $\tan\left(\frac{\text{their } \theta}{2}\right) = \frac{\text{height of triangle } ACB}{\text{their } \frac{1}{2}AB}$ Height of triangle = 8.44 Area of triangle = 98.8	3	DepM1 for a correct attempt to find the height of the triangle M1 for attempt to find the area of the triangle using <i>their</i> height and <i>their</i> AB A1 must be at least 3 significant figures.
	Or $\cos\left(\frac{\text{their } \theta}{2}\right) = \frac{\text{their } \frac{1}{2}AB}{AC}$ $AC = 14.4$ $\text{Area of triangle} = \frac{1}{2} \times \text{their } AB \times \text{their } AC \times \sin\left(\frac{\theta}{2}\right)$ Area of triangle = 98.8	(3)	DepM1 for a correct attempt to find CA M1 for attempt to find the area of the triangle using the sine rule with <i>their</i> CA . A1 must be at least 3 significant figures.
	Area of the segment = $\frac{1}{2} \times 20^2 \times (1.25 - \sin 1.25)$ Area of the segment = 60.2	B1	
	Area = 38.6	A1	

Question	Answer	Marks	Guidance
10	Alternative 1		
	$40 + 20\theta = 65$	(*M1)	
	$\theta = 1.25$	(A1)	
	$\tan\left(\frac{\text{their } \theta}{2}\right) = \frac{AC}{20}$ oe soi $AC = 14.43$	(2)	DepM1 for a correct attempt to find the AC
	Area of triangle $ACO = \frac{1}{2} \times 20 \times 14.43 = 144.3$	(2)	M1 for a correct attempt to find the area of the triangle using <i>their</i> AC
	Area of the sector = 250	(B1)	
	Area of half shaded region = $(144.3 - 125) \times 2$	(M1)	Dependent on a valid method for finding triangle ACO . Allow use of 144
	Area = 38.6	(A1)	
	Alternative 2		
	$40 + 20\theta = 65$	(*M1)	
	$\theta = 1.25$	(A1)	
	$\sin\left(\frac{\text{their } \theta}{2}\right) = \frac{\frac{1}{2}AB}{20}$ $AB = 23.4$	(2)	Dep M1 for an attempt to find AB or $\frac{1}{2}AB$
	$\tan\left(\frac{\text{their } \theta}{2}\right) = \frac{AC}{20}$ oe soi $AC = 14.43$	(2)	DepM1 for a correct attempt to find AC
	Shaded area = $14.4 \times 20 - \frac{1}{2} \times 20^2 \times \frac{5}{4}$ Area = 38.6	(3)	M1 for area of Kite B1 for area of sector

Question	Answer	Marks	Guidance
10	Alternative 3		
	$40 + 20\theta = 65$	(*M1)	
	$\theta = 1.25$	(A1)	
	$\tan\left(\frac{\text{their } \theta}{2}\right) = \frac{AC}{20}$ oe soi $AC = 14.43$	(2)	DepM1 for a correct attempt to find AC
	Area of triangle AOB $= \frac{1}{2} \times 20^2 \times \sin(\text{their } \theta)$ $= 189.[7969\dots]$	(M1)	
	Area of triangle ACB $= \frac{1}{2} \times \text{their } AC \times \text{their } AB \times \sin \frac{\theta}{2}$ $= 98.8$	(M1)	for a correct attempt to find the area of the triangle using <i>their</i> AC and <i>their</i> AB
	Area of the sector = 250	(B1)	
	Area of half shaded region = area of triangle ACB + area of triangle AOB – area of sector $= 189.8 + 98.8 - 250$	(M1)	
	Area = 38.6	(A1)	

Question	Answer	Marks	Guidance
10	Alternative 4		
	$40 + 20\theta = 65$	(*M1)	
	$\theta = 1.25$	(A1)	
	$\sin\left(\frac{\text{their } \theta}{2}\right) = \frac{\frac{1}{2}AB}{20}$ $AB = 23.4 \text{ or } \frac{1}{2}AB = 11.7$	(2)	Dep M1 for an attempt to find AB or $\frac{1}{2}AB$
	$\tan\left(\frac{\text{their } \theta}{2}\right) = \frac{\text{height of triangle } ACB}{\text{their } \frac{1}{2}AB}$ <p>Height of triangle = 8.44</p>	(M1)	DepM1 for a correct attempt to find the height of the triangle
	<p>Height of triangle ABO</p> $= \sqrt{20^2 - \left(\frac{1}{2}AB\right)^2}$ $= 16.22$	(M1)	for a correct attempt to find to find the height of the triangle
	Area of the sector = 250	(B1)	
	<p>Area of kite</p> $= \frac{1}{2} \times 23.4 \times (16.22 + 8.44)$ $= 288.5$	(M1)	
	Area = $288.5 - 250 = 38.5$	(A1)	
11(a)	$\vec{XY} = -\vec{OX} + \mathbf{a} + \frac{1}{3}\vec{AB} \text{ oe soi}$ <p>or $\vec{XY} = \vec{XB} - \frac{2}{3}\vec{AB} \text{ oe soi}$</p>	M1	
	$\vec{XY} = -\frac{4}{5}\mathbf{b} + \mathbf{a} + \frac{1}{3}(\mathbf{b} - \mathbf{a}) \text{ oe soi}$ <p>or $\vec{XY} = \frac{1}{5}\mathbf{b} + \frac{2}{3}(\mathbf{a} - \mathbf{b}) \text{ oe soi}$</p>	M1	For $\pm\frac{1}{3}(\mathbf{b} - \mathbf{a})$ or $\pm\frac{4}{5}\mathbf{b}$ For $\pm\frac{1}{5}\mathbf{b}$ or $\pm\frac{2}{3}(\mathbf{a} - \mathbf{b})$
	$\vec{XY} = \frac{2}{3}\mathbf{a} - \frac{7}{15}\mathbf{b} \text{ cao}$	A1	AG
11(b)	$\vec{YZ} = \lambda\left(\frac{2}{3}\mathbf{a} - \frac{7}{15}\mathbf{b}\right) \text{ cao}$	B1	

Question	Answer	Marks	Guidance
11(c)	$\vec{YZ} = \mu \mathbf{a} - \frac{1}{3} \vec{AB}$ oe soi	M1	
	$\vec{YZ} = \mu \mathbf{a} - \frac{1}{3} (\mathbf{b} - \mathbf{a})$ oe	A1	Allow unsimplified ISW from correct answer
11(d)	$\mu \mathbf{a} - \frac{1}{3} (\mathbf{b} - \mathbf{a}) = \lambda \left(\frac{2}{3} \mathbf{a} - \frac{7}{15} \mathbf{b} \right)$ soi	M1	For equating <i>their</i> (b) and <i>their</i> (c) and attempt to equate coefficients of a or b at least once.
	$\lambda = \frac{5}{7}$	A1	nfww
	$\mu = \frac{1}{7}$	A1	nfww
12	$\sin\left(\frac{2x}{3} - \frac{\pi}{3}\right) = \pm \frac{\sqrt{3}}{2}$ or $\tan\left(\frac{2x}{3} - \frac{\pi}{3}\right) = \pm \sqrt{3}$	B1	Allow if \pm is missing
	$x = \pi, \frac{3\pi}{2}, \frac{5\pi}{2}, 3\pi$	4	M1dep on B1 for obtaining $\frac{2x}{3} - \frac{\pi}{3} = \frac{\pi}{3}$ or any valid value A1 for one correct solution A1 for a 2nd correct solution A1 for a 3rd and 4th correct solutions and no extras in the range



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/11

Paper 1

May/June 2023

MARK SCHEME

Maximum Mark: 80

Published

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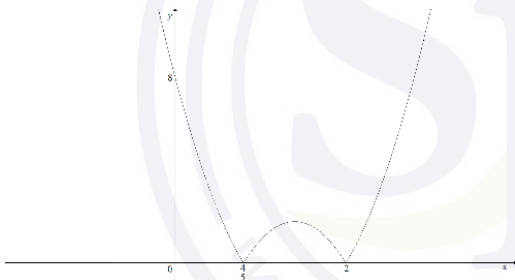
Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

- awrt answers which round to
 cao correct answer only
 dep dependent
 FT follow through after error
 isw ignore subsequent working
 nfwf not from wrong working
 oe or equivalent
 rot rounded or truncated
 SC Special Case
 soi seen or implied

Question	Answer	Marks	Guidance
1(a)	$5\left(x - \frac{7}{5}\right)^2 - \frac{9}{5}$	3	B1 for $5(x \pm b)^2$ B1 for $\left(x - \frac{7}{5}\right)^2$ B1 for $-\frac{9}{5}$
	Alternative By comparing coefficients: $a(x^2 + 2bx + b^2) + c = 5x^2 - 14x + 8$. $2abx = -14x$ $ab^2 + c = 8$	(3)	B1 for $a = 5$ B1 for $b = \frac{-14}{10}$ oe B1 for $c = \frac{-18}{10}$ oe
1(b)	$\left(\frac{7}{5}, -\frac{9}{5}\right)$	2	FTB1 for each, follow through on <i>their</i> a and b from (a) or SC1 if differentiation is used in <i>their</i> (a) or restarted in (b) $\frac{dy}{dx} = 10x - 14 = 0$ then $\left(\frac{7}{5}, -\frac{9}{5}\right)$
1(c)		3	B1 for the correct shape. Must have the parabola part of the curve with maximum in the first quadrant and cusps on the x -axis. Ignore labelling of their maximum point if incorrect coordinates B1 for $\left(\frac{4}{5}, 0\right)$ and $(2, 0)$, must have a correct shape in the first quadrant. B1 for $(0, 8)$ must have a correct shape.
1(d)	$0 < k < \frac{9}{5}$	2	B1FT follow through from 0 and <i>their</i> $-b$ in part (a)
2(a)	$p'(x) = 3ax^2 + 14x + b$ $p''(x) = 6ax + 14$ leading to $3a + 14 = 32$ $a = 6$	2	M1 for attempt to differentiate twice and substitute $x = \frac{1}{2}$

Question	Answer	Marks	Guidance
2(b)	$p\left(\frac{4}{3}\right): 80 + 4b + 3c = 0$ oe	M1	Must have 3 terms. For use of $x = \frac{4}{3}$, at least once and equating to 0 with an attempt at simplification leading to an equation in b and c only Allow one sign error.
	$p(-1): -b + c = 6$ oe	M1	Must have 3 terms. For use of $x = -1$ and equating to 7 with an attempt at simplification leading to an equation in b and c only
	$b = -14, c = -8$	2	M1 dep on both previous M marks and attempt to solve simultaneously to obtain both b and c A1 for both
2(c)	$(3x - 4)(2x^2 + 5x + 2)$	2	B1 for two terms correct in the quadratic factor. Allow if seen as a quotient in long division. For both marks, need to see both factors together. $\left(x - \frac{4}{3}\right)(6x^2 - 15x + 6)$ from synthetic method gets 0 marks unless recovered.
2(d)	$(3x - 4)(2x + 1)(x + 2)$	B1	Must be all integers
3(a)	Mid-point $(6, -5)$	B1	
	Gradient of $AB = -\frac{5}{2}$	B1	
	Perpendicular gradient $\frac{2}{5}$	M1	For <i>their</i> perp gradient
	$-9 + 5 = \frac{2}{5}(x - 6)$ oe $x = -4$	2	Dep M1 for attempt at the equation of the perpendicular bisector with <i>their</i> mid-point and <i>their</i> perpendicular gradient and use of $y = -9$
3(b)	$(16, -1)$	2	B1 for each, FT on 12 – <i>their a</i> for the x -coordinate.
4(a)	Area under graph = 800 $\frac{1}{2}(10 \times 10) + (10 \times 10) + \frac{1}{2}(10(10 + V)) + \frac{15V}{2} = 800$	M1	For attempt to find the area, allow one error and one omission.
	$V = 48$	A1	

Question	Answer	Marks	Guidance
4(b)	$(-)\frac{\text{their } V}{15}$	M1	Allow omission of negative sign.
	$-\frac{16}{5} \text{ ms}^{-2}$ oe	A1	FT on <i>their V</i> but must be negative.
5(a)	$(5\sqrt{3} - 6)^2 + (5\sqrt{3} + 6)^2 - 2(5\sqrt{3} - 6)(5\sqrt{3} + 6)\cos 120^\circ$ soi	M1	For the correct use of the cosine rule Condone missing brackets if intention is clear
	$75 + 36 - 60\sqrt{3} + 75 + 36 + 60\sqrt{3} + 75 - 36$	M1	M1 Dep must see sufficient detail to be sure that a calculator is not being used. This is the minimum acceptable $75 + 36 - 60\sqrt{3} + 75 + 36 + 60\sqrt{3} + 39$
	261	A1	Maybe implied by $\sqrt{261}$
	$3\sqrt{29}$	A1	
5(b)	$\frac{2+5\sqrt{5}}{4} = \frac{1}{2}(3+2\sqrt{5}) \times QR \times \sin 30^\circ$ soi	M1	For the correct use of the area of the triangle. Condone missing brackets if intention is clear
	$\frac{2+5\sqrt{5}}{3+2\sqrt{5}} \times \frac{3-2\sqrt{5}}{3-2\sqrt{5}}$ or $\frac{2+5\sqrt{5}}{3+2\sqrt{5}} \times \frac{-3+2\sqrt{5}}{-3+2\sqrt{5}}$	M1	M1 dep for a correct attempt to rationalise <i>their QR</i> . must be the same two terms in the numerator and denominator to rationalise
	$\frac{6+15\sqrt{5}-4\sqrt{5}-50}{9-20}$ $\frac{11\sqrt{5}-44}{-11}$	M1	M1 dep , must see sufficient detail to be sure that a calculator is not being used. This is the minimum acceptable $\frac{6+15\sqrt{5}-4\sqrt{5}-50}{-11}$
	$4 - \sqrt{5}$	A1	

Question	Answer	Marks	Guidance
6(a)	$\frac{\cos \theta + \frac{\sin \theta}{\cos \theta}}{\frac{1}{\cos \theta}}$ soi	2	B1 for $\tan \theta$ and $\cot \theta$ in terms of \sin and \cos . B1 for $\sec \theta = \frac{1}{\cos \theta}$
	$\frac{\cos^2 \theta + \sin^2 \theta}{\sin \theta \cos \theta} \times \cos \theta$ soi oe	M1	For dealing with the fractions in the numerator.
	$\frac{1}{\sin \theta} \times \operatorname{cosec} \theta$ cso	A1	For correct use of $\cos^2 \theta + \sin^2 \theta = 1$ to obtain the given answer.
	$\frac{\frac{1}{\tan \theta} + \tan \theta}{\frac{1}{\cos \theta}} = \frac{1 + \tan^2 \theta}{\tan \theta} \times \cos \theta$ soi oe	(2)	B1 for $\sec \theta = \frac{1}{\cos \theta}$ M1 for dealing with the fractions in the numerator.
	$\frac{\sec^2 \theta}{\tan \theta} \times \cos \theta$	(B1)	For correct use of $\tan^2 \theta + 1 = \sec^2 \theta$
	$\frac{1}{\sin \theta} \times \operatorname{cosec} \theta$ cso	(A1)	For correct use of $\tan \theta$ and $\sec^2 \theta$ to obtain the given answer.
6(b)	$\left(\frac{1}{\sin \frac{\phi}{3}} \right)^2 = 2$ or $\sin \frac{\phi}{3} = \pm \frac{1}{\sqrt{2}}$ soi or $\tan \frac{\phi}{3} = \pm 1$ soi	B2	B1 for \pm missing
	$-405^\circ, -135^\circ, 135^\circ, 405^\circ$	4	M1 for one correct positive or negative solution of <i>their</i> $\sin \frac{\phi}{3} = k$ A1 for another correct solution M1Dep for one negative or positive solution A1 for another correct solution and no extras in the range.
7(a)(i)	6435	B1	Must be evaluated not just ${}^{15}C_8$
7(a)(ii)	With family of 4: 330	B1	Must be evaluated not just ${}^{11}C_4$ or implied by a correct answer
	Without family of 4: 165	B1	Must be evaluated not just ${}^{11}C_8$ or implied by a correct answer
	Total: 495	B1	

Question	Answer	Marks	Guidance
7(b)	$\frac{(n+9) \times n!}{(n-10)!} = \frac{(n^2 + 243)(n-1)!}{(n-1-9)!}$ $n(n+9) = n^2 + 243$ oe	2	B1 for either ${}^nP_{10} = \frac{n!}{(n-10)!}$ or ${}^nP_{10} = \frac{(n-1)!}{(n-1-9)!}$ B1 dep for $n(n+9) = n^2 + 243$
	$n = 27$	B1	
8(a)	$\frac{(2x+1) \times \frac{1}{3} \times 3(3x-4)^{-\frac{2}{3}} - 2(3x-4)^{\frac{1}{3}}}{(2x+1)^2}$ oe or by using the product rule $\frac{1}{3} \times 3 \times (3x-4)^{-\frac{2}{3}} \times (2x+1)^{-1} + -2 \times (2x+1)^{-2} (3x-4)^{\frac{1}{3}}$	3	B1 for $\frac{1}{3} \times 3 \times (3x-4)^{-\frac{2}{3}}$ oe M1 for an attempt to differentiate a quotient. A1 for all terms other than $\frac{1}{3} \times 3 \times (3x-4)^{-\frac{2}{3}}$ correct. Allow unsimplified.
	$\frac{(3x-4)^{-\frac{2}{3}}}{(2x+1)^2} ((2x+1) - 2(3x-4))$	M1	M1 dep for attempt to factorise, must be in the form $\frac{(3x-4)^{-\frac{2}{3}}}{(2x+1)^2} [(ax+1) - b(3x-4)]$
	$\frac{9-4x}{(2x+1)^2 (3x-4)^{\frac{2}{3}}}$	A1	
8(b)	(2.25, 0.255)	2	B1 FT for <i>their</i> x-coordinate only. Do not allow FT if they score M0 in part (a)
9(a)	$n = 57$ cso	3	B1 for $\frac{n}{2}(2 \ln q + 3(n-1) \ln q)$ oe soi Allow if in indices form i.e.: $\frac{n}{2}(\ln q^2 + (n-1) \ln q^3)$ B1 for $3n^2 - n - 9690 = 0$ oe soi
9(b)	Common ratio = p^{-2x}	B1	Allow unsimplified
	nth term = $p^{3x}(p^{-2x})^{n-1}$ soi	B1	Allow unsimplified
	$p^{(5-2n)x}$	B1	

Question	Answer	Marks	Guidance
9(c)	Common ratio = $\frac{4}{3}\cos^2 3\theta$	B1	Allow unsimplified. Must be convinced it is the common ratio not just writing the first term e.g. $r =$ or seeing $\frac{\frac{16}{9}\cos^4 3\theta}{\frac{4}{3}\cos^2 3\theta}$
	$\frac{4}{3}\cos^2 3\theta(*) - 1$ or $\frac{4}{3}\cos^2 3\theta(*) 1$ or oe soi $\frac{4}{3}\cos^2 3\theta(*) 0$	B1	
	$\cos 3\theta(*) \frac{\sqrt{3}}{2}$ or $\cos 3\theta(*) - \frac{\sqrt{3}}{2}$ or soi $\cos 3\theta(*) 0$	B1	
	$3\theta(*) \frac{5\pi}{6}$ and $3\theta(*) \frac{\pi}{6}$ soi	B1	Seeing $\frac{5\pi}{18}$ or $\frac{\pi}{18}$ implied the first 3 marks
	$\frac{\pi}{18} < \theta < \frac{5\pi}{18}$	B1	
10(a)	$\frac{dy}{dx} = 2 \times 3(3x+1) \ln(3x+1) + \frac{3(3x+1)^2}{3x+1}$ Simplified to: $\frac{dy}{dx} = 3(3x+1)(1 + 2 \ln(3x+1))$	3	B1 for $\frac{3}{3x+1}$ M1 for attempt to differentiate a product A1 for all terms other than $\frac{3}{3x+1}$ correct. Allow unsimplified.
10(b)	$k(3x+1)^2 \ln(3x+1)$ soi	B1	
	$\int (3x+1)dx = \frac{3x^2}{2} + x (+c)$	B1	May be a multiple May be seen as $\frac{1}{3} \times \frac{1}{2} \times (3x+1)^2$
	$\frac{1}{6}(3x+1)^2 \ln(3x+1) - \frac{3x^2}{4} - \frac{x}{2} + c$	B2	B1 for two correct algebraic terms For B2 must have $(+c)$



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

May/June 2023

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2023 series for most Cambridge IGCSE, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

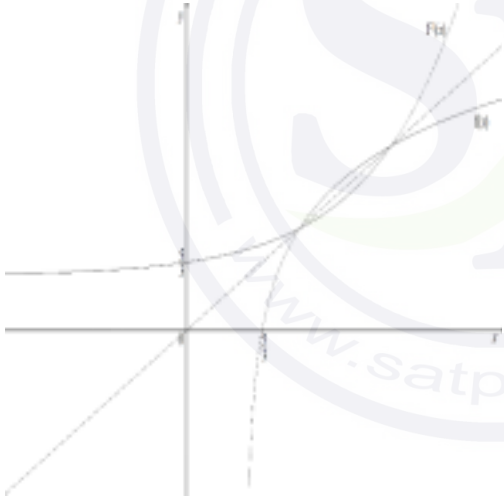
Abbreviations

- awrt answers which round to
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 SC Special Case
 soi seen or implied

Question	Answer	Marks	Guidance
1	$a = 4$	B1	
	$b = \frac{3}{8}$ oe	B1	
	$c = -2$	B1	
2	$(x =) \frac{4 \pm \sqrt{16 + 12(2 + \sqrt{5})(2 - \sqrt{5})}}{2(2 + \sqrt{5})}$ oe with simplification to $\frac{4 \pm \sqrt{16 - k}}{2(2 + \sqrt{5})}$	M1	For attempt to equate to zero and use quadratic formula, must see substitution and $\frac{4 \pm \sqrt{16 - k}}{2(2 + \sqrt{5})}$
	$\frac{4 \pm 2}{2(2 + \sqrt{5})}$ or exact equivalent	2	A1 for one exact solution
	$\frac{3}{2 + \sqrt{5}} \times \frac{2 - \sqrt{5}}{2 - \sqrt{5}}$ or $\frac{1}{2 + \sqrt{5}} \times \frac{2 - \sqrt{5}}{2 - \sqrt{5}}$	M1	For evidence of rationalisation and evaluation
	$-6 + 3\sqrt{5}$ and $-2 + \sqrt{5}$	A1	
	Alternative $((2 + \sqrt{5})x - 3)(x + (2 - \sqrt{5}))$	(B2)	
	$x = -2 + \sqrt{5}$	(B1)	Dep on previous B2
	$\frac{3}{2 + \sqrt{5}} \times \frac{2 - \sqrt{5}}{2 - \sqrt{5}}$ leading to $x = -6 + 3\sqrt{5}$	(2)	M1 for attempt at rationalisation and evaluation
3(a)	$\pm 3(x + 2)(x - 1)(x - 4)$	3	B1 for 3 soi B1 for \pm B1 for $(x + 2)(x - 1)(x - 4)$

Question	Answer	Marks	Guidance
3(b)	$5x - 2 * 4x + 1$ leading to critical value 3	B1	* can be \leq , $=$, \geq
	$5x - 2 * -4x - 1$ oe	M1	* can be \leq , $=$, \geq
	leading to critical value $\frac{1}{9}$	A1	
	$\frac{1}{9} \leq x \leq 3$	A1	Mark final answer
	Alternative $9x^2 - 28x + 3 * 0$	(M1)	Squaring both sides of the inequality and collecting terms, allow one sign error. * can be \leq , $=$, \geq
	$(9x - 1)(x - 3) * 0$	(M1)	Dep for attempt to find two critical values * can be \leq , $=$, \geq
	Critical values $\frac{1}{9}$ and 3	(A1)	
	$\frac{1}{9} \leq x \leq 3$	(A1)	Mark final answer
4(a)	$r\theta = 12$ soi	B1	
	$\frac{1}{2}r^2\theta = 57.6$ soi	B1	
	$r = 9.6$ oe nfww	B1	
	$\theta = 1.25$ oe nfww	B1	
4(b)	$AC = 28.89$	B1	
	Shaded area = $\left(\frac{1}{2} \times 28.89 \times 9.6\right) - 57.6$ soi	M1	Using <i>their AC</i>
	81.1	A1	
	Alternative $OC = 30.45$	(B1)	
	Shaded area = $\left(\frac{1}{2} \times 30.45 \times 9.6 \times \sin 1.25\right) - 57.6$ soi	(M1)	Using <i>their OC</i>
	81.1	(A1)	

Question	Answer	Marks	Guidance
5(a)	$6p^{\frac{2}{3}} - 13p^{\frac{1}{3}} - 5 (= 0)$ soi	B1	May introduce <i>their</i> own variable e.g. x
	$\left(\left(2p^{\frac{1}{3}} - 5 \right) \left(3p^{\frac{1}{3}} + 1 \right) = 0 \right)$ $p^{\frac{1}{3}} = \frac{5}{2} \quad p^{\frac{1}{3}} = -\frac{1}{3}$	M1	For attempt to solve quadratic equation to obtain $p^{\frac{1}{3}} = ..$ or e.g. $x = ...$
	$\frac{125}{8}$ or 15.625 or $15\frac{5}{8}$	A1	Must be simplified and exact
	$-\frac{1}{27}$	A1	Must be simplified and exact
5(b)	$\lg(2x+5)^2$	B1	
	$\lg \frac{(2x+5)^2}{x+2}$	B1	Dep on first B1 , must be a correct statement
	$1 = \lg 10$ soi	B1	
	$\frac{(2x+5)^2}{(x+2)} = k$ oe	M1	Dep on second B mark For correct attempt to obtain a quadratic equation with no log terms, where $k = 1$ or 10
	$4x^2 + 10x + 5 = 0$ $x = \frac{-5 \pm \sqrt{5}}{4}$ or exact equivalent	2	M1 for attempt to solve <i>their</i> quadratic to obtain $x = ...$, implied by decimals of -1.8 or -0.69 or better A1 for both, A0 if one is discarded
6(a)	A correct equation in terms of x and y only	B1	No inverse trig functions
	$y = (x-4)^2 - 3$ or $y = x^2 - 8x + 13$	B1	
6(b)	$\sin\left(2\phi + \frac{3\pi}{4}\right) = \frac{\sqrt{3}}{2}$ soi	B1	May be implied by one correct solution
	$-\frac{5\pi}{24}, -\frac{\pi}{24}, \frac{19\pi}{24}, \frac{23\pi}{24}$ with no extra solutions within the range	4	M1 for explicitly correct order of operations from <i>their</i> $\left(2\phi + \frac{3\pi}{4}\right) = k$, or may be implied by one correct solution A1 for two correct solutions A1 for a third correct solution A1 for a further solution with no extra solutions in the range

Question	Answer	Marks	Guidance
7(a)	${}^{14}C_2 \times {}^{12}C_3 \times {}^9C_4$ oe, soi 2 522 520	3	B1 for a product of 3 combinations (ignore combinations that are equal to 1), one of which must be in the form ${}^{14}C_k$ where $k = 2, 3, 4, 5, 9, 10, 11, 12$ B2 for a correct product of combinations
7(b)(i)	136 080	B1	
7(b)(ii)	15 120	B1	
7(b)(iii)	38 640	3	B1 for 8P_4 or 1680 or $(8 \times 7 \times 6 \times 5)$ B2 for $8 \times {}^8P_4$ (13 440) oe or $15 \times {}^8P_4$ (25 200) oe
8(a)	$(a =) \frac{4}{3}$ or $1.\dot{3}$	B1	Allow a recurring decimal Must not be an inequality in terms of a Allow $x > \frac{4}{3}$
8(b)	$f \in \mathbb{R}$ or $-\infty < f < \infty$ or \mathbb{R}	B1	Allow y or $f(x)$ but not x .
8(c)		4	B1 for a correct shape for $y = f(x)$ in quadrants 1 and 4 B1 for $\left(\frac{5}{3}, 0\right)$, must have a correct shape in either quadrant 1 or quadrant 4 B1 for $y = f^{-1}(x)$, must be a correct shape in quadrants 1 and 2 and intersect twice. B1 for $\left(0, \frac{5}{3}\right)$, must have a reasonable shape for $y = f^{-1}(x)$ in either the first quadrant or the second quadrant
8(d)(i)	$g(g(x)) = 4x - 9$	B1	Must be simplified
8(d)(ii)	$fg(g(x)) = 2\ln(12x - 31)$	M1	allow unsimplified, using <i>their</i> answer to (i)
	$2\ln(12x - 31) = 4$ $x = \frac{e^2 + 31}{12}$	2	Dep M1 for correct order of operations to solve <i>their</i> equation, to get as far as $x = \dots$ Implied by decimal answer of awrt 3.2 A1 Must be exact form.

Question	Answer	Marks	Guidance
9	$\frac{(2x+6)}{3} = 3 + \frac{4}{2x+1}$ $4x^2 - 4x - 15 (= 0)$	2	M1 for equating the line and curve and obtaining a 3 term quadratic expression in terms of x .
	$x = \frac{5}{2}$	A1	For x -coordinate of the point of intersection.
	Either $\int \left(3 + \frac{4}{2x+1} \right) dx = 3x + 2\ln(2x+1)$	2	M1 for attempt to integrate with one term correct
	$\left[3x + 2\ln(2x+1) \right]_0^{\frac{5}{2}} = \frac{15}{2} + 2\ln 6$	2	Dep M1 for using <i>their</i> x -coordinate of C in <i>their</i> integral. Must have a term in $\ln(2x+1)$ Allow for awrt 11.1. A1 Must be exact but allow unsimplified
	Area of trapezium $\frac{1}{2} \left(2 + \frac{11}{3} \right) \times \frac{5}{2} \text{ or } \left[\frac{x^2}{3} + 2x \right]_0^{\text{their } \frac{5}{2}} \text{ or }$ $\left[\frac{(2x+6)^2}{12} \right]_0^{\text{their } \frac{5}{2}} = \frac{85}{12}$	2	M1 for attempt at the trapezium, must have at least one side correct. If using integration, the integral must be correct using <i>their</i> $\frac{5}{2}$
	Shaded area = $2\ln 6 + \frac{5}{12} \text{ or } \ln 36 + \frac{5}{12} \text{ or } \ln 6^2 + \frac{5}{12}$	A1	
	Or $\int \left 1 + \frac{4}{2x+1} - \frac{2}{3}x \right dx$ $x + 2\ln(2x+1) - \frac{x^2}{3} \text{ or }$ $-x - 2\ln(2x+1) + \frac{x^2}{3}$	(5)	M2 for attempt to subtract and integrate with at least one term correct, allow x terms considered separately. If subtraction is reversed allow accuracy marks. Separate x terms should be considered as one term for A marks. A1 for one term only correct A2 for two terms only correct
	$\left[x + 2\ln(2x+1) - \frac{x^2}{3} \right]_0^{\frac{5}{2}} = \frac{5}{2} + 2\ln 6 - \frac{25}{12}$ or $\left[\frac{x^2}{3} - x - 2\ln(2x+1) \right]_0^{\frac{5}{2}} = \frac{25}{12} - \frac{5}{2} - 2\ln 6$	(M1)	Dep M1 for using <i>their</i> x -coordinate of the point of intersection in <i>their</i> integral, must have a term in $\ln(2x+1)$ Allow for awrt ± 4 as appropriate

Question	Answer	Marks	Guidance
9	Shaded area = $2\ln 6 + \frac{5}{12}$ or $\ln 36 + \frac{5}{12}$ or $\ln 6^2 + \frac{5}{12}$	(A1)	
	Or $\int \left 3 + \frac{4}{2x+1} - \frac{11}{3} \right dx$ $2\ln(2x+1) - \frac{2x}{3}$	(3)	M1 for attempt to subtract and integrate with at least one term correct, allow x terms considered separately. Separate x terms should be considered as one term for A marks. A1 for one term only correct
	$\left[2\ln(2x+1) - \frac{2x}{3} \right]_0^5 = 2\ln 6 - \frac{5}{3}$	(M1)	Dep M1 for using <i>their</i> x -coordinate of the point of intersection in <i>their</i> integral, must have a term in $\ln(2x+1)$
	Area of triangle = $\frac{1}{2} \times \left(\frac{11}{3} - 2 \right) \times \frac{5}{2}$ $= \frac{25}{12}$	(2)	M1 for attempt at the area of the triangle
	Shaded area = $2\ln 6 + \frac{5}{12}$ or $\ln 36 + \frac{5}{12}$ or $\ln 6^2 + \frac{5}{12}$	(A1)	
	Alternative $3y^2 - 14y + 11 (= 0)$	(2)	M1 for a correct attempt to equate the line and curve and obtain a 3 term quadratic expression in terms of y .
	$y = \frac{11}{3}$	(A1)	
	$\int \left(\frac{2}{y-3} - \frac{1}{2} \right) dy = 2\ln(y-3) - \frac{1}{2}y$	(2)	M1 for attempt to integrate with one term correct
	$\left[2\ln(y-3) - \frac{1}{2}y \right]_{\frac{11}{3}}^7 = 2\ln 6 - \frac{5}{3}$	(2)	Dep M1 for using <i>their</i> y -coordinate of C in <i>their</i> integral. Allow for awrt 1.92 A1 Must be exact
	Area of triangle $\frac{1}{2} \left(\frac{11}{3} - 2 \right) \times \frac{5}{2}$ or $\left[\frac{3y^2}{4} - 3y \right]_2^{\frac{11}{3}}$ $= \frac{25}{12}$	(2)	M1 for attempt at the triangle, must have at least one side correct. If using integration, the integral must be correct using <i>their</i> $\frac{11}{3}$
	Shaded area = $2\ln 6 + \frac{5}{12}$ or $\ln 36 + \frac{5}{12}$ or $\ln 6^2 + \frac{5}{12}$	(A1)	

Question	Answer	Marks	Guidance
10(a)(i)	$\frac{n}{2}(2x+1)(3n-1)$	2	B1 for $\frac{n}{2}(2(2x+1)+3(n-1)(2x+1))$ or $\frac{n}{2}(2(2x+1)+(6x+3)(n-1))$ oe
10(a)(ii)	$\frac{n}{2}(2x+1)(3n-1) = (54n+37)(2x+1)$ $3n^2 - 109n - 74 = 0$	M1	For equating <i>their</i> answer to (a) to $(54n+37)(2x+1)$ and attempt to solve a 3-term quadratic equation in n to obtain $n = \dots$
	37 only	A1	
10(a)(iii)	$1017.5 = (54(\text{their } n) + 37)(2x+1)$	M1	For attempt to solve to obtain a value for x . n must be a positive integer
	$x = -\frac{1}{4}$	A1	
10(b)	$(2y+1)(3(2y+1))^{n-1} =$ $4(2y+1)(3(2y+1))^{n+1}$ Or $(3(2y+1))^{n-1} = 4(3(2y+1))^{n+1}$ Or $(2y+1)r^{n-1} = 4(2y+1)r^{n+1}$ Or $ar^{n-1} = 4ar^{n+1}$	B1	Award when a correct statement is first seen
	Either $(2y+1)^2 = \frac{1}{36}$ oe or $(6y+3)^2 = \frac{1}{4}$ oe or $r^2 = \frac{1}{4}$ oe	M1	Either M1 for an equation of the form $(2y+1)^2 = k$ or $(6y+3)^2 = m$ where k and m are numerical and not zero (may be expanded) with no terms in n Or M1 for $r^2 = p$, where p is numerical and not zero
	$2y+1 = \pm\frac{1}{6}$ or $6y+3 = \pm\frac{1}{2}$	A1	
	$-\frac{5}{12}, -\frac{7}{12}$ and no others	A1	For both
10(c)	$-1 < 2\sin^2 \theta < 1$ oe soi or $0 < 2\sin^2 \theta < 1$ soi	B1	Allow $2\sin^2 \theta < 1$ May be implied by $\theta < \frac{\pi}{4}$
	$\theta < \frac{\pi}{4}$ or $\theta < 0.785$	B1	
	$0 < \theta < \frac{\pi}{4}$ Or $0 < \theta < 0.785$ or better	B1	



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/13

Paper 1

May/June 2023

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2023 series for most Cambridge IGCSE, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

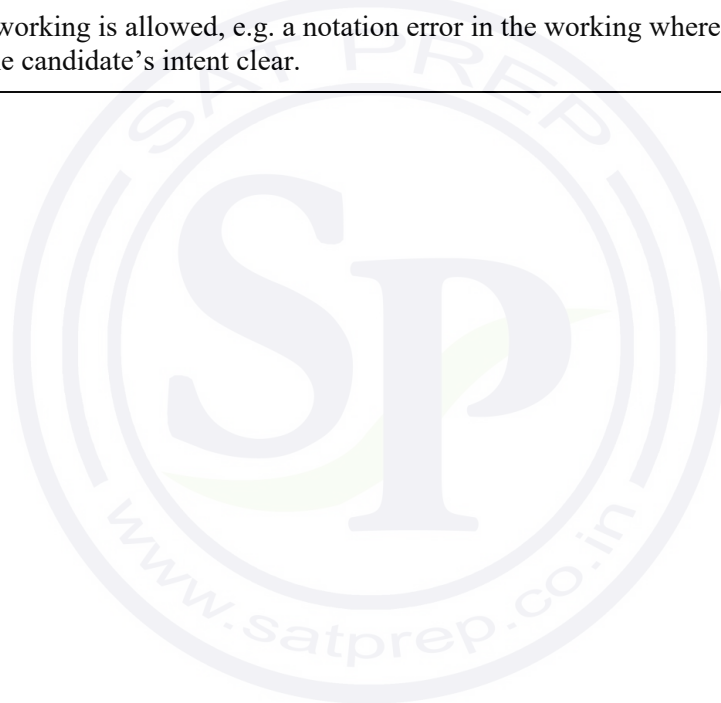
GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.



MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.


Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

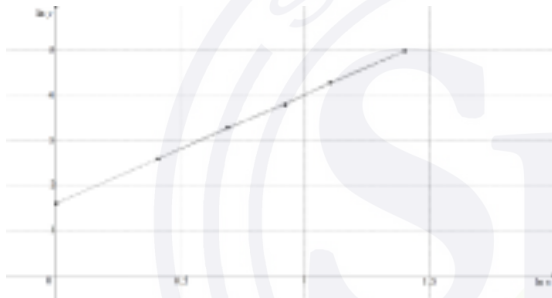
Abbreviations

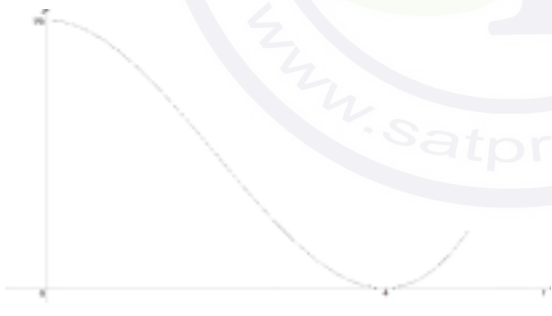
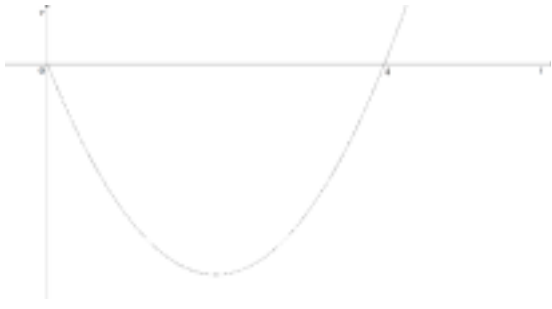
awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

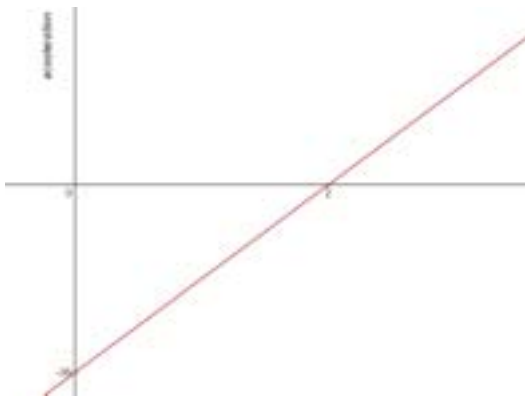
Question	Answer	Marks	Guidance
1(a)	2π	B1	
1(b)		3	B1 for the correct shape, must be tending correctly towards the asymptotes B1 for $(0, -3)$ B1 for $\left(\frac{\pi}{2}, 0\right)$
2(a)	$2\left(x + \frac{5}{4}\right)^2 - \frac{1}{8}$ oe	2	B1 for $2\left(x + \frac{5}{4}\right)^2$ B1 for $-\frac{1}{8}$
2(b)	$\left(-\frac{5}{4}, -\frac{1}{8}\right)$ oe	2	B1 FT for each on <i>their</i> (a).

Question	Answer	Marks	Guidance
2(c)	Use of <i>their</i> (a) or expansion to 3 term quadratic ($= 0$), to obtain two critical values.	M1	
	$-\frac{9}{4}$, $-\frac{1}{4}$	A1	For both critical values
	$-\frac{9}{4} < x < -\frac{1}{4}$	A1	
3(a)	$\lg \frac{500a^2}{b}$ oe	3	B1 for $\lg a^2$, $-\lg 2b$ or $\lg 1000$ B2 for $\lg \frac{a^2}{2b}$, $\lg 1000a^2$ or $\lg \frac{1000}{2b}$
3(b)	$\log_3 c = \frac{1}{\log_c 3}$	B1	
	$2(\log_c 3)^2 - 7\log_c 3 - 4 \quad (= 0)$ $(2\log_c 3 + 1)(\log_c 3 - 4) \quad (= 0)$ $\log_c 3 = -\frac{1}{2}, \log_c 3 = 4$	M1	Attempt to obtain a 3 term quadratic equation ($= 0$) and attempt to solve to obtain $\log_c 3 = \dots$ Allow one sign error
	$c^{\frac{1}{2}} = 3 \quad c^4 = 3$	M1	Dep for attempt to solve at least one of <i>their</i> log equations
	$c = \frac{1}{9}, \quad c = 3^{\frac{1}{4}}$ or exact equivalents	2	A1 for each
	Alternative Method		
	$\log_c 3 = \frac{1}{\log_3 c}$	B1	
	$4(\log_3 c)^2 + 7\log_3 c - 2 \quad (= 0)$ $(4\log_3 c - 1)(\log_3 c + 2) \quad (= 0)$ $\log_3 c = \frac{1}{4}, \log_3 c = -2$	M1	Attempt to obtain a 3 term quadratic equation $= 0$ and attempt to solve to obtain $\log_3 c = \dots$ Allow one sign error
	$c = 3^{\frac{1}{4}}, \quad c = \frac{1}{9}$ or exact equivalents	3	M1 dep for attempt to solve at least one of <i>their</i> log equations. A2 for both or A1 for either

Question	Answer	Marks	Guidance
4	$5x^2 - 8x - 4 \quad (=0)$ or $5y^2 - 36y - 305 \quad (=0)$	M1	For attempt to eliminate one variable to obtain a 3 term quadratic equation ($=0$). Allow one sign error.
	$x = -\frac{2}{5}, x = 2$ $y = -\frac{61}{5}, y = -5$	3	Dep M1 for attempt to solve <i>their</i> quadratic equation A1 for any correct pair A1 for a second correct pair.
	Mid-point $\left(\frac{4}{5}, -\frac{43}{5}\right)$	M1	For attempt to find mid-point using <i>their</i> coordinates
	Gradient of perpendicular $= -\frac{1}{3}$	B1	
	$y + \frac{43}{5} = -\frac{1}{3}\left(x - \frac{4}{5}\right)$	M1	For attempt to find the equation of the perpendicular bisector using <i>their</i> perpendicular gradient and <i>their</i> midpoint. Allow alternative methods
	$a = -1$	A1	
5(a)	$x^{20} - 40x^{16} + 720x^{12}$	3	B1 for each correct term
5(b)	$\left(x^4 + 4 + \frac{4}{x^4}\right)$	B1	Allow unsimplified
	$(4 \times \text{their} - 40) + 4 + \text{their} 720$ soi	M1	Must have 3 terms
	564	A1	
6(a)	$\frac{1}{2}r^2\theta = 25$ $\theta = \frac{50}{r^2}$	B1	
	$P = 2r + \frac{50}{r}$	2	M1 for use of $P = 2r + r\theta$ with attempt to eliminate θ

Question	Answer	Marks	Guidance												
6(b)	$\frac{dP}{dr} = 2 - \frac{50}{r^2}$	M1	For attempt to differentiate <i>their</i> P , must be in terms of r .												
	When $\frac{dP}{dr} = 0$, $r = 5$	A1													
	$\frac{d^2P}{dr^2} = \frac{100}{r^3}$ When $r = 5$, $\frac{d^2P}{dr^2}$ is positive so a minimum oe.	B1	Allow alternative valid methods												
	Minimum $P = 20$	A1													
7(a)	<table border="1"><tr><td>$\ln x$</td><td>0.41</td><td>0.69</td><td>0.92</td><td>1.1</td><td>1.4</td></tr><tr><td>$\ln y$</td><td>2.6</td><td>3.3</td><td>3.8</td><td>4.3</td><td>5</td></tr></table> 	$\ln x$	0.41	0.69	0.92	1.1	1.4	$\ln y$	2.6	3.3	3.8	4.3	5	3	M1 for attempt to find \ln values of all and plotting the graph. A1 for 4 correct points. A0 for fewer than 4 correct points.
$\ln x$	0.41	0.69	0.92	1.1	1.4										
$\ln y$	2.6	3.3	3.8	4.3	5										
7(b)	$\ln y = \ln A + b \ln x$ soi	B1	Allow if seen in (a)												
	Gradient = $b = 2.4$ Allow 2.3 to 2.5	2	Dep M1 for attempt to find the gradient of <i>their</i> graph, must have M1 in part(a) Must be using points on <i>their</i> graph.												
	$\ln A = 1.6$ $A = 5$ Allow awrt 4.8 to awrt 5.5	2	Dep M1 for attempt to find the intercept on the vertical axis and equate to $\ln A$. must have M1 in part (a).												
7(c)	$x = 3.42$ Allow 3.2 to 3.5	2	M1 for a correct attempt to find the estimate either using <i>their</i> graph or <i>their</i> equation.												
8(a)	b – a	B1													

Question	Answer	Marks	Guidance
8(b)	$\frac{2}{5}\mathbf{a} + \frac{1}{2}(\text{their } (\mathbf{b} - \mathbf{a}))$ oe	M1	
	$\frac{1}{2}\mathbf{b} - \frac{1}{10}\mathbf{a}$	A1	Allow unsimplified
8(c)	$(\lambda + 1) \times \left(\frac{1}{2}\mathbf{b} - \frac{1}{10}\mathbf{a}\right)$ oe	2	M1 for $(\lambda + 1) \times \text{their } \left(\frac{1}{2}\mathbf{b} - \frac{1}{10}\mathbf{a}\right)$ A1 allow unsimplified
8(d)	$-\frac{3}{5}\mathbf{a} + (\mu + 1)\mathbf{b}$ oe	2	B1 for each vector, allow unsimplified.
8(e)	$(\lambda + 1) \times \left(\frac{1}{2}\mathbf{b} - \frac{1}{10}\mathbf{a}\right) = -\frac{3}{5}\mathbf{a} + (\mu + 1)\mathbf{b}$ $\lambda = 5$ $\mu = 2$	3	M1 for equating $(\lambda + 1) \times \text{their } \left(\frac{1}{2}\mathbf{b} - \frac{1}{10}\mathbf{a}\right)$ and <i>their</i> $-\frac{3}{5}\mathbf{a} + (\mu + 1)\mathbf{b}$ and then equating like vectors at least once. A1 for each.
9(a)	$v = 9t(t - 4)$ oe	2	M1 for correct attempt to differentiate, allow one arithmetic error.
	$t = 0, t = 4$	2	Dep M1 for equating <i>their</i> v to zero and attempt to solve. A1 for both.
9(b)		3	B1 for correct cubic curve for given domain B1 for (0, 96) and no other intercept on the y-axis B1 for touching at (4, 0) and no other intercept on the x-axis
9(c)		2	B1 for a correct quadratic curve for the given domain, starting from the origin. B1 for (4, 0) and no other x- intercept
9(d)(i)	$18t - 36$	B1	

Question	Answer	Marks	Guidance
9(d)(ii)		2	B1 for a correctly positioned straight line graph for the given domain. Dep B1 for $(0, -36)$ and $(2, 0)$
10(a)	$\cos^4 \theta - \sin^4 \theta =$ $(\cos^2 \theta - \sin^2 \theta)(\cos^2 \theta + \sin^2 \theta)$ soi	B1	
	$\cos^2 \theta - \sin^2 \theta + 1$	M1	Must show sufficient detail to show the given result.
	$2\cos^2 \theta$	A1	
	Alternative 1		
	$\cos^4 \theta - (1 - \cos^2 \theta)^2 + 1$	(B1)	
	$\cos^4 \theta - (\cos^4 \theta - 2\cos^2 \theta + 1) + 1$	(M1)	Must show sufficient detail to show the given result.
	$2\cos^2 \theta$	(A1)	
	Alternative 2		
	$(1 - \sin^2 \theta)^2 - \sin^2 \theta + 1$	(B1)	
	$(1 - 2\sin^2 \theta + \sin^4 \theta) - \sin^4 \theta + 1$ $2 - 2\sin^2 \theta$	(M1)	Must show sufficient detail to show the given result.
	$2\cos^2 \theta$	(A1)	
10(b)	$\cos\left(\frac{\phi}{3}\right) = (\pm)\frac{1}{2}$ soi	B1	
	$\phi = -2\pi, -\pi, \pi, 2\pi$	4	M1 for obtaining one correct solution. A1 for obtaining 2 correct solutions. A1 for obtaining a third correct solution. A1 for a fourth correct solution and no extras within the range.



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

February/March 2023

MARK SCHEME

Maximum Mark: 80

Published

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- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
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2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
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5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
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MARK SCHEME NOTES

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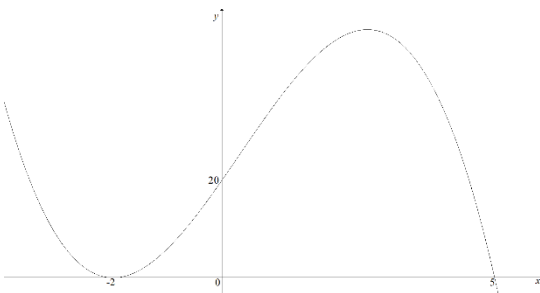
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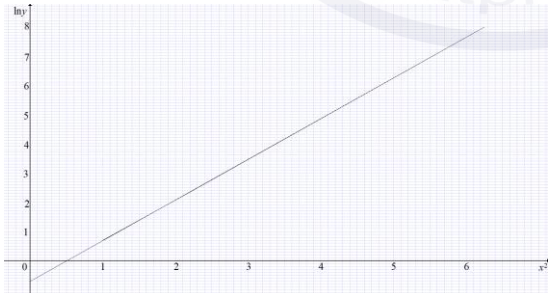
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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$kx^2 + 2x + 3k - 1 [= 0]$	2	M1 for attempt to equate equations of the line and curve, re-arrange and equate to zero. Allow one sign error.
	$4 = 4k \times \text{their}(3k - 1)$ oe	M1	Dep for attempt to use the discriminant of <i>their</i> quadratic equation and solve to obtain k .
	$k = \frac{1 \pm \sqrt{13}}{6}$ isw	A1	
	Alternative method		
	$kx^2 + 2x + 3k - 1 = 0$	2	M1 for attempt to equate equations of the line and curve, re-arrange and equate to zero. Allow one sign error.
	Grad of straight line = -1 Gradient function of curve = $2kx + 1$ Substitution to obtain $3k^2 - k - 1 = 0$ oe with attempt to solve to obtain k	M1	Dep
	$k = \frac{1 \pm \sqrt{13}}{6}$ isw	A1	
2(a)	$\frac{dy}{dx} = 2(x+2)(5-x) + (-1)(x+2)^2$ or $y = -x^3 + x^2 + 16x + 20$ $\frac{dy}{dx} = -3x^2 + 2x + 16$	2	M1 for attempt at differentiation of a product, or expansion and then differentiation. A1 for all correct
	$(x+2)(8-3x) = 0$	M1	Dep for attempt to solve <i>their</i> quadratic $\frac{dy}{dx} = 0$
	$x = -2, \frac{8}{3}$	A1	For both.
2(b)		3	B1 for correctly shaped curve, with maximum point in the first quadrant B1 for $(5, 0)$ and a stationary point at $(-2, 0)$, must have a cubic graph. B1 for $(0, 20)$, must have a cubic graph

Question	Answer	Marks	Guidance
2(c)	When $x = \frac{8}{3}$, $y = \frac{1372}{27}$ or awrt 50.8	M1	For attempt to find the value of y using <i>their</i> $\frac{8}{3}$.
	$k > \frac{1372}{27}$ or awrt 50.8	A1	
	$k < 0$	B1	
3	${}^{10}C_2(2x)^8\left(-\frac{1}{x}\right)^2$ or ${}^{10}C_1(2x)^9\left(-\frac{1}{x}\right)^1$	M1	For attempting to find terms which will give terms of x^8 or x^6 , allow coefficients. Allow as part of an expansion
	$45 \times 256 [x^6]$ oe	A1	
	$[-] 5120 [x^8]$	A1	
	<i>their</i> $(-11520) + \text{their}(-5120)$	M1	Dep
	-16 640	A1	Condone inclusion of x^8
4(a)	$\lg \frac{x^3}{1000y^4}$ oe	3	B1 for $3 = \lg 1000$ M1 for correct use of power rule at least once and division rule at least once A1 cao
4(b)	$\log_x 3 = \frac{1}{\log_3 x}$ soi	B1	For change of base.
	$2(\log_3 x)^2 - 5(\log_3 x) + 2 = 0$	M1	For attempt to obtain a 3-term quadratic equation, equated to zero. Allow one sign error. May be using a substitution.
	$2\log_3 x = 1$ $\log_3 x = 2$	M1	Dep for attempt to solve <i>their</i> quadratic equation and a correct attempt to obtain at least one value of x.
	$x = \sqrt{3}$ oe	A1	Allow 1.73(2...)
	$x = 9$	A1	

Question	Answer	Marks	Guidance
4(b)	Alternative method 1		
	$\log_3 x = \frac{1}{\log_x 3}$ soi	B1	For change of base.
	$2(\log_x 3)^2 - 5(\log_x 3) + 2 = 0$	M1	For attempt to obtain a 3-term quadratic equation, equated to zero. Allow one sign error.
	$2\log_x 3 = 1 \quad \log_x 3 = 2$	M1	Dep for attempt to solve <i>their</i> quadratic equation and a correct attempt to obtain at least one value of x .
	$x = \sqrt{3}$ oe	A1	Allow 1.73(2...)
	$x = 9$	A1	
	Alternative method 2		
	$\log_3 x = \frac{\lg x}{\lg 3}$ and $\log_x 3 = \frac{\lg 3}{\lg x}$ oe	B1	For a consistent change of base.
	$2(\lg x)^2 - 5(\lg x) + 2(\lg 3)^2 = 0$ oe	M1	For attempt to obtain a 3-term quadratic equation, equated to zero. Allow one sign error.
	$2\lg x = \lg 3 \quad \lg x = 2\lg 3$ oe	M1	Dep for attempt to solve <i>their</i> quadratic equation and a correct attempt to obtain at least one value of x .
	$x = \sqrt{3}$ oe	A1	Allow 1.73(2...)
	$x = 9$ oe	A1	
5(a)		2	B1 for 3 or 4 correctly plotted points

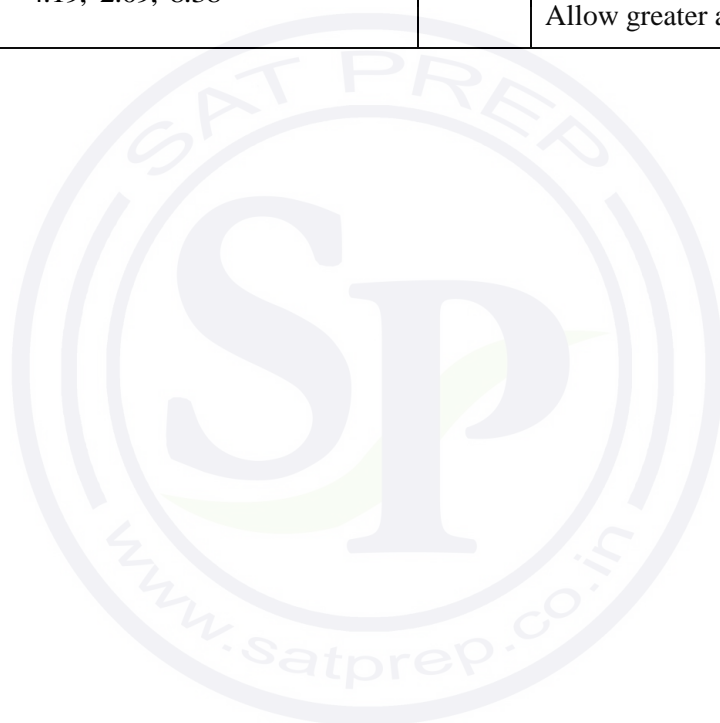
Question	Answer	Marks	Guidance
5(b)	$\ln y = mx^2 + c$ soi	B1	$m \neq \ln A, c \neq \ln b$
	Gradient = $\ln b$	M1	For attempt to find the numerical gradient of <i>their</i> straight line graph and equate to $\ln b$. May be implied by later work
	$b = 4$	A1	
	Intercept on vertical axis = $\ln A$	M1	For use of <i>their</i> intercept on the vertical axis of <i>their</i> straight line graph oe.
	$A = 0.5$	A1	
	Alternative method		
	$\ln y = mx^2 + c$ soi	B1	$m \neq \ln A, c \neq \ln b$
	Forming 2 equations correctly using points on <i>their</i> graph	M1	
	Solving the equations to obtain either A or b	M1	Dep
	$b = 4$	A1	
	$A = 0.5$	A1	
	Special case		
	$A = 0.5$ not using transformed data	B1	
	$b = 4$ not using transformed data	B1	
5(c)	35 nfw Allow answers between 33 and 37	2	M1 for attempt at a complete method using <i>their</i> straight line graph or equation
5(d)	1.63 nfw Allow answers between 1.5 and 1.7	2	M1 for attempt at a complete method using <i>their</i> straight line graph or equation

Question	Answer	Marks	Guidance
6	$k(5x+2)^{\frac{3}{5}}$	M1	
	$f'(x) = \frac{1}{3}(5x+2)^{\frac{3}{5}} \quad (+c)$	A1	Condone omission of c
	$\frac{17}{3} = \frac{1}{3}(32)^{\frac{3}{5}} + c$ oe	M1	Dep for use of $f'(6)$ and attempt to evaluate c
	$c = 3$	A1	
	$k(5x+2)^{\frac{8}{5}}$	M1	
	$\frac{1}{24}(5x+2)^{\frac{8}{5}} + cx$	A1	FT on <i>their</i> c
	$\frac{26}{3} = \frac{1}{24}(32)^{\frac{8}{5}} + d + ((3 \times 6))$ oe	M1	Dep for use of $f(6)$ and attempt to evaluate d .
	$[f(x)] = \frac{1}{24}(5x+2)^{\frac{8}{5}} + 3x - 20$	A1	
7(a)(i)	154 440	B1	
7(a)(ii)	124 200	2	B1 for $^{10}P_5$
	Alternative method		
	124 200	2	B1 for 1 symbol: 75 600 2 symbols: 43 200 3 symbols: 5400
7(b)	$16(n-11) = 12(n+1)$ oe	B2	B1 for correct numbers or correct factors must be using combinations
	$n = 47$	B1	Dep on both previous B marks Must be the only solution

Question	Answer	Marks	Guidance
8	A (2.5, 0) soi	B1	
	C (4.5, 0) soi	B1	
	$2x^2 + x - 21 = 0$	M1	For a correct attempt to find the intersection of the straight line and the curve. Must have attempt to solve the resulting quadratic equation to obtain $x =$.
	$x = 3, \left[-\frac{7}{2} \right]$	A1	
	$B \left(3, \frac{1}{2} \right)$ soi	A1	
	$\int \left(2 - \frac{3}{x-1} \right) dx = 2x - 3\ln(x-1)$	B1	
	e.g. $\left[2x - 3\ln(x-1) \right]_{\frac{5}{2}}^3 =$ $(6 - 3\ln 2) - \left(5 - 3\ln \frac{3}{2} \right)$	M1	Dep for application of appropriate limits e.g. $x = \text{their } \frac{5}{2}$ and $x = \text{their } 3$ $x = \text{their } \frac{5}{2}$ and $x = \text{their } \frac{9}{2}$ $x = \text{their } 3$ and $x = \text{their } \frac{9}{2}$ Integral must be in the form $ax + b\ln(x-1)$
	$1 + 3\ln \frac{3}{4}$ oe	A1	
	Area of an appropriate triangle	B1	FT on $\frac{1}{2} \times \text{their } \frac{1}{2} \times \text{their } \frac{3}{2}$ oe $\frac{1}{2} \times \text{their } 2 \times \text{their } \frac{2}{3}$ oe Must be appropriate for <i>their</i> method
	Area = $\frac{11}{8} + \ln \frac{27}{64}$	2	B1 for each correct term
9(a)(i)	$\begin{pmatrix} 2 \\ 5 \end{pmatrix}$	B1	
9(a)(ii)	Velocity vector = $\begin{pmatrix} 12 \\ -5 \end{pmatrix}$ soi by correct speed	B1	
	Speed = 13	B1	

Question	Answer	Marks	Guidance
9(a)(iii)	$2 + 12t = 158$ and $5 - 5t = -48$ $t = 13$, $t = 10.6$ soi	M1	Either for finding two values of t or for finding one value of t and substitute to obtain a position vector.
	Times are different so P does not pass through the given point or time calculated gives an inconsistent position vector	A1	For a valid conclusion
9(b)	$\overrightarrow{AB} = \mathbf{b} - \mathbf{a}$ and $\overrightarrow{AC} = \mathbf{c} - \mathbf{a}$	B1	
	$4(\mathbf{b} - \mathbf{a}) = \mathbf{c} - \mathbf{a}$ oe	M1	For substitution into a valid equation from <i>their</i> ratio. FT on <i>their</i> \overrightarrow{AB} and <i>their</i> \overrightarrow{AC}
	$\mathbf{c} = 4\mathbf{b} - 3\mathbf{a}$	A1	
	Alternative method		
	$\overrightarrow{AB} = \mathbf{b} - \mathbf{a}$ and $\overrightarrow{AC} = 4\mathbf{b} - 4\mathbf{a}$ oe	B1	
	$(\overrightarrow{OC} =) \mathbf{c} = \mathbf{a} + 4\mathbf{b} - 4\mathbf{a}$	M1	FT on <i>their</i> \overrightarrow{AB} and <i>their</i> \overrightarrow{AC}
	$\mathbf{c} = 4\mathbf{b} - 3\mathbf{a}$	A1	
10(a)	$\cos \theta = x - 2$ and $\sin \theta = \frac{2}{y}$ soi	B1	
	$(x - 2)^2 + \frac{4}{y^2} = 1$	M1	For a correct attempt to use $\cos^2 \theta + \sin^2 \theta = 1$ or other relevant identity
	$y^2 = \frac{4}{1 - (x - 2)^2}$ oe	M1	Dep for attempt to rearrange to obtain y^2
	$y = \frac{2}{\sqrt{1 - (x - 2)^2}}$ or $\frac{2}{\sqrt{4x - x^2 - 3}}$ oe	A1	Must be positive
	Alternative method		
	$\theta = \cos^{-1}(x - 2)$ and $\theta = \sin^{-1}\left(\frac{2}{y}\right)$	B1	
	$\cos^{-1}(x - 2) = \sin^{-1}\left(\frac{2}{y}\right)$	M1	
	$y = \frac{2}{\sin(\cos^{-1}(x - 2))}$	2	Dep M1 for correct attempt to rearrange to obtain $y = \dots$

Question	Answer	Marks	Guidance
10(b)	$\tan \frac{\phi}{2} = \sqrt{3}$ or $\sin \frac{\phi}{2} = \frac{\sqrt{3}}{2}$ or $\cos \frac{\phi}{2} = \frac{1}{2}$	B1	
	$\frac{\phi}{2} = \frac{\pi}{3}$ or awrt 1.05	M1	Dep for a correct attempt to solve <i>their</i> equation, must be using $\frac{\phi}{2}$.
	$\phi = \frac{2\pi}{3}$ or awrt 2.09	M1	Dep for correct order of operations, may be implied by one correct solution.
	$\phi = -\frac{10\pi}{3}, -\frac{4\pi}{3}, \frac{2\pi}{3}, \frac{8\pi}{3}$ or $-10.5, -4.19, 2.09, 8.38$	A2	A1 for a correct pair of solutions. A1 for a second correct pair of solutions and no extra solutions within the range. Allow greater accuracy if decimals used.





Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/11

Paper 1

October/November 2022

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

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GENERIC MARKING PRINCIPLE 2:

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- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

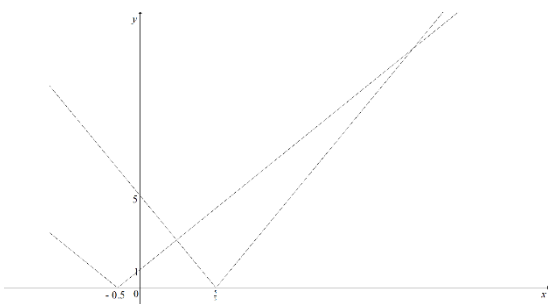
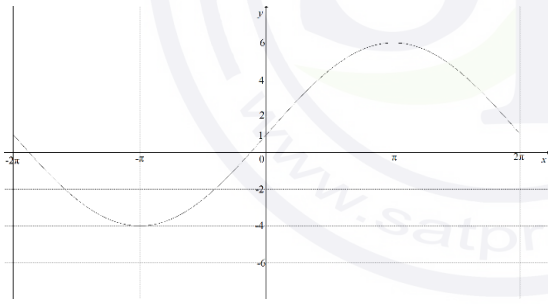
Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

- awrt answers which round to
- cao correct answer only
- dep dependent
- FT follow through after error
- isw ignore subsequent working
- nfwf not from wrong working
- oe or equivalent
- rot rounded or truncated
- SC Special Case
- soi seen or implied

Question	Answer	Marks	Guidance
1(a)		3	B1 for 2 V-shaped graphs with vertices in the 1st and 2nd quadrants, intersecting twice in the first quadrant. Dep B1 for (0,1) and (0,5) B1 for $\left(-\frac{1}{2}, 0\right)$ and $\left(\frac{5}{3}, 0\right)$
1(b)	$x = \frac{4}{5}$	B1	
	$2x + 1 = -5 + 3x$ oe	M1	For considering the negative for one of the functions
	$x = 6$	A1	
	Alternative		
	$5x^2 - 34x + 24 = 0$	(2)	M1 for squaring each function and attempt to form a 3-term quadratic equation = 0. Allow one error. A1 for a correct equation
	$x = \frac{4}{5}, x = 6$	(A1)	For both
2(a)		3	B1 for a complete cycle starting and finishing at $(-2\pi, 1)$ and $(2\pi, 1)$ B1 for intercept at $y = 1$ B1 for a maximum when $y = 6$ and a minimum when $y = -4$
2(b)	5	B1	
2(c)	4π or 720°	B1	

Question	Answer	Marks	Guidance
3	$y^3 = m \ln x + c$	B1	May be implied by subsequent work
	$5 = m + c$ $15 = 6m + c$ $m = 2, c = 3$	2	B1 for $m = 2$ B1 for $c = 3$
	$y = \sqrt[3]{2 \ln x + 3}$	B1	
	Alternative		
	$y^3 = m \ln x + c$	(B1)	May be implied by subsequent work
	Gradient = 2	(B1)	For finding the gradient and equating to m
	$5 = m + c$ $15 = 6m + c$ $c = 3$	(B1)	For at least one correct equation and finding c
	$y = \sqrt[3]{2 \ln x + 3}$	(B1)	
4	$x = \frac{2 \pm \sqrt{4 + 4(\sqrt{5} - 1)(\sqrt{5} + 1)}}{2(\sqrt{5} - 1)}$	M1	For a correct use of the quadratic formula with sufficient detail
	$x = \frac{2 \pm 2\sqrt{5}}{2(\sqrt{5} - 1)}$ or $x = \frac{1 \pm \sqrt{5}}{(\sqrt{5} - 1)}$	2	Dep M1 for attempt to simplify to obtain 2 real roots A1 for either
	$x = \frac{(\sqrt{5} + 1)}{(\sqrt{5} - 1)} \times \frac{(\sqrt{5} + 1)}{(\sqrt{5} + 1)}$	M1	For attempt at rationalisation
	$x = \frac{3}{2} + \frac{\sqrt{5}}{2}$	A1	
	$x = -1$	B1	
5(a)	$a + 3d = 25$ $a + 8d = 50$	M1	For at least one correct equation and attempt to solve to find at least one unknown
	$a = 10$	A1	
	$d = 5$	A1	

Question	Answer	Marks	Guidance
5(b)	$\frac{n}{2}(20+(n-1)5) (=25\,000)$	M1	For attempting the sum to n terms using <i>their</i> a and d
	$5n^2 + 15n - 50\,000 = 0$ $n = 98.5\dots$	A1	
	$n = 99$	A1	
6	$1 - 4x + \frac{68}{9}x^2$	2	B1 for $1 - 4x$ B1 for $\frac{68}{9}x^2$ or $7.56x^2$
	$1 + 9x + 27x^2$	B1	
	Term in x : $-4x + 9x = 5x$ or coefficients of x : $-4 + 9$	M1	For $(\text{their } -4(x)) + (\text{their } 9(x))$
	$a = 5$	A1	
	Term in x^2 : $\frac{68}{9}x^2 + 27x^2 - 36x^2$ or coefficients of x^2 : $\frac{68}{9} + 27 - 36$	M1	For $\left(\text{their } \frac{68}{9}(x)\right) + (\text{their } 27(x)) +$ $((\text{their } -4(x)) \times (\text{their } 9(x)))$
	$b = -\frac{13}{9}$	A1	Must be exact
7(a)	$2\pi r + 4x + 2x\theta$	3	B1 for $2\pi r$ B1 for $+4x$ B1 for $2x\theta$
7(b)	$\pi r^2 - x^2\theta$	B1	
7(c)	Least value when $x = r$	B1	
	Least value = $r^2(\pi - \theta)$ oe	B1	
8	$2\ln(x+1) - \ln(x+2)$	2	B1 for $2\ln(x+1)$ B1 for $-\ln(x+2)$
	$(2\ln(a+1) - \ln(a+2)) + \ln 2$	M1	For attempt to apply limits correctly, dependent on having 2 log terms.
	$\ln \frac{2(a+1)^2}{(a+2)}$	2	M1 for use of either power rule or the division rule.

Question	Answer	Marks	Guidance
9	$2\log_p y + \frac{10}{\log_p y} - 9 = 0$ or $\frac{2}{\log_y p} + 10\log_y p - 9 = 0$	B1	For a change of base
	$2(\log_p y)^2 - 9\log_p y + 10 = 0$ or $10(\log_y p)^2 - 9\log_y p + 2 = 0$	M1	For attempt to obtain a 3-term quadratic equation = 0, in either $\log_p y$ or $\log_y p$
	$\log_p y = \frac{5}{2}, \log_p y = 2$ or $\log_y p = \frac{2}{5}, \log_y p = \frac{1}{2}$	M1	Dep M mark for attempt to solve the quadratic to obtain 2 solutions
	$y = p^{\frac{5}{2}}$	A1	
	$y = p^2$	A1	
10	$\frac{65n!}{(n-5)!5!} = \frac{2(n-1)(n+1)!}{(n-5)!6!}$ $65 = \frac{n^2 - 1}{3}$	2	B1 for simplifying numerical factorials to 3 B1 for simplifying algebraic factorials to either $(n-1)(n+1)$ or $n^2 - 1$
	$n = 14$	B1	
11(a)	$\overrightarrow{AC} = \mathbf{c} - \mathbf{a}$	B1	
	$\overrightarrow{AB} = \frac{2}{5}(\mathbf{c} - \mathbf{a})$ or $\overrightarrow{BC} = \frac{3}{5}(\mathbf{c} - \mathbf{a})$	B1	
	$\frac{2}{5}(\mathbf{c} - \mathbf{a}) = \mathbf{b} - \mathbf{a}$ or $\frac{3}{5}(\mathbf{c} - \mathbf{a}) = \mathbf{c} - \mathbf{b}$	M1	For equating two different forms of \overrightarrow{AB} or 2 different forms of \overrightarrow{BC}
	$5\mathbf{b} - 3\mathbf{a} = 2\mathbf{c}$	A1	Simplification to obtain the given answer
11(b)	$\overrightarrow{XC} = \mathbf{c} - \frac{3\mathbf{a}}{4}$	B1	
	$\overrightarrow{XC} = \frac{5\mathbf{b}}{2} - \frac{9\mathbf{a}}{4}$	B1	

Question	Answer	Marks	Guidance
11(c)	$m\mathbf{b} - \frac{3}{4}\mathbf{a} = \lambda\left(\frac{5\mathbf{b}}{2} - \frac{9\mathbf{a}}{4}\right)$	B1	
	$\lambda = \frac{1}{3}, \quad m = \frac{5}{6}$	3	M1 for equating like vectors at least once A1 for $\lambda = \frac{1}{3}$ A1 for $m = \frac{5}{6}$
12(a)	$\frac{\operatorname{cosec} \theta + 1 + \operatorname{cosec} \theta - 1}{\operatorname{cosec}^2 \theta - 1}$	B1	Allow denominator unsimplified
	$\frac{2\operatorname{cosec} \theta}{\cot^2 \theta}$	B1	
	$\frac{2}{\sin \theta} \times \frac{\sin^2 \theta}{\cos^2 \theta}$ $2 \sin \theta \sec^2 \theta$	B1	Sufficient detail must be seen
12(b)	$2 \sin 2\phi \sec^2 2\phi = 4 \sin 2\phi$ Leading to $\sin 2\phi = 0$ $\phi = \pm 90^\circ, 0^\circ$	2	M1 for attempt to solve $\sin 2\phi = 0$ obtaining at least one correct solution A1 for all solutions
	$2 \sin 2\phi \sec^2 2\phi = 4 \sin 2\phi$ $\cos 2\phi = (\pm) \frac{1}{\sqrt{2}}$	M1	For dealing with $\sec^2 2\phi$ to obtain $\cos 2\phi = k$, where $0 \leq k \leq 1$
	$\phi = \pm 67.5^\circ, \pm 22.5^\circ$	3	M1 for solution to obtain at least one correct solution A1 for a correct pair of solutions A1 for a second correct pair of solutions with no extra solutions within the range

Question	Answer	Marks	Guidance
13	$f'(x) = 4(3x+4)^{\frac{1}{2}} \quad (+c)$	2	M1 for $a(3x+4)^{\frac{1}{2}}$ A1 for $4(3x+4)^{\frac{1}{2}}$
	$18 = 4(4) + c$	M1	Dep M mark for attempting correctly to find the value of the arbitrary constant
	$c = 2$	A1	
	$f(x) = \frac{8}{9}(3x+4)^{\frac{3}{2}} \quad (+2x+d)$	M1	For $b(3x+4)^{\frac{3}{2}}$
	$f(x) = \frac{8}{9}(3x+4)^{\frac{3}{2}} + 2x \quad (+d)$	A1	Allow unsimplified
	$\frac{64}{9} = \frac{64}{9} \quad (+8) + d$	M1	Dep M mark for attempt to find a second arbitrary constant
	$f(x) = \frac{8}{9}(3x+4)^{\frac{3}{2}} + 2x - 8$	A1	



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

October/November 2022

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Maximum Mark: 80

<p>Published</p>

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GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

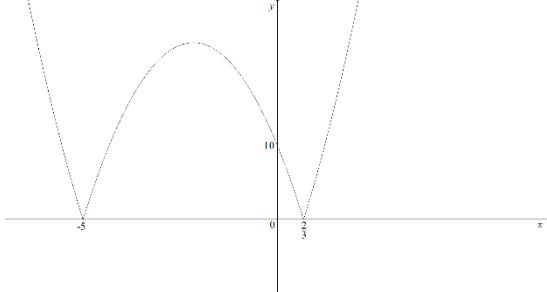
Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

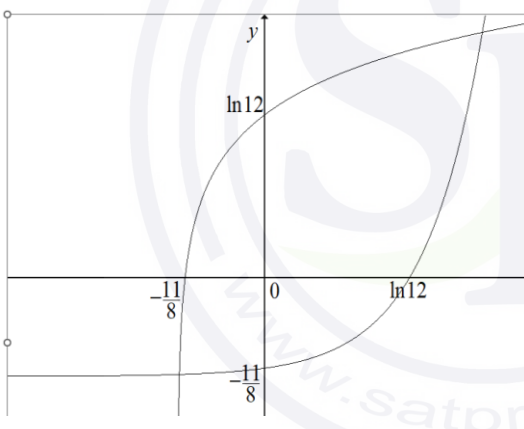
Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$a = 2$	B1	
	$b = 3$	B1	
	$c = -4$	B1	
2(a)		4	<p>B1 for a correct basic shape, allow 'construction curve'</p> <p>Dep B1 for (0, 10) must have correct basic shape, must be convinced that this is the vertical intercept</p> <p>B1 for $(-5, 0)$ and $(\frac{2}{3}, 0)$ or $(0.667, 0)$</p> <p>or better</p> <p>Dep B1 on all previous B marks for all correct with cusps and the correct shape for $x < -5$ and $x > \frac{2}{3}$</p>
2(b)	Stationary point when $x = -\frac{13}{6}$ so	M1	For differentiation or completing the square or use of symmetry
	$(-\frac{289}{12})$ or (-24.1) or better	A1	For y-value of stationary point, allow +ve or -ve value.
	$k > \frac{289}{12}$ or $k > 24.1$ or better	A1	
	$k = 0$	B1	
	Alternative		
	$3x^2 + 13x - (10 + k)$ Using discriminant, $169 + 12(10 + k)$	(M1)	Allow a sign error in $3x^2 + 13x - (10 + k)$, but must have a term in k not k^2
	Critical value $(-\frac{289}{12})$ or (-24.1) or better	(A1)	
	$k > \frac{289}{12}$ or $k > 24.1$ or better	(A1)	One solution only from correct work
	$k = 0$	(B1)	

Question	Answer	Marks	Guidance
3	$\frac{3}{8}p^{-2}q^{\frac{3}{2}}r^{-\frac{16}{5}}$	4	B1 for $k = \frac{3}{8}$ or 0.375 B1 for $a = -2$ B1 for $b = \frac{3}{2}$ oe B1 for $c = -\frac{16}{5}$, -3.2, $-3\frac{1}{5}$
4	$\tan\left(2x + \frac{\pi}{4}\right) = \frac{1}{\sqrt{3}}$ or $\sin^2\left(2x + \frac{\pi}{4}\right) = \frac{1}{4}$ or $\cos^2\left(2x + \frac{\pi}{4}\right) = \frac{3}{4}$	B1	Must be from correct working Allow if $\theta = 2x + \frac{\pi}{4}$ oe
	$2x + \frac{\pi}{4} = \frac{\pi}{6}, \frac{7\pi}{6}, \frac{13\pi}{6}$ $x = -\frac{\pi}{24}$	M1	Dep on previous B1 For attempt at the correct order of operations, may be implied by a correct solution or $x = -\frac{\pi}{24}$.
	$x = \frac{11\pi}{24}$ or $\frac{23\pi}{24}$ oe 0.458 π or 0.958 π 1.44 or 3.01	2	Dep M1 for an attempt to find a solution within the given range. Must be working with $\frac{7\pi}{6}$ or $\frac{13\pi}{6}$ A1 for either
	$x = \frac{11\pi}{24}$ or $\frac{23\pi}{24}$ oe 0.458 π or 0.958 π 1.44 or 3.01	A1	For a second solution within the given range with no extra solutions within the range.
5(a)	25	B1	soi
	$\begin{pmatrix} 56 \\ -192 \end{pmatrix}$ or $8\begin{pmatrix} 7 \\ -24 \end{pmatrix}$	B1	
5(b)	$\overrightarrow{AC} = \frac{1}{3}(\mathbf{b} - \mathbf{a})$ or $\overrightarrow{CB} = \frac{2}{3}(\mathbf{b} - \mathbf{a})$ oe	B1	
	$\overrightarrow{OC} = \mathbf{a} + \frac{1}{3}(\mathbf{b} - \mathbf{a})$ or $\mathbf{b} - \frac{2}{3}(\mathbf{b} - \mathbf{a})$ oe	M1	For using $\overrightarrow{OA} + \text{their } \overrightarrow{AC}$ or $\overrightarrow{OB} + \text{their } \overrightarrow{BC}$ oe
	$\frac{2}{3}\mathbf{a} + \frac{1}{3}\mathbf{b}$	A1	

Question	Answer	Marks	Guidance
5(c)	$2p + 2q = -5p + 5$ or $p + 4q = 5p + 5q$	M1	For equating like vectors to obtain at least one equation
	$p = -5, q = 20$	2	Dep M mark for attempt to solve <i>their</i> equations to obtain both p and q A1 for both
6	1144	3	B1 With the brothers: 220 or $^{12}C_3$ B1 Without the brothers: 924 or $^{12}C_6$
7(a)	2.8 oe	B1	
7(b)	$(BC = AC =) 10 \tan 1.4$ or $\frac{10 \sin 1.4}{\sin 0.1708}$	M1	
	Perimeter = $10(\text{their } 2.8) + 2(\text{their } AC \text{ or } BC)$	M1	
	144	A1	
7(c)	Area of triangle AOC or $BOC =$ $\frac{1}{2} \text{their } (AC \text{ or } BC) \times 10$ or $\frac{1}{2} \text{their } OC \times 10 \sin 1.4$ soi	M1	Allow premature approximation for OC
	Area of minor sector $AOB = 140$	B1	FT on $50 \times \text{their } 2.8$
	Shaded area = 439 to 440	A1	Must have $579 \leq \text{kite area} \leq 580$
8(a)	-1.5	B1	
8(b)	$f \in \mathbb{R}$	B1	Allow $y \in \mathbb{R}, \mathbb{R}, -\infty < f(x) < \infty$ oe, $f(x) \in \mathbb{R}$

Question	Answer	Marks	Guidance
8(c)	$\ln(8x+12)$ or $\ln(4(2x+3))$	B1	May be implied
	$f^{-1}(x) = \frac{e^x - 12}{8}$ oe	2	M1 for attempt to find the inverse, allow one sign error A1 allow $y = \dots$
	Range: $f^{-1} > \text{their}(-1.5)$	B1	Must be correct notation, follow through on <i>their</i> (a) $f^{-1}(x) > \text{their}(-1.5)$, $y > \text{their}(-1.5)$
	Alternative		
	$f^{-1}(x) = \frac{e^{x-\ln 4} - 3}{2}$ oe	(3)	B1 for $e^{x-\ln 4}$ or $e^{y-\ln 4}$ M1 for attempt to find the inverse, allow one sign error A1 allow $y = \dots$
	Range: $f^{-1} > \text{their}(-1.5)$	(B1)	Must be correct notation, follow through on <i>their</i> (a) $f^{-1}(x) > \text{their}(-1.5)$, $y > \text{their}(-1.5)$
8(d)		4	B1 for correct shape of $f(x)$ in quadrants 1, 2 and 3, with asymptotic behaviour B1 for $\ln 12$ and $-\frac{11}{8}$ or -1.375 in correct position, must have a correct shape. B1 for correct shape of $f^{-1}(x)$ in quadrants 1, 3 and 4, with asymptotic behaviour B1 for $\ln 12$ and $-\frac{11}{8}$ or -1.375 in correct position, must have a correct shape and intersect at least once with $y = f(x)$
9(a)	$\frac{(4x-1)(2x+1) - (4x-1) + 4(2x+1)^2}{(2x+1)^2(4x-1)}$	M1	For attempt to obtain a single fraction An extra term of $(2x+1)$ throughout must be dealt with correctly before awarding M1
	$\frac{24x^2 + 14x + 4}{(2x+1)^2(4x-1)}$	A1	Must see sufficient detail of expansion and collecting terms cso as AG

Question	Answer	Marks	Guidance
9(b)	$\frac{1}{2} \ln(2x+1)$	B1	
	$\frac{1}{2(2x+1)}$	B1	Allow $\frac{-(2x+1)^{-1}}{-1 \times 2}$ oe
	$\ln(4x-1)$	B1	
	$\left(\frac{1}{2} \ln 3 + \frac{1}{6} + \ln 3\right) - \left(\frac{1}{2} \ln 2 + \frac{1}{4}\right)$	M1	For correct application of limits, must have at least one log term. Must be using individual fractions from (a) Fractions and log terms must be bracketed correctly and manipulated correctly
	$\frac{1}{2} \ln \frac{27}{2} - \frac{1}{12}$	3	M1 for application of log laws using $\frac{1}{2} \ln 3 + \ln 3 - \frac{1}{2} \ln 2$ to obtain the correct form A1 for $\frac{1}{2} \ln \frac{27}{2}$ B1 for $-\frac{1}{12}$
10(a)	Common difference = $4 \lg x$	B1	
	Sum to n terms = $\frac{n}{2}(2 \lg x + (n-1)(4 \lg x))$	M1	For use of the sum formula with <i>their</i> common difference
	$n(2n-1) \lg x$	2	Dep M1 for a correct attempt to rearrange to the required form A1 cao
10(b)	$n(2n-1) = 4950$	M1	For $n((\text{their } p)n-1) = 4950$ together with an attempt to solve to obtain n
	50	A1	cao
10(c)	$50(99) \lg x = -14850$	M1	For use of <i>their</i> n and p in a complete method to find x or use of part (b)
	10^{-3} or equivalent	A1	

Question	Answer	Marks	Guidance
11(a)	$\frac{\left((t+1) \times \frac{3}{2} \times 2 \times (2t+1)^{\frac{1}{2}} \right) - (2t+1)^{\frac{3}{2}}}{(t+1)^2}$	3	B1 for $\frac{3}{2} \times 2 \times (2t+1)^{\frac{1}{2}}$ M1 for a correct attempt at a quotient or a product A1 for all terms apart from $\frac{3}{2} \times 2 \times (2t+1)^{\frac{1}{2}}$ correct
	$\frac{(2t+1)^{\frac{1}{2}}}{(t+1)^2} (t+2)$	2	M1 dep on previous M mark for attempt to obtain in the required form
	Alternative		
	$s = \frac{(2t+1)^{\frac{3}{2}} - t - 1}{(t+1)}$ $\frac{\left((t+1) \times \left(3 \times (2t+1)^{\frac{1}{2}} - 1 \right) \right) - \left((2t+1)^{\frac{3}{2}} - t - 1 \right)}{(t+1)^2}$	(3)	B1 for $\frac{3}{2} \times 2 \times (2t+1)^{\frac{1}{2}}$ M1 for a correct attempt at a quotient or a product A1 for all terms apart from $\frac{3}{2} \times 2 \times (2t+1)^{\frac{1}{2}}$ correct
	$\frac{(2t+1)^{\frac{1}{2}}}{(t+1)^2} (t+2)$	(2)	M1 dep on previous M mark for attempt to obtain in the required form
11(b)	$(2t+1)^{\frac{1}{2}} (t+2) = 0$ oe has no real positive solutions so velocity is never zero	B1	FT on <i>their</i> positive linear factor Reference needs to be made to both factors.

Question	Answer	Marks	Guidance
12	$a^5x^5 + 2a^4x^4 + \frac{8}{5}a^3x^3$	3	B1 for each correct term, allow when first seen
	$1 - \frac{2b}{x} + \frac{b^2}{x^2}$	B1	
	$a = 2$	B1	
	$32 - 64b = -160$	M1	For using <i>their</i> expansions and <i>their</i> value for a to obtain two terms involving x^4
	$b = 3$	A1	
	$\frac{64}{5} - 192 + 288 = c$	M1	For using <i>their</i> expansions and <i>their</i> value for a to obtain three terms involving x^3
	$c = \frac{544}{5}$ oe	A1	
	Alternative		
	$a^5 (= 32)$	(B1)	
	$a = 2$	(B1)	
	$-2ba^5 + 2a^4 = -160$ soi $32 - 64b = -160$	(2)	B1 for $2a^4$ soi M1 For using <i>their</i> expansions and <i>their</i> value for a to obtain two terms involving x^4
	$b = 3$	(A1)	
	$\frac{8}{5}a^3 - 4a^4b + a^5b^2 = c$ $\frac{64}{5} - 192 + 288 = c$	(3)	B2 for both $\frac{8}{5}a^3$ and a^5b^2 B1 for either $\frac{8}{5}a^3$ or a^5b^2 if only one correct M1 for using <i>their</i> expansions and <i>their</i> value for a to obtain three terms involving x^3
	$c = \frac{544}{5}$ oe	(A1)	



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/13

Paper 1

October/November 2022

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2022 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

This document consists of **10** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

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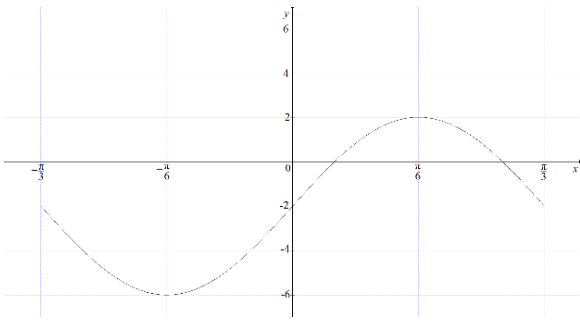
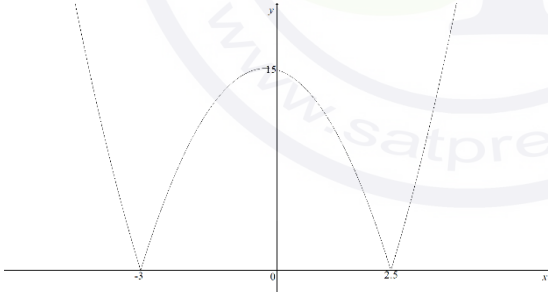
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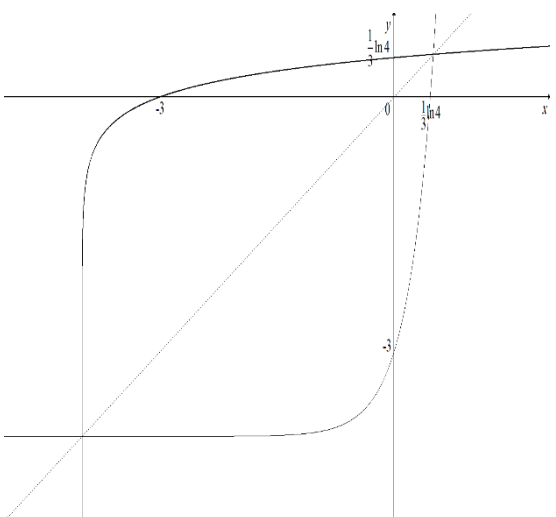
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- nfwf not from wrong working
- oe or equivalent
- rot rounded or truncated
- SC Special Case
- soi seen or implied

Question	Answer	Marks	Guidance
1		3	<p>B1 for a curve starting at $\left(-\frac{\pi}{3}, -2\right)$ and finishing at $\left(\frac{\pi}{3}, -2\right)$</p> <p>B1 for a curve, must have implied symmetry about $\frac{\pi}{6}$ and $-\frac{\pi}{6}$, one complete cycle only.</p> <p>B1 for a curve passing through $(0, -2)$ and distinct maximum at $\left(\frac{\pi}{6}, 2\right)$ and distinct minimum at only $\left(-\frac{\pi}{6}, -6\right)$</p>
2(a)	$2\left(x + \frac{1}{4}\right)^2 - \frac{121}{8}$	2	<p>B1 for $a = \frac{1}{4}$</p> <p>B1 for $b = -\frac{121}{8}$</p>
2(b)	$\left(-\frac{1}{4}, -\frac{121}{8}\right)$	2	<p>FTB1 for each, follow through on <i>their</i> a and b from (a) or SC1 if differentiation is used ie $\frac{dy}{dx} = 4x + 1 = 0$ then $\left(-\frac{1}{4}, -\frac{121}{8}\right)$</p>
2(c)		3	<p>B1 for a correct shape. Must have the parabola part of the curve in the first and second quadrant with cusps and correct curvature and a max in the 2nd quadrant. Ignore labelling of their maximum point if incorrect coordinates</p> <p>B1 for a curve $\left(\frac{5}{2}, 0\right)$ and $(-3, 0)$</p> <p>B1 for a curve $(0, 15)$</p>
2(d)	$k = \frac{121}{8}$	B1	FT Follow through on <i>their</i> $-b$

Question	Answer	Marks	Guidance
3(a)	$3y^2 + 2y - 1 [= 0]$ oe or $4x^2 - 4x - 3 [= 0]$ oe	M1	M1 for obtaining a 3 term quadratic equation in y or x and an attempt to solve
	$x = \frac{3}{2}, x = -\frac{1}{2}$ oe	A1	
	$y = \frac{1}{3}, y = -1$ oe	A1	Allow A1 for the one correct pair e.g. $\left(\frac{3}{2}, \frac{1}{3}\right)$ or $\left(-\frac{1}{2}, -1\right)$
3(b)	$[\log_3 x + 3] = \frac{10}{\log_3 x}$ oe or $\frac{1}{\log_x 3} [+3 = 10 \log_x 3]$ oe	B1	For change of base
	$(\log_3 x)^2 + 3 \log_3 x - 10 = 0$ or $10(\log_x 3)^2 - 3 \log_x 3 - 1 = 0$ $\log_3 x = -5 \quad \log_3 x = 2$ or $\log_x 3 = -\frac{1}{5} \quad \log_x 3 = \frac{1}{2}$	M1	Dep on previous B mark, for attempt to obtain a 3-term quadratic equation and attempt to solve to obtain 2 solutions of the form $\log_3 x = p$ or $\log_x 3 = q$
	$3^{-5} \quad 3^2$ isw	2	A1 for each
4(a)	$p'(x) = 3ax^2 + 26x + b$ $p'(0) = b$	B1	Must see at least $p'(x) = 3ax^2 + 26x + b$ to award the mark
4(b)	$p\left(-\frac{2}{3}\right): 8a - 27c = 318$ oe	M1	For use of $x = -\frac{2}{3}$, at least once and attempt at simplification leading to an equation in a and c only Allow one sign error.
	$p(-1): a - c = 16$ oe	M1	For use of $x = -1$ and attempt at simplification leading to an equation in a and c only
	$a = 6, c = -10$	2	M1 dep on both previous M marks and attempt to solve simultaneously to obtain both a and c A1 for both
4(c)	$2x^2 + 3x - 5$	B1	Allow if seen embedded i.e.: $(3x + 2)(2x^2 + 3x - 5)$ or as a quotient in long division

Question	Answer	Marks	Guidance
4(d)	$(3x+2)(x-1)(2x+5)$	B1	
5(a)	$r^3 = \frac{1}{8}$ soi	M1	Allow unsimplified $ar^{14} = \frac{1}{8}ar^{11}$ or $\frac{5r^{11} - 5r^{12}}{5r^{14} - 5r^{15}} = 8$ oe
	$r = \frac{1}{2}$	A1	
	$5 = \frac{a}{1-r}$	M1	For use of sum to infinity with <i>their</i> r , must be $-1 < r < 1$
	$a = \frac{5}{2}$	A1	
5(b)	$their(a) \times \frac{(1 - (their\ r)^n)}{(1 - their\ r)}$	M1	For use of the sum to n terms
	$(their\ r)^n = 0.0002$ (12.29)	M1	M1 dep For simplification and attempt to obtain the critical value using either an equation or an inequality leading to $n =$ or $n >$
	13	A1	Accept $n \geq 13$
6(a)	$f > -4$	B1	Allow $y > -4$ or $-4 < f < \infty$ or $f \in (-4, \infty)$
6(b)	$[f^{-1}(x)] = \frac{1}{3}\ln(x+4)$	2	M1 for a correct method to find the inverse, allow one sign error Must be in the form of $3x = \ln(y \pm 4)$ or $3y = \ln(x \pm 4)$ A1 allow $y =$

Question	Answer	Marks	Guidance
6(c)		4	B1 for $f(x)$ with correct shape in quadrant 1, 3 and 4 and appropriate asymptotic behaviour B1 for -3 on the y -axis and $\frac{1}{3}\ln 4$ on the x -axis for $f(x)$ must have the correct shape B1 for $f^{-1}(x)$ with correct shape in quadrant 1, 2 and 3 and appropriate asymptotic behaviour B1 for -3 on the x -axis and $\frac{1}{3}\ln 4$ on the y -axis for $f^{-1}(x)$ must have correct shape and intersect at least once
7	$\frac{1}{3}\sin 3x - 2\cos 2x + x$	2	M1 for $a\sin 3x + b\cos 2x + x$, $a \neq \pm 3$ and $b \neq \pm 8$ A1 all correct
	$\left(\frac{1}{3}\sin \frac{3\pi}{2} - 2\cos \pi + \frac{\pi}{2}\right) - (-2)$	M1	Dep on previous M mark for correct substitution (seen or implied) of both limits in x
	$\frac{11}{3}$	A1	
	$\frac{\pi}{2}$	B1	From correct substitution (seen or implied) of both limits in x
8(a)	1.75	B1	
8(b)	$\cos BOC = \frac{7}{25}$, $\tan BOC = \frac{24}{7}$, $\sin BOC = \frac{24}{25}$ $BOC = 1.287$ soi	B1	
	Arc length = $r \times \text{their } 1.287$	B1	Follow through on <i>their</i> BOC
	Perimeter = $12.25 + \text{their } 9.009 + 14$	M1	For a complete method
	35.3	A1	
8(c)	$\left(\frac{1}{2} \times 7^2 \times 1.75\right) + \left(\frac{1}{2} \times 7^2 \times \text{their } BOC\right)$ oe or $\pi \times 7^2 - \frac{1}{2} \times 7^2 \times (2\pi - 1.75 - \text{their } 1.287)$	M1	For a complete method
	74.4	A1	
9(a)(i)	665 280	B1	
9(a)(ii)	221 760	B1	

Question	Answer	Marks	Guidance
9(b)	$8 \times 4 \times 3 \times 2 \times 1 \times 7$	M1	For either 8×7 or $4!$ or 24 as part of a product
	1344	A1	
10	$\tan(3x + 1.2) \left[= \frac{1}{\sqrt{2}} \right]$ or $\cos^2(3x + 1.2) \left[= \frac{2}{3} \right]$ or $\sin^2(3x + 1.2) \left[= \frac{1}{3} \right]$	M1	For an attempt to obtain an equation in $\sin(3x + 1.2)$, $\cos(3x + 1.2)$ or $\tan(3x + 1.2)$
	$x = -1.24, -0.195, 0.852$ or better	4	M1 dep for a correct attempt to obtain one correct solution A1 for one correct solution in the range M1 dep for an attempt to obtain another solution within the range A1 for 2 more correct solutions within the range and no extra solutions within the range
11	$\ln(3x + 2) - \ln(2x + 1) - \ln x$	2	B1 for 1 correct term B1 for the other two terms correct
	$\ln \frac{(3a + 2)}{a(2a + 1)} - \ln \frac{5}{3}$ $\ln \frac{3(3a + 2)}{5a(2a + 1)} = \left[\ln \frac{1}{5} \right]$ or $\ln \frac{(3a + 2)}{a(2a + 1)} = \ln \frac{1}{3}$	2	M1 for application of limits correctly, dep on at least one B mark M1 for application of log laws to obtain a single logarithm, dep on at least one B mark
	$a^2 - 4a - 3 = 0$ $a = 2 + \sqrt{7}$	2	M1 for equating to $\ln \frac{1}{5}$ and attempt to solve resulting 3-term quadratic equation, dep on at least one B mark A1 for $2 + \sqrt{7}$ must reject $2 - \sqrt{7}$

Question	Answer	Marks	Guidance
12(a)	$\left(\frac{dy}{dx} = \frac{(x-1) \times \frac{2}{3} \times 6x(3x^2-2)^{-\frac{1}{3}} - (3x^2-2)^{\frac{2}{3}}}{(x-1)^2}\right)$ or $\left(\frac{dy}{dx} = \frac{(x-1)^{-1} \times \frac{2}{3} \times 6x(3x^2-2)^{-\frac{1}{3}} - (x-1)^{-2} (3x^2-2)^{\frac{2}{3}}}{(x-1)^2}\right)$	3	B1 for $\frac{2}{3} \times 6x(3x^2-2)^{-\frac{1}{3}}$ M1 for differentiation of a quotient or product A1 for all terms other than $\frac{2}{3} \times 6x(3x^2-2)^{-\frac{1}{3}}$ correct
	$\frac{(3x^2-2)^{-\frac{1}{3}}}{(x-1)^2} (x^2-4x+2)$	2	M1 dep for attempt to factorise, must be in the form $\frac{(3x^2-2)^{-\frac{1}{3}}}{(x-1)^2} [ax(x-1) - (3x^2-2)]$ A1 all correct
12(b)	When $x=2$, $\frac{dy}{dx} = -\frac{2}{\sqrt[3]{10}}$ oe	M1	Dep on the differentiation M mark from part (a) For attempt to find the value of $their \frac{dy}{dx}$ when $x=2$
	$-\frac{2}{\sqrt[3]{10}} p$ or $-0.928p$	A1	
13(a)	Midpoint (10, -9)	B1	
	Gradient of $l = -\frac{5}{3}$	B1	
	Equation of l : $y+9 = -\frac{5}{3}(x-10)$ oe	M1	Must be using <i>their</i> perpendicular gradient and <i>their</i> mid-point
	$y = -4$	A1	

Question	Answer	Marks	Guidance
13(b)	Attempt to use <i>their</i> R and displacement vectors or Pythagoras to find S	M1	May be implied by one correct coordinate If Pythagoras is used: M1 for an attempt to reach to a 3-term quadratic with one variable using <i>their</i> equation and <i>their</i> midpoint from (a) e.g. $34x^2 - 680x + 646 = 0$
	(1, 6)	A1	
	(19, -24)	A1	





Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/11

Paper 1

May/June 2022

MARK SCHEME

Maximum Mark: 80

Published

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This document consists of **9** printed pages.

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- the specific skills defined in the mark scheme or in the generic level descriptors for the question
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GENERIC MARKING PRINCIPLE 3:

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- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
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- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

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GENERIC MARKING PRINCIPLE 5:

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2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

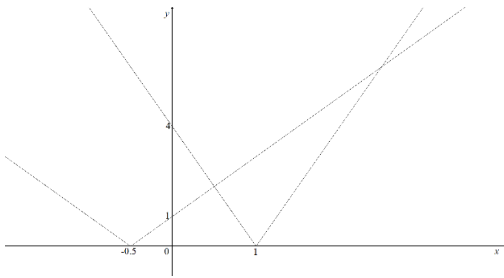
- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$p^{\frac{3}{2}}q^3r^{-2}$	3	B1 for $a = -\frac{3}{2}$ B1 for $b = \frac{8}{3}$ B1 for $c = -2$
2(a)	$\frac{ds}{dt} = -\frac{3}{2}(1+3t)^{-\frac{3}{2}}$	2	M1 for $a(1+3t)^{-\frac{3}{2}}$ A1 all correct
	When $t = 1$, $\frac{ds}{dt} = -\frac{3}{16}$ Speed = $\frac{3}{16}$	A1	
2(b)	Acceleration = $\frac{27}{4}(1+3t)^{-\frac{5}{2}}$	B1	Allow unsimplified
	$(1+3t)^{-\frac{5}{2}}$ is always positive (so acceleration can never be zero.)	B1	Any valid explanation.
3(a)	$f(x) \in \mathbb{R}$ oe	B1	Must be using correct notation, allow $y \in$
3(b)	$5(\ln(3x+1)) - 7 = 13$	M1	For correct order
	$x = \frac{e^4 - 1}{2}$	2	M1 for a correct attempt to solve to get $x =$, allow one sign error Dep on previous M mark A1 all correct must be exact
3(c)	$(f'(x)) = \frac{2}{2x+1}$	2	M1 for $\frac{a}{2x+1}$ A1 all correct
	$(g^{-1}(x)) = \frac{x+7}{5}$	B1	soi
	$2x^2 + 15x - 3 = 0$	M1	for equating and forming a 3-term quadratic equation = 0
	$x = 0.195, -7.69$	M1	For solution of <i>their</i> 3-term quadratic
	$x = 0.195$	A1	For discounting negative root.
4(a)	$[f(x)] = \pm 4(x+2)(x-1)(x-3)$	3	B1 for \pm B1 for 4 B1 for $(x+2)(x-1)(x-3)$

Question	Answer	Marks	Guidance
4(b)(i)		3	B1 for 2 V shapes which intersect twice in the first quadrant, with vertices on the x -axis, must be straight lines, not curves. B1 for -0.5 and 1 on the x -axis B1 for 1 and 4 on the y -axis
4(b)(ii)	$2x + 1 = 4(x - 1)$	M1	For attempt to solve to get $x =$
	$x = 2.5$	A1	
	$2x + 1 = -4(x - 1)$ oe	M1	For attempt to solve to get $x =$
	$x = 0.5$	A1	
	Alternative $4x^2 + 4x + 1 = 16x^2 - 32x + 16$	(M1)	For attempt to square each equation and equate
	$12x^2 - 36x + 15 = 0$ oe	(M1)	Dep on previous M mark for attempt to simplify to a 3-term quadratic equation, equated to zero and attempt to solve
	$x = 2.5 \quad x = 0.5$	(A2)	A1 for each
5(a)	$\begin{pmatrix} -7.5 \\ 4 \end{pmatrix}$ or $-\frac{1}{2}\begin{pmatrix} 15 \\ -8 \end{pmatrix}$ oe	2	B1 for $\begin{pmatrix} 7.5 \\ -4 \end{pmatrix}$ oe or B1 for $\begin{pmatrix} -15 \\ 8 \end{pmatrix}$
5(b)	$15a + 2a + 1 = 6b + 6a$ $5b + 2 = 2$	M1	For equating like vectors in order to obtain at least one equation
	$a = 1, b = 2$	2	Dep M1 for attempt to solve both equations A1 for both
6(a)	$k = 14$	B1	
	$k = 6$	B1	

Question	Answer	Marks	Guidance
6(b)(i)	$\frac{(1 + \tan \theta)(1 + \cos \theta) + (1 - \tan \theta)(1 - \cos \theta)}{1 - \cos^2 \theta}$	M1	Allow $(1 + \cos \theta)(1 - \cos \theta)$ in the denominator
	Expansion of numerator and simplification of denominator	M1	Dep on previous M mark
	Use of $\tan \theta \cos \theta = \sin \theta$	B1	soi
	$\frac{2(1 + \sin \theta)}{\sin^2 \theta}$	A1	Sufficient simplification to justify obtaining the given answer
6(b)(ii)	$2(1 + \sin \theta) = 3 \sin^2 \theta$ $3 \sin^2 \theta - 2 \sin \theta - 2 = 0$	M1	For use of part (a) and attempt to simplify to a 3-term quadratic equation equated to zero.
	$\sin \theta = \frac{1 - \sqrt{7}}{3} \text{ or } -0.5485\dots$	M1	M1 for attempt to solve and obtain a value for θ , may be implied by one correct solution
	213.3° and 326.7°	A2	A1 for one solution If 0 scored SC1 for awrt 213 and 327 Penalise excess solutions in the range
7(a)	Common difference = $2 \lg 3$	B1	Must be exact
	$\frac{n}{2}(2 \lg 3 + (n - 1)2 \lg 3) = 256 \lg 81$ or $\frac{n}{2}(\lg 9 + (n - 1)\lg 9) = 512 \lg 9$	M1	For use of the sum formula
	$\lg 81 = 4 \lg 3$ soi or $\lg 81 = 2 \lg 9$ soi	B1	Allow when working with decimal
	$n^2 = 1024$ oe	M1	Dep on first M mark, for attempt to simplify the sum equation by dividing through by $\lg 3$ oe to obtain an equation in n only
	$n = 32$ cao	A1	Must have exact working through out
7(b)	$\ln 256 = 4 \ln 4, \ln 16 = 2 \ln 4$ oe	M1	For use of power rule to obtain the common ratio
	Common ratio = 0.5	A1	
	$S_\infty = \frac{4 \ln 4}{1 - \text{their } r}$ oe	M1	Allow $\ln 256$ for first term and <i>their</i> r provided it is positive and < 1
	$16 \ln 2$	A1	

Question	Answer	Marks	Guidance
8(a)	$x^2 + 2\sqrt{5}x - 20 = 3\sqrt{5}x + 10$ $x^2 - \sqrt{5}x - 30 = 0$	M1	For equating x terms and simplifying to a 3-term quadratic equation equated to zero.
	$x = \frac{\sqrt{5} \pm \sqrt{5 - (4 \times -30)}}{2}$ oe	M1	Dep on previous M mark for attempt to solve to obtain $x =$, sufficient detail must be shown
	$x = 3\sqrt{5}$ $x = -2\sqrt{5}$	A1	For both
	$y = 55, y = -20$	A1	For both
8(b)	Use of $\operatorname{cosec}^2 \theta = 1 + \cot^2 \theta$	B1	May be implied by later work
	$\operatorname{cosec}^2 \theta = 1 + \frac{(2 + \sqrt{3})^2}{(\sqrt{3} - 1)^2}$	M1	For attempting to deal with tan correctly, forming a single fraction and simplifying, with sufficient detail – at least 4 terms in the numerator
	$\operatorname{cosec}^2 \theta = \frac{11 + 2\sqrt{3}}{4 - 2\sqrt{3}}$	A1	
	$\operatorname{cosec}^2 \theta = \frac{11 + 2\sqrt{3}}{4 - 2\sqrt{3}} \times \frac{4 + 2\sqrt{3}}{4 + 2\sqrt{3}}$	M1	For attempt to rationalise <i>their</i> expression, with sufficient detail in the simplification of the numerator – at least 3 terms
	$14 + \frac{15\sqrt{3}}{2}$	A1	
	Alternative 1 Use of $\operatorname{cosec}^2 \theta = 1 + \cot^2 \theta$	(B1)	May be implied by later work
	$\cot \theta = \frac{2 + \sqrt{3}}{\sqrt{3} - 1}$ $= \frac{3\sqrt{3} + 5}{2}$	(2)	M1 for attempting to rationalise $\cot \theta$ or tan with sufficient detail in the simplification of the numerator – at least 3 terms
	$\operatorname{cosec}^2 \theta = 1 + \left(\frac{3\sqrt{3} + 5}{2} \right)^2$ $= 14 + \frac{15\sqrt{3}}{2}$	(2)	M1 for expressing as a single fraction and attempt to simplify to required form.

Question	Answer	Marks	Guidance
8(b)	Alternative 2 Use of $\operatorname{cosec}^2 \theta = 1 + \cot^2 \theta$ and $\cot^2 \theta = \frac{1}{\tan^2 \theta}$	(B1)	May be implied by later work
	$\tan^2 \theta = \frac{4 - \sqrt{3}}{7 + 4\sqrt{3}}$ $= 52 - 30\sqrt{3}$	(2)	M1 for attempting to rationalise $\tan^2 \theta$ with sufficient detail in the simplification of the numerator – at least 3 terms
	$\operatorname{cosec}^2 \theta = 1 + \left(\frac{1}{52 - 30\sqrt{3}} \right)^2$ $= 14 + \frac{15\sqrt{3}}{2}$	(2)	M1 for attempting to rationalise $\cot^2 \theta$ with sufficient detail in the simplification of the numerator – at least 3 terms and expressing as a single fraction and attempt to simplify to required form.
	Alternative 3 Use of right-angled triangle $\text{Hyp}^2 = 11 + 2\sqrt{3}$	(2)	M1 For attempt to calculate the square of hypotenuse
	$\operatorname{cosec}^2 \theta = \frac{11 + 2\sqrt{3}}{4 - 2\sqrt{3}}$	(B1)	for correct use of $\operatorname{cosec}^2 \theta$ with <i>their</i> squared hypotenuse
	$\operatorname{cosec}^2 \theta = \frac{11 + 2\sqrt{3}}{4 - 2\sqrt{3}} \times \frac{4 + 2\sqrt{3}}{4 + 2\sqrt{3}}$	(M1)	For attempt to rationalise <i>their</i> expression, with sufficient detail in the simplification of the numerator – at least 3 terms
	$14 + \frac{15\sqrt{3}}{2}$	A1	
9(a)	$\frac{1}{2}r^2\theta = 10, \theta = \frac{20}{r^2}$	B1	
	$[P =] 2r + r\theta$	M1	For substituting <i>their</i> θ in P
	$[P =] 2r + \frac{20}{r^2}$	A1	
9(b)	$\frac{dP}{dr} = 2 - \frac{20}{r^2}$	M1	For attempt to differentiate <i>their</i> answer to part (a) to obtain the form of $\left[\frac{dP}{dr} = \right] 2 + \frac{a}{r^2}$
	When $\frac{dP}{dr} = 0, r = \sqrt{10}$	2	Dep M1 for equating <i>their</i> $\frac{dP}{dr}$ to zero and attempt to solve A1 cao

Question	Answer	Marks	Guidance
9(c)	$\frac{d^2P}{dr^2} = \frac{40}{r^3}$ As r is positive, $\frac{d^2P}{dr^2}$ is also positive so minimum	2	M1 for a complete method, allow valid alternatives, if differentiated, must be in the form of $\left[\frac{d^2P}{dr^2} = \right] \frac{k}{r^3}$ A1 for a correct conclusion
9(d)	$\theta = 2$	B1	
10	$-1 = \tan\left(3p + \frac{\pi}{2}\right)$ $p = \frac{\pi}{12}$	2	M1 for a complete method to find the value of p
	$\frac{dy}{dx} = 3 \sec^2\left(3x + \frac{\pi}{2}\right)$	2	M1 for $a \sec^2\left(3x + \frac{\pi}{2}\right)$ A1 all correct
	When $x = \frac{\pi}{12}$, $\frac{dy}{dx} = 6$	M1	For attempt to find the gradient using <i>their</i> p from differentiation
	Equation of normal: $y + 1 = -\frac{1}{6}\left(x - \frac{\pi}{12}\right)$	M1	For attempt at normal equation using <i>their</i> p and $-\frac{1}{\text{their value for } \frac{dy}{dx}}$
	When $x = 0$, $y = \frac{\pi}{72} - 1$	M1	For attempt to find B using <i>their</i> normal equation (must be from differentiation)
	When $y = 0$, $x = \frac{\pi}{12} - 6$	M1	For attempt to find A using <i>their</i> normal equation (must be from differentiation)
	Mid-point $\left(\frac{\pi}{24} - 3, \frac{\pi}{144} - \frac{1}{2}\right)$	2	A1 for x value (must be exact) A1 for y value (must be exact)



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

May/June 2022

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Maximum Mark: 80

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Question	Answer	Marks	Guidance
1	$a = 5$	B1	
	$b = 4$	B1	
	$c = -3$	B1	
2	$\tan^2 \theta = \frac{1}{y+2}$ soi or $x = 1 + \tan^2 \theta$ soi	B1	Must be in terms of $\tan^2 \theta$
	Use of $\tan^2 \theta + 1 = \sec^2 \theta$ $\frac{1}{y+2} + 1 = x$ oe	M1	For a valid attempt to eliminate θ
	$y = \frac{1}{x-1} - 2$ or $y = \frac{3-2x}{x-1}$ oe	2	Dep M1 for attempt to rearrange to obtain in the required form A1 for a correct form
	Alternative $x = \frac{1}{\cos^2 \theta}$ and $y + 2 = \frac{\cos^2 \theta}{\sin^2 \theta}$ soi	(B1)	
	$y + 2 = \frac{\frac{1}{x}}{1 - \frac{1}{x}}$ oe	(M1)	For a valid attempt to eliminate θ , making use of $\sin^2 \theta + \cos^2 \theta = 1$
	$y = \frac{1}{x-1} - 2$ or $y = \frac{3-2x}{x-1}$ oe	(2)	Dep M1 for attempt to rearrange to obtain in the required form A1 for a correct form
3(a)	Gradient = 4 soi	B1	
	Intercept = -3 soi	B1	
	$\lg(2y+1) = 4x^2 - 3$ oe	M1	For $\lg(2y+1) = \text{their } m(x^2) + \text{their } c$
	$y = \frac{1}{2} \left(10^{4x^2-3} - 1 \right)$ or $y = \frac{10^{4x^2} - 1}{2}$	A1	
3(b)	$y = 0$	B1	Must have at least 3 marks from part (a)

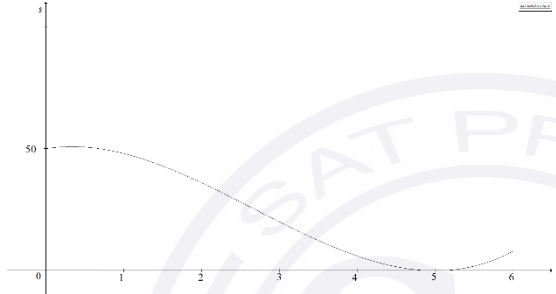
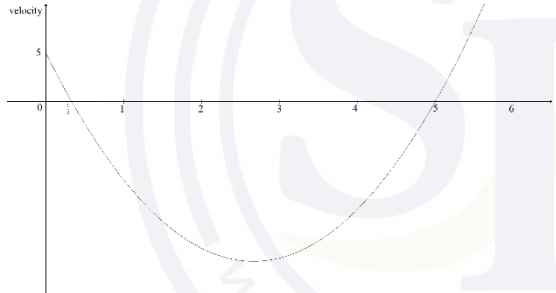
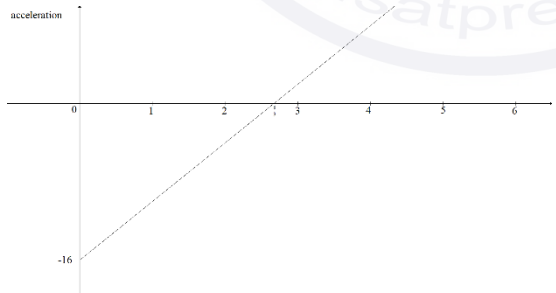
Question	Answer	Marks	Guidance
3(c)	$2 = \frac{1}{2}(10^{4x^2-3} - 1)$ oe and attempt to obtain $x = \dots$	M1	Dep on M mark in part (a) for use of $y = 2$ in <i>their</i> $y = \frac{1}{2}(10^{4x^2-3} - 1)$, $\frac{10^{4x^2} - 1}{2}$ $y = \frac{1000}{2}$ or $\lg(2y + 1) = 4x^2 - 3$ and attempt to obtain $x = \dots$
	$x = (\pm) 0.962$ or better	A1	
4(a)	$\frac{1}{17} \begin{pmatrix} -15 \\ 8 \end{pmatrix}$ oe	2	B1 for 17 seen
4(b)	$2a + 4b - 12 = 4b - 4a$ $-5 + 3 = 4a + 8b$	M1	For equating like vectors to obtain at least one equation
	$a = 2, b = -\frac{5}{4}$ oe	2	Dep M mark for solving <i>their</i> 2 equations to obtain both a and b
5	$\left(1 + \frac{x}{6}\right)^{12} = 1 + 2x + \frac{11x^2}{6}$	2	B2 for 3 correct terms B1 for 2 correct terms
	$(2 - 3x)^3 = 8 - 36x + 54x^2 \dots$	2	B2 for 3 correct terms B1 for 2 correct terms
	Term in x : $-36x + 16x$	M1	A correct method using <i>their</i> terms or coefficients, must be considering 2 terms
	$p = -20$ soi	A1	
	Term in x^2 : $\frac{88}{6}x^2 + 54x^2 - 72x^2$	M1	A correct method using <i>their</i> terms or coefficients, must be considering 3 terms
	$q = -\frac{10}{3}$ soi	A1	
6(a)	$p\left(\frac{1}{2}\right): a + 4b + 15 = 0$ oe	B1	For $p\left(\frac{1}{2}\right)$ equated to zero
	$p(2): 4a + b = 60$ oe	B1	For $p(2)$ equated to 120
	$a = 17, b = -8$	2	Dep M1 on both previous B marks, for solving <i>their</i> equations to obtain a and b A1 for both

Question	Answer	Marks	Guidance
6(b)	−8	B1	FT on <i>their integer b</i>
6(c)	$p'(x) = 18x^2 + 34x + 6$ $p''(x) = 36x + 34$	M1	For attempt to differentiate <i>their</i> $p(x)$, may be implied by correct FT answer
	$p''(0) = 34$	A1	FT on $2 \times$ <i>their integer a</i>
7(a)	$\frac{2(x-1)^2 - (x-1)(2x+3) + (2x+3)}{(x-1)^2(2x+3)}$	M1	Attempt at a fraction, allow with an extra $(x-1)$ term in each term of the numerator and the denominator
	$= \frac{8-3x}{(x-1)^2(2x+3)}$	A1	AG – must see sufficient detail to justify the given result, if an extra $(x-1)$ term involved, it must be dealt with correctly
7(b)	$\left[\ln(2x+3) - \ln(x-1) - \frac{1}{(x-1)} \right]_2^a$	3	B1 for each correct term
	$\left(\ln(2a+3) - \ln(a-1) - \frac{1}{a-1} \right) - (\ln 7 - 1)$	M1	Dep on at least one \ln term from integration, for applying limits correctly in <i>their</i> integral
	$\frac{a-2}{a-1} + \ln \left(\frac{2a+3}{7(a-1)} \right) \text{ oe}$	2	A1 for $\frac{a-2}{a-1}$ or $1 - \frac{1}{a-1}$ A1 for $\ln \left(\frac{2a+3}{7(a-1)} \right)$
	Alternative 1 final 2 marks $\frac{-1}{a-1} + \ln \left(\frac{e(2a+3)}{7(a-1)} \right) \text{ oe}$	(2)	A1 for $\frac{-1}{a-1}$ A1 for $\ln \left(\frac{e(2a+3)}{7(a-1)} \right)$
	Alternative 2 final 2 marks $\frac{a-2}{a-1} - \ln 7 + \ln \left(\frac{2a+3}{(a-1)} \right) \text{ oe}$	(2)	A1 for $\frac{a-2}{a-1} - \ln 7$ or $1 - \frac{1}{a-1} - \ln 7$ Allow 1.946 or better for $\ln 7$ A1 for $\ln \left(\frac{2a+3}{(a-1)} \right)$

Question	Answer	Marks	Guidance
7(b)	Alternative 3 final 2 marks $\frac{-1}{a-1} - \ln 7 + \ln \left(\frac{e(2a+3)}{(a-1)} \right)$ oe	2	A1 for $\frac{-1}{a-1} - \ln 7$ Allow 1.946 or better for $\ln 7$ A1 for $\ln \left(\frac{e(2a+3)}{(a-1)} \right)$
8(a)	With the sisters: 70 or 8C_4 oe	B1	
	Without the sisters: 28 or 8C_6 oe	B1	
	Total: 98	B1	
8(b)(i)	60480	B1	
8(b)(ii)	The start of the password and the end of the password can each be chosen 6 ways	B1	6 or 3P_2 oe seen twice
	The remaining characters can be chosen in 20 ways	B1	20 or 5P_2 oe seen
	Total number of ways: 720	B1	

Question	Answer	Marks	Guidance
9	When $x = 0$, $y = \ln 2$ soi	B1	May be implied in later work
	$\frac{dy}{dx} = \frac{(x+1)\frac{6x}{(3x^2+2)} - \ln(3x^2+2)}{(x+1)^2}$	3	B1 for $\frac{6x}{(3x^2+2)}$ allow when seen M1 for attempt at a quotient or product A1 for all other terms apart from $\frac{6x}{(3x^2+2)}$ correct
	When $x = 0$, $\frac{dy}{dx} = -\ln 2$	M1	Dep on previous M mark for attempt to find the gradient using <i>their</i> $\frac{dy}{dx}$
	Equation of normal: $y - \ln 2 = \frac{1}{\ln 2}x$	M1	For attempt at a normal equation using <i>their</i> y (not $3 \ln 2$) and $-\frac{1}{\text{their}(-\ln 2)}$, must be from an attempt at differentiation
	When $y = 0$, $x = -(\ln 2)^2$	M1	For attempt to find the value of x when $y = 0$ using <i>their</i> normal equation
	Gradient $BC = \frac{3 \ln 2}{(\ln 2)^2}$	M1	Dep on both previous M marks
	$\frac{3}{\ln 2}$ or $3(\ln 2)^{-1}$	A1	Must have correct exact working throughout

Question	Answer	Marks	Guidance
10(a)(i)	xy^2 soi	B1	Simplification of the left-hand side of the first equation
	$1 = \lg 10$ soi	B1	Simplification of right-hand side of equation
	$x - 3\left(\frac{10}{x}\right) = 13$	M1	For substitution of y^2 into linear equation oe and attempt to simplify
	$x^2 - 13x - 30 = 0$	A1	AG – must see sufficient detail to justify the given answer
	Alternative $y^2 = \frac{(x-13)}{3}$	(B1)	
	$\lg x + \lg \frac{(x-13)}{3} = 1$	(M1)	For attempt at substitution in the log equation
	$\frac{x(x-13)}{3} = 10$ oe	(B1)	
	$x^2 - 13x - 30 = 0$	(A1)	AG – must see sufficient detail to justify the given answer
10(a)(ii)	$x = 15$ only	B1	
	$y = \sqrt{\frac{2}{3}}$ or $\frac{\sqrt{6}}{3}$ or exact equivalent only	B1	isw once exact value seen
10(b)	$\log_a x + \frac{3}{\log_a x}$ or $\frac{1}{\log_x a} + 3\log_x a$	B1	For an appropriate change of base
	$(\log_a x)^2 - 4\log_a x + 3 = 0$ or $3(\log_x a)^2 - 4\log_x a + 1 = 0$	M1	For an attempt to obtain a 3-term quadratic equation in terms of $\log_a x$ or $\log_x a$, equated to zero.
	$\log_a x = 3$ $\log_a x = 1$ or $\log_x a = \frac{1}{3}$, $\log_x a = 1$	M1	Dep on previous M mark for correct solution of <i>their</i> quadratic equation
	$x = a$	A1	Must be from completely correct work
	$x = a^3$	A1	Must be from completely correct work

Question	Answer	Marks	Guidance
11(a)	$\frac{ds}{dt} = 3t^2 - 16t + 5$ oe	2	M1 for attempt at differentiation of a product or expansion and differentiation with at least two out of three terms of <i>their</i> expansion differentiated correctly A1 all correct, allow factorised
	$t = \frac{1}{3}, t = 5$	2	Dep M1 for attempt to solve <i>their</i> $\frac{ds}{dt} = 0$, must be in quadratic form A1 for both
11(b)		2	B1 for a correct curve in the first quadrant only. There must be an indication of a max point in the correct position and a min point at (5, 0) B1 for (0, 50) provided basic curve shape is correct
11(c)		2	B1 for a quadratic curve in the first and fourth quadrants B1 for (0, 5), $(\frac{1}{3}, 0)$ or (0.333, 0) marked and passing through (5, 0) on the x -axis
11(d)(i)	Acceleration = $6t - 16$	B1	
11(d)(ii)		2	B1 for a straight line with a positive gradient in the first and fourth quadrants, meeting the vertical axis Dep B1 for $(\frac{8}{3}, 0)$ or (2.67, 0) and (0, -16)



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/13

Paper 1

May/June 2022

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

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- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

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Maths-Specific Marking Principles	
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2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

- awrt answers which round to
- cao correct answer only
- dep dependent
- FT follow through after error
- isw ignore subsequent working
- nfwf not from wrong working
- oe or equivalent
- rot rounded or truncated
- SC Special Case
- soi seen or implied

Question	Answer	Marks	Guidance
1(a)	$243x^{10} - 45x^7 + \frac{10}{3}x^4$	3	B1 for $243x^{10}$ B1 for $-45x^7$ B1 for $\frac{10}{3}x^4$
1(b)	$\left(1 + \frac{1}{x^3}\right)^2 = 1 + \frac{2}{x^3} + \frac{1}{x^6}$ oe	B1	
	Coefficient of term in x^4 $= 243 - (2 \times 45) + \frac{10}{3}$	M1	For <i>their</i> $243 + 2 \times \text{their}(-45) +$ <i>their</i> $\frac{10}{3}$ Must have 3 terms
	$\frac{469}{3}$ oe	A1	
2(a)	$\cos BOA = \frac{7}{32}$ or $\sin \frac{BOA}{2} = \frac{5}{8}$	M1	
	$BOA = 1.350(263\dots)$ $BOA = 1.35$ (correct to 2 dp)	A1	Must see detail of extra decimal places to justify 2 dp answer
2(b)	$8\theta = 18$	M1	
	$\theta = 2.25$	A1	
2(c)	$\angle AOC = 2\pi - 2.25 - 1.35\dots$ (2.683)	M1	For use of $2\pi - \text{their}(b) - 1.35\dots$
	Area = $\frac{1}{2}64(\text{their } 2.683\dots)$	M1	For use of sector area formula
	85.9 or 85.8	A1	Allow awrt 85.9
	Alternative Area = $64\pi - \left(\frac{1}{2} \times 64 \times 1.35\dots\right) - \left(\frac{1}{2} \times 64 \times 2.683\right)$	(2)	M1 for a correct plan M1 for one correct use of sector area formula
	85.9 or 85.8	(A1)	Allow awrt 85.9 or 85.8

Question	Answer	Marks	Guidance
3(a)	$(2e^{3x} - 5)(e^{3x} + 1) = 0$	M1	For attempt to solve a 3-term quadratic equation in e^{3x} , or using an appropriate substitution. May also be implied by correct use of quadratic formula
	$x = \frac{1}{3} \ln \frac{5}{2}$	2	Dep M1 for a correct attempt to obtain $x = \dots$ A1 cao with negative root discounted.
3(b)	$e^{-x-7-7y} = e^{-2}$	M1	For correct attempt to deal with powers of e
	$x + 7y = -5$	A1	
	$x^2 + 5x - 126 = 0$ or $7y^2 + 5y - 18 = 0$	M1	Dep for attempt to obtain a 3-term quadratic equation equated to zero in either x or y
	$x = -14, x = 9$	A1	For both
	$y = \frac{9}{7}, y = -2$	A1	For both
4(a)	Intercept = -2 soi	B1	
	$e^{4y} = \frac{2}{5}x - 2$	M1	For attempt at straight line equation with <i>their</i> intercept
	$y = \frac{1}{4} \ln \left(\frac{2}{5}x - 2 \right)$ oe	A1	
4(b)	$y = \frac{1}{4} \ln 16$	M1	Dep on M1 in part (a)
	$y = \ln 2$	A1	
4(c)	$x > 5$	1	
5(a)	Acceleration = $18 \cos 3t$	2	B1 for $k \cos 3t$, $k \neq 2$, $k > 0$
	$\cos 3t = -\frac{1}{2}$ oe	M1	For attempt to solve <i>their</i> $\cos 3t = -\frac{1}{2}$ to obtain a value for t
	$t = \frac{2\pi}{9}$ or 0.698	A1	

Question	Answer	Marks	Guidance												
5(b)	$-2 \cos 3t \quad (+c)$	2	B1 for $k \cos 3t$, $k \neq 18$, $k < 0$												
	Displacement = $2 - 2 \cos 3t$	M1	For attempt to find value of c												
	2.92	A1													
	Alternative $-2 \cos 3t$	(2)	B1 for $k \cos 3t$, $k \neq 18$, $k < 0$												
	$[-2 \cos 3t]_0^{5.6}$ $= (-2 \cos 16.8) - (-2)$	(M1)	For correct application of limits using <i>their</i> $k \cos 3t$, $k \neq 18$, $k < 0$												
	2.92	(A1)													
6(a)	<table><tr><th>Expression</th><th>Function notation</th></tr><tr><td>0</td><td>g''</td></tr><tr><td>$4x$</td><td>f'</td></tr><tr><td>$8x^2 + 8x + 2$</td><td>fg</td></tr><tr><td>$4x + 3$</td><td>g^2</td></tr><tr><td>$\frac{x-1}{2}$</td><td>g^{-1}</td></tr></table>	Expression	Function notation	0	g''	$4x$	f'	$8x^2 + 8x + 2$	fg	$4x + 3$	g^2	$\frac{x-1}{2}$	g^{-1}	5	B1 for each one correct
Expression	Function notation														
0	g''														
$4x$	f'														
$8x^2 + 8x + 2$	fg														
$4x + 3$	g^2														
$\frac{x-1}{2}$	g^{-1}														
6(b)(i)	$a = 1$	B1													
6(b)(ii)	$h(x) \geq 3$	B1													
6(b)(iii)	$x = (y - 1)^2 + 3$ $y = 1 + \sqrt{x - 3}$	M1	For a correct attempt to find the inverse, allow one sign error												
	$h^{-1}(x) = 1 + \sqrt{x - 3}$	A1	Must be using correct notation												
	$x \geq 3$	B1	Must be using correct notation												

Question	Answer	Marks	Guidance
7(a)	$\frac{dy}{dx} = \frac{\left((x+5) \times \frac{3}{2} \times 2(2x+1)^{\frac{1}{2}} - (2x+1)^{\frac{3}{2}} \right)}{(x+5)^2}$	3	B1 for $\frac{3}{2} \times 2(2x+1)^{\frac{1}{2}}$ oe M1 for attempt to differentiate a quotient or product A1 for all terms other than $\frac{3}{2} \times 2(2x+1)^{\frac{1}{2}}$ correct
	$\frac{(2x+1)^{\frac{1}{2}}}{(x+5)^2} (x+14)$	A1	
7(b)	When $\frac{dy}{dx} = 0$, $x = -14$ and $x = -0.5$ but $x \geq 0$ so no stationary point	B1	FT on <i>their</i> $(x+14)$
7(c)	$\frac{5\sqrt{3}p}{12}$, $\frac{15\sqrt{3}p}{36}$ or $0.722p$	2	M1 for calculation of $\frac{dy}{dx}$ when $x = 1$ and multiplication by p
7(d)	$\frac{25\sqrt{3}}{24}$ or 1.80 oe	2	M1 for multiplication of <i>their</i> $\frac{dy}{dx}$ calculated in (c) by 2.5, must be numeric
8(a)(i)	17640	B1	
8(a)(ii)	Ends in a 5: 2160 or ${}^6P_1 \times {}^6P_4$	B1	
	Ends in a 0 : 2520 or ${}^7P_1 \times {}^6P_4$	B1	
	4680	B1	
8(a)(iii)	Starts with 85 : 360 Starts with 86 : 360 Starts with 87 : 360 Starts with 89: 360 oe 1440 or $4 \times {}^6P_4$	B1	
	Starts with 9 : 2520 or 7P_5	B1	
	3960	B1	

Question	Answer	Marks	Guidance
8(b)	With brothers : 126 or 9C_5	B1	
	Without brothers : 9 or 9C_8	B1	
	135	B1	
9(a)	$\sin^2\left(2\phi - \frac{\pi}{3}\right) = \frac{3}{4}$ soi	B1	
	$\phi = \frac{\pi}{3}, \frac{\pi}{2}, \frac{5\pi}{6}$	3	M1 for a correct method of solution, may be implied by one correct solution. A1 for a second correct solution A1 for a third correct solution and no extra solutions within the range
9(b)	$\cot^2 \theta = \frac{1}{y+1}$	B1	
	Attempt to use $\cot^2 \theta + 1 = \operatorname{cosec}^2 \theta$	M1	For attempt to eliminate θ
	$y = \frac{1}{2x-2} - 1$ oe	2	Dep M1 for attempt to rearrange to obtain the required form
	Alternative $\frac{1}{\sin^2 \theta} = 2x-1$ and $y+1 = \frac{\sin^2 \theta}{\cos^2 \theta}$	(B1)	
	$y+1 = \frac{\frac{1}{2x-1}}{1 - \frac{1}{2x-1}}$ oe	(M1)	For attempt to eliminate θ
	$y = \frac{1}{2x-2} - 1$ oe	(2)	Dep M1 for attempt to rearrange to obtain the required form
10(a)	$\frac{6(x+1)^2 + 4(2+3x) - 2(2+3x)(x+1)}{(2+3x)(x+1)^2}$	M1	For dealing with the fractions, allow an extra $(x+1)$ in each of the terms in the numerator and in the denominator Allow one sign error
	$\frac{(14x+10)}{(2x+3)(x+1)^2}$	A1	AG - Must have sufficient evidence of expansion and simplification to obtain the given answer

Question	Answer	Marks	Guidance
10(b)	$\left[2 \ln(2x+3) - \frac{4}{(x+1)} - 2 \ln(x+1) \right]$	3	B1 for each term, must have the correct signs with each term Must be using part (a)
	$\left(2 \ln 8 - \frac{4}{3} - 2 \ln 3 \right) - (2 \ln 2 - 4)$	M1	Dep on at least one log term in <i>their</i> integral, for use of limits
	$\frac{8}{3} + \ln \frac{16}{9}$	2	A1 for $\ln \frac{16}{9}$ A1 for $\frac{8}{3}$





Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

February/March 2022

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

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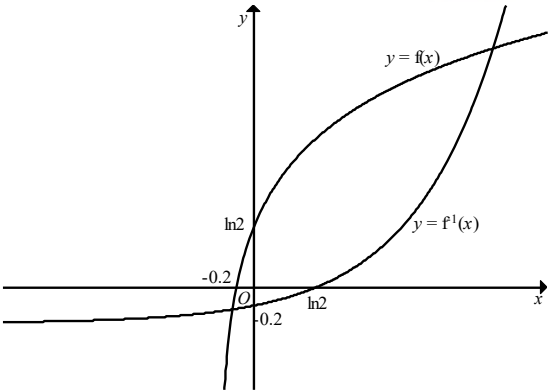
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- cao correct answer only
- dep dependent
- FT follow through after error
- isw ignore subsequent working
- nfwf not from wrong working
- oe or equivalent
- rot rounded or truncated
- SC Special Case
- soi seen or implied

Question	Answer	Marks	Guidance
1	$9kx + 1 = kx^2 + 3(2k + 1)x + 4$, leading to $kx^2 + x(3 - 3k) + 3 [= 0]$	M1	For equating the two equations and attempt to obtain a 3 term quadratic equation equated to zero.
	$(3 - 3k)^2 - (4 \times 3k)$ oe	M1	Dep on previous M mark for attempt to use the discriminant in any form
	$3k^2 - 10k + 3$ oe	M1	Dep on previous M mark for simplification to a 3 term quadratic expression in terms of k
	Critical values 3 and $\frac{1}{3}$	A1	For both
	$\frac{1}{3} < k < 3$	A1	Mark the final answer
2	$x = \frac{-(2\sqrt{3} + 5) \pm \sqrt{(2\sqrt{3} + 5)^2 - 4(3 - 5\sqrt{3})(-1)}}{2(3 - 5\sqrt{3})}$	M1	For the use of the quadratic formula
	$x = \frac{-(2\sqrt{3} + 5) \pm \sqrt{12 + 20\sqrt{3} + 25 + 12 - 20\sqrt{3}}}{2(3 - 5\sqrt{3})}$	M1	For expansion of the square root, must see at least 4 terms
	$x = \frac{-12 - 2\sqrt{3}}{2(3 - 5\sqrt{3})}$ oe, $x = \frac{2 - 2\sqrt{3}}{2(3 - 5\sqrt{3})}$ oe	A1	For both
	$x = \frac{-12 - 2\sqrt{3}}{2(3 - 5\sqrt{3})} \times \frac{3 + 5\sqrt{3}}{3 + 5\sqrt{3}}$ oe or $x = \frac{2 - 2\sqrt{3}}{2(3 - 5\sqrt{3})} \times \frac{3 + 5\sqrt{3}}{3 + 5\sqrt{3}}$ oe with an attempt to simplify	M1	For attempt to rationalise at least one of <i>their</i> solutions (must be similar structure) Sufficient detail must be seen, at least 3 terms in the numerator
	$\frac{1}{2} + \frac{\sqrt{3}}{2}$	A1	Must have sufficient detail shown
	$\frac{2}{11} - \frac{\sqrt{3}}{33}$	A1	Must have sufficient detail shown

Question	Answer	Marks	Guidance
3(a)	$b = \frac{1}{8}$	B1	
	$11 = a \sin \frac{4\pi}{8} + c$ $5 = a \sin \left(\frac{-4\pi}{3 \times 8} \right) + c$	M1	For attempt to form two simultaneous equations using given points, together with an attempt to obtain at least one unknown. Allow use of <i>their</i> b .
	$a = 4$	A1	
	$c = 7$	A1	
3(b)	Using symmetry	M1	For e.g. period is 16π , symmetrical about the line $x = 8\pi$
	For obtaining max at 4π and min at 12π	M1	
	$x = 12\pi$	A1	
	$y = 3$	A1	
	Alternative method 1		
	Minimum value when $y = 3$	(B2)	FT on <i>their</i> $-a + c$
	When $y = 3$, $x = 12\pi$.	(2)	M1 for attempt to solve <i>their</i> $3 = a \sin bx + c$ using <i>their</i> values of a , b and c to get $x = \dots$
	Alternative method 2		
	Min occurs $\frac{3}{4}$ through sine cycle so $x = 12\pi$	(B2)	
	When $x = 12\pi$, $y = 3$	(2)	M1 for attempt to solve $y = a \sin b(12\pi) + c$ using <i>their</i> values of a , b and c
	Alternative method 3		
	$\frac{dy}{dx} = ab \cos bx$ $(ab) \cos bx = 0$	(M1)	
	$x = 4\pi, 12\pi$	(M1)	Dep for attempt to solve to obtain $x =$
	$x = 12\pi$	(A1)	
	$y = 3$	(A1)	cao

Question	Answer	Marks	Guidance
4(a)	$\frac{(2x-1)+4}{(2x-1)^2} = \frac{2x+3}{(2x-1)^2}$	B1	
	Alternative method		
	$\frac{(2x-1)^2 + 4(2x-1)}{(2x-1)^3} = \frac{4x^2 + 4x - 3}{(2x-1)^3}$ $= \frac{(2x-1)(2x+3)}{(2x-1)^3} = \frac{2x+3}{(2x-1)^2}$	(B1)	
4(b)	Use of $\int \frac{1}{2x-1} + \frac{4}{(2x-1)^2} dx$ to obtain $\frac{1}{2} \ln(2x-1) - \frac{2}{(2x-1)}$	2	B1 for $\frac{1}{2} \ln(2x-1)$ or equivalent B1 for $-\frac{2}{(2x-1)}$, allow unsimplified
	$\left[\frac{1}{2} \ln(2x-1) - \frac{2}{(2x-1)} \right]_2^5$ $\left(\frac{1}{2} \ln 9 - \frac{2}{9} \right) - \left(\frac{1}{2} \ln 3 - \frac{2}{3} \right)$	M1	For application of limits, must be in the form $a \ln(2x-1) + \frac{b}{(2x-1)}$
	$= \frac{4}{9} + \ln \sqrt{3}$	2	A1 for $\ln \sqrt{3}$ A1 for $\frac{4}{9}$
5(a)	$\frac{dy}{dx} = \frac{\left(3x \times \frac{4x}{(2x^2-3)} \right) - 3 \ln(2x^2-3)}{9x^2}$ oe	3	B1 for $\frac{4x}{(2x^2-3)}$ M1 for attempt to differentiate a quotient or product A1 for all terms other than $\frac{4x}{(2x^2-3)}$ correct.
5(b)	When $x=2$, $\frac{dy}{dx} = 0.133$	M1	For substitution of $x=2$ into <i>their</i> $\frac{dy}{dx}$ and use of h
	$0.133h$	A1	
5(c)	$\frac{dx}{dt} = \frac{4}{0.133}$	M1	For $\frac{4}{\text{their value of } \frac{dy}{dx} \text{ from (b)}}$
	30.2	A1	

Question	Answer	Marks	Guidance
6	$\frac{dy}{dx} = 3\sec^2 3x$	2	M1 for $a\sec^2 3x$
	When $x = \frac{\pi}{12}$, $y = 2$	B1	
	When $x = \frac{\pi}{12}$, $\frac{dy}{dx} = 6$	M1	
	Gradient of perpendicular is $-\frac{1}{6}$	M1	For $-\frac{1}{\text{their } \frac{dy}{dx}}$, must be numeric
	Equation of normal $y - 2 = -\frac{1}{6}\left(x - \frac{\pi}{12}\right)$	M1	For attempt at a normal equation using <i>their</i> $-\frac{1}{6}$ and 2
	Area of triangle = 12	2	M1 dep for attempt at correct area using <i>their</i> 2 and <i>their</i> $12 + \frac{\pi}{12}$
7	$-\frac{1}{2}(2-3x)^{\frac{2}{3}}$	2	M1 for $a(2-3x)^{\frac{2}{3}}$, $a \neq -\frac{1}{2}$ Allow unsimplified
	When $x = -2$, $\frac{dy}{dx} = -6$ leading to $c = -4$	2	M1 Dep for correct attempt to find the value of the arbitrary constant
	$\frac{1}{10}(2-3x)^{\frac{5}{3}}$ nfw	2	M1 for $b(2-3x)^{\frac{5}{3}}$, $b \neq \frac{1}{10}$ Allow unsimplified
	When $x = -2$, $y = 10.2$ leading to $d = -1$	M1	Dep on previous M mark for attempt to find the value of a second arbitrary constant
	$y = \frac{1}{10}(2-3x)^{\frac{5}{3}} - 4x - 1$	A1	
8(a)	$\begin{pmatrix} -40 \\ 42 \end{pmatrix}$	B1	Allow $2\begin{pmatrix} -20 \\ 21 \end{pmatrix}$

Question	Answer	Marks	Guidance
8(b)	$\begin{pmatrix} 5 \\ -3 \end{pmatrix} + \begin{pmatrix} -40 \\ 42 \end{pmatrix} t$	B1	FT on <i>their</i> answer to (a), must be numeric but not $\begin{pmatrix} -20 \\ 21 \end{pmatrix}$
8(c)	$\begin{pmatrix} -35t + 4 \\ 44t - 2 \end{pmatrix} - \begin{pmatrix} 5 - 40t \\ -3 + 42t \end{pmatrix}$	M1	Allow if in the incorrect order, FT on <i>their</i> (b), must have correct structure
	$\begin{pmatrix} 5t - 1 \\ 2t + 1 \end{pmatrix}$	A1	
8(d)	$AB = \sqrt{(5t - 1)^2 + (2t + 1)^2}$	M1	For attempt at modulus and square root using <i>their</i> answer to (c)
	$\sqrt{29t^2 - 6t + 2}$	A1	
8(e)	$29t^2 - 6t - 4 = 0$	M1	For attempt to solve the square of <i>their</i> answer to (d) $-6 = 0$
	0.49 only	A1	
9(a)(i)	-0.4	B1	
9(a)(ii)	$f(x) \in \mathbb{R}$ oe	B1	
9(a)(iii)	$x = \ln(5y + 2)$ oe $e^x = 5y + 2$ oe	M1	For a correct attempt to find the inverse
	$f^{-1}(x) = \frac{e^x - 2}{5}$	A1	Must be in the correct form
	$x \in \mathbb{R}$	B1	
9(a)(iv)		4	B1 for two correctly shaped graphs in the correct quadrants B1 for a correct graph for $y = f(x)$ with correct intercepts B1 for a correct graph for $y = f^{-1}(x)$ with correct intercepts B1 all correct with symmetry implied, exact intercepts and two points of intersection

Question	Answer	Marks	Guidance
9(b)	$g^2(x) = \left(\left(x^{\frac{1}{2}} - 4 \right)^{\frac{1}{2}} - 4 \right)$	M1	For a correct order of operations
	$\left(\left(x^{\frac{1}{2}} - 4 \right)^{\frac{1}{2}} - 4 \right) = -2$ leading to $x^{\frac{1}{2}} = 8$,	M1	Dep on previous M mark for a correct attempt at a solution. Must deal with $x^{\frac{1}{2}}$ correctly to obtain the final solution
	$x = 64$	A1	
10(a)	Common difference = $4 \sin 3x$ soi	B1	
	$390 = \frac{20}{2} (2 \sin 3x + 19(4 \sin 3x))$	M1	M1 for attempt at sum to 20 terms using <i>their</i> common difference, equating to 390 and attempt to solve to obtain $\sin 3x = \dots$
	$\sin 3x = 0.5$	A1	
	$x = \frac{\pi}{18}, \frac{5\pi}{18}$	3	M1 for a correct attempt to solve, may be implied by one correct solution, allow if not exact A1 for 1 correct solution A1 for a second correct solution and no others in the range
10(b)(i)	Common ratio = $0.5 \cos y$	B1	
	$-0.5 < 0.5 \cos y < 0.5$	B1	Correct use of $ \text{common ratio} < 1$
10(b)(ii)	$9 = \frac{20 \cos y}{1 - 0.5 \cos y}$	B1	For attempt to use sum to infinity equation correctly and solve
	$\cos y = \frac{18}{49}$ or 0.367...	2	M1 for solution of <i>their</i> equation, must have r as a multiple of $\cos y$, to obtain $\cos y = \dots$
	1.19	A1	



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/11

Paper 1

October/November 2021

MARK SCHEME

Maximum Mark: 80

Published

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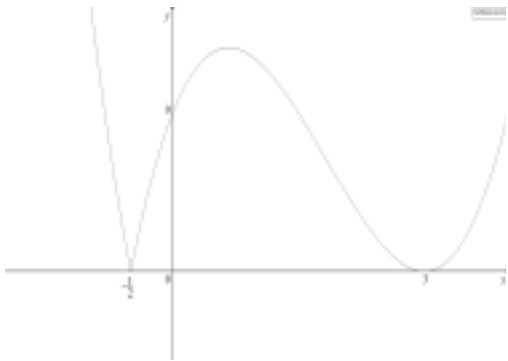
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Question	Answer	Marks	Guidance
1(a)	1080°	B1	
1(b)	$a = 4$	B1	
	$b = 3$	B1	
	$c = -2$	B1	
2(a)	(0, 14)	2	B1 for x -coordinate B1 for y -coordinate
2(b)	$y - 14 = -\frac{1}{2}x$	2	M1 for finding the gradient of a perpendicular line and attempt at the straight line equation using <i>their</i> B A1 Allow unsimplified
2(c)	Area = $\frac{1}{2} \times 14 \times 28$	M1	Must be a complete method making use of <i>their</i> answer to (b)
	196	A1	
3(a)	13 soi	B1	For finding the magnitude of $\begin{pmatrix} 12 \\ -5 \end{pmatrix}$
	$\begin{pmatrix} 36 \\ -15 \end{pmatrix}$	B1	
3(b)	$10 + 4\lambda = -4\mu$ or $-5 + 6\lambda = 5\mu$	2	M1 for equating like vectors Dep M1 for attempt to solve <i>their</i> simultaneous equations to obtain 2 solutions
	$\mu = -\frac{20}{11}$	A1	
	$\lambda = -\frac{15}{22}$	A1	
4(a)	$a = \frac{7}{2}$	B1	
	$b = 1$	B1	
	$c = \frac{1}{6}$	B1	

Question	Answer	Marks	Guidance
4(b)	$\left(3x^{\frac{2}{5}} - 5\right)\left(x^{\frac{2}{5}} - 1\right) = 0$	2	M1 for recognition of a quadratic in $x^{\frac{2}{5}}$ Dep M1 for solution and a correct attempt to get at least one solution for x
	3.59	A1	
	1	A1	
5(a)	$0 = 8a + 4b + 12 + 4$	B1	For $p(2)$
	$p'(x) = 3ax^2 + 2bx + 6$	M1	For an attempt to obtain $p'(x)$
	$3a - 2b + 6 = -7$	M1	Dep for $p'(-1)$
	$0 = 2a + b + 4$ $-13 = 3a - 2b$	M1	Dep on both previous M marks for solution of equations to obtain both a and b
	$a = -3 \quad b = 2$	A1	
5(b)	$p''(x) = -18x + 4$	M1	For differentiation of <i>their</i> $p'(x)$ to obtain $p''(x)$
	4	A1	FT on twice <i>their</i> b .
6	$\frac{dy}{dx} = me^{3x} + 2x^2 (+c)$	M1	
	$\frac{dy}{dx} = 2e^{3x} + 2x^2 (+c)$	A1	
	$5 = 2 + c$ $c = 3$	M1	Dep on previous M mark
	$f(x) = pe^{3x} + qx^3 \dots$	M1	
	$y = \frac{2}{3}e^{3x} + \frac{2}{3}x^3 \dots$	A1	
	$\frac{5}{3} = \frac{2}{3} + d$ $d = 1$	M1	Dep on previous M mark
	$(f(x) =) \frac{2}{3}e^{3x} + \frac{2}{3}x^3 + 3x + 1$	A1	
7(a)	6	B1	

Question	Answer	Marks	Guidance
7(b)	$b = 192a$	B1	May be implied by the term in x
	$c = 240a^2$	B1	May be implied by the term in x^2
	$\frac{c}{240} = \frac{b^2}{192^2}$	M1	For elimination of a
	$5b^2 = 768c$	A1	For correct manipulation to verify the given answer
7(c)	$a = \frac{1}{16}$	B1	
	$c = \frac{15}{16}$	B1	
8(a)	$\sin \frac{AOC}{2} = \frac{3}{5}$ or $6^2 = 5^2 + 5^2 - (2 \times 5 \times 5) \cos AOC$	M1	For a complete method to find AOC
	$AOC = 1.2870$ $AOC = 1.287$	A1	AG Must see $AOC = 1.2870$ or better before rounding for A1
8(b)	Arc length = 1.287×5	B1	
	Perimeter = 32.4	B1	
8(c)	Sector area = $\frac{1}{2} \times 5^2 \times 1.287$	B1	
	Area of triangle = $\frac{1}{2} \times 5^2 \times \sin 1.287$	B1	
	Total area = 28.1	B1	
9(a)	$\frac{dy}{dx} = 2(2x+1)(x-3) + 2(x-3)^2$ or $\frac{dy}{dx} = 6x^2 - 22x + 12$	M1	For differentiation of a quotient, or expansion and subsequent differentiation
	$0 = 2(x-3)(3x-2)$	M1	Dep for simplification, equating to zero and attempt to solve
	$(3, 0)$	A1	
	$\left(\frac{2}{3}, \frac{343}{27}\right)$	A1	

Question	Answer	Marks	Guidance
9(b)		4	B1 for correct shape with maximum in the first quadrant B1 for $\left(-\frac{1}{2}, 0\right)$ and $(3, 0)$ with a cubic curve with one max only B1 for $(0, 9)$ with a cubic curve with one max only B1 All correct with a cusp at $x = -\frac{1}{2}$ and a minimum at $x = 3$
9(c)	$\frac{343}{27}$	B1	FT on <i>their</i> answer from (a)
10(a)(i)	$2 + (n-1)0.5 = 16$ oe	M1	For use of $a + (n-1)d$
	$n = 29$	A1	
10(a)(ii)	$\frac{8}{2}(2(2) + 7(0.5))$	M1	For use of sum formula, may be implied if distances have been multiplied by 5 first.
	$\frac{8}{2}(2(2) + 7(0.5)) \times 5$	M1	For multiplication by 5
	150 (km)	A1	
10(b)(i)	$r = 1.25$ oe	B1	
10(b)(ii)	$2(1.25)^{n-1} > 16$ or $2(1.25)^{n-1} = 16$	M1	For use of ar^{n-1}
	$n-1 > \frac{\ln 8}{\ln 1.25}$ or $n-1 = \frac{\ln 8}{\ln 1.25}$	M1	Dep for correct method of solution to obtain $n-1$
	11	A1	
10(b)(iii)	$\frac{2(1.25^8 - 1)}{1.25 - 1}$	M1	For use of sum formula may be implied by multiplication by 5
	$\frac{2(1.25^8 - 1)}{1.25 - 1} \times 5$	M1	For multiplication by 5
	198 (km)	A1	Allow greater accuracy

Question	Answer	Marks	Guidance
11(a)	$3\cot^2 \theta - 5\cot \theta - 2 = 0$	M1	For use of correct identity and simplification to a 3 term quadratic equated to zero.
	$\tan \theta = -3, \tan \theta = \frac{1}{2}$	M1	Dep for solution of quadratic and dealing with cot
	108.4°	A1	
	26.6°	A1	
11(b)	$\phi + \frac{\pi}{3} = -\frac{\pi}{6}$	M1	For a correct order of operations
	$\phi = -\frac{\pi}{2}$	A1	
	$\phi + \frac{\pi}{3} = \frac{7\pi}{6}$	M1	For a correct order of operations
	$\phi = \frac{5\pi}{6}$	A1	



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

October/November 2021

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Maximum Mark: 80

<p>Published</p>

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- dep dependent
- FT follow through after error
- isw ignore subsequent working
- nfwf not from wrong working
- oe or equivalent
- rot rounded or truncated
- SC Special Case
- soi seen or implied

Question	Answer	Marks	Guidance
1(a)	$-3 < x < 1 \quad x > 5$	B1	
1(b)	$-\frac{1}{3}(x+3)(x-1)(x-5)$	3	B1 for a negative cubic function B1 for a cubic function multiplied by $\frac{1}{3}$ B1 for $(x+3)(x-1)(x-5)$
2(a)	$a = \frac{10}{3}$ or $3\frac{1}{3}$	B1	
	$b = \frac{7}{3}$ or $2\frac{1}{3}$	B1	
	$c = \frac{9}{2}$ or $4\frac{1}{2}$ or 4.5	B1	
2(b)	$10(2^p)^2 - 17(2^p) + 3 = 0$ $(5(2^p) - 1)(2(2^p) - 3) = 0$ $2^p = \frac{1}{5}, \quad 2^p = \frac{3}{2}$	M1	For recognition of a quadratic in 2^p , attempt to factorise and solve for 2^p
	$p = \frac{\ln \frac{1}{5}}{\ln 2}$ or $p = \frac{\ln 1.5}{\ln 2}$ oe	M1	For correct attempt to deal with $2^p = k$
	-2.32	A1	
	0.585	A1	
3(a)	$\lg \frac{1000a^2}{b^4}$	4	B1 for $3 = \lg 1000$
			B1 for use of power rule once
			B1 for use of addition or subtraction rule once
			B1 All correct

Question	Answer	Marks	Guidance
3(b)	Either $3\log_a 4 = \frac{3}{\log_4 a}$	B1	
	$2(\log_4 a)^2 - 7\log_4 a + 3 = 0$ $(2\log_4 a - 1)(\log_4 a - 3) = 0$ $\log_4 a = \frac{1}{2}$ or $\log_4 a = 3$	M1	For obtaining a quadratic equation and solution
	$a = 4^{\frac{1}{2}}$ or $a = 4^3$	M1	Dep For dealing with the logarithm correctly once, may be implied by a correct solution
	64	A1	
	2	A1	
	Or $2\log_4 a = \frac{2}{\log_a 4}$	(B1)	
	$3(\log_a 4)^2 - 7\log_a 4 + 2 = 0$ $(3\log_a 4 - 1)(\log_a 4 - 2) = 0$ $\log_a 4 = \frac{1}{3}$ or $\log_a 4 = 2$	(M1)	For obtaining a quadratic equation and solution
	$a^{\frac{1}{3}} = 4$ or $a^2 = 4$	(M1)	Dep For dealing with the logarithm correctly once, may be implied by a correct solution
	64	(A1)	
	2	(A1)	
4	$\tan\left(2x + \frac{\pi}{3}\right) = \frac{1}{\sqrt{3}}$	B1	
	$x = -\frac{7\pi}{12}, -\frac{\pi}{12}, \frac{5\pi}{12}, \frac{11\pi}{12}$	3	M1 for using correct order of operations A1 for two correct solutions A1 for two further correct solutions and no other solutions in range

Question	Answer	Marks	Guidance
5	Either Maximum when $\sin \frac{x}{3} = 1$ or minimum when $\sin \frac{x}{3} = -1$	M1	For recognition that value of maximum or minimum is necessary
	$c = 9$	A1	
	$c = -1$	A1	
	or $\frac{dy}{dx} = \frac{5}{3} \cos \frac{x}{3}$ When $\frac{dy}{dx} = 0$, $\sin \frac{x}{3} = +1$ or -1	(M1)	For differentiation, equating to zero to obtain values for $\sin \frac{x}{3}$
	$c = 9$	(A1)	
	$c = -1$	(A1)	
6(a)	$0 = -\frac{5}{4} + \frac{a}{4} + 5 + b$	M1	For use of the factor theorem
	$-24 = -10 + a + 10 + b$	M1	For use of the remainder theorem
	$a + 4b = -15$ $a + b = -24$ leading to	M1	Dep on both previous M marks for solution of <i>their</i> equations without using a calculator
	$a = -27$, $b = 3$	A1	
6(b)	$(2x+1)(5x^2 \dots\dots\dots + \text{their } b)$	M1	Allow for observation or algebraic long division. <i>Their</i> a and b must be integers.
	$(2x+1)(5x^2 - 16x + 3)$	A1	
	$(2x+1)(5x-1)(x-3)$	2	M1 for attempt to factorise <i>their</i> 3-term quadratic A1 all correct from fully correct working
6(c)	3	B1	FT on <i>their</i> (integer) b
7(a)(i)	b – a	B1	
7(a)(ii)	c – b	B1	

Question	Answer	Marks	Guidance
7(a)(iii)	$n\overrightarrow{AB} = m\overrightarrow{BC}$	M1	For substitution of <i>their</i> (i) and (ii) into $n\overrightarrow{AB} = m\overrightarrow{BC}$
	$na + mc = (m + n)b$	A1	For correct manipulation to obtain the given answer
7(b)	$2\lambda - 4\mu + 4 = 4\lambda + 4$ or $\lambda + 7\mu - 7 = -2\lambda - 2$	M1	For equating like components at least once, allow unsimplified
		M1	Dep for solving <i>their</i> equations to obtain both λ and μ
	$\mu = 5$	A1	
	$\lambda = -10$	A1	
8(a)	Either Starting with a 6: 120 ways	B1	May be implied by final answer
	Starting with 5, 7 or 9: 540 ways	B1	May be implied by final answer
	Total 660	B1	
	Or Alternative 1 Ending with a 6: 180 ways	(B1)	May be implied by final answer
	Ending with 0 or 4: 480ways	(B1)	May be implied by final answer
	Total 660	(B1)	
	Or Alternative 2 11 ways of obtaining even 5-digit numbers which start with 5, 6, 7, 9	(B1)	For $11 \times k$ May be implied by final answer
	5P_3 ways of arranging remaining 3 digits: 60	(B1)	For $m \times 60$ where m is from an attempt to list all cases for first and last digits May be implied by final answer
	$11 \times 60 = 660$	(B1)	
	Or Alternative 3 Total arrangements 7P_5 minus (all odds + evens starting with 1 + evens starting with 0 or 4) $= 2520 - (1440 + 180 + 240)$	(B2)	For $2520 - (1440 + 180 + 240)$
	660	(B1)	

Question	Answer	Marks	Guidance
8(b)	$\frac{n!}{(n-4)!4!} = \frac{6n!}{(n-2)!2!}$	B1	
	$(n-2)(n-3) = 72$	2	B1 for $(n-2)(n-3)$
			B1 for 72
	$n = 11$ only	2	M1 for correct attempt to form and solve a quadratic equation A1 for $n = 11$ only
9(a)	$AOD = 2 \times \tan^{-1}\left(\frac{2}{3}\right)$	M1	For correct method to find AOD
	$AOD = 1.1760...$ $AOD = 1.176$ [to 3dp]	A1	Need to see 4 dp or more to justify 3 dp answer
9(b)	Major arc $MN = (2\pi - 1.176)12$	B1	
	ND or $MA = 12 - \sqrt{13}$	B1	
	Perimeter = major arc $MN + MA + ND + 16$ oe	B1	For <i>their</i> values in a correct plan, may be implied by a correct answer
	Perimeter = 94.1	B1	
9(c)	Minor sector area = $\frac{1}{2} \times 1.176 \times 12^2$ or Major sector area = $\frac{1}{2} \times (2\pi - 1.176) \times 12^2$	B1	
	Area = major sector area – remainder of rectangle or Area = area of circle – minor sector area – remainder of rectangle or Area = circle – rectangle – minor sector + triangle AOD	B1	For <i>their</i> values in a correct plan, may be implied by a correct answer
	Area = 350	B1	Allow greater accuracy
10(a)	At A $y = 4$	B1	
	At B $y = \frac{13}{16}$ or 0.8125	B1	

Question	Answer	Marks	Guidance
10(b)	Either Area of trapezium = $\frac{231}{32}$	B1	Allow unsimplified
	$\int_{-1}^2 \frac{1}{(x+2)^2} + \frac{3}{x+2} dx$ $= \left[-\frac{1}{x+2} + 3\ln(x+2) \right]_{-1}^2$	2	B1 for $-\frac{1}{x+2}$ B1 for $3\ln(x+2)$
	$\left[\left(-\frac{1}{4} + 3\ln 4 \right) - (-1) \right]$	M1	For correct use of limits in <i>their</i> integral, but must have at least one of the two preceding B marks
	Area = $\frac{207}{32} - \ln 64$	2	A1 for $\frac{207}{32}$ A1 for $-\ln 64$
	Or $\int_{-1}^2 -\frac{17}{16}x + \frac{47}{16} - \frac{1}{(x+2)^2} - \frac{3}{x+2} dx$ $\left[-\frac{17}{32}x^2 + \frac{47}{16}x + \frac{1}{x+2} - 3\ln(x+2) \right]_{-1}^2$	(3)	B1 for $-\frac{17}{32}x^2 + \frac{47}{16}x$ B1 for $\int \frac{1}{(x+2)^2} dx = -\frac{1}{(x+2)}$ B1 for $\int \frac{3}{x+2} dx = 3\ln(x+2)$
	$\left(-\frac{17}{8} + \frac{47}{8} + \frac{1}{4} - 3\ln 4 \right) - \left(-\frac{17}{32} - \frac{47}{16} + 1 \right)$	(M1)	For correct use of limits in <i>their</i> integral, but must have at least one of the two preceding B marks
	Area = $\frac{207}{32} - \ln 64$	(2)	A1 for $\frac{207}{32}$ A1 for $-\ln 64$
11(a)(i)	0	B1	
11(a)(ii)	−3	B1	
11(a)(iii)	$\left(\frac{1}{2}(25+15) \times 30 \right) + \left(\frac{1}{2}(30+60) \times 10 \right) + \left(\frac{1}{2} \times 20 \times 60 \right)$	M1	For an unsimplified expression for the required area allowing at most one incorrect length
	Total distance = 1650	A1	
11(b)(i)	$v = 4 \cos \frac{5\pi}{3} - 4$ $= -2$	M1	
	Speed = 2	A1	

Question	Answer	Marks	Guidance
11(b)(ii)	$a = -12 \sin 3t$	B1	
	$\sin 3t = 0$ $3t = \pi$ Leading to	M1	For equating to zero and attempt to solve to obtain t , allow if in degrees
	$t = \frac{\pi}{3}$	A1	
11(b)(iii)	$s = k \sin 3t - 4t (+c)$	M1	
	$s = \frac{4}{3} \sin 3t - 4t$	A1	





Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/13

Paper 1

October/November 2021

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2021 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

This document consists of **11** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

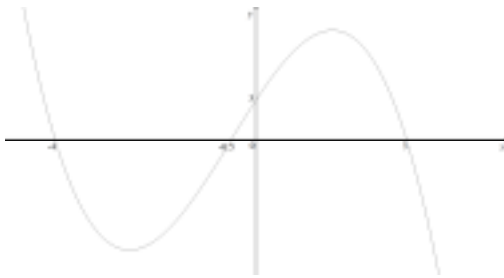
Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

- awrt answers which round to
- cao correct answer only
- dep dependent
- FT follow through after error
- isw ignore subsequent working
- nfwf not from wrong working
- oe or equivalent
- rot rounded or truncated
- SC Special Case
- soi seen or implied

Question	Answer	Marks	Guidance
1		3	B1 for a cubic shape with a maximum in the first quadrant, a minimum in the third quadrant, extending into the second and 4 th quadrants. The extensions must not curve incorrectly and not lead to a complete stationary point. B1 for x -intercepts $-4, -\frac{1}{2}, 3$ either on diagram or stated but must be with a cubic graph. B1 for y -intercept 3 either on diagram or stated but must be with a cubic graph.
2	$v = -4.91$ soi	B1	
	Speed = 4.91	B1	
3	$\tan\left(2x - \frac{\pi}{3}\right) = \pm\sqrt{3}$ soi or $\sin\left(2x - \frac{\pi}{3}\right) = \pm\frac{\sqrt{3}}{2}$ soi	B1	B0 if negative root is rejected Allow truncated decimals May be implied by subsequent work From use of $\operatorname{cosec}^2\left(2x - \frac{\pi}{3}\right) - 1 = \cot^2\left(2x - \frac{\pi}{3}\right)$
	$2x - \frac{\pi}{3} = -\frac{\pi}{3}, \frac{\pi}{3}, \frac{2\pi}{3}, \frac{4\pi}{3}$ $2x = 0, \frac{2\pi}{3}, \pi, \frac{5\pi}{3}$ $x = 0, \frac{\pi}{3}, \frac{\pi}{2}, \frac{5\pi}{6}$ or 0, 1.05, 1.57, 2.62 or greater accuracy	4	M1 for correct order of operations to obtain one solution in the range using $\tan\left(2x - \frac{\pi}{3}\right) = k$ or $\sin\left(2x - \frac{\pi}{3}\right) = m, m < 1$ Dep M1 for correct order of operations to obtain a second solution in the range using $\left(2x - \frac{\pi}{3}\right) = \tan^{-1}(k) \pm \pi$ or $\left(2x - \frac{\pi}{3}\right) = \pi - \sin^{-1}(m), m < 1$ oe $\left(2x - \frac{\pi}{3}\right) = -\sin^{-1}(m), m < 1$ oe A1 for any pair of correct solutions A1 for remaining pair of solutions, with no extra solutions within the range
4(a)	$\frac{1}{256} - \frac{x^2}{24} + \frac{7x^4}{36}$	3	B1 for $\frac{1}{256}$ B1 for $-\frac{x^2}{24}$ B1 for $\frac{7x^4}{36}$

Question	Answer	Marks	Guidance
4(b)	$4x^2 + 4 + \frac{1}{x^2}$ soi	B1	
	Coefficient of x^2 $\left(\text{their } 4 \times \text{their } \frac{1}{256} \right)$ $+ \left(\text{their } 4 \times \text{their } -\frac{1}{24} \right)$ $+ \left(\text{their } \frac{7}{36} \right)$	M1	Allow one sign error, but must have 3 terms in x^2 only, with an attempt at addition.
	$\frac{25}{576}$	A1	
5(a)	$\frac{a(r^4 - 1)}{r - 1} = 17 \frac{a(r^2 - 1)}{r - 1}$	M1	Allow equivalents Allow if 'a' terms missing (assume to have been cancelled)
	$(r^2 - 1)(r^2 + 1) = 17(r^2 - 1)$ or better $r^4 - 17r^2 + 16 = 0$ oe $r^3 + r^2 - 16r - 16 = 0$ oe	M1	Dep M1 for a correct simplified equation in r only
	$r = 4$ only, from correct working	A1	
5(b)	$ar^5 = 64$	M1	For use of ar^5 with <i>their</i> positive r
	$a = 0.0625$ or $\frac{1}{16}$	A1	Must be exact A0 if $r = 4$ not from correct working in (a)
5(c)	Because $r > 1$ oe	B1	FT on <i>their</i> $r > 1$ Must have a value for r

Question	Answer	Marks	Guidance
6(a)	Either Starts with 8: 1680	B1	1680 must not be part of a product. May be implied by final answer
	Starts with 7 or 9: 2688	B1	May be implied by final answer
	Total: 4368	B1	
	Or Alternative 1 Starts with 7, 8 or 9 and ends in 1, 3 or 5: 3024	(B1)	Allow for 1008 three times May be implied by final answer
	Starts with 8 or 9 and ends in 7: 672 Starts with 7 or 8 and ends in 9: 672	(B1)	For both May be implied by final answer
	Total: 4368	(B1)	
	Or Alternative 2 13 ways of obtaining odd 5-digit numbers which start with 7, 8 or 9	(B1)	Needs to be part of a product. May be implied by final answer
	8P_3 ways of arranging the remaining 3 digits: 336	(B1)	Needs to be part of a product. May be implied by final answer
	Total = $13 \times 336 = 4368$	(B1)	
	Or Alternative 3 Last digit is 7 or 9: 1344	B1	May be implied by final answer
	Last digit is 1, 3 or 5: 3024	B1	May be implied by final answer
	Total: 4368	B1	
	Or Alternative 4 ${}^{10}P_5 - ({}^9P_4 \times 7) - ({}^8P_3 \times 5) - ({}^8P_3 \times 4) - ({}^8P_3 \times 5)$	B2	Must be complete
	Total: 4368	B1	
6(b)	$\frac{n!}{(n-3)!3!} = \frac{2n!}{(n-2)!2!}$ soi	B1	
	$(n-2)=6$ soi	B2	Dep B1 on first B for $(n-2)$ soi Dep B1 on first B for 6 soi
	$n=8$	B1	Dep on previous B marks

Question	Answer	Marks	Guidance
7(a)	$\sin AOQ = \frac{7}{10}$ $POA = \pi - AOQ$ or $14^2 = 10^2 + 10^2 - 200 \cos AOB$ oe $POA = \frac{2\pi - AOB}{2}$	M1	Allow alternatives, but must be a complete method to find POA
	$POA = 2.366195157 = 2.366$ to 3 dp	A1	Must see an angle correct to more than 3dp used in order to justify 3 dp
7(b)	Area of sector = $\frac{1}{2}10^2(2.366)$ (118.3)	B1	Allow unsimplified. Also allow use of 2.37
	Area of triangle = $\frac{1}{2}10^2 \sin 2.366$ (35)	B1	Allow unsimplified. Also allow use of 2.37
	Total area = awrt 153	B1	Allow greater accuracy
7(c)	Major arc $PB = 10 \times 2.366$	B1	Allow unsimplified. Also allow use of 2.37
	$\sin \frac{POA}{2} = \frac{AP/2}{10}$ or $AP^2 = 10^2 + 10^2 - 200 \cos POA$	M1	For a valid attempt to find AP – may be seen in (a) or (b) but AP must be stated in this part.
	$AP = 18.5$	A1	Allow awrt 18.5
	Perimeter: major arc $PB + 20 + \text{their } AP$	B1	For plan, may be implied, but must have an attempt to calculate AP
	Total perimeter = 62.2	A1	Allow awrt 62.2
8(a)	$2x^2 + 2x - 2 = x^2 + 6x - 2$ $x^2 - 4x = 0$ $x(x-4) = 0$ $x = 0, x = 4$	M1	For obtaining an equation in one variable
		M1	Dep for a correct attempt to obtain at least one solution
	(0, -1)	A1	nfww
	(4, 19)	A1	nfww
	Mid-point (2, 9) with sufficient detail	B1	AG

Question	Answer	Marks	Guidance
8(b)	Either Gradient of perpendicular $= -\frac{1}{5}$	M1	
	$y - 9 = -\frac{1}{5}(x - 2)$	M1	Dep on previous M mark for perpendicular bisector using <i>their</i> mid-point and <i>their</i> perpendicular gradient
	$7 - 9 = -\frac{1}{5}(12 - 2)$ oe	A1	For checking by substitution, must see evidence.
	Or Alternative 1 Gradient of perpendicular $= -\frac{1}{5}$	(M1)	
	$y - 7 = -\frac{1}{5}(x - 12)$	(M1)	Dep on previous M mark for perpendicular bisector using $(12, 7)$ and <i>their</i> perpendicular gradient
	$9 - 7 = -\frac{1}{5}(2 - 12)$ oe	(A1)	For checking by substitution, must see evidence
	Or Alternative 2 Gradient of perpendicular $= -\frac{1}{5}$	(M1)	
	Gradient of line joining <i>their</i> $(2, 9)$ to $(12, 7) = -\frac{1}{5}$	(M1)	
	$(2, 9)$ is a common point and gradients of perpendicular bisector and l are the same so C lies on l .	(A1)	
8(c)	$(22, 5)$	2	B1 for 22 B1 for 5
	$(-18, 13)$	2	B1 for -18 B1 for 13

Question	Answer	Marks	Guidance
9(a)	$e^{2y} = mx^2 + c$	B1	May be implied by later work
	Either $7.96 = 4m + c$ $3.76 = 2m + c$	M1	
	$m = 2.1$ oe	A1	
	$c = -0.44$ oe	A1	
	$y = \frac{1}{2} \ln(2.1x^2 - 0.44)$ oe	A1	Do not isw
	Or gradient = 2.1 oe	(B1)	
	Use of either $7.96 = 4m + c$ or $3.76 = 2m + c$	(M1)	For use with <i>their m</i>
	$c = -0.44$ oe	(A1)	
	$y = \frac{1}{2} \ln(2.1x^2 - 0.44)$ oe	(A1)	Must be bracketed correctly
9(b)	$y = \frac{1}{2} \ln(\text{their } 2.1x^2 - \text{their } 0.44)$ oe	M1	Must use the form $y = k \ln(px^2 \pm q)$ $p \neq 1$ and $q \neq 0$ or $e^{2y} = mx^2 + c$
	0.253	A1	
9(c)	$\text{their } 2.1x^2 - \text{their } 0.44 > 0$ or $= 0$ or ≥ 0 soi	B1	
	Correct attempt to obtain the critical value using $\text{their } 2.1x^2 - 0.44 = 0$	M1	Must be from the form $y = k \ln(px^2 - q)$, $p \neq 1$ and $q > 0$
	$x > 0.458$ or $x > \sqrt{\frac{22}{105}}$ oe	A1	

Question	Answer	Marks	Guidance
10(a)	$\frac{dy}{dx} = (2x+3)^{\frac{1}{2}} + 5x(+c)$	B1	For $(2x+3)^{\frac{1}{2}}$, allow unsimplified
		M1	For $k(2x+3)^{\frac{1}{2}} + 5x$
	$10 = 3 + 15 + c$	M1	Dep for use of 10 and $x=3$ in <i>their</i> $\frac{dy}{dx}$ to obtain c
	$\frac{dy}{dx} = (2x+3)^{\frac{1}{2}} + 5x - 8$ soi	A1	
	When $x=11$, $\frac{dy}{dx} = 5 + 55 - 8$ oe $= 52$	A1	AG – need to see sufficient detail
10(b)	$f(x) = \frac{1}{3}(2x+3)^{\frac{3}{2}} + \frac{5x^2}{2}(-8x+d)$	B1	For $\frac{1}{3}(2x+3)^{\frac{3}{2}}$, must be $\int (2x+3)^{\frac{1}{2}} dx$
		M1	For $k(2x+3)^{\frac{3}{2}} + \frac{5x^2}{2}$
	$\frac{19}{2} = \frac{27}{3} + \frac{45}{2} - 24 + d$ $d = 2$	M1	For use of $y = \frac{19}{2}$ and $x = 3$ in <i>their</i> y
	$(f(x) =) \frac{1}{3}(2x+3)^{\frac{3}{2}} + \frac{5x^2}{2} - 8x + 2$	A1	Allow -8 if obtained from using $\frac{dy}{dx} = 52$ in (a) rather than $\frac{dy}{dx} = 10$
11(a)	$\frac{dy}{dx} =$ $\frac{(x+1)\left(\frac{1}{3} \times 2x \times (x^2-5)^{-\frac{2}{3}}\right) - (x^2-5)^{\frac{1}{3}}}{(x+1)^2}$ or $(x+1)^{-1} \left(\frac{1}{3} \times 2x \times (x^2-5)^{-\frac{2}{3}} \right) + (x^2-5)^{\frac{1}{3}} \left(-(x+1)^{-2} \right)$	3	B1 for $\frac{1}{3} \times 2x \times (x^2-5)^{-\frac{2}{3}}$ M1 for an attempt at a quotient or a correct product A1 for all other terms correct
	$\frac{-x^2 + 2x + 15}{3(x+1)^2 (x^2-5)^{\frac{2}{3}}}$	3	Dep on first 3 marks A1 for $-x^2$ in a quadratic numerator A1 for $2x$ in a quadratic numerator A1 for 15 in a quadratic numerator

Question	Answer	Marks	Guidance
11(b)	$-x^2 + 2x + 15 = 0$	M1	For attempt to solve <i>their</i> $-x^2 + 2x + 15 = 0$ to obtain $x = ..$ Must be a quadratic equation.
	$x = 5$ only	A1	
11(c)	Either Find the gradient either side of the stationary point	B1	
	If gradient changes from +ve to -ve: max If gradient changes from -ve to +ve: min	B1	Dep on previous B1
	Or Alternative 1 Take the second derivative and substitute in the value of x obtained in (b)	(B1)	Allow alternative valid methods Allow a general method as this is not dependent on (a) or (b)
	If second derivative is + ve, then a min If second derivative is – ve, then a max	(B1)	Dep on previous B1
	Or Alternative 2 Consider a y -value to one side of the stationary point	(B1)	Allow alternative valid methods Allow a general method as this is not dependent on (a) or (b)
	If y value of stationary point is greater, then a max. If y value of stationary point is less, then a min.	(B1)	Dep on previous B1



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/11

Paper 1

May/June 2021

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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This document consists of **9** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

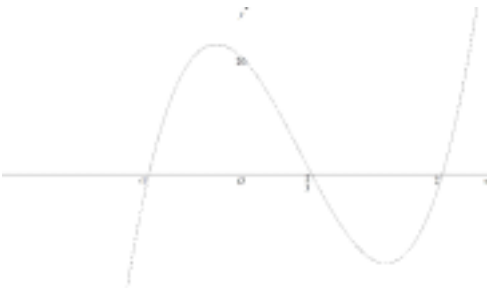
Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.


When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfww	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(a)		3	B1 for a well-drawn cubic graph in the correct orientation with both arms extending beyond x -axis B1 for $x = -1$, $x = 2$ and $x = \frac{2}{3}$ either on the graph or stated with a cubic graph B1 for $y = 20$ either on the graph or stated with a cubic graph
1(b)	$-1 < x < \frac{2}{3}$	B1	Must be found from a cubic graph
	$x > 2$	B1	
2	$\left[\ln(x-1) + \frac{1}{x-1} \right]_3^5$	2	B1 for $\ln(x-1)$ B1 for $+\frac{1}{x-1}$
	$\left(\ln 4 + \frac{1}{4} \right) - \left(\ln 2 + \frac{1}{2} \right)$	M1	Dep on at least one B mark, for correct use of limits
	$\ln 2 - \frac{1}{4}$	2	A1 for $\ln 2$ A1 for $-\frac{1}{4}$ oe
3(a)	$p(2): 8a - 36 + 2b - 6 = 0$	B1	
	$p(3): 27a - 81 + 3b - 6 = 66$	B1	
		M1	Dep on at least one of the previous B marks, for attempt to solve <i>their</i> equations and obtain a solution for both a and b
	$a = 6, b = -3$	A1	For both
3(b)	$(x-2)(6x^2 + 3x + 3)$	2	M1 for attempt at quadratic factor either by observation to obtain $6x^2 + px + 3$ or by algebraic long division to obtain at least $6x^2 + 3x...$ A1 all correct

Question	Answer	Marks	Guidance
3(c)	Discriminant of $q(x) = 3^2 - 4 \times 6 \times 3 = -63$ which is < 0	M1	For calculation of discriminant and confirmation that it is < 0
	$q(x) = 0$ has no real solutions hence $p(x) = 0$ has only one real solution	A1	For a correct conclusion from correct work.
4	$(a+x)^3 = a^3 + 3a^2x + 3ax^2 + x^3$	B1	
	$\left(1 - \frac{x}{3}\right)^5 = 1 - \frac{5}{3}x + \frac{10}{9}x^2 \dots$	2	M1 allow one sign error or one arithmetic slip
	$a^3 = 27, \quad a = 3$	B1	
	Term in x : $3a^2 - \frac{5}{3}a^3 = b$	M1	For multiplying <i>their</i> terms, must have sum of 2 relevant products = b
	$b = -18$	A1	
	Term in x^2 : $3a - \frac{5}{3}(3a^2) + \frac{10}{9}a^3 = c$	M1	For multiplying <i>their</i> terms, must have sum of 3 relevant products = c
	$c = -6$	A1	
5(a)	$f \geq -4$	2	M1 for a valid method to find the least value of $x^2 + 4x$ A1 for $f \geq -4, y \geq -4$ or $f(x) \geq -4$
5(b)	$g > 1$	B1	Allow $y > 1$ or $g(x) > 1$
5(c)	$(1 + e^{2x})^2 + 4(1 + e^{2x}) [= 21]$	M1	
	$e^{4x} + 6e^{2x} - 16 = 0$ $(e^{2x} + 8)(e^{2x} - 2) = 0$	M1	Dep for quadratic in terms of e^{2x} and attempt to solve to obtain $e^{2x} = k$
	$e^{2x} = 2$ $x = \frac{1}{2} \ln k$	M1	Dep on both previous M marks, for attempt to solve $e^{2x} = k$
	$x = \ln \sqrt{2}$ or $\ln 2^{\frac{1}{2}}$	A1	
6(a)(i)	720	B1	
6(a)(ii)	480	B1	

Question	Answer	Marks	Guidance
6(a)(iii)	[Starts with 6 or 8]: 192	B1	
	[Starts with 9]: 72	B1	
	Total = 264	B1	
	Alternative [Ends with 9]:48	(B1)	
	[Ends with 1,3 or 5]:216	(B1)	
	Total = 264	(B1)	
6(b)	$\frac{45n!}{(n-4)!4!} = \frac{(n+1)(n+1)!}{((n+1)-5)!5!}$	B1	
	$45 = \frac{(n+1)^2}{5}$ leading to $15 = n+1$ or $n^2 + 2n - 224 = 0$	M2	M1 for 15 M1 for $n+1$ OR M1 for $n^2 + 2n - 224 = 0$ oe M1 for $(n-14)(n+16) = 0$
	$n = 14$ only	A1	
7(a)(i)	110 (m)	B1	
7(a)(ii)		B2	B1 for a line joining (0,5) and (10,5) B1 for a line joining (10,-2) and (40,-2)
7(b)(i)	$v = (2t+4)^{\frac{1}{2}} (+c)$	M1	For $k(2t+4)^{\frac{1}{2}}$
	$9 = 4 + c$	M1	Dep for attempt to find c using $v = 9$ and $t = 6$ in <i>their</i> v
	$(2t+4)^{\frac{1}{2}} + 5$	A1	

Question	Answer	Marks	Guidance
7(b)(ii)	$s = \frac{1}{3}(2t+4)^{\frac{3}{2}} \quad (+5t+d)$	M1	For $k(2t+4)^{\frac{3}{2}}$
	$\frac{1}{3} = \frac{64}{3} + 30 + d$	M1	Dep for attempt to find d using $s = \frac{1}{3}$ and $t = 6$ in <i>their</i> s
	$\frac{1}{3}(2t+4)^{\frac{3}{2}} + 5t - 51$	A1	
8(a)	$x = \frac{\sqrt{3}+1}{2-\sqrt{3}} \times \frac{2+\sqrt{3}}{2+\sqrt{3}}$ leading to $x = \frac{5+3\sqrt{3}}{1}$	M1	For attempt to rationalise and simplify showing all working
	$x = 5 + 3\sqrt{3}$	A1	
	Either: Using $x = 5 + 3\sqrt{3}$ $y = (2 - \sqrt{3})(52 + 30\sqrt{3}) + 5 + 3\sqrt{3} - 1$ $= 14 + 8\sqrt{3} + 4 + 3\sqrt{3}$ Or: Using $x = \frac{\sqrt{3}+1}{2-\sqrt{3}}$ $y = (2 - \sqrt{3}) \frac{(\sqrt{3}+1)^2}{(2-\sqrt{3})^2} + \frac{\sqrt{3}+1}{2-\sqrt{3}} - 1$ $= \frac{4 + 2\sqrt{3} + \sqrt{3} + 1 - 2 + \sqrt{3}}{2-\sqrt{3}}$ $= \frac{(4\sqrt{3}+3)(2+\sqrt{3})}{(2-\sqrt{3})(2+\sqrt{3})}$ $= \frac{8\sqrt{3}+6+12+3\sqrt{3}}{1}$	M1	For complete method, showing all steps. Allow one slip in arithmetic
	$11\sqrt{3} + 18$	2	A1 for 18 A1 for $11\sqrt{3}$

Question	Answer	Marks	Guidance
8(b)	$\frac{dy}{dx} = 2x(2 - \sqrt{3}) + 1$	M1	For attempt at differentiation to obtain form of $\frac{dy}{dx} = kx + 1$
	$0 = 2x(2 - \sqrt{3}) + 1$ $x = -\frac{1}{2(2 - \sqrt{3})} \times \frac{(2 + \sqrt{3})}{(2 + \sqrt{3})}$ leading to $x = -\frac{1}{2} \frac{(2 + \sqrt{3})}{1}$	M1	Dep on previous M for equating to zero, rationalisation and attempt to simplify
	$x = -1 - \frac{\sqrt{3}}{2}$	A1	
9(a)(i)	$(3y + 2)(2x + 1)$	B1	
9(a)(ii)	$(3\cos\theta + 2)(2\sin\theta + 1) = 0$ $\cos\theta = -\frac{2}{3}$, $\sin\theta = -\frac{1}{2}$	M1	For relating to part (i) and a correct attempt to obtain $\cos\theta = \dots$ or $\sin\theta = \dots$
	$\theta = 131.8^\circ$, 228.2° $\theta = 210^\circ$, 330°	3	M1 for solving one of the equations to obtain one correct solution A1 for any two correct solutions A1 for a further two correct solutions with no extra solutions within the range
9(b)	$\cos\left(2\phi + \frac{\pi}{4}\right) = \frac{\sqrt{3}}{2}$ oe	B1	
	$\phi = -\frac{5\pi}{24}, -\frac{\pi}{24}, \frac{19\pi}{24}, \frac{23\pi}{24}$	4	M1 for solving to obtain one correct positive solution M1 for solving to obtain one correct negative solution A1 for any two correct solutions A1 for a further two correct solutions with no extra solutions within the range
10(a)	$\sin \frac{AOB}{2} = \frac{7.5}{10}$	M1	For a valid method
	$AOB = 1.696$ $= 1.70$ to 2 dp	A1	Must see greater accuracy to justify given answer

Question	Answer	Marks	Guidance
10(b)	$AC^2 = 10^2 + 25^2 - \left(2 \times 10 \times 25 \cos \left(\frac{AOB}{2} \right) \right)$	M1	For a complete and valid method to find AC
	$AC = \text{awrt } 19.9$	A1	
	Major arc $AB = \text{awrt } 45.9$ or $\text{awrt } 45.8$	B1	
	Perimeter = $\text{awrt } 85.5$ or $\text{awrt } 85.6$	A1	
10(c)	Area of major sector $AOB = \frac{1}{2} \times 10^2 (2\pi - AOB)$	M1	
	$\text{awrt } 229$	A1	
	Area of kite $OACB = \frac{1}{2} \times 15 \times 25$	B1	Allow working with 2 separate triangles
	Area of <i>their</i> major sector plus area of <i>their</i> kite	M1	
	Total area = $\text{awrt } 417$	A1	



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

May/June 2021

MARK SCHEME

Maximum Mark: 80

Published

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Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
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isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$p^0 q^{-5} r^{-\frac{2}{3}}$	3	B1 for $a = 0$ B1 for $b = -5$ B1 for $c = -\frac{2}{3}$
2(a)		2	B1 for symmetrical V shape in the correct quadrant, touching the x -axis. Must have straight lines. B1 for $x = \frac{4}{3}$ and $y = 4$ only, either seen or stated on a modulus graph.
2(b)	$x \leq -1, x \geq \frac{11}{3}$ or 3.67 or better	3	B1 for -1 from a correct method. B1 for $\frac{11}{3}$ or 3.67 or better, from a correct method.
3(a)	$\overrightarrow{AC} = \mathbf{c} - \mathbf{a}$	B1	May be implied
	$\overrightarrow{OP} = \mathbf{a} + \frac{3}{5}\overrightarrow{AC}$ or $\mathbf{c} - \frac{2}{5}\overrightarrow{AC}$	M1	Maybe implied, for correct use of ratio $\overrightarrow{OP} = \mathbf{a} + \frac{3}{5}(\text{their } \overrightarrow{AC})$ or $\mathbf{c} - \frac{2}{5}(\text{their } \overrightarrow{AC})$
	$\overrightarrow{OP} = \frac{2}{5}\mathbf{a} + \frac{3}{5}\mathbf{c}$	A1	Allow unsimplified
3(b)	$\overrightarrow{OP} = \frac{2}{5}\mathbf{b}$ oe	B1	
	$\frac{2}{5}\mathbf{b} = \frac{2}{5}\mathbf{a} + \frac{3}{5}\mathbf{c}$ $2\mathbf{b} = 2\mathbf{a} + 3\mathbf{c}$	B1	Dep on previous B mark for equating vectors and rearrangement to obtain AG
	Alternative $\mathbf{b} = \frac{2}{5}\mathbf{a} + \frac{3}{5}\mathbf{c} + \frac{3}{5}\mathbf{b}$	(B1)	Need a clear indication of the method used, in the form of a correct unsimplified statement.
	$2\mathbf{b} = 2\mathbf{a} + 3\mathbf{c}$	(B1)	Dep for simplification to obtain AG

Question	Answer	Marks	Guidance
4	$\left(\frac{dy}{dx} = \right) \frac{1}{2}(3x+2)^{\frac{2}{3}} \quad (+c)$	M1	For $k_1(3x+2)^{\frac{2}{3}}$ where k_1 a constant.
	$4 = 2 + c$	M1	Dep for use of 4 and $x = 2$ in <i>their</i> $\frac{dy}{dx}$ to obtain c
	$\left(\frac{dy}{dx} = \right) \frac{1}{2}(3x+2)^{\frac{2}{3}} + 2$	A1	May be implied by subsequent integration or by $c = 2$
	$y = \frac{1}{10}(3x+2)^{\frac{5}{3}} \quad (+2x+d)$	M1	For $k_2(3x+2)^{\frac{5}{3}}$ where k_2 is a constant.
	$6.2 = \frac{1}{10}(32) + 4 + d$	M1	Dep on previous M1 for use of $x = 2$ and $y = 6.2$ in <i>their</i> y
	$y = \frac{1}{10}(3x+2)^{\frac{5}{3}} + 2x - 1$	A1	Must be an equation
5(a)	$p = 16$	2	B1 for $\log_a \frac{5p}{4} = \log_a 20$ oe B1 for 16, nfw
5(b)	$(3(3^x) - 1)(3^x + 3) = 0$	M1	For recognition of a correct quadratic in 3^x and attempt to factorise or use quadratic formula
	$3^x = \frac{1}{3}$ $x = -1$	2	M1 dep for a correct attempt to solve $3^x = k, k > 0$ A1 for one solution only, must be from a correct solution.

Question	Answer	Marks	Guidance
5(c)	$\log_y 2 = \frac{1}{\log_2 y}$ or $\log_2 y = \frac{1}{\log_y 2}$ or $\log_y 2 = \frac{\log_a 2}{\log_a y}$ and $\log_2 y = \frac{\log_a y}{\log_a 2}$	B1	May be implied
	$4(\log_y 2)^2 - 4(\log_y 2) + 1 = 0$ $(2\log_y 2 - 1)^2 = 0, \log_y 2 = \frac{1}{2}$ or $(\log_2 y)^2 - 4(\log_2 y) + 4 = 0$ $(\log_2 y - 2)^2 = 0, \log_2 y = 2$ or $(\log_a y)^2 - 4(\log_a 2)(\log_a 4)\log_a y + 4(\log_a 2)^2 = 0$ $(\log_a y - 2\log_a 2)^2 = 0$ $\log_a y = 2\log_a 2$	M1	For obtaining a 3 term quadratic equation in either $\log_y 2$ or $\log_2 y$ and solving to obtain $\log_y 2 = k$ or $\log_2 y = k$, may be implied or equivalent using an alternative base.
	$y = 4$	A1	nfw
6(a)	$\frac{dy}{dx} = 2(3 + \sqrt{5})x - 8\sqrt{5}$ or $x = \frac{8\sqrt{5}}{2(3 + \sqrt{5})}$	M1	Either For differentiation must have one correct term. or for use of ' $b^2 - 4ac = 0$ ', so $x = -\frac{b}{2a}$ at the stationary point.
	$x = \frac{4\sqrt{5}}{3 + \sqrt{5}} \times \frac{(3 - \sqrt{5})}{(3 - \sqrt{5})}$ oe leading to $\frac{12\sqrt{5} - 20}{4}$ oe, this is the minimum acceptable working for this method.	M1	Dep for equating <i>their</i> $\frac{dy}{dx}$ to zero with attempt to solve and rationalisation using a two term factor, or rationalisation of $x = -\frac{b}{2a}$, using a two term factor with sufficient detail to imply no use of a calculator. Allow multiple equivalents. Allow one numerical slip or sign error.
	$x = -5 + 3\sqrt{5}$	2	A1 for -5 A1 for $3\sqrt{5}$

Question	Answer	Marks	Guidance
6(b)	$y = (3 + \sqrt{5})(3\sqrt{5} - 5)^2$ $-8\sqrt{5}(3\sqrt{5} - 5) + 60$ $= (3 + \sqrt{5})(45 + 25 - 30\sqrt{5})$ $-120 + 40\sqrt{5} + 60$ $= 210 + 70\sqrt{5} - 90\sqrt{5} - 150$ $-120 + 40\sqrt{5} + 60$	M1	For substitution of <i>their</i> x and simplification with sufficient detail to imply no use of a calculator. Allow one numerical slip or sign error in the expansion of $(3 + \sqrt{5})(3\sqrt{5} - 5)^2$ or one sign error in the other terms.
	$= 20\sqrt{5}$	2	A1 for all non surd terms = 0 A1 for $20\sqrt{5}$
7(a)(i)	20160	B1	
7(a)(ii)	7200	2	B1 for 6P_4 or $6 \times 5 \times 4 \times 3 (= 360)$ for ‘inner’ characters or 5P_2 or $4 \times 5 (= 20)$ for ‘outer’ characters Must be part of a product
7(a)(iii)	360	2	B1 for 3P_3 or $3!$ or 6 for arrangements of symbols or 5P_3 or $5 \times 4 \times 3 (= 60)$ for the digits Must be part of a product
7(b)	$\frac{n!}{(n-5)!5!} = \frac{6(n-1)!}{((n-1)-4)!4!}$	B1	May be implied by simplification e.g. $\frac{n!}{5!} = 6 \frac{(n-1)!}{4!}$ or $\frac{n(n-1)(n-2)(n-3)(n-4)}{5!}$ $= \frac{6(n-1)(n-2)(n-3)(n-4)}{4!}$
	Simplification of either the numerical factorials or the algebraic factorials	M1	
	$n = 30$	A1	

Question	Answer	Marks	Guidance
8(a)	$\lg y = b \lg x + \lg A$	B1	May be implied by subsequent work
	$4.37 = 5.36b + \lg A$ $0.57 = 0.61b + \lg A$	M1	For at least one correct equation
	$b = 0.8$	A1	
	$\lg A = k \quad (0.082)$ $A = 10^k$	M1	Dep for substitution to obtain $\lg A = k$ and hence A
	$A = 1.21$	A1	
	Alternative 1 $\lg y = b \lg x + \lg A$	(B1)	May be implied by subsequent work
	Gradient = $\frac{4.37 - 0.57}{5.36 - 0.61}$	(M1)	
	$b = 0.8$	(A1)	
	$\lg A = k \quad (0.082)$ $A = 10^k$	(M1)	Dep for substitution into a correct equation to obtain $\lg A = k$ and hence A
	$A = 1.21$	(A1)	
	Alternative 2 $10^{4.37} = A \times 10^{5.36b}$ or $10^{0.57} = A \times 10^{0.61b}$	(B1)	
	$3.8 = 4.75b$	(M1)	For eliminating A correctly Must have B1.
	$b = 0.8$	(A1)	
	$A = 10^{4.37 - (5.36 \times (theirb))}$ oe	(M1)	For a correct attempt to find A . Must have B1
	$A = 1.21$	(A1)	
8(b)	$y = 1.21(3)^{0.8}$ or $\lg y = 0.8 \lg 3 + 0.082$	B1	FT for substitution into <i>their</i> equation
	$y = \text{awrt } 2.9$	B1	
8(c)	$3 = 1.21x^{0.8}$ or $\lg 3 = 0.8 \lg x + 0.082$	B1	FT for substitution into <i>their</i> equation
	$x = \text{awrt } 3.1$	B1	

Question	Answer	Marks	Guidance
9(a)	$d = 12$	B1	
	$\frac{n}{2}(-8 + (n-1)12) > 2000$ $3n^2 - 5n - 1000 > 0$	M1	For use of sum formula to obtain a three term quadratic inequality or equation
	$n = \frac{5 \pm \sqrt{25 + 12000}}{6}$ $n = 19.1$	M1	Dep for attempt at critical value(s) using <i>their</i> quadratic, may be using a calculator, so may be implied by a correct answer of 20.
	$n = 20$	A1	
9(b)(i)	$r = 3$	2	M1 For $ar^6 = 27$ and $ar^8 = 243$ with an attempt to eliminate a to obtain r^2 . Allow other valid methods.
9(b)(ii)	3^{26}	2	B1 for $a = \frac{1}{27}$ or 3^{-3} nfw
9(c)	Common ratio or $r = \sin \theta$	B1	May be implied by e.g. $\frac{1}{1 - \sin \theta}$ or $\frac{1 - \sin^n \theta}{1 - \sin \theta}$
	$-1 < \sin \theta < 1$ or $ \sin \theta < 1$ or $-1 < r < 1$ or $ r < 1$ with no incorrect statements seen.	B1	Dep on previous B1
10(a)	$\frac{1}{\sin \alpha} + \frac{1}{\cos \alpha} (=0)$	B1	For dealing correctly with $\operatorname{cosec}^2 \alpha$ and $\sec^2 \alpha$ to obtain an expression in $\sin \alpha$ and $\cos \alpha$ only
	$\tan \alpha = -1$ or $\sin \alpha = -\cos \alpha$	B1	For an equation in $\tan \alpha$, may be implied by a correct solution.
	$\alpha = -\frac{\pi}{4}$ or -0.785 $\alpha = \frac{3\pi}{4}$ or 2.36	2	B1 for one correct solution B1 for a second correct solution and no extra solutions in the range.

Question	Answer	Marks	Guidance
10(b)(i)	$\frac{\cos^2 \theta + 1 - 2 \sin \theta + \sin^2 \theta}{\cos \theta (1 - \sin \theta)}$	M1	For dealing with the fractions correctly and expansion of $(1 - \sin \theta)^2$
	$\frac{1 + 1 - 2 \sin \theta}{\cos \theta (1 - \sin \theta)}$ or better	M1	Dep for use of identity, may be implied by $\frac{2(1 - \sin \theta)}{\cos \theta (1 - \sin \theta)}$
	$\frac{2(1 - \sin \theta)}{\cos \theta (1 - \sin \theta)}$	M1	Dep on previous M mark for simplification
	$\frac{2}{\cos \theta} = 2 \sec \theta$	A1	Need to see this detail for A1 Need to have had θ in every trigonometric ratio.
	Alternative 1 $\left(\frac{\cos \theta}{1 - \sin \theta} \times \frac{1 + \sin \theta}{1 + \sin \theta} \right) + \frac{1 - \sin \theta}{\cos \theta}$	(M1)	
	$\frac{\cos \theta (1 + \sin \theta)}{\cos^2 \theta} + \frac{1 - \sin \theta}{\cos \theta}$	(M1)	Dep for use of identity
	$\frac{1 + \sin \theta}{\cos \theta} + \frac{1 - \sin \theta}{\cos \theta}$	(M1)	Dep on previous M mark for simplification
	$\frac{2}{\cos \theta} = 2 \sec \theta$	(A1)	Need to see this detail for A1 Need to have had θ in every trigonometric ratio.
	Alternative 2 $\frac{(1 - \sin^2 \theta) + (1 - \sin \theta)^2}{\cos \theta (1 - \sin \theta)}$	(M1)	For dealing with the fractions and using $\cos^2 \theta = 1 - \sin^2 \theta$.
	$\frac{(1 - \sin \theta)(1 + \sin \theta) + (1 - \sin \theta)^2}{\cos \theta (1 - \sin \theta)}$	(M1)	Dep for factorising $1 - \sin^2 \theta$
	$\frac{1 + \sin \theta + 1 - \sin \theta}{\cos \theta}$	(M1)	Dep for simplification
	$\frac{2}{\cos \theta} = 2 \sec \theta$	(A1)	Need to see this detail for A1 Need to have had θ in every trigonometric ratio.

Question	Answer	Marks	Guidance
10(b)(ii)	$\cos 3\phi = \frac{1}{2}$	B1	
	$\phi = 20^\circ, 100^\circ, 140^\circ$	3	M1 for one correct solution of <i>their</i> $\cos 3\phi = k$ using a correct order of operations A1 for 2 correct solutions A1 for a third correct solution with no extra solutions in the range
11	$\frac{dy}{dx} = \frac{(2x-3)\frac{2x}{x^2+2} - 2\ln(x^2+2)}{(2x-3)^2}$	3	B1 for $\frac{2x}{x^2+2}$ M1 for differentiation of a quotient
	When $x = 2$, $\frac{dy}{dx} = \frac{4}{6} - 2\ln 6$, -2.92 Gradient of normal = 0.3428	M1	For $-\frac{1}{\text{their } \frac{dy}{dx}}$
	When $x = 2$, $y = \ln 6$ or 1.79(176)	B1	
	Equation of normal: $y - \ln 6 = -\frac{1}{\text{their } \frac{dy}{dx}}(x - 2)$ or $\ln 6 = -\frac{1}{\text{their } \frac{dy}{dx}} \times (2) + c$	M1	Dep for equation of normal using $-\frac{1}{\text{their } \frac{dy}{dx}}$ and <i>their</i> y with $x = 2$.
	When $x = 0$, $y = \text{awrt } 1.11$	A1	Must be evaluated.



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/13

Paper 1

May/June 2021

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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This document consists of **9** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

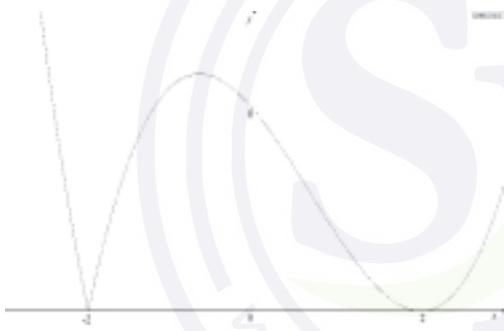
Abbreviations

- awrt answers which round to
- cao correct answer only
- dep dependent
- FT follow through after error
- isw ignore subsequent working
- nfwf not from wrong working
- oe or equivalent
- rot rounded or truncated
- SC Special Case
- soi seen or implied

Question	Answer	Marks	Guidance
1	$(4k)^2 - 4k(3k + 1)$	M1	For use of the discriminant to obtain a two term quadratic expression.
	$4k^2 - 4k = 0$	M1	Dep to find critical values, allow if only one is found
	$k = 0, k = 1$	A1	For both critical values
	$k < 0 \quad k > 1$	A1	
2(a)	$x^2(3e^{3x}) + 2xe^{3x}$	3	M1 for differentiation of a product A1 for $x^2(3e^{3x})$ A1 for $+2xe^{3x}$
2(b)(i)	$2x(3x^2 + 4)^{-\frac{2}{3}}$	2	M1 for $kx(3x^2 + 4)^{-\frac{2}{3}}$
2(b)(ii)	$\left[\frac{1}{2}(3x^2 + 4)^{\frac{1}{3}} \right]_0^2$	M1	For $k(3x^2 + 4)^{\frac{1}{3}}$
	$\left[\frac{1}{2} \left(16^{\frac{1}{3}} \right) - \frac{1}{2} \left(4^{\frac{1}{3}} \right) \right]$	M1	Dep for correct substitution of limits into <i>their</i> integral
	0.466	A1	
3	$(\cot^2 \theta + 1) + 2 \cot^2 \theta = 2 \cot \theta + 9$	B1	For use of correct identity
	$(3 \cot \theta + 4)(\cot \theta - 2) = 0$ $\cot \theta = -\frac{4}{3}, \cot \theta = 2$	M1	For attempt to solve <i>their</i> quadratic in $\cot \theta$ to obtain $\cot \theta = k$
	$\tan \theta = -\frac{3}{4}, \tan \theta = \frac{1}{2}$	M1	For dealing with $\cot \theta = k$ correctly to get $\tan \theta = \frac{1}{k}$
	$\theta = -0.644$	A1	
	$\theta = 0.464$	A1	
4(a)	$64 - 48x^2 + 15x^4$	3	B1 for 64 B1 for $-48x^2$ B1 for $15x^4$

Question	Answer	Marks	Guidance
4(b)	$9 - \frac{6}{x^2} + \frac{1}{x^4}$	B1	
	$(\text{their } 64 \times 9) + (\text{their } -48 \times -6) + (\text{their } 15)$	M1	For considering terms independent of x , must have 3 terms
	879	A1	
5	$e^y = mx^2 + c$	B1	May be implied by later work
	$10 = 4.74m + c$ $5 = 2.24m + c$	M1	For at least one correct equation
	$5 = 2.5m$	M1	Dep for attempt to solve for m
	$m = 2, c = 0.52$	A1	For both
	$y = \ln(2x^2 + 0.52)$	A1	
	Alternative $e^y = mx^2 + c$	(B1)	May be implied by later work
	Gradient = $m = \frac{10 - 5}{4.74 - 2.24}$	(M1)	
	$10 = 4.74(\text{their } m) + c$ or $5 = 2.24(\text{their } m) + c$	(M1)	
	$m = 2, c = 0.52$	(A1)	For both
	$y = \ln(2x^2 + 0.52)$	(A1)	
6(a)	$\frac{\pi}{3}$	B1	
6(b)	$\frac{\pi a}{3} + 4a$	2	B2 FT for $\left(\text{their } \frac{\pi}{3} \times a\right) + 4a$ or B1 FT for $\text{their } \frac{\pi}{3} \times a$

Question	Answer	Marks	Guidance
6(c)	$\frac{1}{2}(2a)^2 \sin \frac{\pi}{3}$	B1	FT <i>their</i> $\frac{\pi}{3}$
	$\frac{1}{2}a^2 \frac{\pi}{3}$	B1	FT <i>their</i> $\frac{\pi}{3}$
	$\sqrt{3}a^2 - \frac{\pi a^2}{6}$	B1	FT <i>their</i> $\frac{\pi}{3}$
7(a)(i)	8C_4	M1	For realisation that there are 4 places left and 8 people available to fill them
	70	A1	
7(a)(ii)	1 teacher on committee: 5 ways	B1	
	${}^{12}C_8 - 5$	M1	
	490	A1	
	Alternative 2 teachers: 70 3 teachers: 210 4 teachers: 175 5 teachers: 35	(2)	B1 for 2 correct cases
	490	(B1)	
7(b)	$\frac{n!}{(n-5)!} = 6 \frac{(n-1)!}{(n-1-4)!}$	B1	
	$\frac{n}{(n-5)!} = \frac{6}{(n-5)!}$	M1	For simplification of either $n!$ and $(n-1)!$ or ‘cancelling out’ of the terms of $(n-5)!$
	$n = 6$	A1	nfw
8(a)	$b = 2$	B1	
	At $(0, 3)$: $3 = a + c$	B1	
	At $\left(\frac{5\pi}{6}, 0\right)$: $0 = a \cos \frac{5\pi}{3} + c$ $0 = \frac{a}{2} + c$	M1	For use of <i>their</i> b and $\left(\frac{5\pi}{6}, 0\right)$
	$a = 6$ $c = -3$	A1	For both

Question	Answer	Marks	Guidance
8(b)	$\left(\frac{\pi}{6}, 0\right)$	B1	Allow for $x = \frac{\pi}{6}$
8(c)	$\left(\frac{\pi}{2}, -9\right)$	2	B1 for $\frac{\pi}{2}$ B1 for -9
9(a)	$y = x^3 - 2x^2 - 4x + 8$	B1	
	$\frac{dy}{dx} = 3x^2 - 4x - 4$ $(3x + 2)(x - 2) = 0$	M1	For attempt to differentiate, allow one slip and for equating <i>their</i> $\frac{dy}{dx}$ to zero and attempt to solve to obtain $x = k$
	$\left(-\frac{2}{3}, \frac{256}{27}\right)$	A1	
	$(2, 0)$	A1	
9(b)		4	B1 for curve with maximum in the second quadrant B1 for $y = 8$ either on the curve or stated B1 for $x = \pm 2$ either on the curve or stated B1 for a cusp at $x = -2$ and a min at $x = 2$
9(c)	$0 < k < \frac{256}{27}$	2	FT on <i>their</i> $\frac{256}{27}$ B1 for either $0 < k$ or $k < \frac{256}{27}$
10(a)	$\overrightarrow{CD} = \frac{3}{4}\mathbf{a}$	B1	
	$\overrightarrow{OD} = \mathbf{c} + \frac{3}{4}\mathbf{a}$	B1	
	$\overrightarrow{OE} = h\left(\mathbf{c} + \frac{3}{4}\mathbf{a}\right)$	B1	
	$\overrightarrow{DE} = h\left(\mathbf{c} + \frac{3}{4}\mathbf{a}\right) - \left(\mathbf{c} + \frac{3}{4}\mathbf{a}\right)$ oe cao	B1	
10(b)	$\overrightarrow{DE} = \frac{1}{4}\mathbf{a} + k\mathbf{c}$	B1	

Question	Answer	Marks	Guidance
10(c)	$\mathbf{c}(h-1) + \mathbf{a}\left(\frac{3h}{4} + \frac{3}{4}\right) = \frac{1}{4}\mathbf{a} + k\mathbf{c}$	M1	For equating <i>their</i> answer to (a) to <i>their</i> answer to (b)
	$\mathbf{c}(h-1) + \mathbf{a}\left(\frac{3h}{4} + \frac{3}{4}\right) = \frac{1}{4}\mathbf{a} + k\mathbf{c}$ $h-1 = k$	M1	For attempt to equate like vectors once.
	$h = \frac{4}{3}$	A1	
	$k = \frac{1}{3}$	A1	
11(a)	$x + 2y = 10$ $x + y = 2$	M1	For attempt to solve simultaneously
	$(-6, 8)$	A1	
	$x + 2y = 10$ $x + y = -2$	M1	For attempt to solve simultaneously
	$(-14, 12)$	A1	
	Alternative $x^2 + x(10-x) + \frac{(10-x)^2}{4} = 4$ or $(10-2y)^2 + 2y(10-2y) + y^2 = 4$	(M1)	For attempt to eliminate one of the variables using $(x+y)^2 = 4$
	$x^2 + 20x + 84 = 0$ or $y^2 - 20y + 96 = 0$	(M1)	Dep for attempt to obtain a 3 term quadratic equation = 0 and solve to obtain at least one solution, allow 1 arithmetic error
	$(-14, 12)$	(A1)	
	$(-6, 8)$	(A1)	
	Mid-point of AB: $(-10, 10)$	M1	For attempt to obtain the mid-point using <i>their</i> coordinates for A and B.
	Gradient of line perpendicular to AB = 2	M1	For attempt to obtain the perpendicular gradient using <i>their</i> coordinates for A and B.
	$y - \text{their } 10 = \text{their } 2(x - \text{their } (-10))$	M1	
	$20 - 10 = 2(-5 + 10)$ oe	A1	For verification

Question	Answer	Marks	Guidance
11(b)	(10, 50)	2	FT on <i>their</i> midpoint B1 for each coordinate
	(-20, -10)	2	FT on <i>their</i> midpoint B1 for each coordinate





Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

March 2021

MARK SCHEME

Maximum Mark: 80

Published

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- marks are not deducted for errors
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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$(3\ln 5x - 1)(\ln 5x + 1) = 0$ $\ln 5x = \frac{1}{3}, \ln 5x = -1$	M1	For recognition of a quadratic in $\ln 5x$ and attempt to solve to obtain $\ln 5x = k$
	$x = \frac{1}{5}e^{\frac{1}{3}}, \frac{\sqrt[3]{e}}{5}, e^{\frac{1}{3}-\ln 5}$ oe $x = \frac{1}{5e}, \frac{e^{-1}}{5}, e^{-1-\ln 5}$ oe	3	Dep M1 for dealing with <i>their</i> $\ln 5x = k$ correctly once A1 for $x = \frac{1}{5}e^{\frac{1}{3}}$ oe isw A1 for $x = \frac{1}{5e}$ oe isw
2	$a = 3$	B1	
	$b = \frac{1}{2}$	B1	
	$c = 4$	B1	
3(a)	Gradient of line perp to $AB = -\frac{3}{4}$	B1	
	Mid-point of $AB (-1, 10)$ soi	B1	
	$y - 10 = -\frac{3}{4}(x + 1)$ soi	M1	For attempt at straight line using <i>their</i> perp gradient and <i>their</i> mid-point
	$a - 10 = -\frac{3}{4}(7 + 1)$ $a = 4$	A1	Allow $y = 4$
3(b)	$(-9, 16)$	2	B1 for $x = -9$ B1 FT on <i>their</i> a , dep on M1 from (a) for $y = 16$ or $20 - \text{their } a$ B1 for $-9, 16$
4(a)	$2\left(x + \frac{5}{4}\right)^2 - \frac{49}{8}$	3	B1 for $b = \left(x + \frac{5}{4}\right)^2$ or $(x + 1.25)^2$ B1 for $c = -\frac{49}{8}$ or -6.125

Question	Answer	Marks	Guidance
4(b)	$\left(-\frac{5}{4}, -\frac{49}{8}\right)$ oe	2	<p>B1 for $-\frac{5}{4}$ as part of a set of coordinates or $x = -\frac{5}{4}$,</p> <p>FT on <i>their b</i></p> <p>B1 for $-\frac{49}{8}$ as part of a set of coordinates or $y = -\frac{49}{8}$ FT on <i>their c</i></p> <p>Need to be using <i>their</i> answer to (a) and not using differentiation as ‘Hence’.</p> <p>B1 for $-\frac{5}{4}, -\frac{49}{8}$</p>
4(c)		3	<p>B1 for correct shape, with maximum in the second quadrant and cusps on the x-axes and reasonable curvature for $x < -3$ and $x > 0.5$.</p> <p>B1 for $(-3, 0)$ and $(0.5, 0)$ either seen on the graph or stated, must have attempted a correct shape</p> <p>B1 for $(0, 3)$ either seen on the graph or stated, must have attempted a correct shape</p>
4(d)	$\frac{49}{8}$ oe	B1	<p>FT on <i>their c </i> from (a)</p> <p>Allow $\frac{49}{8}$ from other methods</p>
5(a)	$\begin{pmatrix} -4 \\ 3 \end{pmatrix}t$ or $\begin{pmatrix} 0 \\ 0 \end{pmatrix} + \begin{pmatrix} -4 \\ 3 \end{pmatrix}t$ oe	B1	
5(b)	$\begin{pmatrix} 12 \\ 6 \end{pmatrix} + \begin{pmatrix} -5 \\ 8 \end{pmatrix}t$ or $\begin{pmatrix} 12-5t \\ 6+8t \end{pmatrix}$	B1	

Question	Answer	Marks	Guidance
5(c)	$\overrightarrow{PQ} = \begin{pmatrix} 12 \\ 6 \end{pmatrix} + \begin{pmatrix} -5 \\ 8 \end{pmatrix} t - \begin{pmatrix} -4 \\ 3 \end{pmatrix} t$	M1	For <i>their</i> (<i>b</i>) – <i>their</i> (<i>a</i>), or <i>their</i> (<i>a</i>) – <i>their</i> (<i>b</i>) Allow unsimplified. Both vectors must be in terms of <i>t</i>
	$\begin{pmatrix} 12-t \\ 6+5t \end{pmatrix}$ soi	B1	
	$\left \overrightarrow{PQ} \right ^2 = (12-t)^2 + (6+5t)^2$ $\left \overrightarrow{PQ} \right ^2 = 26t^2 + 36t + 180$	A1	Allow FT for use of modulus with $\begin{pmatrix} t-12 \\ -6-5t \end{pmatrix}$ and simplification to obtain the given result.
5(d)	Attempt to solve or consider the discriminant of $26t^2 + 36t + 180 = 0$	M1	Must be using the equation from part (c) as ‘Hence’.
	Conclusion from either $36^2 - 4(26)(180) < 0$ or $t > 0$	A1	Must have stated somewhere that $\left \overrightarrow{PQ} \right ^2 = 0$ oe has been considered not just $\left \overrightarrow{PQ} \right ^2$.
6(a)(i)	$a = 10, \quad 6 = \frac{a}{1-r}$ $10 = 6 - 6r$	M1	For use of first term and sum to infinity to obtain an equation in <i>r</i> only
	$r = -\frac{2}{3}$	A1	
6(a)(ii)	$S_7 = 10 \frac{(1 - (\text{their } r)^7)}{1 - \text{their } r}$	M1	For sum formula with $ \text{their } r < 1$.
	$S_7 = 6.35$	A1	
6(b)(i)	$\log_x 3$	B1	
6(b)(ii)	$S_n = \frac{n}{2}(2\log_x 3 + (n-1)\log_x 3)$	M1	For use of sum formula with <i>their</i> (i)
	$\frac{n}{2}(n+1)\log_x 3, \quad \frac{n}{2}\log_x 3^{n+1}, \quad \frac{n+1}{2}\log_x 3^n$	A1	Allow other similar equivalents
6(b)(iii)	$\frac{n}{2}(n+1) = 3081$	M1	For a correct attempt to solve <i>their</i> (ii) = $3081\log_x 3$ to obtain an answer for <i>n</i> . Must be a 3 term quadratic in <i>n</i> only.
	$n = 78$	A1	

Question	Answer	Marks	Guidance
6(b)(iv)	$1027 = \frac{78}{2}(79)\log_x 3$ or $3081 \log_x 3$	M1	For using <i>their</i> 78 in a sum equation or using 3081 to obtain x
	$x = 27$	A1	
7(a)	$AE^2 = (\sqrt{17} - 1)^2 + (\sqrt{17} + 1)^2$ $= 18 + 2\sqrt{17} + 18 - 2\sqrt{17}$	M1	For attempt to find AE . Must see at least 3 terms in an expansion that is not the difference of two squares to be convinced a calculator is not being used.
	$AE = 6$	A1	
	Perimeter = $4\sqrt{17} + 8 + \text{their } AE$ $= 4\sqrt{17} + 14$	B1	FT on <i>their</i> AE
7(b)	Area = $\frac{1}{2}(3\sqrt{17} + 7)(\sqrt{17} + 1)$ oe $= \frac{1}{2}(51 + 3\sqrt{17} + 7\sqrt{17} + 7)$ oe	M1	For attempt at a trapezium or triangle and rectangle. Must see at least 3 terms in an expansion that is not the difference of two squares to be convinced a calculator is not being used. Allow one arithmetic slip.
	Area = $29 + 5\sqrt{17}$	A1	
7(c)	$\tan AED = \frac{\sqrt{17} + 1}{\sqrt{17} - 1} \times \frac{\sqrt{17} + 1}{\sqrt{17} + 1}$	M1	For attempt at rationalisation.
	$\frac{9 + \sqrt{17}}{8}$	A1	Must come from $\frac{18 + 2\sqrt{17}}{16}$ to be convinced a calculator is not being used.
7(d)	$\sec^2 AED = \tan^2 AED + 1$ $= \frac{(9 + \sqrt{17})^2}{64} + 1$ $\frac{81 + 17 + 18\sqrt{17} + 64}{64}$ oe if $\frac{(9 + \sqrt{17})^2}{64}$ and 1 are considered separately.	M1	For use of <i>their</i> (c) in the correct identity and attempt to simplify to obtain a single fraction. Must see at least 3 terms in an expansion that is not the difference of two squares to be convinced a calculator is not being used. Allow one arithmetic slip
	$\frac{81 + 9\sqrt{17}}{32}$ oe	A1	cao

Question	Answer	Marks	Guidance
8(a)(i)	$\sin x \frac{\sin x}{\cos x} + \cos x$	B1	
	$\frac{\sin^2 x + \cos^2 x}{\cos x}$ oe	B1	
	$\frac{1}{\cos x} = \sec x$	B1	Poor notation is B0
8(a)(ii)	$\sec \frac{\theta}{2} = 4$ $\cos \frac{\theta}{2} = \frac{1}{4}$	M1	For use of (i) and dealing with sec to obtain $\cos \frac{\theta}{2} = \frac{1}{4}$
	$\frac{\theta}{2} = 1.3181, 4.9651$ $\theta = 2.64$ or 0.839π $\theta = 9.93$ or 3.16π	3	Dep M1 for a correct attempt to solve to obtain at least one solution for θ A1 for one correct solution A1 for a second correct solution and no extra solutions
8(b)	$\tan(y + 38^\circ) = \frac{1}{\sqrt{3}}$ $y = 172^\circ$ $y = 352^\circ$	3	M1 for dealing with cot and a correct attempt to obtain at least one correct solution, allow for -8° A1 for one correct solution A1 for a second correct solution and no extra solutions
9(a)	$(2x-1)(x^2-x-1)$	M1	For attempt at factorisation by observation or by algebraic long division
	$(2x-1)(x^2-x-1)$	A1	cao
9(b)	At A $x = \frac{1}{2}$	B1	
	$x^2 - x - 1 = 0$	M1	For a valid attempt to solve <i>their</i> quadratic equation, allow for decimal solutions
	$x = \frac{1 \pm \sqrt{5}}{2}$ soi	A1	
	At B $x = \frac{1 + \sqrt{5}}{2}$	A1	

Question	Answer	Marks	Guidance
9(c)	$\int \frac{1}{x} dx = \ln x$	B1	
	$[\ln x]_{\frac{1}{2}}^{1+\sqrt{5}} = \ln(1+\sqrt{5})$	B1	Allow $\ln\left(\frac{1+\sqrt{5}}{2}\right) - \ln \frac{1}{2}$
	$\left(\int -2x^2 + 3x + 1\right) dx = -\frac{2}{3}x^3 + \frac{3x^2}{2} + x$	M1	M1 for attempt at $-\frac{2}{3}x^3 + \frac{3x^2}{2} + x$, must have 2 correct terms.
	$\left[-\frac{2}{3}x^3 + \frac{3x^2}{2} + x\right]_0^{\frac{1}{2}}$ $= \left(-\frac{2}{3} \times \frac{1}{8}\right) + \left(\frac{3}{2} \times \frac{1}{4}\right) + \frac{1}{2}$ oe	M1	Dep for correct application of the limits 0 and $\frac{1}{2}$ and attempt to evaluate – may be implied by 0.792 or $\frac{19}{24}$.
	$\frac{19}{24}$	A1	
	$\ln(1+\sqrt{5}) + \frac{19}{24}$	A1	isw
10(a)	$\frac{(x-1)(6x)(2x^2+10)^{\frac{1}{2}} - (2x^2+10)^{\frac{3}{2}}}{(x-1)^2}$	3	B1 for $\frac{3}{2} \times 4x \times (2x^2+10)^{\frac{1}{2}}$ oe M1 for correct attempt at differentiation of a quotient A1 for all the other terms correct
	$\left(\frac{(2x^2+10)^{\frac{1}{2}}}{(x-1)^2}\right) (4x^2 - 6x - 10)$	2	A2 for all 3 terms correct in the quadratic A1 for 2 terms correct and 1 incorrect term in the quadratic A0 for 1 term correct or no terms correct in the quadratic

Question	Answer	Marks	Guidance
10(b)	$4x^2 - 6x - 10 = 0$ $(2x - 5)(x + 1) = 0$	M1	For attempt to solve <i>their</i> quadratic = 0 and obtain at least one solution or state that <i>their</i> quadratic equation has no real roots.
	$x = \frac{5}{2}$	A1	
	Rejecting $x = -1$ correctly	A1	May be implied by the statement $x > 1$.
	Discounting $(2x^2 + 10)^{\frac{1}{2}} = 0$	B1	





Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/11

Paper 1

October/November 2020

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

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GENERIC MARKING PRINCIPLE 3:

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- marks are not deducted for errors
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GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
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2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.


Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

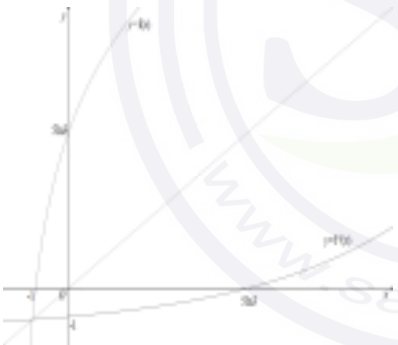
When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfww	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$y = \pm 3(x+2)(x+1)(x-4)$	3	B1 for 3 B1 for $(x+2)(x+1)(x-4)$ B1 for \pm
2(a)	4	B1	
2(b)	1080° or 6π	B1	
2(c)		3	B1 for shape, it must be symmetrical about the y-axis. B1 for y-intercept of 5 B1 for $(\pm 180^\circ, 3)$
3(a)	$a = \frac{3}{2}$ or $p^{\frac{3}{2}}$	B1	
	$b = \frac{10}{3}$ or $q^{\frac{10}{3}}$	B1	
	$c = -\frac{7}{3}$ or $r^{\frac{7}{3}}$	B1	
3(b)	$\left(3x^{\frac{1}{3}} - 1\right)\left(2x^{\frac{1}{3}} - 1\right) = 0$	M1	For recognising as a quadratic in $x^{\frac{1}{3}}$ and attempt to solve to obtain $x^{\frac{1}{3}} = k$
	$x^{\frac{1}{3}} = \frac{1}{3}, x^{\frac{1}{3}} = \frac{1}{2}$ leading to $x = \frac{1}{27}$ or 0.0370 $x = \frac{1}{8}$ or 0.125	2	Dep M1 for a valid method of solving $x^{\frac{1}{3}} = k$ where $k > 0$ A1 for both
4(a)	$\frac{dy}{dx} = \frac{\sin x \times 3 \sec^2 3x - \tan 3x \cos x}{\sin^2 x}$	3	B1 for $3 \sec^2 3x$ M1 for differentiation of a quotient or equivalent product A1 for all other terms apart from $3 \sec^2 3x$ correct
	When $x = \frac{\pi}{3}$ $\frac{dy}{dx} = 2\sqrt{3}$	A1	
4(b)	$2\sqrt{3}h$	B1	FT on <i>their</i> answer to (a)

Question	Answer	Marks	Guidance
4(c)	$\frac{dy}{dx} \times \frac{dx}{dt} = \frac{dy}{dt}$ $2\sqrt{3} \times 3 = \frac{dy}{dt}$	M1	For correct use of rates of change using <i>their</i> answer to (a)
	$\frac{dy}{dt} = 6\sqrt{3}$	A1	
5(a)(i)	360	B1	
5(a)(ii)	Starts with 6: $1 \times 4 \times 3 \times 1 = 12$	B1	
	Starts with 7 or 9 : $= 2 \times 4 \times 3 \times 2 = 48$	B1	
	Total = 60	B1	
	Alternative		
	Ending in 4: $\frac{1}{6} \times 360 \times \frac{3}{5} = 36$	(B1)	Allow unsimplified
	Ending in 6: $\frac{1}{6} \times 360 \times \frac{2}{5} = 24$	(B1)	Allow unsimplified
	Total = 60	(B1)	
5(b)(i)	1287	B1	
5(b)(ii)	$1287 - {}^7C_5$ or 1 doctor: 210 2 doctors: 525 3 doctors: 420 4 doctors: 105 5 doctors: 1	M1	For <i>their</i> (b)(i) $- {}^7C_5$ or listing all the other separate cases which must be evaluated, allow 1 error
	1266	A1	
5(b)(iii)	45	B1	
6(a)	Velocity vector = $\begin{pmatrix} -8 \\ 6 \end{pmatrix}$	2	M1 for obtaining 5
	$\begin{pmatrix} 30 \\ 10 \end{pmatrix} + \begin{pmatrix} -8 \\ 6 \end{pmatrix} t$	B1	FT for $\begin{pmatrix} 30 \\ 10 \end{pmatrix} + (\text{their velocity vector})t$
6(b)	13	B1	

Question	Answer	Marks	Guidance
6(c)	$P: \begin{pmatrix} -50 \\ 70 \end{pmatrix}$ $Q: \begin{pmatrix} -30 \\ 210 \end{pmatrix}$	M1	Using $t = 10$ to find position vector of each particle
	$\sqrt{20^2 + 140^2}$	M1	Dep on previous M mark, for use of Pythagoras on difference of the 2 position vectors
	$100\sqrt{2}$	A1	
7(a)	$f \in \mathbb{R}$	B1	Allow y but not x
7(b)	$x = 5 \ln(2y + 3)$ $e^{\frac{x}{5}} = 2y + 3$	M1	For a complete attempt to obtain inverse
	$f^{-1}(x) = \frac{e^{\frac{x}{5}} - 3}{2}$	A1	Must be using correct notation
	Domain $x \in \mathbb{R}$	B1	FT on <i>their (a)</i> . Must be using correct notation
7(c)		5	B1 for shape of $y = f(x)$ B1 for shape of $y = f^{-1}(x)$ B1 for $5 \ln 3$ or 5.5 and -1 on both axes for $y = f(x)$ B1 for $5 \ln 3$ or 5.5 and -1 on both axes for $y = f^{-1}(x)$ B1 All correct, with apparent symmetry which may be implied by previous 2 B marks or by inclusion of $y = x$, and implied asymptotes, may have one or two points of intersection
8(a)(i)	$\frac{1}{\left(1 + \frac{1}{\sin \theta}\right)(\sin \theta - \sin^2 \theta)}$	B1	For use of $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$, may be implied
	$\frac{1}{\sin \theta + 1 - \sin \theta - \sin^2 \theta}$	M1	For expansion of brackets
	$\frac{1}{\cos^2 \theta}$	M1	For simplification and use of identity
	$\sec^2 \theta$	A1	For final result, must see $\frac{1}{\cos^2 \theta}$

Question	Answer	Marks	Guidance
8(a)(ii)	$\cos^2 \theta = \frac{3}{4}$	B1	For relating to and making use of (a)
	$\cos \theta = \pm \frac{\sqrt{3}}{2}$	M1	For attempt to solve, may be implied by one correct solution
	$\theta = -150^\circ, -30^\circ, 30^\circ, 150^\circ$	2	A1 for any correct pair A1 for a second correct pair and no extra solutions within the range
8(b)	$\tan\left(3\phi + \frac{2\pi}{3}\right) = 1$	B1	
	$3\phi + \frac{2\pi}{3} = \frac{\pi}{4}, \frac{5\pi}{4}, \frac{9\pi}{4}$ $3\phi = \frac{7\pi}{12}, \frac{19\pi}{12}$	M1	For correct order of operations
	$\phi = \frac{7\pi}{36}$	A1	
	$\phi = \frac{19\pi}{36}$	A1	
9(a)	$\left[\ln x - \frac{1}{2}\ln(2x+3)\right]_1^a$	2	B1 for $\ln x$ B1 for $\frac{1}{2}\ln(2x+3)$
	$\ln a - \frac{1}{2}\ln(2a+3) + \frac{1}{2}\ln 5$	M1	For correct application of limits, must have at least one B1
	$\ln a \sqrt{\frac{5}{2a+3}}$	M1	Dep on previous M mark, for application of log laws
	$5a^2 - 18a - 27 = 0$	M1	Dep on previous M mark for equating to $\ln 3$ and simplification to a 3 term quadratic = 0
	$a = \frac{9+6\sqrt{6}}{5}$	A1	Must have one solution only

Question	Answer	Marks	Guidance
9(b)	$-\frac{1}{2}\cos\left(2x + \frac{\pi}{3}\right) + \frac{1}{2}\sin 2x - x$	3	B1 for $-\frac{1}{2}\cos\left(2x + \frac{\pi}{3}\right)$ B1 for $+\frac{1}{2}\sin 2x$ B1 for $-x$
	$\left(-\frac{1}{2}\cos \pi + \frac{1}{2}\sin \frac{2\pi}{3} - \frac{\pi}{3}\right)$ $-\left(-\frac{1}{2}\cos \frac{\pi}{3}\right)$	M1	For correct use of limits in <i>their</i> integral, must have at least one B1 term
	$\frac{3}{4} + \frac{\sqrt{3}}{4} - \frac{\pi}{3}$	A1	
10(a)	$a + d = 8$ $a + 3d = 18$	2	B1 for both equations M1 for attempt to solve <i>their</i> equations
	$a = 3, d = 5$	A1	For both
	$\frac{n}{2}(6 + (n-1)5) > 1560$	M1	For correct use of sum formula with <i>their</i> a and d , allow equality
	$5n^2 + n - 3120 > 0$	M1	For attempt to solve, allow equality, to obtain at least one critical value
	Positive critical value 24.9 25 terms	A1	
10(b)(i)	$\frac{a}{1-r} = 72$ and either $a + ar + ar^2 = \frac{333}{8}$ or $\frac{a(1-r^3)}{1-r} = \frac{333}{8}$	B1	For both
	$a = 72(1-r)$ and $a(1+r+r^2) = \frac{333}{8}$ oe $72(1-r)(1+r+r^2) = \frac{333}{8}$ or $72(1-r^3) = \frac{333}{8}$	M1	For attempt to obtain an equation in terms of r only
	$1-r^3 = \frac{333}{576}$	A1	
	$r = 0.75$	2	M1 for attempt to solve <i>their</i> equation in r

Question	Answer	Marks	Guidance
10(b)(ii)	$a = 18$	B1	FT on their r provided $ r < 1$





Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

October/November 2020

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

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6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

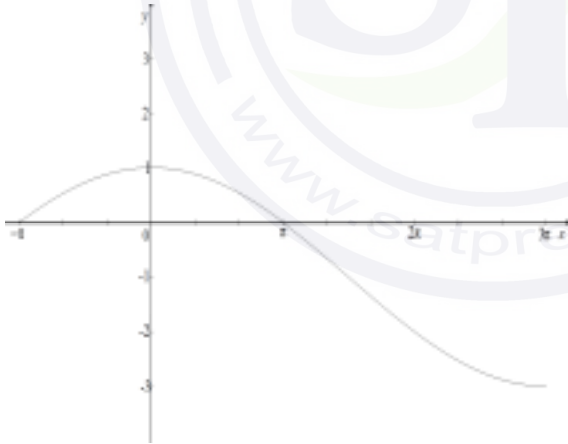
Types of mark

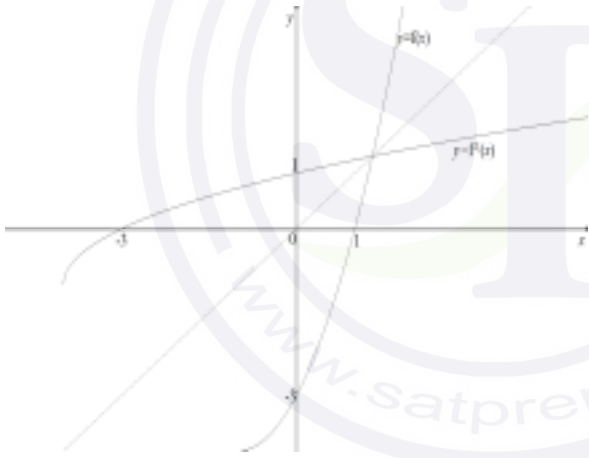
- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$2x^2 - (k+4)x + (k+4) \quad (=0)$ $2x^2 + (-k-4)x + (k+4) \quad (=0)$	B1	
	Discriminant: $(k+4)^2 - (4 \times 2 \times (k+4))$	M1	Use of discriminant to obtain 2 critical values using <i>their</i> 3 term quadratic
	± 4	A1	For critical values
	$k < -4 \quad k > 4$	A1	
2(a)	$y = -\frac{1}{2}(x+5)(x+1)(x-2)$	3	B1 for negative soi B1 for $\frac{1}{2}$ soi B1 for $(x+5)(x+1)(x-2)$ or $x^3 + 4x^2 - 7x - 10$
2(b)	$-5 < x < -1$	B1	
	$x > 2$	B1	
3(a)	2	B1	
3(b)	6π or 1080°	B1	
3(c)		3	B1 for passing through $(-\pi, 0)$ and $(3\pi, -3)$ – must be a curve B1 for correct shape with max on y -axis and a min at $x = 3\pi$ B1 for passing through $(0, 1)$ and $(\pi, 0)$ only on the positive x -axis
4(a)	$a + 6d = 158$ $a + 9d = 149$	B1	For both equations, may be implied by a correct a and d
	$d = -3,$	B1	
	$a = 176$	B1	

Question	Answer	Marks	Guidance
4(b)	$\frac{n}{2}(352 + (n-1)(-3)) \quad (< 0)$	M1	For correct attempt at sum formula with <i>their a</i> and <i>their d</i> ,
	$\frac{355}{3}$ or 118.3 oe	A1	
	119	A1	
5	$x^5 + 10x^3 + 40x + \dots$	3	M1 for attempt to expand $\left(x + \frac{2}{x}\right)^5$, with at least 2 correct terms A1 for $10x^3$ A1 for $40x$
	Term in $x^2 : (1 \times 40) - (3 \times 10)$	M1	For $(1 \times \text{their } 40) \pm (3 \times \text{their } 10)$
	10	A1	
6(a)	It is a one-one function because of the given restricted domain or because $x \geq -1$	B1	
6(b)		4	B1 for $y = f(x)$ for $x > -1$ only B1 for 1 on x -axis and -3 on y -axis for $y = f(x)$ B1 for $y = f^{-1}(x)$ as a reflection of $y = f(x)$ in the line $y = x$, maybe implied by intercepts with axes B1 for 1 on y -axis and -3 on x -axis for $y = f^{-1}(x)$

Question	Answer	Marks	Guidance
7(a)	$\frac{dy}{dx} = \frac{(2x+1)\frac{6x}{3x^2-5} - 2\ln(3x^2-5)}{(2x+1)^2} \text{ or }$ $\frac{dy}{dx} = (2x+1)^{-1} \frac{6x}{3x^2-5} - 2(2x+1)^{-2} \ln(3x^2-5)$	3	B1 for $\frac{6x}{3x^2-5}$ M1 for attempt at a quotient or equivalent product A1 for all terms other than $\frac{6x}{3x^2-5}$ correct
	When $x = \sqrt{2}$, $y = 0$	B1	May be implied
	When $x = \sqrt{2}$, $\frac{dy}{dx} = \frac{6\sqrt{2}}{2\sqrt{2}+1}$ or $\frac{24-6\sqrt{2}}{7}$ or 2.22 oe Normal: $y = -\frac{(2\sqrt{2}+1)}{6\sqrt{2}}(x-\sqrt{2})$ oe or $y = -\frac{7}{24-6\sqrt{2}}(x-\sqrt{2})$ oe or $y = -\frac{1}{2.22}(x-\sqrt{2})$ oe or $y = -\frac{4+\sqrt{2}}{12}(x-\sqrt{2})$ oe or $y = -\frac{9+4\sqrt{2}}{24+6\sqrt{2}}(x-\sqrt{2})$ oe $y = -0.451x + 0.638$	2	M1 for attempt at normal using <i>their</i> y and <i>their</i> perp gradient A1 Allow equivalent surd forms
7(b)	$\left(\frac{6\sqrt{2}}{2\sqrt{2}+1}\right)h$ or $\frac{24-6\sqrt{2}}{7}h$ or other equivalent surd forms, or 2.22h	B1	FT on <i>their</i> $\frac{dy}{dx}$ from (a)
8(a)	${}^{12}C_3 \times {}^9C_4 = 220 \times 126$ or ${}^{12}C_5 \times {}^7C_4 = 792 \times 35$ or ${}^{12}C_4 \times {}^8C_5 = 495 \times 56$ or other equivalents 27720	3	B1 for one correct combination in a product of 2 or 3 combinations Must be numeric B1 for a second appropriate combination in the same product Must be numeric
8(b)(i)	120	B1	
8(b)(ii)	48	B1	

Question	Answer	Marks	Guidance							
8(b)(iii)	Starts with 7 or 9 24	B1	May be implied by 12 and 12							
	Starts with 8 18	B1								
	42	B1								
	Alternative Ends with 3 18	(B1)								
	Ends with 7 or 9 24	(B1)	May be implied by 12 and 12							
	42	(B1)								
9(a)	$\frac{dy}{dx} = (2x-1) \times \frac{1}{2} \times 4(4x+3)^{-\frac{1}{2}} + 2(4x+3)^{\frac{1}{2}}$	3	B1 for $\frac{1}{2} \times 4(4x+3)^{-\frac{1}{2}}$ oe M1 for a correct attempt at a product A1 for all other terms correct							
	$\frac{dy}{dx} = 2(4x+3)^{-\frac{1}{2}}(2x-1+4x+3)$ or equivalent	M1	For attempt to simplify to the given form							
	$\frac{dy}{dx} = \frac{4(3x+1)}{(4x+3)^{\frac{1}{2}}}$	A1								
9(b)	$-\frac{1}{3}$	B1	FT on <i>their</i> $3x+1=0$							
9(c)	For a complete method using 2 nd derivative, or gradient or y values either side or one side of <i>their</i> stationary point e.g.		M1 Must be using values of $x > -\frac{3}{4}$							
	<table><tr><td>x</td><td>$< -\frac{1}{3}$</td><td>$-\frac{1}{3}$</td><td>$> -\frac{1}{3}$</td></tr><tr><td>$\frac{dy}{dx}$</td><td>-</td><td>0</td><td>+</td></tr></table>	x		$< -\frac{1}{3}$	$-\frac{1}{3}$	$> -\frac{1}{3}$	$\frac{dy}{dx}$	-	0	+
	x	$< -\frac{1}{3}$		$-\frac{1}{3}$	$> -\frac{1}{3}$					
	$\frac{dy}{dx}$	-		0	+					
<table><tr><td>x</td><td>$< -\frac{1}{3}$</td><td>$-\frac{1}{3}$</td><td>$> -\frac{1}{3}$</td></tr><tr><td>y</td><td>< -2.15</td><td>-2.15</td><td>> -2.15</td></tr></table>	x	$< -\frac{1}{3}$	$-\frac{1}{3}$	$> -\frac{1}{3}$	y	< -2.15	-2.15	> -2.15		
x	$< -\frac{1}{3}$	$-\frac{1}{3}$	$> -\frac{1}{3}$							
y	< -2.15	-2.15	> -2.15							
Minimum	A1	Must be from correct work								

Question	Answer	Marks	Guidance
10(a)	$p(2): 48 + 4a + 2b + 2 = 0$ $2a + b + 25 = 0$	B1	For $2a + b + 25 = 0$ or multiple
	$p(1) = -2p(0)$ $a + b + 12 = 0$	B1	For $a + b + 12 = 0$
	$a = -13, \quad b = 1$	2	M1 for attempt to solve <i>their</i> equations in a and b leading to 2 values A1 for both
10(b)(i)	$p\left(\frac{1}{2}\right) = \frac{6}{8} - \frac{13}{4} + \frac{1}{2} + 2$	M1	For attempt to find $p\left(\frac{1}{2}\right)$ using <i>their</i> a and b
	0	A1	
10(b)(ii)	$(x - 2)(2x - 1)(3x + 1)$	2	M1 for realising that 2 factors are known and 3 rd factor can be got by observation or algebraic long division, or for making use of $x - 2$ or $2x - 1$ in order to obtain a quadratic factor A1 Must see all factors together
11(a)	$\angle BOC = 1.5 \text{ rad}$	B1	
	$\sin 0.75 = \frac{BC/2}{r}$	M1	For a complete attempt to find BC – must be using a right-angled triangle to get required result – Given answer
	$BC = 2r \sin 0.75$	A1	
	Perimeter = $2r + 2r \sin 0.75 + 4r + 1.5r$	M1	Dep on first M mark for attempt at perimeter
	$r(7.5 + 2 \sin 0.75)$	A1	Given answer
11(b)	Area = $(2r + 2r \sin 0.75)r - \frac{1}{2}r^2(1.5 - \sin 1.5)$ Area = $3.36r^2 - 0.75r^2 + 0.4987r^2$	3	M1 for a correct plan M1 for $(2r + 2r \sin 0.75)r$, using <i>their</i> $2r \sin 0.75$ B1 for segment $\frac{1}{2}r^2(1.5 - \sin 1.5) = 0.251r^2$
	Area = $3.11r^2$	A1	

Question	Answer	Marks	Guidance
12(a)(i)	Area under graph: $\frac{1}{2}(60+40)\times 30 + \frac{1}{2}(30+V)\times 30 \quad (=2775)$ or $\frac{1}{2}(20\times 30) + (40+30) + \frac{1}{2}(30+V)\times 30$	2	M1 for attempt to find the area under the graph Dep M1 on previous M mark for attempt to equate to 2775 and simplify in order to find V or $V - 30$
	55	A1	
12(a)(ii)	0	B1	
12(b)(i)	$v = 3\sin 2t \quad (+c)$	M1	Must have $\pm 3\sin 2t$
	$10 = c$	M1	Dep for attempt to find $+c$,
	$v = 3\sin 2t + 10$	A1	
12(b)(ii)	$s = -\frac{3}{2}\cos 2t + 10t + d$	M1	For attempt to integrate <i>their</i> v , must have $\pm \frac{3}{2}\cos 2t$
	$d = \frac{3}{2}$	M1	Dep on previous M mark for attempt to find d .
	$s = -\frac{3}{2}\cos 2t + 10t + \frac{3}{2}$	A1	



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/13

Paper 1

October/November 2020

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2020 series for most Cambridge IGCSE™, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

This document consists of **10** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently, e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
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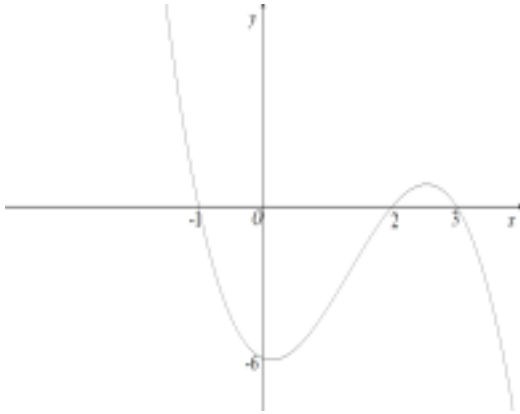
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Question	Answer	Marks	Guidance
1(a)		3	B1 for a well-drawn cubic graph in correct orientation Both arms extending beyond x -axis Maximum above x -axis B1 for x -intercepts B1 for y -intercept
1(b)	$x < -1$	B1	Dep on a cubic curve in the correct orientation and -1 correct on x -axis
	$2 < x < 3$ or $3 > x > 2$	B1	Dep on a cubic curve in the correct orientation and 2 and 3 correct on x -axis
2(a)	$\frac{dy}{dx} = \frac{(x^2 + 1)2e^{2x-3} - 2xe^{2x-3}}{(x^2 + 1)^2} \text{ oe}$ or $\frac{dy}{dx} = \frac{2e^{2x-3}}{(x^2 + 1)} - \frac{2xe^{2x-3}}{(x^2 + 1)^2} \text{ oe}$	3	B1 for $\frac{d}{dx}(e^{2x-3}) = 2e^{2x-3}$ seen in a quotient rule or product rule expression M1 for correct method for differentiating a quotient or equivalent product A1 FT from <i>their</i> $2e^{2x-3}$
2(b)	When $x = 2$, $\frac{dy}{dx} = \frac{6e}{25}$	M1	For evaluation of <i>their</i> $\frac{dy}{dx}$ when $x = 2$
	$\frac{6e}{25} \times \frac{dx}{dt} = 2 \text{ oe}$	M1	For correct substitution of <i>their</i> evaluated $\frac{dy}{dx}$ and $\frac{dy}{dt} = 2$ in a correct rates of change equation
	$\frac{dx}{dt} = \frac{25}{3e}, \frac{50}{6e}$	A1	
3(a)(i)	$x > \frac{1}{2}$	B1	Must be using x

Question	Answer	Marks	Guidance
3(a)(ii)	$x = 4 \ln(2y - 1)$ $e^{\frac{x}{4}} = 2y - 1$ $y = \frac{1}{2} \left(1 + e^{\frac{x}{4}} \right)$	M1	For full method for inverse using correct order of operations
	$f^{-1}(x) = \frac{1}{2} \left(1 + e^{\frac{x}{4}} \right)$ or $f^{-1}(x) = \frac{1}{2} \left(1 + \sqrt[4]{e^x} \right)$	A1	Must be using correct notation
	$x \in \mathbb{R}$	B1	
3(b)	$\sqrt{2x - 3} + 5 = 7$	M1	For correct order
	$x = \frac{2^2 + 3}{2}$	M1	Dep on previous M mark, for obtaining x by simplifying and solving using correct order of operations, including squaring
	$x = \frac{7}{2}$ or 3.5	A1	
4(a)(i)		3	B1 For $v = 2$ for $0 \leq t \leq 50$ B1 For $v = 2.5$ for $65 \leq t \leq 85$ B1 For $v = 3.75$ for $85 \leq t \leq 125$ and $v = 0$ for $50 \leq t \leq 65$
4(a)(ii)	300	B1	
4(b)	$\frac{dx}{dt} = -18 \sin \left(3t + \frac{\pi}{3} \right)$	M1	$\pm 18 \sin \left(3t + \frac{\pi}{3} \right)$
	$\frac{d^2x}{dt^2} = -54 \cos \left(3t + \frac{\pi}{3} \right)$	M1	$\pm 54 \cos \left(3t + \frac{\pi}{3} \right)$
	-27 nfw	A1	

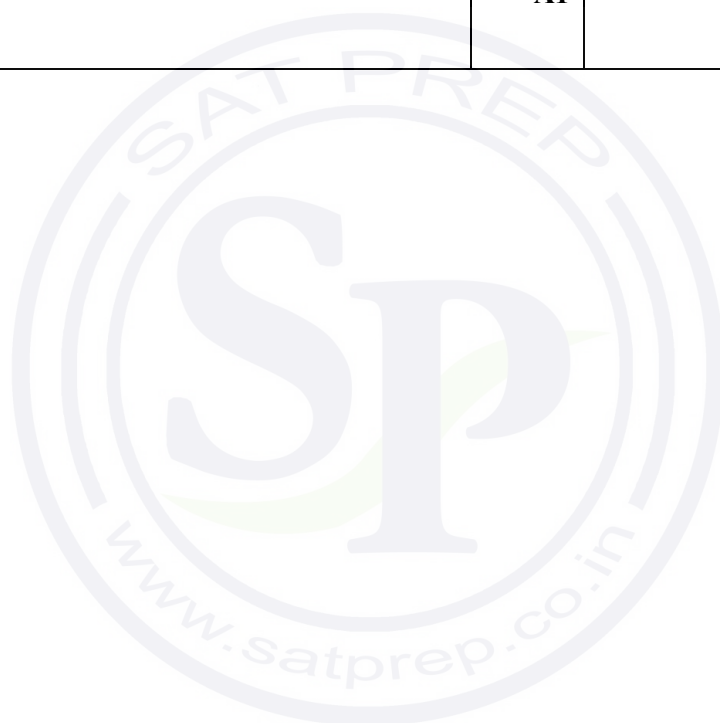
Question	Answer	Marks	Guidance
5	$(1+x)\left(1+n\left(-\frac{x}{2}\right)+\frac{n(n-1)}{2}\left(\frac{x^2}{4}\right)\dots\right)$	2	B1 For $\binom{n}{1}\left(-\frac{x}{2}\right)$ B1 For $\binom{n}{2}\left(\frac{x^2}{4}\right)$
	$\frac{1}{4}\binom{n}{2}x^2 - \frac{1}{2}\binom{n}{1}x^2 = \frac{25}{4}x^2$	M1	Correctly using two terms in n to obtain an x^2 term and equating to $\frac{25}{4}x^2$ Dep on one B1
	$\frac{n(n-1)}{8} - \frac{n}{2} = \frac{25}{4}$ oe	A1	
	$n = 10$ only	A1	
6(a)	$\lg y = \lg A + bx^2$	B1	Stated or may be implied by later work
	If using $\lg y = \lg A + bx^2$ as a starting point $5.25 = \lg A + 3.63b$ and $6.88 = \lg A + 4.83b$ or $5.25 = \lg A + 1.358(3.63)$ or $6.88 = \lg A + 1.358(4.83)$ OR If finding the equation of the straight line and then finding $\lg A$ and b by inspection $\lg y - 6.88 = 1.358(x^2 - 4.83)$ or $\lg y - 5.25 = 1.358(x^2 - 3.63)$ or $\lg y = 1.358x^2 + 0.31\dots$ (or 0.32..)	M1	For correctly finding required equation(s)
	$b = 1.36, \frac{163}{120}$ or $1\frac{43}{120}$	B1	Must be $b =$ and from correct working
	A in range 2.05 to 2.09	A1	
6(b)	$\lg y = 0.3132 + (4 \times 1.36)$ $y = 2.09 \times 10^{4 \times 1.36}$	M1	For $\lg y = (\text{their } \lg A) + 4(\text{their } b)$ or $y = (\text{their } A)(10^{4(\text{their } b)})$
	Allow 553 000 to 576 000	A1	
6 (c)	$4 = 2.09(10^{1.36x^2})$ or $\lg 4 = 0.3132 + 1.36x^2$	M1	$4 = (\text{their } A)(10^{\text{their } bx^2})$ or $\lg 4 = (\text{their } \lg A) + (\text{their } b)x^2$
	awrt 0.46	A1	

Question	Answer	Marks	Guidance
7(a)	$-4a + b + 5 = 0$ oe	B1	Allow multiples of equation
	$a + b - 25 = 0$ oe	B1	Allow multiples of equation
	$a = 6, b = 19$	2	M1 for solving <i>their</i> 2 equations and obtaining two solutions A1 for both $a = 6, b = 19$
	$(x + 4)(6x^2 - 5x + 1)$ $A = 6, B = -5, C = 1$	2	M1 for attempt to obtain quadratic factor by inspection or by algebraic long division A1 $(6x^2 - 5x + 1)$ or $A = 6, B = -5, C = 1$
	Alternative $a + b - 25 = 0$ oe	(B1)	Allow multiples of equation
	Comparing coefficients $C = 1$ and $A = a$	(B1)	
	$4A + B = b$	(B1)	
	Leading to $5A + B = 25$	(M1)	For use of <i>their</i> $a + b - 25 = 0$ to obtain an equation in A and B
	$4B + 1 = -19$	(B1)	
	$(x + 4)(6x^2 - 5x + 1)$ $A = 6, B = -5, C = 1$	(A1)	
7(b)	$(x + 4)(3x - 1)(2x - 1)$	B1	Must follow from a correct solution to (a)
7(c)	-19	B1	
8(a)	$\angle AOB = 1.45$ (radians)	B1	
8(b)	Sector area $= \frac{1}{2}(r^2)(1.45)$	B1	For correct sector area. Allow unsimplified
	Area of triangle $= \frac{1}{2} \times 0.5r \times r \times \sin(\pi - \text{their } 1.45)$	B1	For correct area of triangle Allow unsimplified
	Total area $= 0.973r^2$	B1	

Question	Answer	Marks	Guidance
8(c)	$(AC^2) = r^2 + 0.25r^2 - (2 \times r \times 0.5r \cos(\pi - 1.45))$	M1	For correct substitution in cosine rule using ($\pi -$ their 1.45)
	$AC = 1.17r$	A1	
	Perimeter = $2.95r + 1.17r$	B1	FT on their AC
	$r = 2.91$	A1	
9(a)	$\overrightarrow{AB} = \mathbf{b} - \mathbf{a}$ or $\overrightarrow{BA} = \mathbf{a} - \mathbf{b}$	B1	
	$\overrightarrow{OX} = \mathbf{a} + \frac{3}{4}\overrightarrow{AB}$ or $\overrightarrow{OX} = \mathbf{b} + \frac{1}{4}\overrightarrow{BA}$ $\overrightarrow{OX} = \mathbf{a} + \frac{3}{4}(\mathbf{b} - \mathbf{a})$ or $\overrightarrow{OX} = \mathbf{b} + \frac{1}{4}(\mathbf{a} - \mathbf{b})$	M1	For correct use of ratio, using their \overrightarrow{AB} or \overrightarrow{BA}
	$\overrightarrow{OX} = \frac{\mathbf{a}}{4} + \frac{3}{4}\mathbf{b}$	A1	
9(b)	$\overrightarrow{AC} = 2\mathbf{b} - \mathbf{a}$	B1	
9(c)	$\overrightarrow{AY} = -\mathbf{a} + h\left(\frac{\mathbf{a}}{4} + \frac{3}{4}\mathbf{b}\right)$	B1	FT on their \overrightarrow{OX}
9(d)	$-\mathbf{a} + h\left(\frac{\mathbf{a}}{4} + \frac{3}{4}\mathbf{b}\right) = m(2\mathbf{b} - \mathbf{a})$	M1	For equating appropriate vectors and attempt to equate like vectors
	$-1 + \frac{h}{4} = -m$	A1	FT from their \overrightarrow{AY} and \overrightarrow{AC}
	$\frac{3h}{4} = 2m$	A1	FT from their \overrightarrow{AY} and \overrightarrow{AC}
	$h = \frac{8}{5}, m = \frac{3}{5}$	A1	For both
10(a)	$\frac{3x+10+2(x+1)}{(x+1)(3x+10)} = \frac{3x+10+2x+2}{(x+1)(3x+10)}$ $= \frac{5x+12}{3x^2+13x+10}$	B1	For expansion and simplification to obtain given answer

Question	Answer	Marks	Guidance
10(b)	$P\left(0, \frac{6}{5}\right)$ and $Q\left(-\frac{6}{5}, 0\right)$ oe	B1	
	Area of triangle = $\frac{18}{25}$ or 0.72	B1	
	Area under curve = $\int_0^2 \frac{1}{x+1} + \frac{2}{3x+10} dx$	M1	For use of part (a) and attempt to integrate to obtain at least one ln term.
	$= \left[\ln(x+1) + \frac{2}{3} \ln(3x+10) \right]_0^2$	2	B1 For $\ln(x+1)$ B1 For $\frac{2}{3} \ln(3x+10)$
	$= \ln 3 + \frac{2}{3} \ln 16 - \frac{2}{3} \ln 10$	M1	For correct use of limits. Dep on previous M mark.
	$= \frac{2}{3} \ln 3\sqrt{3} + \frac{2}{3} \ln 16 - \frac{2}{3} \ln 10$	M1	For use of $\ln 3 = \frac{2}{3} \ln 3\sqrt{3}$
	$= \frac{2}{3} \ln 3\sqrt{3} + \frac{2}{3} \ln \left(\frac{16}{10}\right) = \frac{2}{3} \ln \left(\frac{48\sqrt{3}}{10}\right)$	M1	For use of multiplication and division rule
	Total area = $\frac{18}{25} + \frac{2}{3} \ln \left(\frac{24\sqrt{3}}{5}\right)$ oe	A1	For correct answer in the required form dep on the three preceding M marks Must not be obtained using a calculator
11(a)	$2 \cos x = 3 \frac{\sin x}{\cos x} \Rightarrow 2 \cos^2 x = 3 \sin x$	M1	For use of $\tan x = \frac{\sin x}{\cos x}$ and multiplying by $\cos x$
	$2(1 - \sin^2 x) = 3 \sin x$	M1	For use of correct identity
	$2 \sin^2 x + 3 \sin x - 2 = 0$	A1	For correct rearrangement to obtain the given answer
	Alternative $2 \sin^2 x + 3 \sin x - 2$ $= 2(1 - \cos^2 x) + 3 \sin x - 2$	(M1)	For use of correct identity
	$= -2 \cos x \cos x + 3 \sin x$ $= -3 \tan x \cos x + 3 \sin x$	(M1)	For use of $2 \cos x = 3 \tan x$
	$-3 \sin x + 3 \sin x = 0$	(A1)	For use of $\tan x \cos x = \sin x$ and answer 0

Question	Answer	Marks	Guidance
11(b)	$\sin\left(2\alpha + \frac{\pi}{4}\right) = \frac{1}{2}$ only	B1	For solution of quadratic from (a) to obtain $\sin\left(2\alpha + \frac{\pi}{4}\right) = \frac{1}{2}$ only
	$2\alpha + \frac{\pi}{4} = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{13\pi}{6}$ $2\alpha = \frac{7\pi}{12}, \frac{23\pi}{12}$	M1	For correct order of operations in attempt to solve $\sin\left(2\alpha + \frac{\pi}{4}\right) = \frac{1}{2}$, may be implied by one correct solution
	$\alpha = \frac{7\pi}{24}$	A1	
	$\alpha = \frac{23\pi}{24}$	A1	





Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/11

Paper 1

May/June 2020

MARK SCHEME

Maximum Mark: 80

Published

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This mark scheme is published to support teachers and students and should be read together with the question paper. It shows the requirements of the exam. The answer column of the mark scheme shows the proposed basis on which Examiners would award marks for this exam. Where appropriate, this column also provides the most likely acceptable alternative responses expected from students. Examiners usually review the mark scheme after they have seen student responses and update the mark scheme if appropriate. In the June series, Examiners were unable to consider the acceptability of alternative responses, as there were no student responses to consider.

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This document consists of **9** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

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GENERIC MARKING PRINCIPLE 2:

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- marks are awarded when candidates clearly demonstrate what they know and can do
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- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
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2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

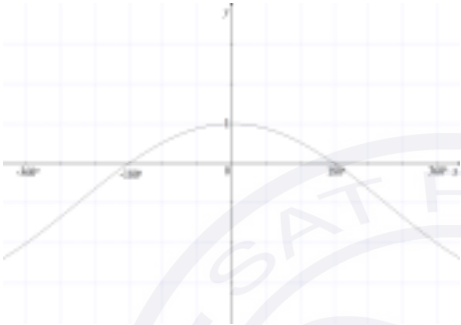
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- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
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When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Partial Marks
1(a)	$y = -\frac{1}{2}(x+2)(x+1)(x-5)$	B1	For $-\frac{1}{2}$
		B1	For $(x+2)(x+1)(x-5)$
1(b)	$-2 \leq x \leq -1$	B1	
	$x \geq 5$	B1	
2(a)	1080°	B1	
2(b)		B1	For correct shape and symmetry about the y-axis
		B1	For correct x-intercepts
		B1	For correct y-intercept
3	$\frac{dr}{dt} = 5$	B1	
	$\frac{dA}{dr} = 2\pi r$	B1	
	$\frac{dA}{dt} = \frac{dA}{dr} \times \frac{dr}{dt}$ leading to $\frac{dA}{dt} = 10\pi r$	M1	Use of the chain rule, may be implied by $5 \times 6\pi$
	$\frac{dA}{dt} = 30\pi$	A1	

Question	Answer	Marks	Partial Marks
4	$x = \frac{-(4-2\sqrt{7}) + \sqrt{(4-2\sqrt{7})^2 - 4(5+4\sqrt{7})(-1)}}{2(5+4\sqrt{7})}$	M1	For correct use of quadratic formula, allow inclusion of \pm until final answer
	$x = \frac{-(4-2\sqrt{7}) + \sqrt{16+28-16\sqrt{7}+20+16\sqrt{7}}}{2(5+4\sqrt{7})}$ $x = \frac{-(4-2\sqrt{7})+8}{2(5+4\sqrt{7})}$	M1	For attempt to simplify discriminant, must see attempt at expansion and subsequent simplification
	$x = \frac{4+2\sqrt{7}}{2(5+4\sqrt{7})} \quad \text{or} \quad x = \frac{2+\sqrt{7}}{(5+4\sqrt{7})}$	A1	For either
	$x = \frac{2+\sqrt{7}}{(5+4\sqrt{7})} \times \frac{5-4\sqrt{7}}{5-4\sqrt{7}}$ $x = \frac{10+5\sqrt{7}-8\sqrt{7}-28}{25-112}$	M1	For attempt to rationalise, must see attempt at expansion and subsequent simplification
	$x = \frac{6}{29} + \frac{\sqrt{7}}{29}$	A1	
5	$\frac{dy}{dx} = \frac{(x+2) \frac{6x}{3x^2-1} - \ln(3x^2-1)}{(x+2)^2}$	B1	B1 for $\frac{6x}{3x^2-1}$
		M1	For attempt to differentiate a quotient or an equivalent product, must have correct order of terms and correct sign
		A1	
	When $x=1$, $y = \frac{\ln 2}{3}$ or 0.231(0)	B1	
	When $x=1$, $\frac{dy}{dx} = 0.92298$, allow 0.923	B1	
	$y = 0.923x - 0.692$	B1	
6(a)	$x(5x+6)=8$ $5x^2+6x-8=0$	M1	For attempt to equate and obtain a 3-term quadratic in either x or y
	$\left(\frac{4}{5}, 10\right)$	A1	Allow A1 if only x -coordinates or only y -coordinates are given
	$(-2, -4)$	A1	

Question	Answer	Marks	Partial Marks
6(b)	Midpoint $\left(-\frac{3}{5}, 3\right)$	B1	
	Gradient 5	B1	
	$y - 3 = -\frac{1}{5}\left(x + \frac{3}{5}\right)$	M1	Attempt at perp bisector using <i>their</i> midpoint and perp gradient
	$x - 3 = -\frac{1}{5}\left(x + \frac{3}{5}\right)$	M1	For use of $y = x$ and attempt to solve
	$\left(\frac{12}{5}, \frac{12}{5}\right)$	A1	
7(a)	0.8	B1	
7(b)	Sector area = $\frac{1}{2}12^2(0.8)$ 57.6	B1	Allow unsimplified
	$\tan 0.4 = \frac{AM}{12}$ $AM = 12 \tan 0.4$ 5.074	M1	Attempt at AM using <i>their</i> $\frac{\theta}{2}$ Allow unsimplified
	Area of triangle $= \frac{1}{2}(5.074 \times 2) \times 2 \times 12$ 60.88	M1	Area of triangle using <i>their</i> AM , allow unsimplified
	Shaded area 3.28	A1	
7(c)	$\sin 0.4 = \frac{AM}{OA}$ $OA = \frac{5.074}{\sin 0.4}$ 13.03	M1	Attempt to find OA using <i>their</i> $\frac{\theta}{2}$ and <i>their</i> AM
	Perimeter = $2(1.03) + 9.6 + 2(5.074)$	M1	Allow if using <i>their</i> $\frac{\theta}{2}$ and <i>their</i> CM
	Perimeter = 21.8	A1	
8(a)	$\frac{3(2x+3)+3(2x-3)}{4x^2-9}$	M1	Must see for M1
	$\frac{12x}{4x^2-9}$	A1	

Question	Answer	Marks	Partial Marks
8(b)	$\int \frac{3}{2x-3} + \frac{3}{2x+3} dx$ $= \frac{3}{2} \ln(2x-3) + \frac{3}{2} \ln(2x+3)$	B2	B1 for each correct term, having made use of (a)
	$\frac{3}{2} \ln(4x^2 - 9) + c \quad \text{or}$ $\frac{3}{2} \ln((2x-3)(2x+3)) + c \quad \text{or}$ $\ln(4x^2 - 9)^{\frac{3}{2}} + c$	B1	
8(c)	$\ln(4a^2 - 9)^{\frac{3}{2}} - \ln 7^{\frac{3}{2}} = \ln 5^{\frac{3}{2}}$	M1	For correct application of limits, allow equivalent forms
	$4a^2 - 9 = 35$	A1	For a correct method of dealing with logarithms and eliminating them
	$a = \sqrt{11}$	M1	For solving a quadratic equation, dep on first M mark
		A1	
9(a)	Second term: $a + d = -14$	B1	
	Sum: $4 = a + 10d$	B1	
	$d = 2$	B1	
	$a = -16$	B1	
	Last term = 24	B1	Ft on <i>their d</i> and <i>their a</i>
9(b)(i)	$ar = 27p^2$ $ar^4 = p^5$	B1	For both equations
	$r = \frac{p}{3}$	B1	
9(b)(ii)	$a = 81p$	M1	M1 for attempt to find a in terms of p
		A1	
	$S_{\infty} = \frac{81p}{1 - \frac{p}{3}} \quad \text{or} \quad \frac{243p}{3-p}$	B1	Follow through on <i>their a</i> and <i>their r</i>

Question	Answer	Marks	Partial Marks
9(b)(iii)	$81 = \frac{81p}{1 - \frac{p}{3}}$ or $81 = \frac{243p}{3 - p}$	M1	For attempt to solve using <i>their</i> answer to (ii) as far as $p = \dots$
	$p = \frac{3}{4}$	A1	
10(a)(i)	$\frac{(\sec \theta + 1) - (\sec \theta - 1)}{\sec^2 \theta - 1}$	M1	For dealing with the fractions
	$\frac{2}{\tan^2 \theta}$	M1	For use of the correct identity
	$2 \cot^2 \theta$	A1	A1 for given answer, must see $\frac{8}{\tan^2 \theta}$ first
10(a)(ii)	$2 \cot^2 2x = 6$ $\tan 2x = \pm \frac{1}{\sqrt{3}}$	M1	M1 for use of (i) and attempt to simplify
		A1	
		M1	M1 for attempt to solve, may be implied by one correct solution
	$2x = -150^\circ, -30^\circ, 30^\circ, 150^\circ$ $x = -75^\circ, -15^\circ, 15^\circ, 75^\circ$	A2	A1 for each pair of correct solutions
10(b)	$\sin\left(y + \frac{\pi}{3}\right) = \frac{1}{2}$	M1	For dealing with cosec and an attempt to solve
	$y + \frac{\pi}{3} = \frac{5\pi}{6}, \frac{13\pi}{6}$	M1	M1 for a complete method of solution, may be implied by a correct solution
	$y = \frac{\pi}{2}$	A1	
	$y = \frac{11\pi}{6}$	A1	

Question	Answer	Marks	Partial Marks
11	$\frac{dy}{dx} = \frac{5}{2} \sin 2x (+c)$	M1	M1 for $k \sin 2x$
		A1	Condone omission of c
	$\frac{3}{4} = \frac{5}{2} \sin\left(-\frac{\pi}{6}\right) + c$	M1	Dep on first M1 for attempt to find c
	$c = 2$	A1	
	$y = -\frac{5}{4} \cos 2x + 2x (+d)$	M1	M1 for attempt to integrate <i>their</i> $\frac{dy}{dx}$
		A1	Condone omission of d
	$\frac{5\pi}{4} = -\frac{5}{4} \cos\left(-\frac{\pi}{6}\right) - \frac{\pi}{6} + d$	M1	Dep on previous M1 for attempt to find d
	$d = \frac{17\pi}{12} + \frac{5\sqrt{3}}{8}$ $y = -\frac{5}{4} \cos 2x + 2x + \frac{17\pi}{12} + \frac{5\sqrt{3}}{8}$ or $y = -\frac{5}{4} \cos 2x + 2x + 5.53$	A1	Must have the equation for A1



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 1

May/June 2020

MARK SCHEME

Maximum Mark: 80

Published

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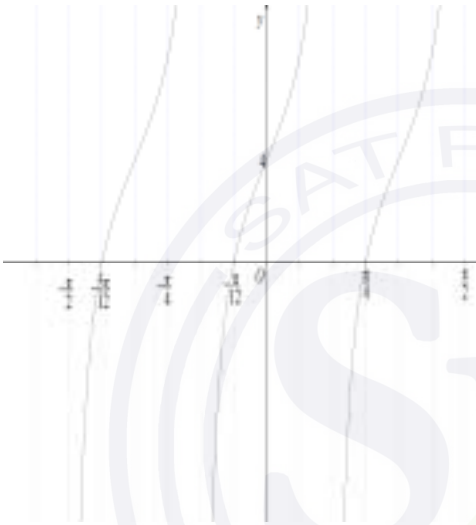
Question	Answer	Marks	Partial Marks
1		B1	Shape
		B1	Correct x -coordinates
		B1	Correct y -coordinate and max in first quadrant
2	$\frac{dr}{dt} = 0.5$	B1	
	$\frac{dV}{dr} = 4\pi r^2$	B1	
	$\frac{dV}{dt} = \frac{dV}{dr} \times \frac{dr}{dt}$ $\frac{dV}{dt} = \pi r^2$	M1	For attempt to use a correct form of the chain rule
	When $r = \frac{1}{4}$, $\frac{dV}{dt} = 0.125\pi$	A1	
3(a)	$4096 - 384x + 15x^2$	B1	For 4096
		B1	For $-384x$
		B1	For $15x^2$
3(b)	$(4096 - 384x + 15x^2) \left(x^2 - 2 + \frac{1}{x^2} \right)$	B1	For $\left(x^2 - 2 + \frac{1}{x^2} \right)$
	Term independent of x : $-2(4096) + 15$	M1	For use of 2 appropriate terms
	-8177	A1	
4(a)(i)	720	B1	
4(a)(ii)	600	B1	FT on <i>their</i> (i) $\times \frac{5}{6}$

Question	Answer	Marks	Partial Marks
4(a)(iii)	Starting with 8: $1 \times 4 \times 3 \times 2 \times 1 = 24$	B1	
	Starting with 3, 5 or 7: $3 \times 4 \times 3 \times 2 \times 2 = 144$	M1	May be considering each case separately, need all three cases for M1
		A1	
	Total = 168	A1	
4(a)(iii)	Alternative		
	Plan for adding numbers ending in 2 and numbers ending in 8	M1	
	Ending in 2: $\left(\frac{1}{6} \times 720\right) \times \frac{4}{5} = 96$	B1	Allow unsimplified
	Ending in 8: $\left(\frac{1}{6} \times 720\right) \times \frac{3}{5} = 72$	B1	Allow unsimplified
	Total = 168	A1	
4(b)	${}^nC_3 = 6{}^nC_2$	B1	$\frac{n(n-1)(n-2)}{3!}$
	$\frac{n(n-1)(n-2)}{3!} = \frac{6n(n-1)}{2!}$	B1	$\frac{6n(n-1)}{2!}$
	$n(n-1)[(n-2)-18] = 0$	M1	Valid attempt to solve, must have at least one previous B mark
	$n = 20$	A1	
4(b)	Alternative		
	${}^nC_3 = 6{}^nC_2$ $(n-2)!2! = (n-3)!3!$	B1	For dealing with $(n-2)!$ and $(n-3)!$ to obtain $(n-2)$
	$(n-2) = 6 \times 3$	B1	For dealing with 2! and 3! To obtain 6
	$n = 20$	M1	Valid attempt to solve, must have at least one previous B mark
		A1	
5(a)	$f > 9$	B1	Allow y but not x
5(b)	It is a one-one function because of the restricted domain	B1	

Question	Answer	Marks	Partial Marks
5(c)	$x = (2y + 3)^2$ or equivalent	M1	For a correct attempt to find the inverse
	$y = \frac{\sqrt{x} - 3}{2}$	M1	For correct rearrangement
	$f^{-1} = \frac{\sqrt{x} - 3}{2}$	A1	Must have correct notation
5(d)	$x > 9$	B1	FT on <i>their</i> (a)
5(e)	$f(\ln(x + 4)) = 49$	M1	For correct order
	$(2 \ln(x + 4) + 3)^2 = 49$ $\ln(x + 4) = 2$	M1	For correct attempt to solve, dep on previous M mark, as far as $x =$
	$x = e^2 - 4$	A1	
6(a)	$A \left(-\frac{5}{2}, 0 \right)$	B1	
	$x(-5 - 2x) + 3 = 0$ $2x^2 + 5x - 3 = 0$ $(2x - 1)(x + 3) = 0$	M1	For attempt to eliminate one variable, obtain a 3-term quadratic equation = 0 and attempt to solve
	$B \left(\frac{1}{2}, -6 \right)$	A1	Allow A1 if just the x-coordinates or just the y-coordinates are given
6(b)	Area of triangle = $\frac{1}{2} \left(\frac{5}{2} + \frac{1}{2} \right) \times 6, = 9$	M1	For attempt at triangle using <i>their</i> values
	$\int_{\frac{1}{2}}^1 -\frac{3}{x} dx = [-3 \ln x]_{\frac{1}{2}}^1$	M1	For attempt to integrate, must have ln
	$= 3 \ln \frac{1}{2}$	M1	correct application of limits, dep on previous M mark
	$= -3 \ln 2$	M1	realisation that value of integral is negative and making the adjustment
		M1	application of log law, dep on previous M mark
	Area = $9 + \ln 8$	A1	

Question	Answer	Marks	Partial Marks
7(a)	$\frac{dy}{dx} = (x^2 - 1) \frac{5}{2} (5x + 2)^{-\frac{1}{2}} + 2x(5x + 2)^{\frac{1}{2}}$	B1	For $\frac{5}{2} (5x + 2)^{-\frac{1}{2}}$
		M1	For differentiation of a product
		A1	
	$\frac{dy}{dx} = \frac{(5x + 2)^{-\frac{1}{2}}}{2} (5(x^2 - 1) + 4x(5x + 2))$ or equivalent	M1	Dep on previous M mark for attempt to simplify
	$\frac{dy}{dx} = \frac{25x^2 + 8x - 5}{2\sqrt{5x + 2}}$	A1	
7(b)	$25x^2 + 8x - 5 = 0$	M1	Equating their numerator in (a) to zero and attempt to solve
	$x = 0.315$	A1	
	$y = -1.70$	A1	
7(c)	Consideration of gradient or y values either side of stationary point, remembering that $x > 0$.	M1	Must be a complete method making use of <i>their</i> (a). Allow consideration of $25x^2 + 8x - 5$ as a 'minimum curve'. Accept 2nd derivative method.
	Minimum	A1	
8(a)	b – a	B1	
8(b)	$\frac{1}{4}\mathbf{a} + \frac{1}{2}(\mathbf{b} - \mathbf{a})$ or $-\frac{3}{4}\mathbf{a} + \frac{1}{2}(\mathbf{a} + \mathbf{b})$	B1	For $\frac{1}{4}\mathbf{a}$ or $-\frac{3}{4}\mathbf{a}$
		B1	For $\frac{1}{2}(\mathbf{b} - \mathbf{a})$ or $\frac{1}{2}(\mathbf{a} + \mathbf{b})$
	$\frac{1}{2}\mathbf{b} - \frac{1}{4}\mathbf{a}$	B1	Correct and simplified
8(c)	$n\left(\frac{1}{2}\mathbf{b} - \frac{1}{4}\mathbf{a}\right)$	B1	FT on <i>their</i> answer to (b)
8(d)	$\frac{1}{2}(\mathbf{b} - \mathbf{a}) + k\mathbf{b}$	M1	For use of <i>their</i> (a) and $k\mathbf{b}$
		A1	

Question	Answer	Marks	Partial Marks
8(e)	$\frac{1}{2}(\mathbf{b} - \mathbf{a}) + k\mathbf{b} = n\left(\frac{1}{2}\mathbf{b} - \frac{1}{4}\mathbf{a}\right)$ $-\frac{1}{2} = -\frac{n}{4}$ $\frac{1}{2} + k = \frac{n}{2}$	M1	For equating <i>their</i> (c) and (d) and then equating like vectors to obtain 2 equations
	$n = 2$	A1	
	$k = \frac{1}{2}$	A1	
9(a)(i)	$v = 20 \cos 2t$ when $t = \pi$, $v = 20$	B1	
9(a)(ii)	$20 \cos 2t = 0$	M1	Equating <i>their</i> (i) to zero, must be a cosine and attempt to solve
	$t = \frac{\pi}{4}$	A1	
9(a)(iii)	$a = -40 \sin 2t$	M1	Attempt to differentiate <i>their</i> v , dep on previous M mark, and use <i>their</i> value for (ii)
	-40	A1	
9(b)(i)	35	B1	
9(b)(ii)	$112.5 = \frac{1}{2}(35 + x) \times 5$	M1	Use of area under appropriate part of the graph
		A1	
	$x = 10$	A1	
9(b)(iii)	$\frac{25}{5} = \frac{10}{t'}$	M1	Using a ratio method or otherwise, find extra time to stop = 2s or equivalent
	$t' = 2$	A1	
	27	A1	

Question	Answer	Marks	Partial Marks
10(a)	$3x = -\frac{5\pi}{4} - \frac{\pi}{4}, \frac{3\pi}{4}$	M1	For a correct attempt to solve, may be implied by one correct solution
	$x = -\frac{\pi}{12}$	A1	
	$x = \frac{\pi}{4}$	A1	
	$x = -\frac{5\pi}{12}$	A1	
10(b)		B1	Shape – must have three ‘parts’ with asymptotes
		B1	For correct x -coordinates
		B1	For correct y -coordinate



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/13

Paper 1

May/June 2020

MARK SCHEME

Maximum Mark: 80

Published

Students did not sit exam papers in the June 2020 series due to the Covid-19 global pandemic.

This mark scheme is published to support teachers and students and should be read together with the question paper. It shows the requirements of the exam. The answer column of the mark scheme shows the proposed basis on which Examiners would award marks for this exam. Where appropriate, this column also provides the most likely acceptable alternative responses expected from students. Examiners usually review the mark scheme after they have seen student responses and update the mark scheme if appropriate. In the June series, Examiners were unable to consider the acceptability of alternative responses, as there were no student responses to consider.

Mark schemes should usually be read together with the Principal Examiner Report for Teachers. However, because students did not sit exam papers, there is no Principal Examiner Report for Teachers for the June 2020 series.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the June 2020 series for most Cambridge IGCSE™ and Cambridge International A & AS Level components, and some Cambridge O Level components.

This document consists of **8** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

Maths-Specific Marking Principles	
1	Unless a particular method has been specified in the question, full marks may be awarded for any correct method. However, if a calculation is required then no marks will be awarded for a scale drawing.
2	Unless specified in the question, answers may be given as fractions, decimals or in standard form. Ignore superfluous zeros, provided that the degree of accuracy is not affected.
3	Allow alternative conventions for notation if used consistently throughout the paper, e.g. commas being used as decimal points.
4	Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored (isw).
5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

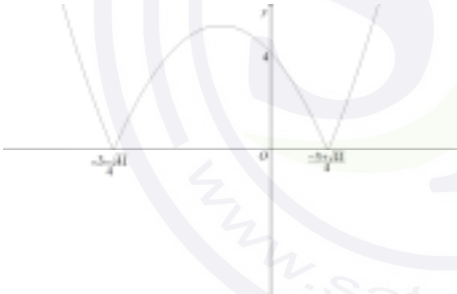
- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation '**dep**' is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Partial Marks
1(a)	$f > 3$	B1	Allow y but not x
	$g \in \mathbb{R}$	B1	Allow y but not x
1(b)	$\ln(x-3)$	B1	
	$\ln(x-3) = 9$ $x-3 = e^9$	M1	For attempt to equate to 9 and solve, must get rid of \ln
	$x = e^9 + 3$	A1	
1(c)	$9(9x-5)-5=112$	M1	For correct order of operation
	$x = 2$	A1	
2(a)	Either $2\log_4 y = \log_2 y$ Or $\log_2 x = 2\log_4 x$	B1	
	Either $\log_2 x + \log_2 y = 8$ leading to $\log_2 xy = 8$ Or $2\log_4 x + 2\log_4 y = 8$ leading to $\log_4 xy = 4$	M1	For use of log law
	$xy = 256$	A1	
2(b)	$2y^2 - 3y + 1 = 0$	B1	
	$y = \frac{1}{2}, 1$	M1	For attempt to solve for y
	$x = -1$	A1	
	$x = 0$	A1	
3(a)	$v = (2t+1)^{\frac{1}{2}}(+c)$	B1	For $v = (2t+1)^{\frac{1}{2}}$ condone absence of c
	$8 = 1 + c, \quad c = 7$	M1	For attempt to find c must have $k(2t+1)^{\frac{1}{2}}$
	$v = (2t+1)^{\frac{1}{2}} + 7$	A1	

Question	Answer	Marks	Partial Marks
3(b)	$s = \frac{1}{3}(2t+1)^{\frac{3}{2}} + 7t(+d)$	B1	For $\frac{1}{3}(2t+1)^{\frac{3}{2}}$
		M1	For attempt to integrate <i>their</i> answer to (a), must have $k(2t+1)^{\frac{1}{2}}$ in (a)
	$4 = \frac{1}{3} + d, \quad d = \frac{11}{3}$	M1	Attempt to find d
	$s = \frac{1}{3}(2t+1)^{\frac{3}{2}} + 7t + \frac{11}{3}$	A1	
4(a)	$2\left(x + \frac{3}{4}\right)^2 - \frac{41}{8}$	B3	B1 for 2 B1 for $\frac{3}{4}$ B1 for $-\frac{41}{8}$
4(b)	$\left(-\frac{3}{4}, -\frac{41}{8}\right)$	B2	B1 for $-\frac{3}{4}$ or FT on <i>their</i> $-b$ B1 for $-\frac{41}{8}$ or FT on <i>their</i> c
4(c)		B1	For shape with max in 2 nd quadrant
		B1	For x -intercepts $\frac{-3 \pm \sqrt{41}}{4}$
		B1	For y -intercept of 4 and cusps
4(d)	$\frac{41}{8}$	B1	FT on <i>their</i> c

Question	Answer	Marks	Partial Marks
5(a)	$p(3): 162 + 9a + 36 + b = 11$ $p(-1): -6 + a - 12 + b = -21$	M1	For attempt at $p(3)$ and $p(-1)$
	$9a + b + 187 = 0$ $a + b + 3 = 0$	A1	for both, may be implied by correct work later
	$a = -23, \quad b = 20$	M1	attempt to solve simultaneous equations
		A1	For both
	$p(x) = (x - 2)(6x^2 - 11x - 10)$	M1	For attempt to factorise or use algebraic long division
		A1	For $(6x^2 - 11x - 10)$
5(b)	$p(x) = (x - 2)(3x + 2)(2x - 5)$	M1	For attempt to factorise or use quadratic formula – must be seen
	$2, -\frac{2}{3}, \frac{5}{2}$	A1	For all three solutions
6(a)	$\frac{1}{13} \begin{pmatrix} 5 \\ -12 \end{pmatrix}$	B1	
6(b)	$4 - 2k = -10r$ $1 + 3k = 5r$	M1	equating like vectors to obtain 2 equations
	$r = -\frac{7}{10}, \quad k = -\frac{3}{2}$	M1	Dep on previous M mark, for attempt to solve simultaneously
		A1	
6(c)(i)	$3\mathbf{q} - 2\mathbf{p}$	B1	
6(c)(ii)	$9\mathbf{q} - 6\mathbf{p}$	B1	
6(c)(iii)	A common point of A and the same direction vector	B1	
6(c)(iv)	1:2	B1	
7(a)	$\frac{1}{2} \times 10^2 \times \theta = 35$ so $\theta = 0.7$	B1	

Question	Answer	Marks	Partial Marks
7(b)	Arc length CD : 7	B1	
	$\sin(0.35) = \frac{AB/2}{12}$	M1	For a complete method to find AB , could be using cosine rule
	$AB = 8.23(0)$	A1	
	Perimeter = $7 + 4 + 8.23 = 19.2$	A1	
7(c)	Area of triangle = $\frac{1}{2}12^2 \sin 0.7$	M1	For complete attempt at triangle area, may use equivalent method
	Area of triangle = 46.4	A1	
	Shaded area = 11.4	A1	Follow through on <i>their</i> area of the triangle
8(a)	$\frac{n}{2}(14 + (n-1)0.4)$	B1	
	$\frac{n}{2}(14 + (n-1)0.4) > 300$ $0.4n^2 + 13.6n - 600 > 0$	M1	Attempt to form a 3 term inequality and find the positive critical value
	Positive critical value 25.29	A1	
	26 terms	A1	
8(b)	$a + ar = 9$	B1	
	$\frac{a}{1-r} = 36$	B1	
	$36(1+r)(1-r) = 9$	M1	attempt at solution of simultaneous equations
	$r = \frac{\sqrt{3}}{2}$	A1	

Question	Answer	Marks	Partial Marks
9	$x(5x-3)=2$ $5x^2-3x-2=0$	M1	attempt at a 3-term quadratic equation in one variable with solution
	$x=1, x=-\frac{2}{5}$	A1	Allow if $x=-\frac{2}{5}$ not seen
	$A (1, 2)$	A1	
	$B \left(\frac{3}{5}, 0\right)$	B1	
	Area of triangle $= \frac{2}{5}$	M1	Using <i>their</i> A and B
	Area under curve: $\int_1^3 \frac{2}{x} dx = [2 \ln x]_1^3$	B1	For $[2 \ln x]_1^3$
	$= 2 \ln 3$	M1	For use of limits
	Total area $= \frac{2}{5} + \ln 9$	A1	
10(a)	$\frac{dy}{dx} = \frac{1}{2}x(x+2)^{-\frac{1}{2}} + (x+2)^{\frac{1}{2}}$	B1	For $\frac{1}{2}(x+2)^{-\frac{1}{2}}$
		M1	For differentiation of a product
		A1	
	$\frac{dy}{dx} = \frac{1}{2}(x+2)^{-\frac{1}{2}}[x+2(x+2)]$	M1	For attempt to simplify
	$\frac{dy}{dx} = \frac{3x+4}{2\sqrt{x+2}}$	A1	
10(b)	$3x+4=0$	M1	For setting <i>their</i> numerator in (a) to zero and attempt to solve
	$x = -\frac{4}{3}$	A1	
	$y = -\frac{4\sqrt{6}}{9}$ oe	A1	
10(c)	Using the gradient method or inspection of y -coordinates either side of stationary point. Allow use of second derivative	M1	complete method
	Minimum	A1	Must be from correct work



Cambridge IGCSE™

ADDITIONAL MATHEMATICS

0606/12

Paper 12

March 2020

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the March 2020 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

This document consists of **10** printed pages.

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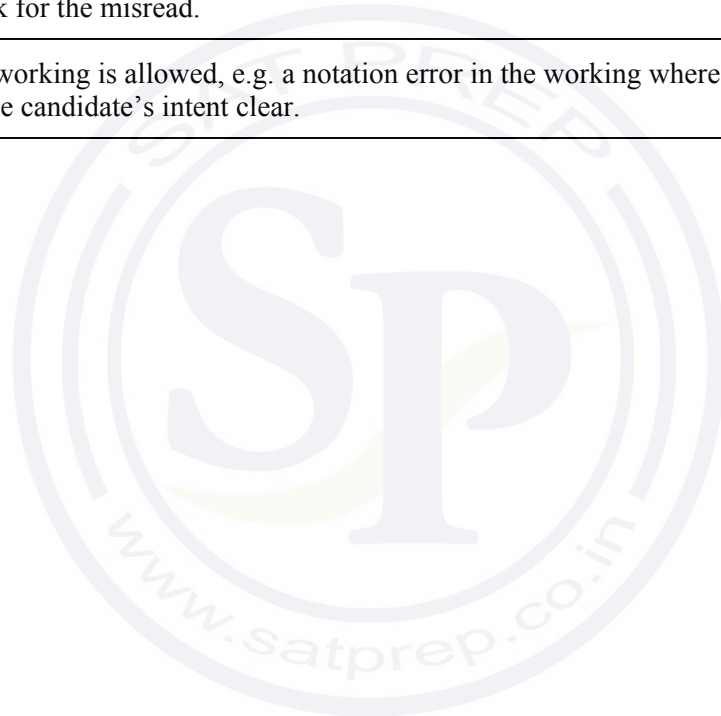
GENERIC MARKING PRINCIPLE 5:

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5	Where a candidate has misread a number in the question and used that value consistently throughout, provided that number does not alter the difficulty or the method required, award all marks earned and deduct just 1 mark for the misread.
6	Recovery within working is allowed, e.g. a notation error in the working where the following line of working makes the candidate's intent clear.



MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.


Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

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Abbreviations

awrt	answers which round to
cao	correct answer only
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oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(a)		3	B1 For correct shape with minimum point in the fourth quadrant and the maximum point in the first quadrant. Ends of the curve must be in the 2nd and 4th quadrants B1 for correct x- intercepts $(-1,0)$, $(2,0)$, $(4,0)$ B1 for correct y-intercept $(0,-24)$
1(b)	$x < -1$	B1	
	$2 < x < 4$	B1	

Question	Answer	Marks	Guidance
2	$2x^2 + 4x + k - 1 = kx + 3$ $2x^2 + (4 - k)x + (k - 4) = 0$	2	M1 for attempt to equate the line and curve and simplify to a 3 term quadratic equation = 0 A1 for a correct equation, allow equivalent form
	$(4 - k)^2 = 4 \times 2 \times (k - 4)$	M1	Use of discriminant in any form
	$k^2 - 16k + 48 = 0$ $k = 12, k = 4$ Do not isw	2	Dep M1 on previous M mark, for attempt to solve a quadratic equation in k A1 for both
	Alternative 1		
	$2x^2 + 4x + k - 1 = kx + 3$ $2x^2 + (4 - k)x + (k - 4) = 0$	(2	M1 for attempt to equate the line and curve and simplify A1 for a correct equation, allow equivalent form
	$k = 4x + 4$ $2\left(\frac{k - 4}{4}\right)^2 + (4 - k)\left(\frac{k - 4}{4}\right) + (k - 4) = 0$	M1	Equating gradients and substitution to obtain a quadratic equation in terms of k
	$k^2 - 16k + 48 = 0$ $k = 12$ and $k = 4$ Do not isw	2)	Dep M1 on previous M mark, for attempt to solve a quadratic equation in k A1 for both
	Alternative 2		
	$2x^2 + 4x + k - 1 = kx + 3$ $2x^2 + (4 - k)x + (k - 4) = 0$	(2	M1 for attempt to equate the line and curve and simplify A1 for a correct equation, allow equivalent form
	$k = 4x + 4$ $2x^2 - 4x = 0$ $x = 0, 2$	M1	Equating gradients and substitution to obtain a quadratic equation in terms of x and solution of this equation to obtain 2 x values
	$k = 4x + 4$ $k = 12$ and $k = 4$ Do not isw	2)	Dep M1 on previous M mark, for substitution of their x values to obtain k values A1 for both

Question	Answer	Marks	Guidance
3	$b = 243$	B1	Must be evaluated
	${}^5C_1 \times 3^4 \times (-a) = -81$	M1	Allow equivalent with no negative signs, allow sign error
	$a = \frac{1}{5}$ oe	A1	
	${}^5C_2 \times 3^3 \times (-a)^2$	M1	Allow with <i>their</i> a^2
	$c = \frac{54}{5}$ or 10.8 oe	A1	Must be from correct working
4	$\frac{dy}{dx} = \frac{6x}{3x^2 - 4} - \frac{x^2}{2}$	2	M1 for attempt to differentiate, must have at least one term correct A1 All correct
	When $x = 2$, $\frac{dy}{dx} = -\frac{1}{2}$	B1	
	When $x = 2$, $y = \ln 8 - \frac{4}{3}$, or exact equivalent	B1	Allow $\ln 8 - \frac{8}{6}$
	Equation of tangent $y - \left(\ln 8 - \frac{4}{3}\right) = -\frac{1}{2}(x - 2)$ oe	M1	Dep on first M mark, allow unsimplified, allow use of decimals
	$\left(0, \ln 8 - \frac{1}{3}\right)$, or exact equivalent	A1	Allow $x = 0, y = \ln 8 - \frac{1}{3}$
5(a)	$\frac{1}{2}(5 - \sqrt{3})(2 + 4\sqrt{3})$ $\frac{1}{2}(10 - 2\sqrt{3} + 20\sqrt{3} - 12)$	M1	Need to see $\frac{1}{2}(10 - 18\sqrt{3} - 12)$ or $(5 - 9\sqrt{3} - 6)$ minimum for M1
	$9\sqrt{3} - 1$	A1	
5(b)	$\tan ABC = \frac{5 - \sqrt{3}}{1 + 2\sqrt{3}} \times \frac{1 - 2\sqrt{3}}{1 - 2\sqrt{3}}$ $= \frac{5 - \sqrt{3} - 10\sqrt{3} + 6}{1 - 12}$	M1	Attempt at trig ratio and attempt to rationalise. Need to see $5 - 11\sqrt{3} + 6$ in the numerator as a minimum for M1 Allow one error only
	$= \sqrt{3} - 1$	2	A1 for $\sqrt{3}$, A1 for -1

Question	Answer	Marks	Guidance
5(c)	$\sec^2 ABC = \tan^2 ABC + 1$ $= (\sqrt{3} - 1)^2 + 1$ oe	M1	Allow use of correct identity with <i>their</i> (b)
	$= 5 - 2\sqrt{3}$	A1	
	Alternative		
	$\sec^2 ABC = \left(\frac{\sqrt{(5-\sqrt{3})^2 + (1+2\sqrt{3})^2}}{1+2\sqrt{3}} \right)^2$ leads to $\frac{41-6\sqrt{3}}{13+4\sqrt{3}}$ leads to $\frac{533+72-242\sqrt{3}}{121}$	(M1)	For a complete method using triangle <i>ABD</i> , with sufficient detail in the expansions and rationalisation
	$= 5 - 2\sqrt{3}$	A1)	
6(a)	Midpoint = (2, 7)	B1	
	Gradient of <i>AB</i> = $\frac{6}{8}$ oe	B1	
	Perp bisector: $y - 7 = -\frac{4}{3}(x - 2)$	M1	Must be using a perp gradient and a mid-point
	$4x + 3y - 29 = 0$	A1	Allow in any order but must be equated to zero.
6(b)	3	B1	FT on <i>their</i> (a)
6(c)	Displacement vector $\overrightarrow{CM} = \begin{pmatrix} -3 \\ 4 \end{pmatrix}$	M1	Allow equivalent vectors or other methods. May be implied by one correct coordinate.
	(-1, 11)	A1	Allow $x = -1$, $y = 11$

Question	Answer	Marks	Guidance
7(a)	$p\left(-\frac{1}{2}\right): -\frac{a}{8} + \frac{3}{4} - \frac{b}{2} - 12 = 0$ $p(3): 27a + 27 + 3b - 12 = 105$	M1	For attempt at an equation using either $p\left(-\frac{1}{2}\right)$ or $p(3)$
	$a + 4b = -90$	A1	Allow equivalent with constants collected
	$9a + b = 30$	A1	Allow equivalent with constants collected
	$a = 6, b = -24$	2	M1 for attempt to solve <i>their</i> equations, dep on first M mark A1 for both
7(b)	$(2x + 1)(3x^2 - 12)$	2	B1 for $3x^2$ B1 for -12 and no extra term in x
7(c)	$x = -\frac{1}{2}$	B1	
	$x = \pm 2$	B1	Dep on both B marks in part (b)
8(a)	$\begin{pmatrix} -20 \\ 48 \end{pmatrix}$	B1	
8(b)	$\begin{pmatrix} -20 \\ 48 \end{pmatrix} t$	B1	Follow through on <i>their</i> (a)
8(c)	$\begin{pmatrix} 12 \\ 8 \end{pmatrix} + \begin{pmatrix} -25 \\ 45 \end{pmatrix} t$ oe	B1	
8(d)	$\begin{pmatrix} 12 \\ 8 \end{pmatrix} + \begin{pmatrix} -5 \\ -3 \end{pmatrix} t$ oe	B1	
8(e)	$ \overrightarrow{PQ} ^2 = (12 - 5t)^2 + (8 - 3t)^2$	M1	Attempt to find modulus of <i>their</i> (d) which must contain terms in t
	$ \overrightarrow{PQ} = \sqrt{144 - 120t + 25t^2 + 64 - 48t + 9t^2}$	A1	Must see correct expansion leading to given answer.
	$PQ = \sqrt{34t^2 - 168t + 208}$		

Question	Answer	Marks	Guidance
8(f)	$34t^2 - 168t + 204 = 0$	M1	For dealing with square root correctly and attempt to solve a 3 term quadratic equation
	2.15 only	A1	
9(a)(i)	360	B1	
9(a)(ii)	60	B1	FT on <i>their</i> (b)(i) divided by 6
9(a)(iii)	A complete plan for dealing with odd numbers and numbers greater than 7000, see below	M1	Must be considering each case
	Starts with 8 and ends with odd = 48	B1	
	Starts with 7 or 9 and ends with odd = 72	B1	
	120	A1	
	Alternative		
	Their answer to (a)(i) – odd numbers starting with 2 – odd number starting with 3 or 5 – all even numbers	(M1	Must be considering each case
	All even numbers = 120 Odd and starting with 2 = 48 Odd and starting with 3 or 5 = 72	2	B1 for 1 correct
	120	A1)	
9(b)	$\frac{n!}{(n-3)!3!} = 92n$	B1	
	$n(n-1)(n-2) = 552n$	M1	Attempt to simplify factorials
	$n(n^2 - 3n - 550) = 0$ $n(n-25)(n+22) = 0$	M1	Dep on previous M mark for expansion and simplification to a cubic or quadratic in n and attempt to solve
	$n = 25$	A1	For $n = 25$ only
10(a)	$\alpha + 45^\circ = 144.7^\circ, 324.7^\circ$ $\alpha = 99.7^\circ, 279.7^\circ$	3	M1 for attempt to solve using a correct order of operations, may be implied by one correct solution A1 for 1 correct solution A1 for a second correct solution and no extras

Question	Answer	Marks	Guidance
10(b)(i)	$\frac{(\sin \theta + 1) - (\sin \theta - 1)}{\sin^2 \theta - 1}$	M1	For dealing with fractions
	$\frac{2}{-\cos^2 \theta}$	M1	For simplification of numerator and use of the correct identity
	$-2 \sec^2 \theta$ $a = -2$	A1	Must see previous line for A1
10(b)(ii)	$-2 \sec^2 3\phi = -8$ oe $\sec 3\phi = \pm 2$	M1	For making use of (i) and attempt to simplify in terms of 3ϕ
	$\cos 3\phi = \pm \frac{1}{2}$	A1	
	$3\phi = -\frac{2\pi}{3}, -\frac{\pi}{3}, \frac{\pi}{3}, \frac{2\pi}{3}$ $\phi = -\frac{2\pi}{9}, -\frac{\pi}{9}, \frac{\pi}{9}, \frac{2\pi}{9}$ or $\pm 0.349, \pm 0.698,$	3	Dep M1 for attempt to solve, may be implied by one correct solution A1 for each pair of correct solutions
11	$[\ln(2x+3) + \ln(3x-1) - \ln x]_1^a$	2	B1 for 1 term correct B1 all correct
	$(\ln(2a+3) + \ln(3a-1) - \ln a)$ $-(\ln 5 + \ln 2)$	M1	Correct substitution of limits, dep on first B1, ignore equality Must have 3 terms involving x
	$\ln \frac{(2a+3)(3a-1)}{10a} = \ln 2.4$	M1	For use of both addition and subtraction rules, ignore equality Or for use of addition rule on each side of an equation.
	$6a^2 - 17a - 3 = 0$	A1	
	$a = 3$	2	M1 for solution of their quadratic A1 for $a = 3$ only

ADDITIONAL MATHEMATICS**0606/11**

Paper 1

October/November 2019

MARK SCHEME

Maximum Mark: 80

Published

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This document consists of **10** printed pages.

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GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

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Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

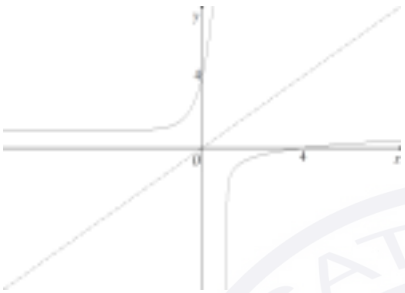
- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$A' \cap B$ oe	B1	
	$(X \cap Y) \cup (X \cap Z)$ or $X \cap (Y \cup Z)$	B1	
2	$2x^2 + 3x + k = kx - 3$	M1	For an attempt to equate and simplify to a 3 term quadratic equation, allow an error in one term
	$2x^2 + (3 - k)x + (k + 3) = 0$	A1	
	$(3 - k)^2 - 4 \times 2 \times (k + 3)$	M1	For attempt to use the discriminant, allow previous error, leading to a quadratic equation in terms of k
	$k^2 - 14k - 15 = 0$ giving critical values of -1 and 15	A1	For critical values
	$-1 < k < 15$	A1	
3	Either $7^x \times 7^{2y}$ or $49^{\frac{x}{2}} \times 49^y$ or $5^{5x} \times 5^{2y}$ or $25^{\frac{5x}{2}} \times 25^y$	M1	For expressing the terms on the left hand side of either one of the 2 equations in terms of powers of 7, 49, 5 or 25
	$7^x \times 7^{2y} = 7^0$ or $49^{\frac{x}{2}} \times 49^y = 49^0$	A1	
	$5^{5x} \times 5^{2y} = 5^{-2}$ or $25^{\frac{5x}{2}} \times 25^y = 25^{-1}$	A1	
	leading to $x + 2y = 0$ and $5x + 2y = -2$	M1	For attempt to solve two linear equations, with integer coefficients and constants, in terms of x and y
	$x = -\frac{1}{2}, y = \frac{1}{4}$	A1	
4(i)	$\frac{d}{dx}(\ln(4x^2 + 1)) = \frac{8x}{4x^2 + 1}$	B1	
	$\frac{dy}{dx} = \frac{(2x - 3) \frac{8x}{(4x^2 + 1)} - 2 \ln(4x^2 + 1)}{(2x - 3)^2}$	M1	For attempt to differentiate a quotient
		A1	For all other terms, not including $\frac{8x}{4x^2 + 1}$, correct
4(ii)	When $x = 2$, $\frac{dy}{dx} = \frac{16}{17} - 2 \ln 17$ $= -4.73$	M1	For attempt to find value of $\frac{dy}{dx}$ when $x = 2$ and multiply by h
	Change in $y = -4.73h$	A1	

Question	Answer	Marks	Guidance
5(i)	$f > 1$	B1	Must be using correct notation
	$g \in \mathbb{R}$	B1	Must be using correct notation
5(ii)	$g(0)=1, g(1)=2$ and attempt at $f(2)$	M1	For attempt at g^2 and correct order
	$f(2)=164.8$ awrt 165	A1	
5(iii)		B3	B1 for correct f and $(0,4)$, must be in first and second quadrant B1 for correct f^{-1} and $(4,0)$, must be in first and fourth quadrant B1 for $y=x$ and/or symmetry implied, by 'matching intercepts'. No intersection.
6	$\frac{dy}{dx} = k(8x+5)^{-\frac{1}{2}}$	M1	For attempt to differentiate, must be in the form $k(8x+5)^{-\frac{1}{2}}$
	$\frac{dy}{dx} = 4(8x+5)^{-\frac{1}{2}}$	A1	
	When $x = \frac{1}{2}, y = 3$	B1	
	Normal: $y - 3 = -\frac{3}{4}\left(x - \frac{1}{2}\right)$	M1	For attempt at the normal when $x = \frac{1}{2}$, using correct process for <i>their</i> $\frac{dy}{dx}$ and <i>their</i> y .
	$6x + 8y - 27 = 0$	A1	

Question	Answer	Marks	Guidance
7(i)	$\lg y = \lg A + x \lg b$	B1	For statement, may be implied by subsequent work
	Either $6 = \lg A + 3.4 \lg b$ or $3.6 = \lg A + 2.2 \lg b$	M1	For one correct equation
		M1	For another correct equation and attempt to solve simultaneously
	$\lg b = 2, b = 100$	A1	
	$\lg A = -0.8, A = 10^{-0.8}$ or 0.158	A1	
	Or Gradient = $\lg b = 2$	M1	equating gradient to $\lg b$ and attempt to evaluate
	$b = 100$	A1	Must be identified as b
	$6 = \lg A + 3.4 \lg b$ or $3.6 = \lg A + 2.2 \lg b$	M1	For a correct equation and attempt to find $\lg A$
	$\lg A = -0.8, A = 10^{-0.8}$ or 0.158	A1	Must be identified as A
7(ii)	$\lg 900 = -0.8 + 2x$ oe	M1	For correct use of $y = 900$
	$x = 1.88$	A1	
8(i)	$BC^2 = (7 + \sqrt{5})^2 + (7 - \sqrt{5})^2$ $= 49 + 14\sqrt{5} + 5 + 49 - 14\sqrt{5} + 5$ $= 108$	M1	For use of Pythagoras' theorem and attempt to expand and simplify
	$BC = 6\sqrt{3}$	A1	
	Perimeter = $22 + 6\sqrt{5} + 6\sqrt{3}$	A1	

Question	Answer	Marks	Guidance
8(ii)	Either $\frac{1}{2}(4+3\sqrt{5}+11+2\sqrt{5})(7+\sqrt{5})$ $= \frac{1}{2}(15+5\sqrt{5})(7+\sqrt{5})$ $= \frac{1}{2}(105+35\sqrt{5}+15\sqrt{5}+25)$	M1	Either For a valid method and attempt to expand out and simplify
	Or $(4+3\sqrt{5})(7+\sqrt{5}) + \frac{1}{2}(7+\sqrt{5})(7-\sqrt{5})$ $= 28 + 21\sqrt{5} + 4\sqrt{5} + 15 + \frac{1}{2}(49-5)$	M1	Or For a valid method and attempt to expand out and simplify
	Area = $65 + 25\sqrt{5}$	A2	A1 for each term
9(i)	Either $15^2 = 10^2 + 10^2 - 200 \cos AOB$ $\cos AOB = -0.125$	M1	For use of cosine rule
	$AOB = 1.696$ so 1.70 to 2 dp	A1	Must have justification to 2 dp
	Or $\sin\left(\frac{AOB}{2}\right) = \frac{7.5}{10}$ $\frac{AOB}{2} = 0.8481$	M1	For use of basic trig
	$AOB = 1.696$ so 1.70 to 2 dp	A1	

Question	Answer	Marks	Guidance
9(ii)	Angle $DOC = \frac{\pi}{3}$	B1	
	Either $AOD = BOC = 0.5 \left(2\pi - \frac{\pi}{3} - 1.696 \right)$ $AOD = BOC = 1.77$	M1	For attempt to get AOD or BOC
	Arc lengths = 17.7	M1	For attempt at arc length using their previous answer
	Perimeter = $15 + 10 + (2 \times 17.7) = 60.4$	A1	
	Or Arc $AB = 17$ or Arc $CD = \frac{10\pi}{3}$	M1	For either arc length
	$(20\pi - \text{arc } AB - \text{arc } CD)$	M1	
	Perimeter = 60.4	A1	
9(iii)	Either Area of each sector = $\frac{1}{2} 10^2 (1.770)$	M1	For area of sector using their BOC
	Area of triangles = $\left(\frac{1}{2} \times 100 \times \sin \frac{\pi}{3} \right) + \left(\frac{1}{2} \times 100 \sin 1.70 \right)$	M1	For area of one triangle using the sine rule oe
	Total area = $177 + 43.3 + 49.6$	M1	For plan
	Area = awrt 270	A1	
	Or Area of upper segment = $\frac{1}{2} 10^2 (1.696 - \sin 1.696)$	M1	For area of a sector or area of a triangle using the sine rule oe
	Area of lower segment = $\frac{1}{2} 10^2 \left(\frac{\pi}{3} - \sin \frac{\pi}{3} \right)$	M1	For whichever has not been obtained in previous part
	Shaded area = $100\pi - \text{are of the 2 segments}$ Area = $314.2 - 35.2 - 9.06$	M1	For plan
	Area = awrt 270	A1	

Question	Answer	Marks	Guidance
10	$1.5 = 2 + \cos 3x$ $\cos 3x = -0.5$	M1	For correct attempt to find points of intersection
	$3x = \frac{2\pi}{3}, \frac{4\pi}{3}$	M1	For dealing with $3x$ correctly
	$x = \frac{2\pi}{9}$ or 40°	A1	
	$x = \frac{4\pi}{9}$ or 80°	A1	
	Either $\int_{\frac{2\pi}{9}}^{\frac{4\pi}{9}} 1.5 - (2 + \cos 3x) \, dx$	M1	For subtraction method – condone omission of or incorrect limits
	$\left[-0.5x - k \sin 3x\right]_{\frac{2\pi}{9}}^{\frac{4\pi}{9}}$	M1	For attempt to integrate – condone omission of or incorrect limits
	$\left[-0.5x - \frac{1}{3} \sin 3x\right]_{\frac{2\pi}{9}}^{\frac{4\pi}{9}}$	A1	All correct – condone omission of or incorrect limits
	$\left(-\frac{2\pi}{9} + \frac{\sqrt{3}}{6}\right) - \left(-\frac{\pi}{9} - \frac{\sqrt{3}}{6}\right)$	M1	Dep for application of limits, must be in radians
	$\text{Area} = \frac{\sqrt{3}}{3} - \frac{\pi}{9}$	A1	
	Or $\left(1.5 \times \frac{2\pi}{9}\right)$	M1	For attempt at rectangle (must include subtraction subsequently)
	$\left[2x + k \sin 3x\right]_{\frac{2\pi}{9}}^{\frac{4\pi}{9}}$	M1	For attempt to integrate – condone omission of or incorrect limits
	$\left[2x + \frac{1}{3} \sin 3x\right]_{\frac{2\pi}{9}}^{\frac{4\pi}{9}}$	A1	All correct – condone omission of or incorrect limits
	$\left(\left(\frac{8\pi}{9} - \frac{\sqrt{3}}{6}\right) - \left(\frac{4\pi}{9} + \frac{\sqrt{3}}{6}\right)\right)$	M1	Dep for application of limits, must be in radians
	$\text{Area} = \frac{\sqrt{3}}{3} - \frac{\pi}{9}$	A1	

Question	Answer	Marks	Guidance
11(a)(i)	362 880	B1	
11(a)(ii)	$7! \times 2$	B1	For 7!
	10 080	B1	For $7! \times 2$ leading to 10080
11(a)(iii)	Total = $4! \times 4! \times 3! = 3456$	B3	B1 for treating as 4 separate units 4! B1 for either number of ways of arranging the maths books amongst themselves 4! or the number of ways of arranging the physics books amongst themselves 3!
11(b)(i)	18 564	B1	
11(b)(ii)	Total 3738	B4	B1 4 boys 3150 B1 5 boys 560 B1 6 boys 28
12	$\frac{dy}{dx} = k \cos\left(x + \frac{\pi}{3}\right) + c$	M1	For attempt to integrate
	$\frac{dy}{dx} = -2 \cos\left(x + \frac{\pi}{3}\right) + c$	A1	All correct, condone omission of +c
	$5 = -2 \cos \frac{2\pi}{3} + c$	M1	Dep for attempt to find c
	$\frac{dy}{dx} = -2 \cos\left(x + \frac{\pi}{3}\right) + 4$	A1	
	$y = p \sin\left(x + \frac{\pi}{3}\right) (+qx + d)$	M1	attempt to integrate a second time to obtain $y = p \sin\left(x + \frac{\pi}{3}\right)$
	$y = -2 \sin\left(x + \frac{\pi}{3}\right) + 4x + d$	A1	All correct, condone omission of +d
	$\frac{5\pi}{3} = -2 \sin \frac{2\pi}{3} + \frac{4\pi}{3} + d$	M1	Dep for attempt to find a second arbitrary constant
	$y = -2 \sin\left(x + \frac{\pi}{3}\right) + 4x + \frac{\pi}{3} + \sqrt{3}$ or $y = -2 \sin\left(x + \frac{\pi}{3}\right) + 4x + 2.78$	A1	

ADDITIONAL MATHEMATICS**0606/12**

Paper 1

October/November 2019

MARK SCHEME

Maximum Mark: 80

Published

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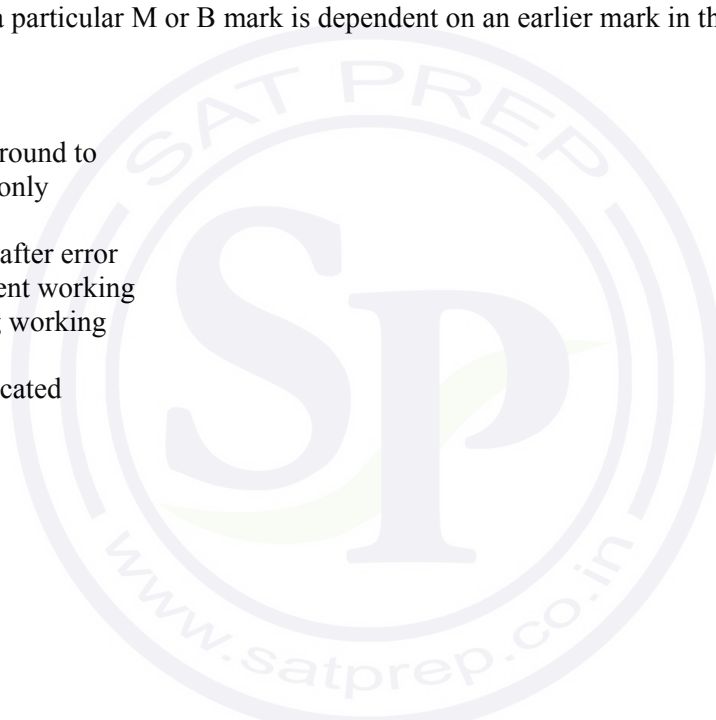
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oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied



Question	Answer	Marks	Guidance
1(i)		B3	B1 for y intercept (0,1), must have a graph B1 for starting and finishing at (±90, -1) B1 for all correct, must be attempt at a curve passing through (±30, -1) and (±60, -3)
1(ii)	2	B1	
1(iii)	120° or $\frac{2\pi}{3}$	B1	
2	$\lg y^2 = mx + c$	B1	May be implied by subsequent work
	Gradient = -4 ($= m$)	B1	
	$c = 32$	B1	
	$y = 10^{\text{their } \frac{c}{2} + \text{their } \frac{mx}{2}}$	M1	Dep on first B1 Use of $\lg y^2 = 2 \lg y$ and $10^{\text{their } \frac{c}{2} + \text{their } \frac{mx}{2}}$ Or use of $y^2 = 10^{(\text{their } c + \text{their } mx)}$ and $10^{\text{their } \frac{c}{2} + \text{their } \frac{mx}{2}}$
	$y = 10^{16-2x}$	A1	
3	$\left(1 - \frac{x}{7}\right)^{14} = 1 - 2x + \frac{13}{7}x^2$	B2	All terms correct or B1 for 2 correct terms
	$(1 - 2x)^4 = 1 - 8x + 24x^2 \dots$	B2	First three terms correct or B1 for one incorrect term
	Product = $1 - 10x + \frac{293}{7}x^2$	M1	For attempt to multiply out to obtain $(1) - 10x + mx^2$, $m \neq 16$
	$a = -10$, $b = \frac{293}{7}$	A1	For both, need to identify a and b
4(i)		B4	B1 for shape, with max in first quadrant B1 for (-0.5, 0) and (5, 0) B1 for (0, 5) B1 all correct, with cusps and correct curvature for $x < 0.5$ and $x > 5$

Question	Answer	Marks	Guidance
4(ii)	$k = 0$	B1	Not from incorrect work
	Stationary point when $y = \pm \frac{121}{8}$ or ± 15.125	M1	For attempt to find y-coordinate of stationary point, must be a complete method i.e. Use of calculus Use of discriminant, Use of completing the square Use of symmetry Allow if seen in part (i), but must be used in (ii)
	$k > \frac{121}{8}$	A1	cao
5a(i)	fg	B1	
5a(ii)	g^{-1}	B1	
5a(iii)	f^{-1}	B1	
5a(iv)	g^2	B1	
5(b)(i)	Undefined at $x = 0$ oe	B1	
5(b)(ii)	$4 = a + b$ $h'(x) = \frac{p}{x^3}$ and attempt at $h'(1)$	M1	For attempt at $h(1)$ and differentiation to obtain $h'(1)$, must have the form $h'(x) = \frac{p}{x^3}$ oe
	$b = -8$ $a = 12$	A1	For both
6(a)	$p^{\frac{7}{2}} q^{\frac{5}{3}} r^{-\frac{7}{3}}$	B3	B1 for each term or for each of $a = \frac{7}{2}$, $b = \frac{5}{3}$, $c = -\frac{7}{3}$

Question	Answer	Marks	Guidance
6(b)	Either $\log_7 x + \frac{2}{\log_7 x} = 3$	M1	For change of base.
	$(\log_7 x)^2 - 3\log_7 x + 2 = 0$ $\log_7 x = 1, \log_7 x = 2$	M1	Dep for forming a 3 term quadratic equation in $\log_7 x$ and a correct attempt to solve
	$x = 7, x = 49$	M1	Dep on both previous M marks for dealing with a base 7 logarithm correctly
		A1	For both
	Or $\frac{1}{\log_x 7} + 2\log_x 7 = 3$	M1	For change of base
	$2(\log_x 7)^2 - 3\log_x 7 + 1 = 0$ $\log_x 7 = 1, \log_x 7 = 0.5$	M1	Dep for forming a 3 term quadratic equation in $\log_x 7$ and a correct attempt to solve
	$x = 7, x = 49$	M1	Dep on both previous M marks for dealing with a base x logarithm correctly
		A1	For both
	Or $\frac{\lg x}{\lg 7} + 2\frac{\lg 7}{\lg x} = 3$ or $\lg 1000$	M1	For change of base
	$(\lg x)^2 - 3\lg 7(\lg x) + 2(\lg 7)^2 = 0$ $\lg x = 2\lg 7 \quad \lg x = \lg 7$	M1	Dep for forming a 3 term quadratic equation in $\lg x$ and a correct attempt to solve
7(i)	$\frac{dy}{dx} = (e^{x^2} + 1) + 2xe^{x^2}(x + 5)$	B1	For $2xe^{x^2}$
		M1	For attempt at differentiating a product or expanding brackets and differentiating a product
		A1	For all other terms, apart from $2xe^{x^2}$, correct

Question	Answer	Marks	Guidance
7(ii)	When $x = 0.5$, $\frac{dy}{dx} = 9.35$	M1	For attempt to find <i>their</i> $\frac{dy}{dx}$ when $x = 0.5$ and multiplication by p
	Approximate change = $9.35p$	A1	
7(iii)	$\frac{dy}{dx} \times \frac{dx}{dt} = \frac{dy}{dt}$ $9.346 \times \frac{dx}{dt} = 2$	M1	For use of correct rates of change equation using <i>their</i> $\frac{dy}{dx}$ when $x = 0.5$ and $\frac{dy}{dt} = 2$
	$\frac{dx}{dt} = 0.214$	A1	FT on $\frac{2}{\text{their } 9.346}$ Must be correct to at least 3 sf
8(a)(i)	Either $\begin{pmatrix} 2 & 1 & 1 \\ 1 & 3 & 0 \\ 1 & 1 & 2 \\ 0 & 1 & 3 \\ 3 & 0 & 1 \end{pmatrix} \begin{pmatrix} 4 \\ 2 \\ 0 \end{pmatrix} \text{ or } \begin{pmatrix} 2 & 1 \\ 1 & 3 \\ 1 & 1 \\ 0 & 1 \\ 3 & 0 \end{pmatrix} \begin{pmatrix} 4 \\ 2 \end{pmatrix}$	B2	For correct matrices in correct order or B1 if one correct matrix and a slip in one element of the other matrix
	Or $(4 \ 2 \ 0) \begin{pmatrix} 2 & 1 & 1 & 0 & 3 \\ 1 & 3 & 1 & 1 & 0 \\ 1 & 0 & 2 & 3 & 1 \end{pmatrix}$ or $(4 \ 2) \begin{pmatrix} 2 & 1 & 1 & 0 & 3 \\ 1 & 3 & 1 & 1 & 0 \end{pmatrix}$	B2	For correct matrices in correct order or B1 if one correct matrix and a slip in one element of the other matrix
8(a)(ii)	$\begin{pmatrix} 10 \\ 10 \\ 6 \\ 2 \\ 12 \end{pmatrix} \text{ or } (10 \ 10 \ 6 \ 2 \ 12)$ Team E	M1	For matrix multiplication of <i>their</i> (i), with at least 2 elements correct, must be in correct form , may be unsimplified
		A1	All correct and identifying team E
8(b)(i)	$\frac{1}{6} \begin{pmatrix} 4 & 1 \\ -2 & 1 \end{pmatrix}$	B2	B1 for $\frac{1}{6}$ and B1 for $\begin{pmatrix} 4 & 1 \\ -2 & 1 \end{pmatrix}$

Question	Answer	Marks	Guidance							
8(b)(ii)	$C = A^{-1}B$	M1	For pre-multiplication by <i>their</i> inverse from (i)							
	$C = \frac{1}{6} \begin{pmatrix} 4 & 1 \\ -2 & 1 \end{pmatrix} \begin{pmatrix} 5 & 0 \\ 1 & -2 \end{pmatrix}$	M1	Dep for matrix multiplication, using <i>their</i> inverse from (i), at least 2 elements correct							
	$= \frac{1}{6} \begin{pmatrix} 21 & -2 \\ -9 & -2 \end{pmatrix}$ oe	A1								
9(i)	$\pi r^2 h = 1200\pi$	B1								
	$h = \frac{1200}{r^2}$ or $\pi r h = \frac{1200\pi}{r}$ and substitution into <i>their</i> S	B1	Must have attempt to use in an equation for S							
	$S = 2\pi r^2 + \left(2\pi r \times \frac{1200}{r^2}\right)$ leading to given answer	B1								
9(ii)	$\frac{dS}{dr} = 4\pi r - \frac{2400\pi}{r^2}$	M1	Must obtain the form $Ar + \frac{B}{r^2}$							
	When $\frac{dS}{dr} = 0$, $r = \sqrt[3]{600}$, 8.43	M1	Dep for equating to zero and attempt to solve to obtain $r = \dots$							
		A1	For correct r							
	$S_{\min} = 1340$ or 1341	A1								
	Either $\frac{d^2S}{dr^2} = 4\pi + \frac{4800\pi}{r^3}$ $\frac{d^2S}{dr^2} > 0$ so minimum	B1	For a correct method to reach a correct conclusion If r is not calculated, then must state that $r > 0$							
	Or Consideration of gradient e.g. <table border="1"> <tr> <td>r</td><td>< 8.43</td><td>8.43</td><td>> 8.43</td></tr> <tr> <td>$\frac{dS}{dr}$</td><td>–</td><td>0</td><td>+</td></tr> </table> Minimum point	r	< 8.43	8.43	> 8.43	$\frac{dS}{dr}$	–	0	+	B1
r	< 8.43	8.43	> 8.43							
$\frac{dS}{dr}$	–	0	+							

Question	Answer	Marks	Guidance
10(i)	Either $18^2 = 10^2 + 10^2 - 200 \cos AOB$	M1	Attempt to use cosine rule
	$\cos AOB = -0.62$	A1	Allow unsimplified
	$AOB = 2.2395$ or greater accuracy, so 2.24 (to 2 dp) or $AOB = 2.239\dots$ so 2.24 (to 2 dp) $AOB = 2.240$ so 2.24 (to 2 dp)	A1	Must justify 2 dp
10(i)	Or $\sin \frac{AOB}{2} = \frac{9}{10}$ or $\tan \frac{AOB}{2} = \frac{9}{\sqrt{19}}$ or $\cos \frac{AOB}{2} = \frac{\sqrt{19}}{10}$	M1	Attempt at trig using a right angled triangle
	$\frac{AOB}{2} = \text{awrt } 1.12$	A1	
	$AOB = 2.2395$ or greater accuracy, so 2.24 (to 2 dp) or $AOB = 2.239\dots$ so 2.24 (to 2 dp) $AOB = 2.240$ so 2.24 (to 2 dp)	A1	Must justify 2 dp
10(ii)	$AOC = 2\pi - 2(2.2395)$ or $\frac{AOC}{2}$ or $ABC = \pi - (2.2395)$ oe	M1	For attempt to find angle AOC or ABC $AOC = 2\pi - 2(\text{their } AOB)$ $ABC = \pi - (\text{their } AOB)$ oe
	$AOC = 1.804$ or 1.803	A1	Condone 1.8 or 1.80
	Arc length = 18.04 or 18.03	M1	For attempt at arc length using $10 \times \text{their } AOC$
	$AC = 20 \sin \frac{AOC}{2}$ or $36 \sin \frac{ABC}{2}$ or $\sqrt{10^2 + 10^2 - 200 \cos AOC}$ or $\sqrt{18^2 + 18^2 - 648 \cos ABC}$ = 15.69 or 15.7	M1	For attempt at AC using $\text{their } AOC$, or ABC but $AOC \neq 2.24$ or $\frac{2\pi}{3}$
	Perimeter = 33.7	A1	Allow awrt 33.7

Question	Answer	Marks	Guidance
10(iii)	Area of sector = 50×1.804 = 90.2 or 90.15	M1	For attempt at sector area $\frac{1}{2} \times 10^2 \times \text{their } AOC$ AOC must be in radians
	Area of triangle = $50 \sin 1.804 = 48.6$ or 48.66	M1	For attempt at area of triangle $\frac{1}{2} \times 10^2 \times \sin \text{their } AOC$ AOC must be in radians
	Shaded area = 41.6 or 41.5	A1	Lack of accuracy is penalised here
11	$\frac{dy}{dx} = 2(3x-1)^{\frac{1}{3}} + c$	M1	For $\left(\frac{dy}{dx} = \right) a(3x-1)^{\frac{1}{3}}$, condone omission of $+ c$
		A1	All correct, condone omission of c
	$6 = 4 + c$	M1	Dep for attempt to find c
	$\left(\frac{dy}{dx} = \right) 2(3x-1)^{\frac{1}{3}} + 2$	A1	All correct, may be implied by $c = 2$
	$y = \frac{1}{2}(3x-1)^{\frac{4}{3}} + 2x + d$	M1	For attempt to integrate <i>their</i> $\frac{dy}{dx}$ to obtain the form $y = b(3x-1)^{\frac{4}{3}} (+mx + d)$
		A1	All correct, condone omission of d
	$11 = 14 + d$	M1	Dep for attempt to find d , a second arbitrary constant, having used an arbitrary constant for $\frac{dy}{dx}$
	$y = \frac{1}{2}(3x-1)^{\frac{4}{3}} + 2x - 3$	A1	

ADDITIONAL MATHEMATICS**0606/13**

Paper 1

October/November 2019

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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This document consists of **9** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

M Method marks, awarded for a valid method applied to the problem.

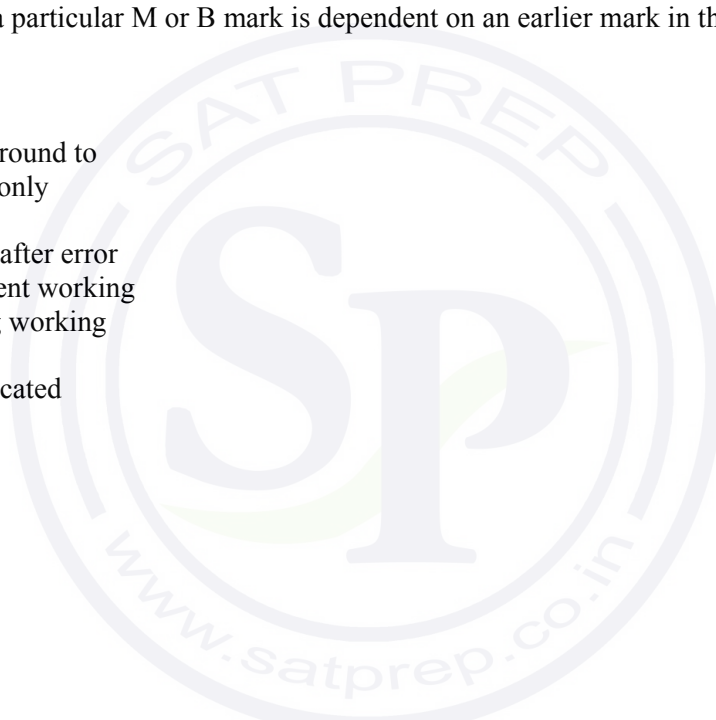
A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.


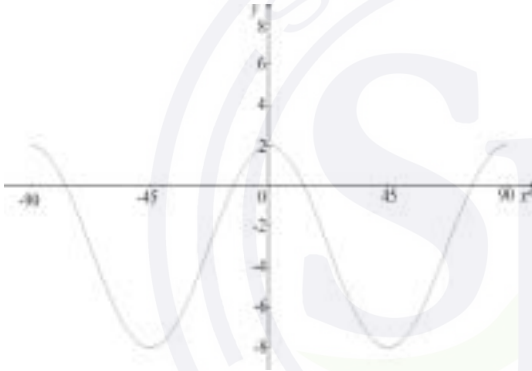
B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

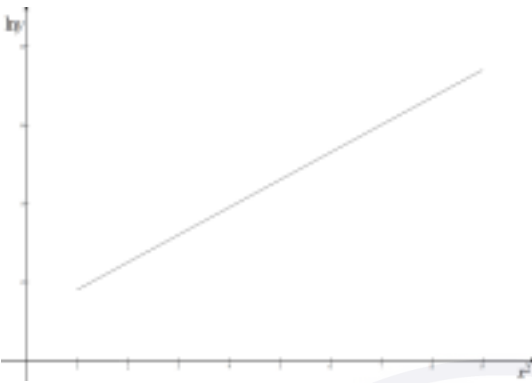
Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied



Question	Answer	Marks	Guidance
1(i)		M1	for a Venn diagram showing at least 4 correct 'parts' in terms of x
		A1	for all 7 'parts' correct in terms of x on a Venn diagram or in working. May be implied by a correct equation.
	$80 + 24 + x + 23 - x + 3 + x = 145$ $50 + 28 + x + 28 - x + 24 + x = 145$ $75 + 28 + x + 24 - x + 3 + x = 145$ $50 + 80 + 75 - (23 + 28 + 24) + x = 145$ or equivalents	M1	for forming an equation in x using sum of 'parts' = 145 or $50 + 80 + 75 - (23 + 28 + 24) + x = 145$ Equations must be seen
	$x = 15$	A1	from correct working only
1(ii)	43	B1ft	for <i>their</i> x plus 28
2(i)		B4	B1 for a maximum at $(0, 2)$ B1 for minimums at $y = -8$ and no other minimums B1 for starting at $(-90^\circ, 2)$ and finishing at $(90^\circ, 2)$ B1 for a fully correct curve with correct shape, particularly at end points, that has earned all three previous B marks.
2(ii)	5	B1	
2(iii)	90°	B1	
3(i)	$\frac{dy}{dx} = kx(3x^2 - 1)^{\frac{4}{3}}$	M1	
	$\frac{dy}{dx} = -\frac{1}{3} \times 6x(3x^2 - 1)^{\frac{4}{3}}$	A1	
3(ii)	When $x = \sqrt{3}$, $\frac{dy}{dx} = -\frac{\sqrt{3}}{8}$ $-\frac{\sqrt{3}}{8}p$ or $-0.217p$	B1	FT on <i>their</i> $\frac{dy}{dx}$ of the form $kx(3x^2 - 1)^{\frac{4}{3}}$

Question	Answer	Marks	Guidance
3(iii)	When $x = \sqrt{3}$, $y = \frac{1}{2}$	B1	for $y = \frac{1}{2}$
	Normal: $y - \frac{1}{2} = \frac{8}{\sqrt{3}}(x - \sqrt{3})$	M1	Dep on M1 in part(i). An equation of the normal using <i>their</i> normal gradient, $\sqrt{3}$ and <i>their</i> y
		A1	allow unsimplified
4(i)	$-\frac{1}{13} \begin{pmatrix} -1 & -2 \\ -4 & 5 \end{pmatrix}$ oe	B2	B1 for $-\frac{1}{13}$ B1 for $\begin{pmatrix} -1 & -2 \\ -4 & 5 \end{pmatrix}$
4(ii)	$\frac{1}{13} \begin{pmatrix} 1 & 2 \\ 4 & -5 \end{pmatrix} \begin{pmatrix} 12 \\ 7 \end{pmatrix}$	M1	for pre-multiplication by <i>their</i> inverse from (i)
	$= \frac{1}{13} \begin{pmatrix} 26 \\ 13 \end{pmatrix}$	M1	for correct method for matrix multiplication
	$= \begin{pmatrix} 2 \\ 1 \end{pmatrix}$	A1	
	$x = 1.11$	B1	
	$y = \frac{\pi}{4}$ or 0.785	B1	
5(i)	$\frac{d}{dx}(\ln(x^2 + 3)) = \frac{2x}{(x^2 + 3)}$	B1	
	$\frac{dy}{dx} = (x^2 + 3) \frac{2x}{(x^2 + 3)} + 2x \ln(x^2 + 3)$	M1	for product rule
		A1	FT <i>their</i> $\frac{2x}{(x^2 + 3)}$
5(ii)	$(x^2 + 3) \ln(x^2 + 3) = \int 2x + 2x \ln(x^2 + 3) dx$	M1	for using <i>their</i> result from (i) for $2x + kx \ln(x^2 + 3)$
	$\int x \ln(x^2 + 3) dx$ $= \frac{1}{2}(x^2 + 3) \ln(x^2 + 3) - \frac{x^2}{2} (+c)$	A1	

Question	Answer	Marks	Guidance
6(i)	$\ln y = \ln A + x^2 \ln b$ or $\lg y = \lg A + x^2 \lg b$	B1	May be implied by a table of values for x^2 and $\ln y$ or $\lg y$ or axes labelled $\ln y$ or $\lg y$ and x^2
		M1	for attempt to plot either $\ln y$ or $\lg y$ against x^2 using an evenly spaced scale on each axis.
		A2	A2 All points on a correct line (for $1 \leq x^2 \leq 9$) with axes correctly labelled A1 One point not on the correct line or a correct line with axes not correctly labelled. A0 Two or more points not on the correct line or one point not on the line and axes incorrect
6(ii)	Gradient = $\ln b$ or $\lg b$ $\ln b \approx 0.7$ or $\lg b \approx 0.3$ leading to	M1	for a complete method using the gradient of <i>their</i> straight-line graph of $\lg y$ or $\ln y$ against x^2 to obtain b
	$b = 2$ (allow 1.6 – 2.4)	A1	from correct working
	Intercept = $\ln A$ or $\lg A$ $\ln A \approx 1.1$ $\lg A \approx 0.5$ leading to	M1	for a complete method using intercept of <i>their</i> straight-line graph of $\lg y$ or $\ln y$ against x^2 to find A
	$A = 3$ (allow 2.5 – 3.6)	A1	from correct working
6(iii)	$100 = 3(2^{x^2})$ or $\ln 100 = \text{their } 1.1 + \text{their } 0.7x^2$ or $\lg 100 = \text{their } 0.5 + \text{their } 0.3x^2$ or reading from $\lg y = 2$ to obtain x^2 or from $\ln y = 4.6$ to obtain x^2	M1	for a valid method to find x^2 Substitution methods should be using values of A and b in range
	leading to $x = 2.25$ (allow 2.0 – 2.7)	A1	for an answer in range from correct working
7(a)(i)	15 120	B1	
7(a)(ii)	1680	B1	
7(a)(iii) Method 1	Total = 2310	B3	B1 1st digit is 7 or 9 1680 or 210×8 B1 1st digit is 8 630 or 210×3
7(a)(iii) Method 2	Total = 2310	B3	B1 for 5th digit is 2, 4 or 6 1890 or 210×9 B1 for 5th digit is 8 420 or 210×2

Question	Answer	Marks	Guidance
7(b)(i)	3003	B1	
7(b)(ii)	28	B1	
7(b)(iii)	Total 1419	B3	B1 Including husband and wife 495 B1 Excluding husband and wife 924
8(a)(i)	$\log_a a + 2\log_a y + \log_a x$	M1	for $\log_a a + \log_a x + \log_a y^2$ and $\log_a y^2 = 2\log_a y$
	$1 + 2q + p$	A1	
8(a)(ii)	$3\log_a x - \log_a y - \log_a a$	M1	for $\log_a x^3 - (\log_a a + \log_a y)$ and $\log_a x^3 = 3\log_a x$
	$3p - q - 1$ or $3p - (q + 1)$	A1	
8(a)(iii)	$\frac{1}{p} + \frac{1}{q}$	B1	
8(b)	$m - 3m^2 + 4 = 0$ $m = \frac{4}{3}, (-1)$ $x = \frac{\lg \frac{4}{3}}{\lg 3}, x = \frac{\ln \frac{4}{3}}{\ln 3}$ or $\lg_3 \frac{4}{3}$	M1	for obtaining a quadratic in m or 3^x
		M1	Dep for attempt to solve quadratic and deal with 3^x correctly
	$x = 0.262$ only	A1	
9(i)	$100 = 2r + 2r\theta + 3r\theta$	M1	for addition of $2r$ and two arc lengths with at least one correct arc length
	$\theta = \frac{100 - 2r}{5r}$ or $\frac{20}{r} - \frac{2}{5}$ oe	A1	
9(ii)	$\frac{1}{2}9r^2\theta - \frac{1}{2}4r^2\theta$	M1	for subtraction of two sector areas with at least one sector area correct.
	$\frac{5r^2}{2} \left(\frac{100 - 2r}{5r} \right)$	A1	Must expand and simplify to obtain given answer $50r - r^2$
9(iii)	$\frac{dA}{dr} = 50 - 2r$ $0 = 50 - 2r$ leading to $r = 25$	M1	for differentiation and equating to zero and obtaining r or for using completing the square $-(25 - r)^2 + 25^2$
	Max when $A = 625$	A1	

Question	Answer	Marks	Guidance
9(iv)	When $r = 10$, $\frac{dA}{dr} = 30$	B1	
	$\frac{dr}{dt} = \frac{3}{30}$	M1	for $\frac{dr}{dt} = \frac{3}{\text{their } 30}$ where <i>their</i> 30 has been obtained from an evaluation of $\frac{dA}{dr}$ at $r = 10$
	$\frac{dr}{dt} = 0.1$ or $\frac{1}{10}$	A1	
9(v)	$\frac{d\theta}{dr} = -\frac{20}{r^2}$ oe	B1	
	$\frac{d\theta}{dr} = -\frac{1}{5}$ oe $\frac{d\theta}{dt} = \frac{1}{10} \times -\frac{1}{5}$ oe	M1	for <i>their</i> $\frac{dr}{dt} \times \text{their } \frac{d\theta}{dr}$ with both evaluated at $r = 10$
	$\frac{d\theta}{dt} = -\frac{1}{50}$ or -0.02	A1	
10(a)(i)	$\pm \frac{20 - -20}{5}$	M1	for finding the gradient of the relevant part
	8	A1	
10(a)(ii)	7.5	B1	
10(a)(iii)	$\frac{1}{2}(5 + 7.5)20 + \left(\frac{1}{2} \times 2.5 \times 20\right)$ or $20 \times 5 + \left(\frac{1}{2} \times 2.5 \times 20\right) + \left(\frac{1}{2} \times 2.5 \times 20\right)$ oe	M1	for a correct expression for total area using <i>their</i> 7.5
	150	A1	
10(b)(i)	$x = 3e^{2t} + t + c$	M1	for $ke^{2t} + t$ Condone omission of c
	$0 = 3e^0 + 0 + c$ When $t = 0$, $x = 0$ so $c = -3$	M1	Dep for substitution to find c
	$x = 3e^{2t} + t - 3$	A1	

Question	Answer	Marks	Guidance
10(b)(ii)	$\frac{dv}{dt} = 12e^{2t}$ so $12e^{2t} = 24$	M1	for ke^{2t} equated to 24
	$2t = \ln 2$	M1	Dep for correct order of operations to obtain $2t$
	$t = \frac{1}{2} \ln 2$, $\ln \sqrt{2}$ or 0.347	A1	



ADDITIONAL MATHEMATICS**0606/11**

Paper 1

May/June 2019

MARK SCHEME

Maximum Mark: 80

Published

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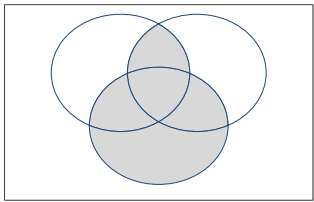
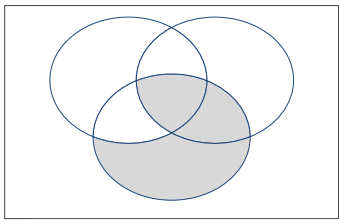
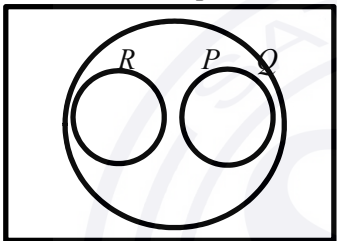
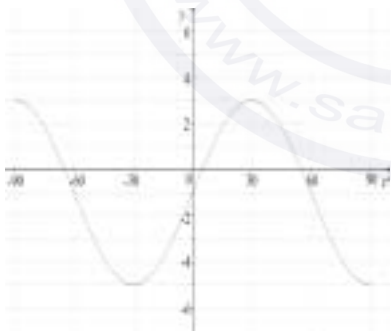
Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
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When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(a)		B1	
		B1	
1(b)		B2	B1 for $P \subset R$ and $Q \subset R$ B1 for $P \cap Q = \emptyset$
2(i)	4	B1	
2(ii)	120° or $\frac{2\pi}{3}$	B1	
2(iii)		B3	B1 for a complete curve starting at $(-90^\circ, 3)$ and finishing at $(90^\circ, -5)$ B1 for $-5 \leq y \leq 3$ for a complete curve Minimum point(s) at $y = -5$ Maximum point(s) at $y = 3$ DepB1 for a fully correct sine curve satisfying both the above and passing through $(-60^\circ, -1)$, $(0^\circ, -1)$ and $(60^\circ, -1)$
3(i)	-12	B1	
3(ii)	$(2 \times -3 - 1)(k - 3) - 12 = 23$ oe or $2(-3)^2 + (2k - 1)(-3) - k - 12 = 23$	M1	
	$k = -2$	A1	

Question	Answer	Marks	Guidance
3(iii)	$(2x-1)(x-2)-12=-25$ $2x^2-5x+15=0$	M1	expansion and simplification to a 3 term quadratic equation equated to zero, using <i>their k</i> .
	Discriminant: $25-(4 \times 2 \times 15)$ $=-95$	M1	using discriminant for their three term quadratic equation
	which is < 0 so no real solutions	A1	cao for correct discriminant and correct conclusion
4(i)	$a = 256$	B1	
	$8 \times 2^7 \times bx [= 256x]$ oe or $\frac{8 \times 7 \times 2^6 \times (bx)^2}{2} [= cx^2]$ oe	M1	
	$b = \frac{1}{4}$ oe, $c = 112$	A2	A1 for each
4(ii)	$(256 + 256x + 112x^2) \left(4x^2 - 12 + \frac{9}{x^2} \right)$	B1	for $\left(4x^2 - 12 + \frac{9}{x^2} \right)$
	Terms independent of x are $(256 \times (-12)) + (112 \times 9)$ $= -3072 + 1008$	M1	adding and selecting (<i>their</i> $256 \times \text{their } (-12)$) + (<i>their</i> $112 \times \text{their } 9$)
	$= -2064$	A1	
5(i)	$v = 20 \times \frac{1}{\sqrt{3^2 + 4^2}} \begin{pmatrix} 3 \\ 4 \end{pmatrix}$ oe	M1	finding and using the magnitude of $\begin{pmatrix} 3 \\ 4 \end{pmatrix}$
	$v = \begin{pmatrix} 12 \\ 16 \end{pmatrix}$	A1	
5(ii)	$\mathbf{r}_p = \begin{pmatrix} 1 \\ 2 \end{pmatrix} + \begin{pmatrix} 12 \\ 16 \end{pmatrix} t$	M1	correct use of position vector and <i>their</i> velocity vector
		A1	

Question	Answer	Marks	Guidance
5(iii)	$\begin{pmatrix} 17 \\ 18 \end{pmatrix} + \begin{pmatrix} 8 \\ 12 \end{pmatrix} t = \begin{pmatrix} 1 \\ 2 \end{pmatrix} + \begin{pmatrix} 12 \\ 16 \end{pmatrix} t$ <p>Leading to $17 + 8t = 1 + 12t$ or $18 + 12t = 2 + 16t$</p>	M1	equating position vectors of both particles at time t and solve either equation for t
	$t = 4$	A1	
	Position vector of collision $\begin{pmatrix} 49 \\ 66 \end{pmatrix}$	A1	
6	<u>Method 1</u> $3x^2 - 2x + 1 = 2x + 5$ leading to	M1	equating the equations of the line and the curve and rearranging to obtain a three term quadratic equated to zero
	$3x^2 - 4x - 4 = 0$	A1	
	$x = -\frac{2}{3}$ and $x = 2$	A1	
	$\int_{-\frac{2}{3}}^2 (2x + 5 - (3x^2 - 2x + 1)) \, dx$	M1	subtraction (either way round)
	$\int_{-\frac{2}{3}}^2 (4 + 4x - 3x^2) \, dx$	M1	integration to $Ax + Bx^2 + Cx^3$
	$\left[4x + 2x^2 - x^3 \right]_{-\frac{2}{3}}^2$	A1	for $4x + 2x^2 - x^3$ oe
	$(8 + 8 - 8) - \left(-\frac{8}{3} + \frac{8}{9} + \frac{8}{27} \right)$ $= 8 - \frac{40}{27}$	M1	Dep on preceding M1 correct use of limits
	$= \frac{256}{27}$ or 9.48 or $9\frac{13}{27}$	A1	

Question	Answer	Marks	Guidance
6	<u>Method 2</u> $3x^2 - 2x + 1 = 2x + 5$ leading to	M1	equating the line and the curve and rearranging to obtain a three term quadratic equated to zero
	$3x^2 - 4x - 4 = 0$	A1	
	$x = -\frac{2}{3}$ and $x = 2$	A1	
	Area of trapezium = $\frac{1}{2}\left(\frac{11}{3} + 9\right) \times \frac{8}{3}$	B1	area of the trapezium, allow unsimplified
	Area under curve = $\int_{-\frac{2}{3}}^2 3x^2 - 2x + 1 \, dx$	M1	integration to $Ax + Bx^2 + Cx^3$
	$= \left[x^3 - x^2 + x \right]_{-\frac{2}{3}}^2$	A1	for $x^3 - x^2 + x$
	$= \left((8 - 4 + 2) - \left(-\frac{8}{27} - \frac{4}{9} - \frac{2}{3} \right) \right)$ $6 - -\frac{38}{27}$	M1	DepM1 for correct use of limits.
	Shaded Area = $\frac{152}{9} - \frac{200}{27}$ $= \frac{256}{27}$ or 9.48 or $9\frac{13}{27}$	A1	
7(a)	<u>Method 1</u> $\log_3 x + \frac{\log_3 x}{\log_3 9} = 12$	B1	change to base 3 logarithm
	$\frac{3\log_3 x}{2} = 12$ $x = 3^8$ or $\sqrt[3]{3^{24}}$	M1	simplification and dealing with base 3 logarithms to obtain a power of 3
	$x = 6561$	A1	

Question	Answer	Marks	Guidance
7(a)	<u>Method 2</u> $\frac{\log_9 x}{\log_9 3} + \log_9 x = 12$	B1	change to base 9
	$3 \log_9 x = 12$ $x = 9^4$ or $\sqrt[3]{9^{12}}$	M1	simplification and dealing with base 9 logarithms to obtain a power of 9
	$x = 6561$	A1	
7(b)	<u>Method 1</u> $\log_4 (3y^2 - 10) = \log_4 (y - 1)^2 + \frac{1}{2}$	B1	use of power rule
	$\log_4 \frac{3y^2 - 10}{(y - 1)^2} = \frac{1}{2}$	B1	DepB1 for use of division rule
	$\frac{3y^2 - 10}{(y - 1)^2} = 2$	B1	for $\frac{1}{2} = \log_4 2$
	$y^2 + 4y - 12 = 0$	M1	Dep on first two B marks simplification to a three term quadratic.
	$y = 2$ only	A1	
7(b)	<u>Method 2</u> $\log_4 (3y^2 - 10) = \log_4 (y - 1)^2 + \frac{1}{2}$	B1	use of power rule
	$\log_4 (3y^2 - 10) = \log_4 (y - 1)^2 + \log_4 2$	B1	for $\log_4 2$
	$3y^2 - 10 = 2(y - 1)^2$	B1	Dep on first B1 use of the multiplication rule
	$y^2 + 4y - 12 = 0$	M1	Dep on first and third B marks. simplification to a 3 term quadratic
	$y = 2$ only	A1	

Question	Answer	Marks	Guidance
8(i)	$f > -1$	B1	or $f(x) > -1$, $y > -1$, $(-1, \infty)$, $\{y: y > -1\}$
8(ii)	$e^y = \frac{x+1}{5}$ oe	M1	a complete valid method to obtain the inverse function
	$y = \ln\left(\frac{x+1}{5}\right)$ or $f^{-1}(x) = \ln\left(\frac{x+1}{5}\right)$ oe	A1	
	Domain $x > -1$ or $(-1, \infty)$	B1	FT <i>their (i)</i> or correct
8(iii)	$g(1) = 5$ so $fg(1) = f(5)$	M1	evaluation using correct order of operations
	$5e^5 - 1 = 741$	A1	awrt 741 or $5e^5 - 1$
8(iv)	$g^2(x) = (x^2 + 4)^2 + 4$	M1	correct use of g^2
	$x^4 + 8x^2 + 16 + 4 = 40$ $(x^2 + 4)^2 = 36$ or $x^4 + 8x^2 - 20 = 0$ $(x^2 + 10)(x^2 - 2) = 0$	M1	DepM1 for forming and solving a quadratic in x^2
	$x = \pm\sqrt{2}$ only	A1	
9(i)	<u>Method 1</u> $600\pi = 2\pi r^2 + 2\pi r h$	B1	
	$h = \frac{600\pi - 2\pi r^2}{2\pi r}$	M1	making h subject from a two term expression for SA.
	$V = \pi r^2 h$ $V = \pi r^2 \left(\frac{600\pi - 2\pi r^2}{2\pi r} \right)$ $V = \pi r^2 \left(\frac{300}{r} - r \right)$ $V = 300\pi r - \pi r^3$	A1	correct substitution and manipulation to obtain given answer

Question	Answer	Marks	Guidance
9(i)	<u>Method 2</u> $600\pi = 2\pi r^2 + 2\pi rh$	B1	
	$600\pi r = 2\pi r^3 + 2\pi r^2 h$	M1	multiplying both sides by r
	$\frac{600\pi r - 2\pi r^3}{2} = \pi r^2 h$ $V = \pi r^2 h$ $V = 300\pi r - \pi r^3$	A1	correct manipulation to obtain $\pi r^2 h$
9(ii)	$\frac{dV}{dr} = 300\pi - 3\pi r^2$	M1	differentiation of given formula to $A + Br^2$
	When $\frac{dV}{dr} = 300\pi - 3\pi r^2 = 0$	M1	equating to zero and attempt to solve
	$r = 10$	A1	
	$V = 2000\pi$ or 6280 or 6283	A1	
	$\frac{d^2V}{dr^2} = -6\pi r$, $\frac{d^2V}{dr^2} < 0$ so maximum	B1	cao for $\frac{d^2V}{dr^2} = -6\pi r$, $\frac{d^2V}{dr^2} = -60\pi$ or other correct method leading to maximum
10(i)	<u>Method 1</u> $\lg y = A + Bx^2$	B1	statement soi
	$16 = A + 6B$ $4 = A + 2B$	M1	one correct equation
	leading to $A = -2$ and $B = 3$	A2	A1 for each
10(ii)	<u>Method 2</u> $\lg y = A + Bx^2$	B1	statement soi
	Gradient = B $B = 3$	B1	
	$16 = A + 6B$ or $4 = A + 2B$	M1	a correct equation
	$A = -2$	A1	

Question	Answer	Marks	Guidance
10(i)	<u>Method 3</u> $\lg y - 4 = 3(x^2 - 2)$ or $\lg y - 16 = 3(x^2 - 6)$ OR $4 = 3(2) + c$ or $16 = 3(6) + c$	M1	correct equation or for correct method for finding constant.
	$\lg y = A + Bx^2$	B1	statement soi by <i>their</i> A and B
	Hence $y = 10^{3x^2-2}$ $B = 3$	B1	
	$A = -2$	A1	
10(ii)	$y = 10^{-2+3\left(\frac{1}{\sqrt{3}}\right)^2}$	M1	correct use of <i>their</i> A and B
	$y = 0.1$ oe	A1	
10(iii)	$2 = 10^{3x^2-2}$	M1	correct use of <i>their</i> A and B
	$\lg 2 = 3x^2 - 2$ $x = \sqrt{\frac{\lg 2 + 2}{3}}$	M1	complete correct method to solve for x
	$x = 0.876$	A1	

Question	Answer	Marks	Guidance
11(i)	$\frac{dy}{dx} = (x^2 + 1)(2x - 3)^{-\frac{1}{2}} + 2x(2x - 3)^{\frac{1}{2}}$	M1	differentiation of a product
		B1	for $\frac{d}{dx}(2x - 3)^{\frac{1}{2}} = \frac{1}{2} \times 2(2x - 3)^{-\frac{1}{2}}$ oe
		A1	all else correct i.e. $\frac{dy}{dx} = (x^2 + 1)f(x) + 2x(2x - 3)^{\frac{1}{2}}$
	$= (2x - 3)^{-\frac{1}{2}}(x^2 + 1 + 2x(2x - 3))$	M1	correctly taking out a factor of $(2x - 3)^{-\frac{1}{2}}$ or correctly using $(2x - 3)^{\frac{1}{2}}$ as denominator
	$= \frac{5x^2 - 6x + 1}{(2x - 3)^{\frac{1}{2}}}$	A1	
11(ii)	When $x = 2$, $y = 5$	B1	
	$\frac{dy}{dx} = 9$, so gradient of normal $= -\frac{1}{9}$	M1	substitution to obtain gradient and correct method for gradient of normal
	Equation of normal $y - 5 = -\frac{1}{9}(x - 2)$	M1	DepM1 for equation of normal
	$x + 9y - 47 = 0$ or $-x - 9y + 47 = 0$	A1	Must be in this form

ADDITIONAL MATHEMATICS**0606/12**

Paper 1

May/June 2019

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the May/June 2019 series for most Cambridge IGCSE™, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

This document consists of **11** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

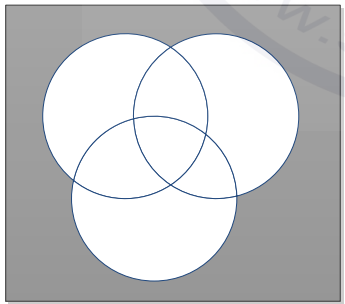
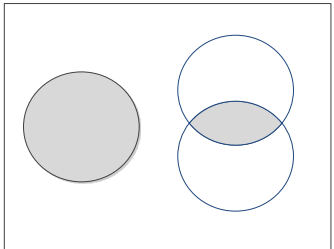
Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

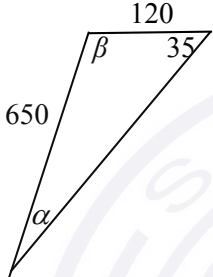
awrt	answers which round to
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FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(a)		B1	
		B1	

Question	Answer	Marks	Guidance
1(b)	$P = \{30^\circ, 150^\circ, 210^\circ, 330^\circ\}$	B1	May be seen or implied in a Venn diagram Allow without set notation
	$Q = \{30^\circ, 150^\circ\}$	B1	May be seen or implied in a Venn diagram Allow without set notation
	$P \cap Q = \{30^\circ, 150^\circ\}$	B1	Dep on both previous B marks Must be in set notation
2	Either: $(2x+3)^2(x-1) = 3(2x+3)$ $(2x+3)(2x^2+x-6) (=0)$	M1	For attempt to equate line and curve and attempt to simplify to $2x+3 \times$ a quadratic factor or cancelling $2x+3$ and obtaining a quadratic factor
	$(2x+3)(2x^2+x-6) = 0$ $(2x+3)(2x-3)(x+2) = 0$	M1	Dep for attempt at 3 linear factors from a linear term and a quadratic term
	$\left(-\frac{3}{2}, 0\right)$	B1	
	$\left(\frac{3}{2}, 18\right)$	A1	Dep on first M mark only
	$(-2, -3)$	A1	Dep on first M mark only
	Or: $(2x+3)^2(x-1) = 3(2x+3)$ $4x^3 + 8x^2 - 9x - 18 (=0)$	M1	For attempt to equate line and curve and attempt to simplify to a cubic equation, by collecting like terms
	$(x+2)(4x^2-9)$ $(2x-3)(2x^2+7x+6)$ $(2x+3)(2x^2+x-6)$ $(2x+3)(2x-3)(x+2) (=0)$	M1	Dep For attempt to find a factor from a 4 term cubic equation (usually $x+2$), do long division or to obtain a quadratic factor and factorise this quadratic factor
	$\left(-\frac{3}{2}, 0\right)$	A1	
	$\left(\frac{3}{2}, 18\right)$	A1	
	$(-2, -3)$	A1	
3(i)	1000	B1	

Question	Answer	Marks	Guidance
3(ii)	$\frac{dB}{dt} = 400e^{2t} - 1600e^{-2t}$	B1	
	$3 = e^{2t} - 4e^{-2t}$ oe	M1	For equating an equation of the form $ae^{2t} + be^{-2t}$ to 1200 and dividing by 400
	$e^{4t} - 3e^{2t} - 4 = 0$	A1	
3(iii)	$(e^{2t} + 1)(e^{2t} - 4) = 0$	M1	For attempt to factorise and solve, dealing with exponential correctly, to obtain $e^{2t} = \dots$
	$t = \ln 2, \frac{1}{2} \ln 4$ or awrt 0.693 only isw if appropriate	A1	
4(a)	$a = \frac{5}{2}$	B1	
	$b = -\frac{3}{2}$	B1	
	$c = \frac{11}{2}$	B1	
4(b)	$9x^{\frac{1}{2}} - 3y^{\frac{1}{2}} = 12$ $4x^{\frac{1}{2}} + 3y^{\frac{1}{2}} = 14$	M1	For attempt to solve simultaneous equations. Must reach $kx^{\frac{1}{2}} = \dots$ or $ky^{\frac{1}{2}} = \dots$ oe
	$x = 4$	A1	
	$y = \frac{1}{4}$	A1	
5(i)	$9.6 = 12\theta$	M1	For use of arc length
	$\theta = 0.8$	A1	

Question	Answer	Marks	Guidance
5(ii)	Either $\tan \theta = \frac{AB}{12}, \quad (AB = 12.36)$ Or $OB = \frac{12}{\cos \theta} \quad (OB = 17.22)$	M1	For attempt to find AB or OB using <i>their</i> θ May be implied by a correct triangle area Allow if using degrees consistently
	Either $\text{Area } \triangle OAB = \frac{1}{2} \times 12 \times \text{their } 12.36$ Or $\text{Area } \triangle OAB = \frac{1}{2} \times 12 \times \text{their } 17.22 \times \sin \theta$ $(= 74.1 \text{ or } 74.2)$	M1	Allow if using degrees consistently For attempt to find area of triangle using <i>their</i> θ
	$\text{Area of sector } OAC = \frac{1}{2} \times 12^2 \times 0.8$ $= 57.6$	B1	Allow unsimplified
	Area of shaded region = 16.5 or 16.6	A1	
6(a)(i)	40320	B1	
6(a)(ii)	No. of ways with maths books as 1 unit = $5!$ or $5 \times 4!$ or 5P_5 or 120	B1	
	No. of ways maths books can be arranged amongst themselves = $4!$ or 4P_4 or 24	B1	
	Total = $(5! \times 4! \text{ oe}) = 2880$	B1	
6(a)(iii)	No. of ways with maths books as 1 unit and geography books as 1 unit = $3!$ or 3P_3 or $3 \times 2!$ or 6	B1	
	No. of ways maths books can be arranged amongst themselves and geography books can be arranged amongst themselves $= 4! \times 3!$ or ${}^4P_4 \times {}^3P_3$ or 144	B1	
	Total = $(3! \times 4! \times 3! \text{ oe})$ $= 864$	B1	
6(b)(i)	${}^{12}C_6 = 924$	B1	

Question	Answer	Marks	Guidance
6(b)(ii)	Either: $924 - {}^8C_6$	M1	For <i>their</i> (i) – the number of teams of just men
	Total = 896	A1	
	Or: $5M\ 1W : {}^8C_5 \times {}^4C_1 \quad (= 224)$ $4M\ 2W : {}^8C_4 \times {}^4C_2 \quad (= 420)$ $3M\ 3W : {}^8C_3 \times {}^4C_3 \quad (= 224)$ $2M\ 4W : {}^8C_2 \times {}^4C_4 \quad (= 28)$	M1	For a complete method
	Total = 896	A1	
7(i)		B1	For correct triangle, may be implied by a correct sine rule or cosine rule.
	$\frac{120}{\sin \alpha}$ or $\frac{120}{\sin(55 - \theta)} = \frac{650}{\sin 35}$ or $\frac{650}{\sin 145}$	M1	For use of a correct sine rule to obtain $\alpha = \dots$ or $\theta = \dots$ Or for a correct cosine rule leading to a value for v , followed by a correct sine rule leading to one of the other angles
	$\alpha = 6.08^\circ$ or $\beta = 138.9$	A1	May be implied by a correct $\theta = \text{awrt } 49^\circ$
	Bearing is 048.9° or 049°	A1	
7(ii)	Either $\frac{v_r}{\sin(145 - \text{their } \alpha)} = \frac{650}{\sin 35}$ or $\frac{120}{\sin(\text{their } \alpha)}$ Or $v_r^2 = 650^2 + 120^2 - (2 \times 650 \times 120) \cos(145 - \text{their } \alpha)$	M1	For use of sine rule or cosine rule to find resultant velocity Do not allow for a right-angled triangle May be seen in (i)
	$v_r = 745$	A1	For correct resultant velocity, allow awrt 745
	Time taken = $\frac{1250}{\text{their } 744.7}$	M1	For correct attempt at finding time using <i>their</i> v , $\neq 650, 120, 770$ or 530
	= 1.68 hours or 1 hour 41 mins or 101 mins	A1	

Question	Answer	Marks	Guidance
8(i)	$e^y = \frac{m}{x} + c$	B1	May be implied by subsequent work
	Either $20 = 2m + c$ $8 = 4m + c$	M1	For at least 1 correct equation
		M1	Dep For attempt to solve <i>their</i> 2 equations simultaneously to obtain at least one unknown
	leading to $m = -6, c = 32$	A1	For both
	$y = \ln\left(32 - \frac{6}{x}\right)$	A1	Must have correct brackets Mark the final answer given
	Or: Gradient = $m = (-6)$	M1	For attempt to find gradient and equate it to m
	$20 = 2m + c$ or $8 = 4m + c$ or $e^y - 8 = m\left(\frac{1}{x} - 4\right)$ or $e^y - 20 = m\left(\frac{1}{x} - 2\right)$	M1	For at least 1 correct equation, may be using <i>their</i> m
	leading to $c = 32$ and $m = -6$	A1	For both $m = -6, c = 32$
	$y = \ln\left(32 - \frac{6}{x}\right)$	A1	
8(ii)	$x > \frac{3}{16}$ oe	B1	
8(iii)	$y = \ln 30$ isw	B1	
8(iv)	$2 = \ln\left(32 - \frac{6}{x}\right)$	M1	For a correct substitution and attempt to re-arrange using 2, <i>their</i> 32 and <i>their</i> -6 , keeping exactness to obtain $x =$
	$x = \frac{6}{32 - e^2}$ oe	A1	Must be exact

Question	Answer	Marks	Guidance
9(i)	$5 = 4 + 2\cos 3x$	M1	For attempt to solve trig equation to obtain one correct solution
	$\frac{\pi}{9}$	A1	
	$-\frac{\pi}{9}$	A1	
9(ii)	Either: $\int_{-\frac{\pi}{9}}^{\frac{\pi}{9}} 4 + 2\cos 3x - 5 \, dx$	M1	For use of subtraction method
	$\left[\frac{2}{3}\sin 3x - x \right]_{-\frac{\pi}{9}}^{\frac{\pi}{9}}$	M1	For attempt to integrate to obtain the form $a \sin 3x + bx$
		B1	For $\frac{2}{3}\sin 3x$
		B1	For $-x$, may be implied by $4x - 5x$
	$\left(\frac{\sqrt{3}}{3} - \frac{\pi}{9} \right) - \left(-\frac{\sqrt{3}}{3} + \frac{\pi}{9} \right)$	M1	Dep on previous M mark for correct application of <i>their</i> limits in radians from (i) retaining exactness
	Shaded area = $\frac{2\sqrt{3}}{3} - \frac{2\pi}{9}$ oe isw	A1	

Question	Answer	Marks	Guidance
9(ii)	Or: Area of rectangle = $5 \times \frac{2\pi}{9}$	M1	5 × the difference of <i>their</i> limits in exact radians
	Area under curve = $\left[4x + \frac{2}{3} \sin 3x \right]_{-\frac{\pi}{9}}^{\frac{\pi}{9}}$	M1	For attempt to integrate to obtain the form $a \sin 3x + bx$
		B1	For $\frac{2}{3} \sin 3x$
		B1	For $4x$
	$\left(\frac{\sqrt{3}}{3} + \frac{4\pi}{9} \right) - \left(-\frac{\sqrt{3}}{3} - \frac{4\pi}{9} \right)$ $\left(= \frac{2\sqrt{3}}{3} + \frac{8\pi}{9} \right)$	M1	Dep on previous M mark for correct application of <i>their</i> limits in exact radians from (i) retaining exactness
	Shaded area = $\frac{2\sqrt{3}}{3} - \frac{2\pi}{9}$ oe isw	A1	
10(i)	$800 = 4x^2 h$	B1	
	$h = \frac{800}{4x^2}$ oe or $xh = \frac{800}{4x}$ oe	B1	
	$(S =) 2hx + 8xh + 4x^2$ oe	M1	Allow if h is substituted at this point
	$S = 4x^2 + \left(\frac{2000}{x} \right)$	A1	Leading to AG, must have $S =$ or surface area = at some point and no errors

Question	Answer	Marks	Guidance
10(ii)	$\left(\frac{dS}{dx}\right) = 8x - \frac{2000}{x^2}$	B1	For correct differentiation
	When $\frac{dS}{dx} = 0$, $x = \sqrt[3]{250}$ oe (6.30)	M1	For equating to zero and attempt to solve, must get as far as $x = \dots$, must be using the form $ax + \frac{b}{x^2}$
		A1	For correct positive x
	$S = 476$ only	A1	
	$\frac{d^2S}{dx^2} = 8 + \frac{4000}{x^3}$ $\frac{d^2S}{dx^2} > 0$ or 24 so minimum	B1	For a correct convincing method, with enough detail to reach a correct conclusion of a minimum. Must be using $x = \sqrt[3]{250}$ oe
11		M1	For attempt at differentiating a product
		B1	For $\frac{2}{3} \times 3(3x+1)^{-\frac{1}{3}}$
	$\left(\frac{dy}{dx}\right) = (x-2) \times \frac{2}{3} \times 3(3x+1)^{-\frac{1}{3}} + (3x+1)^{\frac{2}{3}}$	A1	For all other terms correct
	$y = \frac{4}{3}$	B1	
	When $x = \frac{7}{3}$, $\frac{dy}{dx} = \frac{13}{3}$	M1	For attempt at normal equation using $-\frac{1}{\text{their } m}$ and <i>their</i> y when $x = \frac{7}{3}$
	Equation of normal: $y - \frac{4}{3} = -\frac{3}{13}\left(x - \frac{7}{3}\right)$	A1	For correct normal equation, may be implied by a correct final answer
	At y -axis, $y = \frac{73}{39}$ $\left(0, \frac{73}{39}\right)$ isw	A1	

ADDITIONAL MATHEMATICS**0606/13**

Paper 1

May/June 2019

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Cambridge International is publishing the mark schemes for the May/June 2019 series for most Cambridge IGCSE™, Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

This document consists of **8** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

M Method marks, awarded for a valid method applied to the problem.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.


B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

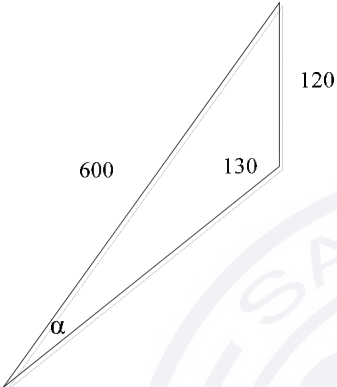
awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	$A \cap B = \emptyset$	B1	
	$Z \subset (X \cap Y)$	B2	B1 for identifying $X \cap Y$
2	$a = \frac{3}{2}$	B1	
	$b = \frac{7}{3}$	B1	
	$c = 3$	B1	
3	$x^2 + (3 - m)x + m - 4 = 0$	M1	For equating line and curve and attempting to obtain a quadratic equation equated to zero
	Discriminant: $(3 - m)^2 - 4(m - 4)$	M1	Dep For use of $b^2 - 4ac$, could be implied by use of quadratic formula
	$(m - 5)^2$	A1	
	Always positive or zero for any m , so line and curve will always touch or intersect	A1	For a suitable comment/conclusion
4(i)		B1	For $\frac{6x^3}{(2x^3 + 5)}$
		M1	For attempt to differentiate a quotient
	$\frac{dy}{dx} = \frac{(x-1) \frac{6x^2}{(2x^3+5)} - \ln(2x^3+5)}{(x-1)^2}$	A1	For all other terms correct
	When $x = 2$, $\frac{dy}{dx} = \frac{24}{21} - \ln 21$ or $\frac{8}{7} - \ln 21$, or -1.90	A1	
4(ii)	$-1.90p$ oe	B1	

Question	Answer	Marks	Guidance
5(i)		B1	For shape with maximum in 1 st quadrant
		B1	For $\left(-\frac{1}{3}, 0\right)$ and $(5, 0)$
		B1	For $(0, 5)$
		B1	All correct with cusps and correct shape for $x < -\frac{1}{3}$ and $x > 5$
5(ii)		M1	For attempt to find maximum point
	Maximum point when $x = \frac{7}{3}$	A1	For $x = \frac{7}{3}$
	$y = \frac{64}{3}$ so $k = \frac{64}{3}$	A1	
6(i)	$\frac{1}{\cos \theta} - \frac{\sin \theta}{\cos \theta} \times \sin \theta$ oe	M1	For dealing with sec, tan and cosec in terms of sin and cos
	$\frac{1 - \sin^2 \theta}{\cos \theta}$	M1	For simplification and use of identity
	$\frac{\cos^2 \theta}{\cos \theta}$	A1	For simplification to AG
6(ii)	$\cos 2\theta = \frac{\sqrt{3}}{2}$	M1	For use of part (i) and attempt to solve to get as far as $2\theta = \dots$
	$2\theta = 30^\circ, 330^\circ$	M1	For dealing with double angle correctly, may be implied by one correct solution
	$\theta = 15^\circ, 165^\circ$	A1	For both
6(iii)	$\sin\left(\phi + \frac{\pi}{3}\right) = \pm \frac{1}{\sqrt{2}}$ $\phi + \frac{\pi}{3} = \frac{\pi}{4}, \frac{3\pi}{4}, \frac{5\pi}{4}, \frac{7\pi}{4}, \frac{9\pi}{4}$	M1	For correct attempt to solve, may be implied by $\phi + \frac{\pi}{3} = \frac{\pi}{4}$
		M1	Dep For dealing with compound angle correctly
	$\phi = \frac{5\pi}{12}, \frac{11\pi}{12}, \frac{17\pi}{12}, \frac{23\pi}{12}$	A2	A1 for one correct pair, A1 for a second correct pair with no extra solutions in the range.

Question	Answer	Marks	Guidance
7(i)	$AC^2 = (2\sqrt{5} - 1)^2 + (2 + \sqrt{5})^2$	M1	For use of Pythagoras' theorem and attempt to expand brackets
	$= 20 - 4\sqrt{5} + 1 + 4 + 4\sqrt{5} + 5$	A1	For correct unsimplified, must be convinced of non-calculator use
	$AC = \sqrt{30}$	A1	
7(ii)	$\tan ACB = \frac{2\sqrt{5} - 1}{2 + \sqrt{5}} \times \frac{2 - \sqrt{5}}{2 - \sqrt{5}}$	M1	For attempt at $\tan ACB$ and rationalisation
	$= \frac{4\sqrt{5} - 2 - 10 + \sqrt{5}}{4 - 5}$ oe	M1	Dep For seeing at least 3 terms in the numerator
	$= 12 - 5\sqrt{5}$	A1	
7(iii)	$\sec^2 ACB = \tan^2 ACB + 1$ $= 144 - 120\sqrt{5} + 125 + 1$	M1	For use of identity using <i>their</i> (ii)
	$= 270 - 120\sqrt{5}$	A1	
8(i)	$g \geq 1$	B1	Must be using correct notation
8(ii)	$g(\sqrt{62}) = 125$	B1	
	$f^{-1}(x) = \frac{1}{3} \ln x$	B1	
	$\frac{1}{3} \ln 125 = \ln 5$	B1	For correct order and manipulation to obtain the given answer, need to see $\frac{1}{3} \ln 125$
8(iii)	$3e^{3x} = 24$	M1	For dealing with derivatives correctly
	$x = \frac{1}{3} \ln 8$	A1	
	$x = \ln 2$	A1	
8(iv)		B3	B1 for correct g with intercept B1 for $y = x$ and/or implication of symmetry B1 for correct g^{-1} with intercept
9(a)(i)	$7! = 5040$	B1	

Question	Answer	Marks	Guidance
9(a)(ii)	Treating the 4 trophies as 1 unit so there are 4! ways	B1	Maybe implied by a correct answer
	There are also 4! ways of arranging the football trophies amongst themselves	B1	
	Total = $4! \times 4! = 576$	B1	
9(a)(iii)	Treating the 4 football trophies as 1 unit and the 2 cricket trophies as 1 unit so there are 3! ways	B1	Maybe implied by a correct answer
	There are also 4! ways of arranging the football trophies amongst themselves and 2 ways of arranging the cricket trophies	B1	Maybe implied by a correct answer
	Total = $3! \times 4! \times 2 = 288$	B1	
9(b)(i)	3003	B1	
9(b)(ii)	28	B1	
9(b)(iii)	$3003 - 1$	M1	For <i>their</i> (i) – 1
	3002	A1	FT
10(i)		M1	Attempt to integrate to obtain $k(2x+3)^{\frac{1}{2}}$
	$\frac{dy}{dx} = (2x+3)^{\frac{1}{2}} (+c)$	A1	All correct, condone omission of $+c$
	$5 = 3 + c$	M1	Dep For attempt at c
	$\frac{dy}{dx} = (2x+3)^{\frac{1}{2}} + 2$	M1	For a further attempt to integrate
	$y = \frac{1}{3}(2x+3)^{\frac{3}{2}} + 2x(+d)$	A1	All correct, condone omission of $+d$
	$-\frac{1}{3} = \frac{8}{3} + 1 + d$	M1	For attempt at d
	$y = \frac{1}{3}(2x+3)^{\frac{3}{2}} + 2x - 4$	A1	Must have $y =$

Question	Answer	Marks	Guidance
10(ii)	When $x = 3$, $y = 11$	M1	For attempt to find y using <i>their</i> (i)
		M1	Dep For attempt at normal
	Normal: $y - 11 = -\frac{1}{5}(x - 3)$	A1	All correct unsimplified
	$x + 5y - 58 = 0$	A1	For correct form
11(i)		B1	For correct triangle, may be implied by subsequent work
	$\frac{120}{\sin \alpha} = \frac{600}{\sin 130}$	M1	For use of the correct sine rule
	$\alpha = 8.81^\circ$	A1	Allow greater accuracy
	Bearing 041.2° or 041°	A1	Allow greater accuracy
11(ii)	$\frac{v_r}{\sin 41.19} = \frac{600}{\sin 130} = \frac{120}{\sin \alpha}$	M1	For use of sine rule using <i>their</i> α or cosine rule
	$v_r = 515.8$ awrt 516	A1	
	Time taken $= \frac{2500}{515.8}$	M1	For attempt to find time using <i>their</i> v_r , not 600, 720 or 480
	$= 4.85$ or 4.84	A1	

ADDITIONAL MATHEMATICS**0606/12**

Paper 12

March 2019

MARK SCHEME

Maximum Mark: 80

Published

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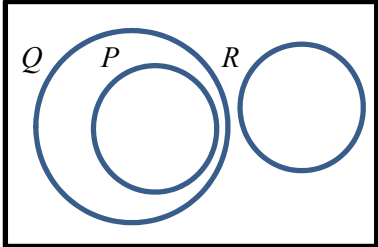
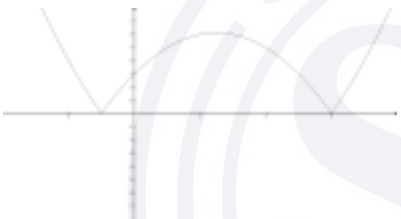
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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Partial Marks
1(a)(i)	6	B1	
1(a)(ii)	1	B1	
1(b)		2	B1 for P contained within Q B1 for Q and R separate
1(c)	$S' \cap T'$ or $(S \cup T)'$ oe	B1	
	$(X \cap Y) \cup (X \cap Z)$ or $X \cap (Y \cup Z)$ oe	B1	
2		4	B1 for general shape with maximum point in 1st quadrant B1 for $\left(-\frac{1}{2}, 0\right)$ and $(3, 0)$ soi B1 for $(0, 3)$ soi B1 dep on first B1, with cusps and correct shape for $x < -\frac{1}{2}$ and $x > 3$
3(i)	$729 - 162x + 15x^2$	3	B1 for 729 B1 for $-162x$ B1 for $15x^2$ Mark final answer
3(ii)	$(729 - 162x + 15x^2) \left(x^2 - 4 + \frac{4}{x^2} \right)$	B1	for expansion of $\left(x - \frac{2}{x} \right)^2$
	Term independent of $x = -2916 + 60$	M1	for attempt to find independent term, must be considering 2 products using <i>their</i> answer to part (i)
	$= -2856$	A1	
4(i)	$p'(x) = 6x^2 + 2ax + b$	B1	for $p'(x) = 6x^2 + 2ax + b$
	$p'(-3) = 54 - 6a + b, = -24$ leading to $6a - b = 78$	B1	must be convinced of correct substitution and simplification AG

Question	Answer	Marks	Partial Marks
4(ii)	$p\left(\frac{1}{2}\right): \frac{2}{8} + \frac{a}{4} + \frac{b}{2} - 49 = 0$	M1	for attempt at $p\left(\frac{1}{2}\right)$ equated to 0
	$6a - b = 78$ $a + 2b = 195$ oe	M1	M Dep on previous M for attempt to solve both equations
	leading to $a = 27$	A1	
	$b = 84$	A1	
4(iii)	$(2x - 1)(x^2 + 14x + 49)$	2	M1 for factorisation by observation or by long division
4(iv)	$(2x - 1)(x + 7)^2$	B1	
5(i)	$\log_4 16 + \log_4 p$	M1	for dealing with product correctly
	$2 + p$	A1	
5(ii)	$7\log_4 x - \log_4 256$	M1	for dealing with power and division correctly
	$7p - 4$	A1	
5(iii)	$2 + p - (7p - 4) = 5$ leading to $p = \frac{1}{6}$	M1	for use of parts (i) and (ii) to obtain a value for p
	so $x = 4^{\frac{1}{6}}$	M1	for correct attempt to deal with \log_4 in order to obtain x
	$x = 1.26$	A1	
6(a)	BA and CB	2	B1 for one correct product of 2 matrices B1 for a second correct product of 2 matrices, with no other incorrect products
6(b)(i)	$\frac{1}{16} \begin{pmatrix} 3 & 2 \\ -5 & 2 \end{pmatrix}$ oe	2	B1 for $\frac{1}{16}$ soi B1 for $\begin{pmatrix} 3 & 2 \\ -5 & 2 \end{pmatrix}$

Question	Answer	Marks	Partial Marks
6(b)(ii)	$\mathbf{X}^{-1}\mathbf{XZ} = \mathbf{X}^{-1}\mathbf{Y}$ $\mathbf{Z} = \frac{1}{16} \begin{pmatrix} 3 & 2 \\ -5 & 2 \end{pmatrix} \begin{pmatrix} 4 & 1 \\ 2 & 0 \end{pmatrix}$	M1	for pre-multiplication by <i>their</i> inverse matrix
	attempt at matrix multiplication	M1	M1 Dep on previous M mark, must have at least 2 correct elements
	$\mathbf{Z} = \frac{1}{16} \begin{pmatrix} 16 & 3 \\ -16 & -5 \end{pmatrix}$ oe	A1	
7(i)	Area = $\frac{1}{2}(8 + 6\sqrt{5})(10 - 2\sqrt{5})$	M1	for a correct method of finding the area of the trapezium
	= $10 + 22\sqrt{5}$	A2	A1 for 10 with sufficient working seen A1 for $22\sqrt{5}$ with sufficient working seen
7(ii)	$\cot \theta = \frac{4}{10 - 2\sqrt{5}}$	B1	
	$= \frac{4(10 + 2\sqrt{5})}{(10 - 2\sqrt{5})(10 + 2\sqrt{5})}$	M1	for attempt to rationalise an expression for $\cot \theta$, some evidence of expansion must be seen
	$= \frac{1}{2} + \frac{\sqrt{5}}{10}$	A1	
8(a)(i)	0	B1	
8(a)(ii)	Area under curve = $\frac{1}{2}(2 \times 10) + (4 \times 10) + \frac{1}{2}(10 + 20) \times 4$	M1	for attempt to find the total area under the graph
	= 110	A1	
8(b)(i)	When $t = \frac{7\pi}{12}$, $v = -2.5$	M1	for substitution of $t = \frac{7\pi}{12}$ and correct attempt to evaluate
	Speed = 2.5	A1	must be positive
8(b)(ii)	$a = 6 \cos 2t$	M1	for differentiation to get acceleration, must be of the form $m \cos 2t$
	When acceleration = 0, $\cos 2t = 0$	M1	M Dep on previous M mark for equating to zero and correct attempt to solve to get a solution in radians.
	$t = \frac{\pi}{4}$ or 0.785	A1	

Question	Answer	Marks	Partial Marks
9(i)	$\frac{1}{2}r^2\theta = 36$ $\theta = \frac{72}{r^2}$	M1	for use of the area of the sector
	$P = 2r + r\theta$	M1	for attempt to find P making use of the area
	$P = 2r + \frac{72}{r}$	A1	for attempt to simplify to obtain AG
9(ii)	$\frac{dP}{dr} = 2 - \frac{72}{r^2}$	M1	for attempt to differentiate to obtain the form $a + \frac{b}{r^2}$ and equate to zero
	When $\frac{dP}{dr} = 0$, $r = 6$	A1	
	$P = 24$	A1	
	$\frac{d^2P}{dr^2} = \frac{144}{r^3}$ positive so minimum	B1	FT on <i>their</i> positive r , for a correct method to determine the nature of the stationary point leading to a correct conclusion. If the second derivative is evaluated, it must be correct for <i>their</i> r .
10(i)	$\frac{dy}{dx} = 2e^{2x} + 3x$ (+c)	2	M1 for attempt to integrate to obtain the form $me^{2x} + nx$ A1 all correct
	$c = 8$	M1	M1 Dep on previous M mark for attempt to get c
	$y = e^{2x} + \frac{3x^2}{2} + 8x$ (+d)	2	M1 for attempt to integrate again to obtain the form $pe^{2x} + qx^2 (+rx)$ A1 all correct, FT on <i>their</i> ke^{2x} and <i>their</i> c
	$d = -6$	M1	M1 Dep on previous M mark for attempt to get d
	$y = e^{2x} + \frac{3x^2}{2} + 8x - 6$	A1	

Question	Answer	Marks	Partial Marks
10(ii)	When $x = \frac{1}{4}$, $y = -2.26$ $\frac{dy}{dx} = 12.0$	M1	for attempt to obtain both y and $\frac{dy}{dx}$ using <i>their</i> work from (i)
	$y + 2.26 = -\frac{1}{12}\left(x - \frac{1}{4}\right)$	2	M1 Dep on previous M mark for attempt to obtain the equation of the normal A1 allow unsimplified, must be using correct accuracy or exact equivalents.
11(a)	$2 \sin x (\cos^2 x - 1) = 0$	M1	for obtaining in terms of sin and cos to obtain one solution correctly
	$\sin x = 0$, $x = 0^\circ$, 180°	B1	for $x = 0^\circ$, 180° and no other in the given range for the solution of this equation
	$\cos x = \pm \frac{1}{\sqrt{2}}$, $x = 45^\circ$, 135°	A1	for $x = 45^\circ$, 135° and no other in the given range for the solution of this equation
11(b)(i)	$\frac{1}{\cos \theta} - \frac{\sin^2 \theta}{\cos \theta}$	M1	for dealing with cot and sec
	$\frac{\cos^2 \theta}{\cos \theta}$	M1	for correct use of identity
	$\cos \theta$	A1	for all correct working to gain AG
11(b)(ii)	$\cos 3\theta = \frac{1}{2}$ $\theta = \frac{5\pi}{9}$ or $\frac{\pi}{9}$	M1	for use of part (i) and attempt to solve correctly to obtain a positive angle, may be implied by one correct solution
	$\theta = -\frac{5\pi}{9}$ or $-\frac{\pi}{9}$	M1	for use of part (i) and attempt to solve correctly to obtain a negative angle, may be implied by one correct solution
	$\theta = \pm \frac{\pi}{9}$, $\pm \frac{5\pi}{9}$	A2	A1 for one correct pair of solutions A1 for a second pair of solutions with no extra solutions within the range

ADDITIONAL MATHEMATICS**0606/11**

Paper 1

October/November 2018

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2018 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

This document consists of **9** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

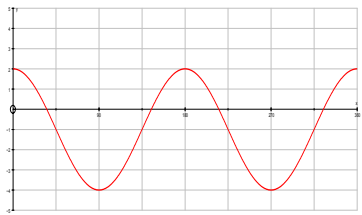
Types of mark


- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(a)		B3	B1 for 2 cycles, one max and 2 min points in the correct places and up to a max at each end B1 for going between 2 and -4 B1 for starting at (0,2) and finishing at (360,2)
1(b)(i)	4	B1	
1(b)(ii)	60° or $\frac{\pi}{3}$	B1	
2(i)	$\left(p\left(-\frac{1}{2}\right)=\right) -\frac{1}{4}+\frac{5}{4}-2+a=2$ $(q(-2)=) 16-6a+b=0$	M1	For either $p\left(-\frac{1}{2}\right)=2$ or $q(-2)=0$
	$a=3$	A1	
	$b=2$	A1	
2(ii)	$r(x)=2x^3+x^2-5x+1$	M1	For $r(x)$ using <i>their</i> $p(x)$ and $q(x)$
	$r\left(\frac{2}{3}\right)=\frac{16}{27}+\frac{4}{9}-\frac{10}{3}+1$	M1	For $r\left(\frac{2}{3}\right)$
	$=-\frac{35}{27}$	A1	Must be exact

Question	Answer	Marks	Guidance
3	$(3 + kx)^6 =$ $729 + 1458kx + 1215k^2x^2$	B2	B1 for $1458kx$ or $1215k^2x^2$
	Terms in x^2 for $(2 - x)(3 + kx)^6$ $= -1458k + 2430k^2$ $2430k^2 - 1458k = 972$	M1	For attempt at further expansion to obtain 2 terms in x^2 and equating to 972
	$5k^2 - 3k - 2 = 0$ $(5k + 2)(k - 1) = 0$	M1	Dep for solution of resulting 3 term quadratic
	$k = -\frac{2}{5}$	A1	
	$k = 1$	A1	
4(i)	$\left(x - \frac{9}{2}\right)^2 - \frac{49}{4}$	B2	B1 for $\frac{9}{2}$ or $\frac{49}{4}$
4(ii)	$\left(\frac{9}{2}, -\frac{49}{4}\right)$	B1	FT <i>their p</i> and <i>q</i>
4(iii)		B3	B1 for shape B1 for cusps at $(1, 0)$ and $(8, 0)$ B1 for all correct, passing through $(0, 8)$ with maximum in correct position
4(iv)	$\frac{49}{4}$	B1	FT <i>their q</i>
5(i)	$\frac{1}{2}r^2\theta = 48$	B1	
	$\theta = \frac{96}{r^2}$	B1	Dep Must have previous B1
5(ii)	$r\theta = 12$	B1	For statement of arc length
	$r \times \frac{96}{r^2} = 12$	M1	For attempt to use part (i) to find either r or θ
	$r = 8$ and $\theta = 1.5$	A1	For both

Question	Answer	Marks	Guidance
5(iii)	$\text{Area} = 48 - \left(\frac{1}{2} r^2 \sin \theta \right)$	M1	For a complete method including a correct attempt for the area of the triangle using their r and θ
	$= 16.1$	A1	
6(i)	For $\frac{4x}{2x^2 + 3}$	B1	
		M1	For attempt to differentiate a quotient or appropriate product
	$\frac{dy}{dx} = \frac{(5x+2) \frac{4x}{2x^2+3} - 5 \ln(2x^2+3)}{(5x+2)^2}$	A1	All other terms correct
	When $x = 0$ $\frac{dy}{dx} = \frac{-5 \ln 3}{4}$	A1	For given answer
6(ii)	$y = \frac{1}{2} \ln 3$ or 0.549	B1	May be implied by tangent equation, allow 0.55
	Equation of tangent $y = \left(-\frac{5}{4} \ln 3 \right) x + \frac{1}{2} \ln 3$ or $y = -1.37x + 0.549$	B1	
7(a)	$\lg 100 = 2$	B1	
	$3 \lg x = \lg x^3$	B1	
	$\lg \frac{100x^3}{y}$	B1	
7(b)(i)	$6x^2 + 7x - 3 = 0$ $(2x+3)(3x-1) = 0$	M1	For obtaining in suitable quadratic form and attempt to solve
	$x = -\frac{3}{2}$ $x = \frac{1}{3}$	A1	For both

Question	Answer	Marks	Guidance
7(b)(ii)	$x = \log_a 3$ $\frac{1}{3} = \log_a 3$	M1	For realising connection with part (i) and attempt to solve $\frac{1}{3} = \log_a 3$ or $-\frac{3}{2} = \log_a 3$
	$a = 27$	A1	
	$-\frac{3}{2} = \log_a 3$	M1	For realising connection with part (i) and attempt to solve $-\frac{3}{2} = \log_a 3$ or $\frac{1}{3} = \log_a 3$
	$a = \left(\frac{1}{3}\right)^{\frac{2}{3}}$ or 0.481 or $\left(\frac{1}{9}\right)^{\frac{1}{3}}$ oe	A1	
8(i)		M1	For attempt to use chain rule to obtain $kx(5x^2 + 4)^{\frac{1}{2}}$ where k is a constant
	$\frac{3}{2}(10x)(5x^2 + 4)^{\frac{1}{2}}$	A1	Allow unsimplified
8(ii)		M1	For attempt to use part (i) if in correct form of $m(5x^2 + 4)^{\frac{3}{2}}$
	$\frac{1}{15}(5x^2 + 4)^{\frac{3}{2}} (+c)$	A1	FT on <i>their</i> $\frac{1}{k}(5x^2 + 4)^{\frac{3}{2}}$
8(iii)		M1	For use of limits if <i>their</i> (ii) Must be in the form $m(5x^2 + 4)^{\frac{3}{2}}$
	$\frac{1}{15}\left((5a^2 + 4)^{\frac{3}{2}} - 4^{\frac{3}{2}}\right) \left[= \frac{19}{15} \right]$	A1	
	$(5a^2 + 4)^{\frac{3}{2}} = 27$	M1	Dep For complete and correct method to deal with the power of $\frac{3}{2}$
	leading to $a = 1$	A1	
9(i)	3	B1	

Question	Answer	Marks	Guidance
9(ii)		M1	For attempt to differentiate to obtain $a + be^{-t}$
	$\frac{ds}{dt} = 4 - 3e^{-t}$	A1	All correct
	$2 = 4 - 3e^{-t}$	M1	Dep for correct attempt to solve equation involving exponential where $e^{-t} > 0$
	leading to $t = \ln \frac{3}{2}$ or $-\ln \frac{2}{3}$	A1	Must be an exact form
9(iii)	When $t = \ln 5$, $\frac{ds}{dt} = \frac{17}{5}$	M1	For attempt to find value of $\frac{ds}{dt}$ when $t = \ln 2$
		M1	Dep for attempt to use method of small changes
	$\partial s = \frac{17h}{5}$	A1	
10(i)	Velocity of A $\begin{pmatrix} 6 \\ 8 \end{pmatrix}$	B1	For velocity, may be implied by later work
	When $t = 6$, $\mathbf{r}_A = \begin{pmatrix} 2 \\ -5 \end{pmatrix} + 6\begin{pmatrix} 6 \\ 8 \end{pmatrix}$	M1	For a complete and correct method
	$= \begin{pmatrix} 38 \\ 43 \end{pmatrix}$	A1	For 43
10(ii)	$\mathbf{r}_B = \begin{pmatrix} 16 \\ 37 \end{pmatrix} + \begin{pmatrix} 4 \\ 2 \end{pmatrix}t$	B1	
10(iii)	$\begin{pmatrix} 16 \\ 37 \end{pmatrix} + \begin{pmatrix} 4 \\ 2 \end{pmatrix}t = \begin{pmatrix} 2 \\ -5 \end{pmatrix} + \begin{pmatrix} 6 \\ 8 \end{pmatrix}t$	M1	For equating position vectors at a time t
	$16 + 4t = 2 + 6t$ or $37 + 2t = -5 + 8t$	M1	Dep for equating like vectors at least once
	$t = 7$	A1	Allow from one correct equation
	Both equations lead to $t = 7$	B1	For showing that $t = 7$ satisfies both equations thus verifying collision, or equivalent
10(iv)	$\begin{pmatrix} 44 \\ 51 \end{pmatrix}$	B1	

Question	Answer	Marks	Guidance
11(a)(i)		B1	For critical values
	$2 \leq f \leq 4$	B1	Dep For correct inequality and notation
11(a)(ii)	$x = 3 \cos y$ $\cos 2y = 0.5$	M1	For attempt to find f^{-1} and equate to 0.5
	$2y = \frac{\pi}{3}$	M1	Dep For correct attempt to solve, dealing with the double angle
	$y = \frac{\pi}{6}$	A1	
11(b)	$g^2(x) = g(3 - x^2)$ $= 3 - (3 - x^2)^2$	M1	For correct attempt at g^2 , allow unsimplified
	$-6 + 6x^2 - x^4 = -6$ $6x^2 - x^4 = 0$	M1	Dep for equating to -6 and attempt to solve to obtain a non-zero root
	$x = 0$	B1	
	$x = \pm\sqrt{6}$	A1	

ADDITIONAL MATHEMATICS**0606/12**

Paper 1

October/November 2018

MARK SCHEME

Maximum Mark: 80

Published

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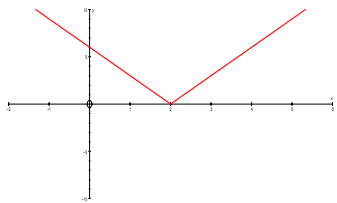
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soi	seen or implied

Question	Answer	Marks	Guidance
1	$\sin(x + 50^\circ) = -\frac{1}{\sqrt{2}}$ $(x + 50^\circ = -45^\circ, 225^\circ)$	M1	For order of operations – subtraction of 1, division by $\pm\sqrt{2}$ and attempt at \sin^{-1}
		M1	Dep For obtaining a solution by subtracting 50°
	$x = -95^\circ, 175^\circ$	A2	A1 for one correct solution A1 for a second correct solution and no others within the range
2	$\frac{dy}{dx} = 5x + \frac{1}{2}e^{2x} \quad (+c)$	M1	For attempt to integrate to get $\frac{dy}{dx}$ in the form $5x + pe^{2x}$. Condone omission of $+c$
	When $x = 0$, $\frac{dy}{dx} = 4$ so $c = \frac{7}{2}$	M1	Dep For attempt to get value of c
	$y = \frac{5x^2}{2} + \frac{1}{4}e^{2x} + \frac{7}{2}x \quad (+d)$	M1	Dep on first M1 only For attempt to get y in the form including $\frac{5x^2}{2} + pe^{2x}$. Condone omission of $+d$.
	When $x = 0$, $y = -3$ so $d = -\frac{13}{4}$	M1	Dep on previous DepM1 For attempt to obtain d , allow if c not found
	$y = \frac{5x^2}{2} + \frac{1}{4}e^{2x} + \frac{7}{2}x - \frac{13}{4}$	A1	Must have an equation
3(i)		B2	B1 for correct shape with vertex at $(2, 0)$ Dep B1 for passing through or starting at $(0, 6)$

Question	Answer	Marks	Guidance
3(ii)	Either $6 - 3x = 2$ $x = \frac{4}{3}$	B1	For $x = \frac{4}{3}$
	$6 - 3x = -2$	M1	For considering -2
	$x = \frac{8}{3}$	A1	
	Or $9x^2 - 36x + 32 = 0$	M1	For squaring each side and attempt to solve a 3 term quadratic = 0
	$x = \frac{4}{3}$	A1	
	$x = \frac{8}{3}$	A1	
3(iii)	$x < \frac{4}{3}, x > \frac{8}{3}$	B1	FT on <i>their</i> solutions in part (ii), must both be positive and written as 2 separate statements
4(i)		B1	For $\frac{2}{2x+1}$
		M1	For attempt to differentiate a product
	$\frac{dy}{dx} = x^3 \frac{2}{2x+1} + 3x^2 \ln(2x+1)$	A1	For all other terms correct
	When $x = 0.3$, $\frac{dy}{dx} = 0.161$	A1	For awrt 0.161
4(ii)	$0.161h$	B1	FT on <i>their</i> numerical answer to part (i)
5(i)	7th term: $924a^6b^6x^6 = 924x^6$ $924a^6b^6 = 924$ $924a^6(bx)^6 = 924x^6$	B1	For any correct statement
	$(ab)^6 = 1$ or $ab = 1$ so $b = \frac{1}{a}$	B1	Dep on first B1 Must be convinced, nfw

Question	Answer	Marks	Guidance
5(ii)	6th term: $792a^7b^5x^5 = 198x^5$ $792a^7b^5 = 198$ $792a^7(bx)^5 = 198x^5$	B1	For any correct statement
	use of $ab=1$ to obtain $a^2 = \dots$ or $b^2 = \dots$	M1	For attempt to solve <i>their</i> equations simultaneously to obtain an equation in a^2 or b^5
	$a = \frac{1}{2}$	A1	
	$b = 2$	A1	
6(i)		M1	For $kx(5x-125)^{\frac{1}{3}}$
	$\frac{2}{3} \times 10x(5x^2-125)^{\frac{1}{3}}$ $\left(\frac{20}{3}x(5x^2-125)^{\frac{1}{3}}\right)$	A1	Allow unsimplified
6(ii)		M1	For $m(5x^2-125)^{\frac{2}{3}} (+c)$
	$\frac{3}{20}(5x^2-125)^{\frac{2}{3}} (+c)$	A1	FT on <i>their k</i> from part (i)
6(iii)	$\frac{3}{20}\left((375)^{\frac{2}{3}} - (55)^{\frac{2}{3}}\right)$	M1	Dep on previous M1 For use of limits in <i>their</i> answer to part (ii), must be in the form $m(5x^2-125)^{\frac{2}{3}} (+c),$
	$= 5.63$	A1	Allow greater accuracy

Question	Answer	Marks	Guidance
7(a)	$\left \begin{pmatrix} -12 \\ 5 \end{pmatrix} \right = 13$	B1	For magnitude, may be implied by a correct v
	$\mathbf{v} = \begin{pmatrix} -36 \\ 15 \end{pmatrix}$ or $3 \begin{pmatrix} -12 \\ 5 \end{pmatrix}$	B1	Must be a vector
7(a) Alternative	If $t \left \begin{pmatrix} -12 \\ 5 \end{pmatrix} \right = 39$, $t = 3$	B1	For value of t , may be implied by a correct v
	$\mathbf{v} = \begin{pmatrix} -36 \\ 15 \end{pmatrix}$ or $3 \begin{pmatrix} -12 \\ 5 \end{pmatrix}$	B1	
7(b)		M1	For equating like vectors at least once
	$17r + 2s + 3 = 0$ $2r + 6s + 9 = 0$	M1	Dep For solution of resulting equations to obtain 2 solutions
	$r = 0$	A1	
	$s = -\frac{3}{2}$ oe	A1	
8(i)	$a(a + 4) - 12 = 0$	M1	For correct use of $\det = 0$
	$a^2 + 4a - 12 = 0$	M1	Dep For solution of resulting quadratic equation
	leading to $a = -6$, $a = 2$	A1	For both
8(ii)	$\mathbf{A}^{-1} = \frac{1}{20} \begin{pmatrix} 8 & -3 \\ -4 & 4 \end{pmatrix}$ oe	B2	B1 for $\frac{1}{20}$ B1 for $\begin{pmatrix} 8 & -3 \\ -4 & 4 \end{pmatrix}$
8(iii)	$\mathbf{B} = \mathbf{A}^{-1} \begin{pmatrix} 2 & 3 \\ 4 & -5 \end{pmatrix}$	M1	For pre-multiplication by their \mathbf{A}^{-1}
		M1	Dep For multiplication of 2 matrices – need to see at least 2 correct elements – may be unsimplified
	$= \frac{1}{20} \begin{pmatrix} 4 & 39 \\ 8 & -32 \end{pmatrix}$	A1	For final matrix oe

Question	Answer	Marks	Guidance
9(i)	$p(-3) = 0$ leading to $-27a + 9b - 3c - 9 = 0$	M1	For substitution of $x = -3$ and equating to zero
	$p'(x) = 3ax^2 + 2bx + c$ $p'(0) = 36$	M1	For differentiation in the form $rx^2 + sx + t$ and substitution of $x = 0$
	$c = 36$	A1	nfww
	$p''(x) = 6ax + 2b$ $p''(0) = 2b$	M1	For further differentiation in the form $vx + w$ of <i>their</i> $p'(x)$ and substitution of $x = 0$
	$b = 43$	A1	nfww
	$a = 10$	A1	nfww
9(ii)	$p\left(\frac{1}{2}\right)$	M1	For use of $x = \frac{1}{2}$ in <i>their</i> $p(x)$ from part (i)
	21	A1	
10(i)	$a = 2$	B1	
	$\cos bx = -\frac{1}{2}$	M1	For a correct attempt to solve $\cos b \frac{\pi}{6} = \pm \frac{a}{4}$ provided $0 < a \leq 4$ to get $b = \dots$
	leading to $b = 4$	A1	
10(ii)	$\cos 4x = -\frac{1}{2}$	M1	Dep For attempt to solve <i>their</i> $\cos bx = \pm \frac{a}{4}$ provided $0 < a \leq 4$ or use of symmetry to get $x = \dots$
	$x = \frac{\pi}{3}$ so $\left(\frac{\pi}{3}, 0\right)$	A1	
10(iii)	At M , $y = -2$	B1	
	$x = \frac{\pi}{4}$	B1	

Question	Answer	Marks	Guidance
11(i)	$2r + r\theta = 10$	M1	For use of arc length and attempt to get perimeter, must have 2 terms involving r
		M1	Dep For attempt to get r in terms of θ
	$r = \frac{10}{2 + \theta}$	A1	
	$A = \frac{1}{2} \left(\frac{10}{2 + \theta} \right)^2 \theta$	M1	For attempt to obtain the area of the sector in terms of θ only, using <i>their</i> r
	$A = \frac{50\theta}{(2 + \theta)^2}$	A1	For manipulation to get the required answer nfw AG
11(ii)		M1	For attempt to differentiate a quotient or an equivalent product
	$\frac{dA}{d\theta} = \frac{50(2 + \theta)^2 - 100\theta(2 + \theta)}{(2 + \theta)^4}$ or $\frac{dA}{d\theta} = 50(2 + \theta)^{-2} - 100\theta(2 + \theta)^{-3}$	A1	All correct, allow unsimplified
	When $\frac{dA}{d\theta} = 0$	M1	For equating <i>their</i> $\frac{dA}{d\theta}$ to 0 and attempt to solve – need to see at least one line of working
	$\theta = 2$	A1	Condone inclusion of -2
	$A = \frac{25}{4}$	A1	

Question	Answer	Marks	Guidance
11(ii) Alternative	Starting again using $\theta = \frac{10-2r}{2}$ so $A = 5r - r^2$	M1	A complete method to obtain $\frac{dA}{dr}$
	$\frac{dA}{dr} = 5 - 2r$	A1	
	When $\frac{dA}{dr} = 0$	M1	For equating to zero and attempt to solve
	$r = 2.5$	A1	
	$A = \frac{25}{4}$	A1	
12	$2x^2 + 7x = 0$ or $y^2 - 3y - 10 = 0$	M1	For attempt to obtain a simplified quadratic equation in one variable equated to 0
		M1	Dep For solution of quadratic
	$(0, 5)$	A1	
	$\left(-\frac{7}{2}, -2\right)$	A1	
	Midpoint $\left(-\frac{7}{4}, \frac{3}{2}\right)$	B1	
	Gradient of $AB = 2$ $\therefore \perp$ gradient $= -\frac{1}{2}$	M1	For attempt to obtain gradient of line perpendicular to AB using <i>their</i> coordinates
	\perp bisector: $y - \frac{3}{2} = -\frac{1}{2}\left(x + \frac{7}{4}\right)$	M1	For a correct attempt to obtain equation of perpendicular bisector using their midpoint and <i>their</i> perpendicular gradient
	Consideration of when $y = x$	M1	Dep on previous M1 For attempt to find intersection with the line $y = x$
	$x = y = \frac{5}{12}$	A1	For both

ADDITIONAL MATHEMATICS

0606/13

Paper 1

October/November 2018

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.

Cambridge International is publishing the mark schemes for the October/November 2018 series for most Cambridge IGCSE™, Cambridge International A and AS Level components and some Cambridge O Level components.

This document consists of **11** printed pages.

Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfwf	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(a)	${}^5C_3 \times 2^2 \times (px)^3$	B1	
	$40p^3 = -\frac{8}{25}$ $p^3 = -\frac{8}{1000}$	M1	equating <i>their</i> coefficient of x^3 to $-\frac{8}{25}$ and finding p^3
	$p = -\frac{1}{5}$ or $p = -0.2$	A1	
1(b)	${}^8C_4 \times (2x^2)^4 \times \left(\frac{1}{4x^2}\right)^4$	B1	
	$70 \times 16 \times \frac{1}{256}$	M1	at least two of 70, 16, $\frac{1}{256}$ correct in an evaluation of a three-term product
	$\frac{35}{8}, 4.375, 4\frac{3}{8}$	A1	cao
2(i)	$\theta = \frac{20-2r}{r}$	B1	
	$\text{Area} = \frac{1}{2}r^2 \left(\frac{20-2r}{r} \right)$	M1	use of <i>their</i> θ in terms of r in formula for sector area
	$A = 10r - r^2$	A1	simplification to get given answer
	Alternative		
	$s = 20 - 2r$	B1	
	$= \frac{1}{2}r(20 - 2r)$	M1	use of formula for sector area using <i>their</i> expression for s in terms of r
	$A = 10r - r^2$	A1	simplification to get given answer
2(ii)	$\frac{dA}{dr} = 10 - 2r$ When $\frac{dA}{dr} = 0$, $r = 5$	M1	for $\frac{dA}{dr} = 10 - kr$, equating to zero and solving for r
	$\theta = \frac{(20 - 2 \times 5)}{5}$	M1	Dep substitution of <i>their</i> value of r to get θ
	$\theta = 2$	A1	

Question	Answer	Marks	Guidance
3(i)	$AC^2 = (5\sqrt{3} + 5)^2 + (5\sqrt{3} - 5)^2$	M1	correct use of Pythagoras or correct use of cosine rule with $\cos 90$
	$= 75 + 25 + 50\sqrt{3} + 75 + 25 - 50\sqrt{3}$ $= 200$	M1	correct expansion to 6 or 8 terms
	$AC = 10\sqrt{2}$	A1	from $AC^2 = 200$
3(ii)	$\tan BCA = \frac{5\sqrt{3} + 5}{5\sqrt{3} - 5}$ oe	B1	
	$= \frac{(5\sqrt{3} + 5)(5\sqrt{3} + 5)}{(5\sqrt{3} - 5)(5\sqrt{3} + 5)}$ oe $= \frac{100 + 50\sqrt{3}}{50}$ oe	M1	for rationalisation
	$= 2 + \sqrt{3}$	A1	
4(i)		M1	for $10(1 + \cos 3x)^9 f(x)$
		M1	for $k \sin 3x(1 + \cos 3x)^9$
	$\frac{dy}{dx} = -30 \sin 3x(1 + \cos 3x)^9$	A1	
	When $x = \frac{\pi}{2}$, $\frac{dy}{dx} = 30$	A1	
4(ii)	Use of $\frac{dy}{dx} \times \frac{dx}{dt} = \frac{dy}{dt}$ with $\frac{dy}{dt} = 6$	M1	<i>their</i> $\frac{dy}{dx} \times \frac{dx}{dt} = 6$
	$\frac{dx}{dt} = \frac{1}{5}$ or 0.2	A1	FT from <i>their</i> answer from part (i)

Question	Answer	Marks	Guidance
5(i)	$\log_9 4 = \frac{\log_3 4}{\log_3 9}$	B1	change of base
	$= \frac{1}{2} \log_3 4$ $= \frac{1}{2} \log_3 2^2$ or $\log_3 \sqrt{4}$ $= \log_3 2$	B1	Dep must have B1 for change of base and full working
	Alternative A		
	$\log_9 4 = 2 \log_9 2$	B1	use of power rule
	$= \frac{2 \log_3 2}{\log_3 9}$ $= \frac{2 \log_3 2}{2 \log_3 3}$ $= \log_3 2$	B1	Dep change of base and full working
	Alternative B		
	$x = \log_9 4 \Rightarrow 9^x = 4$ $9^x = 4 \Rightarrow 3^{2x} = 4$	B1	correct use of indices to reach $3^{2x} = 4$
	$\Rightarrow 3^x = 2 \Rightarrow x = \log_3 2$ $\therefore \log_9 4 = \log_3 2$	B1	Dep full working
	Alternative C		
	$\log_9 4 = \frac{\log_{10} 4}{\log_{10} 9}$ $= \frac{2 \log_{10} 2}{2 \log_{10} 3}$	B1	change of base and use of power rule
	$= \log_3 2$	B1	Dep change of base and full working

Question	Answer	Marks	Guidance
5(ii)	$\log_3 2 + \log_3 x = 3$ $\log_3 2x = 3$	B1	for $\log_3 2x = 3$
	$3^3 = 2x$	B1	
	$x = 13.5, x = \frac{27}{2}$	B1	
	Alternative		
	$\log_3 x = \log_3 27 - \log_3 2$	B1	
	$= \log_3 \frac{27}{2}$	B1	
	$x = 13.5, x = \frac{27}{2}$	B1	
6(i)	$\frac{ds}{dt} = -6e^{-0.5t} + 4$	M1	for $ke^{-0.5t} + 4$
	When $\frac{ds}{dt} = 0, e^{-0.5t} = \frac{2}{3}$ $-0.5t = \ln \frac{2}{3}$ $t = -2 \ln \frac{2}{3}$	M1	Dep equating to zero and correct order of operations to solve for t
	$t = 0.811$	A1	
6(ii)		M1	for $ke^{-0.5t}$
	$\frac{d^2s}{dt^2} = 3e^{-0.5t}$	A1	
6(iii)	$3e^{-0.5t} = 0.3$ $e^{-0.5t} = 0.1$ $t = \frac{\ln 0.1}{-0.5}$	M1	correct order of operations and correct use of \ln to solve $ke^{-0.5t} = 0.3$ for t
	$s = 12e^{-0.5 \times 4.605} + 4 \times 4.605 - 12$	M1	Dep use of t to obtain s
	$s = 7.62$	A1	
6(iv)	$e^{-0.5t}$ is always positive or $e^{-0.5t}$ can never be zero or negative	B1	correct comment about $e^{-0.5t}$

Question	Answer	Marks	Guidance
7(i)	$\overrightarrow{AD} = m(\mathbf{c} - \mathbf{a})$	B1	
7(ii)	$\overrightarrow{AD} = \overrightarrow{OD} - \mathbf{a}$	B1	for $\overrightarrow{OD} = \frac{2}{3}\mathbf{b}$
	$= \frac{2}{3}\mathbf{b} - \mathbf{a}$	B1	FT their \overrightarrow{OD} if $\overrightarrow{OD} = k\mathbf{b}$
7(iii)	$m(\mathbf{c} - \mathbf{a}) = \frac{2}{3}\mathbf{b} - \mathbf{a}$	M1	equating parts (i) and (ii)
	$24\mathbf{a}(1 - m) + 24m\mathbf{c} = 16\mathbf{b}$ Comparing with $15\mathbf{a} + 9\mathbf{c} = 16\mathbf{b}$	M1	attempt to eliminate or compare like vectors using given condition
	$m = \frac{3}{8}$	A1	
8(i)	$5 \leq f(x) \leq 6$ or $[5, 6]$ oe	B2	B1 for $5 \leq f(x) \leq p$ ($p > 5$) or for $q \leq f(x) \leq 6$ ($q < 6$)
8(ii)	$x = \sin \frac{y}{4} + 5$	M1	complete valid attempt to obtain the inverse with operations in correct order.
	$y = 4 \sin^{-1}(x - 5)$	A1	
	Range $0 \leq y \leq 2\pi$	B1	
8(iii)	$2 \left(\sin \left(\frac{x - \frac{\pi}{3}}{4} \right) + 5 \right) (= 11)$	B1	for $\sin \left(\frac{x - \frac{\pi}{3}}{4} \right) + 5$
	$\sin \left(\frac{x - \frac{\pi}{3}}{4} \right) = \frac{1}{2}$	M1	for $\sin \left(\frac{x - \frac{\pi}{3}}{4} \right) = k$
	$x = 4 \sin^{-1} \left(\frac{1}{2} \right) + \frac{\pi}{3}$ oe	M1	Dep for use of \sin^{-1} and correct order of operations to obtain x . Allow one $+/-$ or \times/ \div sign error
	$x = \pi$ or 3.14	A1	$x = \pi$ and no other solutions in range

Question	Answer	Marks	Guidance
9	$\frac{d}{dx}(\ln(3x^2 + 1)) = \frac{6x}{3x^2 + 1}$	B1	for $\frac{6x}{3x^2 + 1}$
	$\frac{dy}{dx} = \frac{x^2 \frac{6x}{3x^2 + 1} - 2x \ln(3x^2 + 1)}{x^4}$ or $\frac{dy}{dx} = \left(\frac{-2}{x^3}\right) \ln(3x^2 + 1) + \left(\frac{1}{x^2}\right) \frac{6x}{(3x^2 + 1)}$	M1	differentiation of a quotient or product
	$\frac{x^2 f(x) - 2x \ln(3x^2 + 1)}{x^4}$ or for $\left(-\frac{2}{x^3}\right) \ln(3x^2 + 1) + \left(\frac{1}{x^2}\right) f(x)$	A1	
	When $x = 2$, $\frac{dy}{dx} = -0.410$	A1	
	Gradient of perp = 2.436...	M1	use of $-\frac{1}{m}$ with a gradient obtained by differentiation
	When $x = 2$, $y = 0.641$ or $\frac{1}{4} \ln 13$	B1	
	Normal: $y - 0.641 = 2.436(x - 2)$	M1	Dep
	$y = 2.44x - 4.23$	A1	
10(i)	$x + 8 = 12 + x - x^2$ $x^2 = 4$, $x = \pm 2$ or $y^2 - 16y + 60 = 0$ $y = 6$ or $y = 10$	M1	correct method of solution to obtain x or y
	$x = 2$, $y = 10$ $x = -2$, $y = 6$	A2	A1 for $x = -2$ and $x = 2$ or for $y = 6$ and $y = 10$ or for either point from a correctly solved equation.
10(ii)		M1	for $12x + px^2 + qx^3$ (+c)
	$12x + \frac{x^2}{2} - \frac{x^3}{3}$ (+c)	A1	

Question	Answer	Marks	Guidance
10(iii)	$\left[12x + \frac{x^2}{2} - \frac{x^3}{3}\right]_{-2}^2 - \left(\frac{1}{2}(6+10) \times 4\right)$	B1	FT area of the trapezium unsimplified $\left(\frac{1}{2}(6+10) \times 4\right)$ or $\left[\frac{2^2}{2} + 8 \times 2\right] - \left[\frac{(-2)^2}{2} + 8 \times (-2)\right]$ (= 32)
	$\left[12 \times 2 + \frac{2^2}{2} - \frac{2^3}{3}\right] - \left[12 \times -2 + \frac{(-2)^2}{2} - \frac{(-2)^3}{3}\right]$	M1	correct use of correct limits for area under the curve using <i>their</i> integral of the form $12x + px^2 + qx^3$
	$= \frac{128}{3}$ oe	A1	
	$= \frac{32}{3}$ oe	A1	
	Alternative		
	$\int_{-2}^2 12 + x - x^2 - x - 8 \, dx$ $= \int_{-2}^2 4 - x^2 \, dx$	M1	subtraction of the two equations with intent to integrate the result
	$= \left[4x - \frac{x^3}{3}\right]_{-2}^2$	A1	
	$\left[4 \times 2 - \frac{8}{3}\right] - \left[4 \times -2 + \frac{8}{3}\right]$	M1	Dep for correct application of limits
	$= \frac{32}{3}$ oe	A1	
11(i)	$p\left(\frac{1}{2}\right) = a\left(\frac{1}{2}\right)^3 + 17\left(\frac{1}{2}\right)^2 + b\left(\frac{1}{2}\right) - 8$	M1	expression for $p\left(\frac{1}{2}\right)$
	$p(-3) = a(-3)^3 + 17(-3)^2 + b(-3) - 8$	M1	expression for $p(-3)$
	$\frac{a}{8} + \frac{17}{4} + \frac{b}{2} - 8 = 0$ $-27a + 153 - 3b - 8 = -35$	A1	both equations correct (allow equivalents and terms not collected but powers should be evaluated)
	Leading to $a = b = 6$	A1	from correct equations with evidence that both have been found correctly in order to verify that $a = b$

Question	Answer	Marks	Guidance
11(ii)	$(2x-1)(3x^2+10x+8)$	B2	B1 for $3x^2$ and +8 from factorisation or for $3x^2+10x...$ from long division
11(iii)	$(2x-1)(x+2)(3x+4)$	B1	cao
11(iv)	$\sin \theta = \frac{1}{2}$	B1	
	$\theta = 30^\circ, 150^\circ$	B2	B1 for a first correct solution B1 for a second correct solution with no extras in range $0 \leq \theta \leq 180$ and no solution arising from other factors.



ADDITIONAL MATHEMATICS**0606/11**

Paper 1

May/June 2018

MARK SCHEME

Maximum Mark: 80

Published

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MARK SCHEME NOTES

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Types of mark

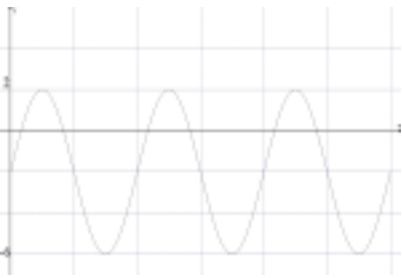
- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
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Abbreviations

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cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Partial Marks																				
1	Substitution and simplification to obtain a 3 term quadratic in one variable	M1	substitution of $y = x + 4$ or $x = y - 4$ and simplification to 3 terms.																				
	$x^2 - 2x - 8 = 0$ or $2x^2 - 4x - 16 = 0$ or $y^2 - 10y + 16 = 0$ or $y^2 - 10y + 16 = 0$	A1	correct equation of the form $ax^2 + bx + c = 0$ or $ay^2 + by + c = 0$																				
	Solution of quadratic equation	M1	M1 dep																				
	$x = 4, y = 8$ $x = -2, y = 2$	A2	A1 for each pair																				
2	Midpoint $\left(\frac{5}{2}, -1\right)$	B1																					
	Gradient of line $= -\frac{8}{3}$	B1																					
	Gradient of perp $= \frac{3}{8}$	M1																					
	Equation of perp bisector: $y + 1 = \frac{3}{8}\left(x - \frac{5}{2}\right)$	M1	M1 dep Using <i>their</i> perpendicular gradient and <i>their</i> midpoint																				
	$6x - 16y - 31 = 0$ or $-6x + 16y + 31 = 0$	A1																					
3	<table border="1"> <tr> <td>A</td><td>B</td><td>C</td><td>D</td></tr> <tr> <td></td><td>✓</td><td></td><td></td></tr> <tr> <td></td><td></td><td>✓</td><td>✓</td></tr> <tr> <td></td><td></td><td>✓</td><td></td></tr> <tr> <td>✓</td><td></td><td></td><td></td></tr> </table>	A	B	C	D		✓					✓	✓			✓		✓				4	B1 for either each row correct or each column correct – mark to candidate's advantage.
A	B	C	D																				
	✓																						
		✓	✓																				
		✓																					
✓																							
4(i)	$b = 4$	B1																					
	$c = 6$	B1																					
	$2 = a + 4\sin\frac{\pi}{2}$	M1	Evaluation of a using <i>their</i> b and <i>their</i> c and the given point.																				
	$a = -2$	A1																					

Question	Answer	Marks	Partial Marks
4(ii)		3	B1 for $-6 \leq y \leq 2$ B1 for 3 complete cycles B1 for all correct
5(i)	The number of bacteria at the start of the experiment	B1	
5(ii)	$20\,000 = 800e^{kt}$ so $\frac{20\,000}{800} = e^{2k}$ or $\ln 20\,000 = \ln 800 + \ln(e^{2k})$	M1	use of given equation and attempt to solve for e^{2k} or use logs correctly
	$2k = \ln 25$	M1	correct method to obtain $2k$
	1.61	A1	
5(iii)	$P = 800e^{3\ln 5}$	M1	Substitution of $t = 3$ in formula using <i>their</i> k
	$= 100\,000$	A1	answer in range 99800 to 100200
6(a)	$\left(\frac{\log_3 p}{\log_3 2} \times \log_3 2 \right) + \log_3 q$ or $\log_3 2^{\log_2 p} + \log_3 q$	B1	
	$\log_3 p + \log_3 q$ or $\log_3 (2^{\log_2 p} \times q)$	B1	B1 dep
	$\log_3 pq$	B1	B1 dep
6(b)	$(\log_a 5 - 1)(\log_a 5 - 3) = 0$	M1	solution of quadratic equation
	$\log_a 5 = 1, a = 5$ $\log_a 5 = 3, a = \sqrt[3]{5} \text{ or } 1.71 \text{ or } 5^{\frac{1}{3}}$	A2	A1 for $a = 5$ A1 for $a = \sqrt[3]{5} \text{ or } 1.71 \text{ or } 5^{\frac{1}{3}}$
7(i)	$\frac{1}{2} \begin{pmatrix} 3 & 2 \\ 5 & 4 \end{pmatrix}$	2	B1 for $\frac{1}{2}$ B1 for $\begin{pmatrix} 3 & 2 \\ 5 & 4 \end{pmatrix}$

Question	Answer	Marks	Partial Marks
7(ii)	$4x - 2y = \frac{5}{2}$ $-5x + 3y = \frac{7}{2}$	B1	Relating solution of these equations to matrix in (i) B1 for adapted equation or $\begin{pmatrix} 2.5 \\ 3.5 \end{pmatrix}$ or $2\begin{pmatrix} x \\ y \end{pmatrix}$
	$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 3 & 2 \\ 5 & 4 \end{pmatrix} \begin{pmatrix} 2.5 \\ 3.5 \end{pmatrix}$ or $2\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 3 & 2 \\ 5 & 4 \end{pmatrix} \begin{pmatrix} 5 \\ 7 \end{pmatrix}$	M1	Correct method for pre-multiplication by <i>their</i> inverse matrix.
	$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 7.25 \\ 13.25 \end{pmatrix}$ or $\begin{pmatrix} \frac{29}{4} \\ \frac{53}{4} \end{pmatrix}$ $x = 7.25, y = 13.25$	A2	A1 for each. Condone in matrix form.
8(a)	$3(2\mathbf{i} - 5\mathbf{j}) - 4(\mathbf{i} - 3\mathbf{j})$	M1	For expansion and collection of terms
	$3\mathbf{p} - 4\mathbf{q} = 2\mathbf{i} - 3\mathbf{j}$	A1	
	Magnitude of their $2\mathbf{i} - 3\mathbf{j}$ $\sqrt{2^2 + (-3)^2}$	M1	For method to find magnitude
	Unit vector = $\frac{2\mathbf{i} - 3\mathbf{j}}{\sqrt{13}}$	A1	
8(b)(i)	$v^2 = 2.73^2 + 1.25^2$	B1	Correct use of Pythagoras
	$v = 3.00$	B1	
8(b)(ii)	$\tan \theta = \frac{1.25}{2.73}$ oe	M1	Use of a trig function to obtain a relevant angle
	Angle to $AB = 24.6^\circ$ or 0.429 radians	A1	
9(i)	$256x^8 - 64x^6 + 7x^4$	3	B1 for each term

Question	Answer	Marks	Partial Marks
9(ii)	$\frac{1}{x^4} + \frac{2}{x^2} + 1$	B1	
	$(256x^8 - 64x^6 + 7x^4)\left(\frac{1}{x^4} + \frac{2}{x^2} + 1\right)$ $(256 \times 1 - 64 \times 2 + 7 \times 1)x^4$	M1	M1 for three correctly obtained products leading to terms in x^4 using <i>their</i> $256x^8 - 64x^6 + 7x^4$ and <i>their</i> $\frac{1}{x^4} + \frac{2}{x^2} + 1$
	Coefficient of x^4 is $256 - 128 + 7 = 135$	A1	
10(a)	$\frac{5+6\sqrt{5}}{6+\sqrt{5}} \times \frac{6-\sqrt{5}}{6-\sqrt{5}}$	M1	for rationalisation
	$= \frac{30 - 5\sqrt{5} + 36\sqrt{5} - 30}{31}$	M1	M1dep for expanding the numerator to obtain four terms.
	$= \frac{31\sqrt{5}}{31} = \sqrt{5}$	A1	A1 for $\sqrt{5}$ from correct working
10(b)	$\sqrt{3} \times (\sqrt{2})^6 \times \sqrt{2} = \sqrt{6} \times 2^3$		
	$8\sqrt{6}$	B2	B1 for $\sqrt{6}$ from $\sqrt{3} \times \sqrt{2}$ B1 for 8 from $(\sqrt{2})^6$ or 2^3

Question	Answer	Marks	Partial Marks
10(c)	EITHER: $x^2 + \sqrt{2}x - 4 = 0$	B1	3 term quadratic equation equated to zero
	$x = \frac{-\sqrt{2} \pm \sqrt{18}}{2}$	M1	use of the quadratic formula
	for use of $\sqrt{18} = 3\sqrt{2}$	M1	M1 dep
	$\sqrt{2}, -2\sqrt{2}$	A1	For both from full working
	OR: $x^2 + \sqrt{2}x - 4 = 0$	B1	
	$\left(x + \frac{\sqrt{2}}{2}\right)^2 = 4 + \frac{1}{2}$ $x = \pm \frac{3}{\sqrt{2}} - \frac{\sqrt{2}}{2}$	M1	Correct use of completing the square method
	$x = -\frac{4}{\sqrt{2}}, \frac{2}{\sqrt{2}}$	M1	M1dep for dealing with $\sqrt{2}$ in denominator
	$x = \sqrt{2}, -2\sqrt{2}$	A1	
11(i)	$\frac{dy}{dx} = 16 - \frac{54}{x^3}$	M1	for $\frac{dy}{dx} = 16 \pm \frac{p}{x^3}$
	Equating to zero and obtaining x^3	M1	M1dep
	$x = \frac{3}{2}, y = 36$	A2	A1 for each

Question	Answer	Marks	Partial Marks
11(ii)	EITHER: When $x = 1$, $y = 43$ When $x = 3$, $y = 51$	B1	B1 for both
	$\left(\frac{1}{2}(43+51) \times 2\right) - \int_1^3 16x + \frac{27}{x^2} dx$		
	Area of trapezium $= \left(\frac{1}{2}(43+51) \times 2\right)$ oe	B1	FT from <i>their P</i> and <i>their Q</i>
	Integration to find area under curve	M1	for $\left[px^2 + \frac{q}{x}\right]$
	$= \left[8x^2 - \frac{27}{x}\right]$	A1	Integration correct
	$= \left[8 \times 3^2 - \frac{27}{3}\right] - \left[8 \times 1^2 - \frac{27}{1}\right]$	M1	M1dep for application of limits
	Required area $= 94 - 82$ $= 12$	A1	
	OR: When $x = 1$, $y = 43$ When $x = 3$, $y = 51$	B1	B1 for both
	Equation of PQ : $y = 4x + 39$	B1	Equation of line FT from <i>their P</i> and <i>their Q</i>
	Integration of their $4x + 39 - 16x - \frac{27}{x^2}$	M1	for $\left[px + qx^2 + \frac{r}{x}\right]$
	$= \left[39x - 6x^2 + \frac{27}{x}\right]$	A1	All correct
	$= \left[39 \times 3 - 6 \times 3^2 + \frac{27}{3}\right]$ $- \left[39 \times 1 - 6 \times 1^2 + \frac{27}{1}\right]$	M1	M1dep for application of limits
	Required area $= 72 - 60$ $= 12$	A1	

Question	Answer	Marks	Partial Marks
12	$\frac{dy}{dx} = (2x-5)^{\frac{1}{2}} \quad (+c)$	M1	for $k(2x-5)^{\frac{1}{2}}$,
	for $(2x-5)^{\frac{1}{2}}$	A1	
	Substitution to obtain arbitrary constant	M1	M1 dep Using $\frac{dy}{dx} = 6$ when $x = \frac{9}{2}$
	$\left(\frac{dy}{dx}\right) = (2x-5)^{\frac{1}{2}} + 4$	A1	for correct $\frac{dy}{dx}$
	Integration of <i>their</i> $k(2x-5)^{\frac{1}{2}} + c$	M1	M1 dep on first M1 for integration of $k(2x-5)^{\frac{1}{2}}$ to obtain $m(2x-5)^{\frac{3}{2}}$
	$y = \frac{1}{3}(2x-5)^{\frac{3}{2}} + 4x \quad (+d)$	A1	for $\frac{1}{3}(2x-5)^{\frac{3}{2}} + 4x$ FT <i>their</i> (non -zero) constant
	Finding constant	M1	M1 dep for obtaining arbitrary constant for $m(2x-5)^{\frac{3}{2}} + nx + d$ using $x = \frac{9}{2}, \quad y = \frac{2}{3}$
	$y = \frac{1}{3}(2x-5)^{\frac{3}{2}} + 4x - 20$	A1	for correct equation



Cambridge Assessment International Education
Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS

0606/12

Paper 1

May/June 2018

MARK SCHEME

Maximum Mark: 80

Published

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This document consists of **10** printed pages.

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GENERIC MARKING PRINCIPLE 1:

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- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

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GENERIC MARKING PRINCIPLE 3:

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- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

MARK SCHEME NOTES

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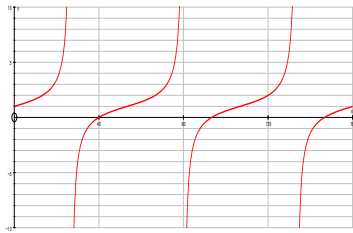
Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Partial Marks
1(i)	$\frac{\pi}{3}$ or 60°	B1	
1(ii)		3	<p>B1 for 3 asymptotes at $x = 30^\circ$, 90° and 150°; the curve must approach but not cross all 3 of the asymptotes and be in the 1st and 4th quadrants</p> <p>B1 for starting at $(0, 1)$ and finishing at $(180, 1)$</p> <p>B1 for all correct</p>
2	For an attempt to obtain an equation in x only	M1	
	$9x^2 - (k+1)x + 4 = 0$	A1	correct 3 term equation
	$(k+1)^2 - (4 \times 9 \times 4)$	M1	M1dep for correct use of $b^2 - 4ac$ oe
	Critical values $k = 11$, $k = -13$	A1	
	$-13 < k < 11$	A1	For the correct range
3	$e^y = ax^2 + b$	B1	may be implied, $b \neq 0$
	either $3 = 5a + b$ $1 = 3a + b$ or Gradient = 1, so $a = 1$	M1	correct attempt to find a or b by use of simultaneous equations or finding the gradient and equating it to a
	Coefficient of x^2 is 1	A1	
	Intercept is -2	A1	
	$y = \ln(x^2 - 2)$	A1	For correct form
4(i)	$3 = \ln(5t + 3)$ $e^3 = 5t + 3$ or better	B1	
	$t = 3.42$	B1	
4(ii)	$\frac{dx}{dt} = \frac{5}{5t + 3}$	M1	for $\frac{k_1}{5t + 3}$
	When $t = 0$, $\frac{dx}{dt} = \frac{5}{3}$, 1.67 or better	A1	all correct

Question	Answer	Marks	Partial Marks
4(iii)	If $t > 0$ each term in $\frac{k_1}{5t+3} > 0$ so never negative oe	B1	dep on M1 in (ii) FT on <i>their</i> $\frac{k_1}{5t+3}$, provided $k_1 > 0$
4(iv)	$\frac{d^2x}{dt^2} = \frac{k_2}{(5t+3)^2}$	M1	
	$\frac{d^2x}{dt^2} = -\frac{25}{(5t+3)^2}$ When $t = 0$, $\frac{d^2x}{dt^2} = -\frac{25}{9}$ or -2.78	A1	all correct
5(i)	$a = 243, b = -45, c = \frac{10}{3}$	3	B1 for each coefficient, must be simplified
5(ii)	$\left(243 - \frac{45}{x} + \frac{10}{3x^2}\right)(4 + 36x + 81x^2)$	B1	For $(4 + 36x + 81x^2)$
	for having 3 terms independent of x	M1	
	Independent term is $972 - 1620 + 270 = -378$	A1	
6	attempt to differentiate quotient or equivalent product	M1	
	$\frac{d}{dx}(2x-1)^{\frac{1}{2}} = (2x-1)^{-\frac{1}{2}}$ for a quotient $\frac{d}{dx}(2x-1)^{-\frac{1}{2}} = -(2x-1)^{-\frac{3}{2}}$ for a product	B1	
	either $\frac{dy}{dx} = \frac{\sqrt{2x-1} - (x+2)\left[(2x-1)^{-\frac{1}{2}}\right]}{(\sqrt{2x-1})^2}$ or $\frac{dy}{dx} = (2x-1)^{-\frac{1}{2}} - (x+2)\left[(2x-1)^{-\frac{3}{2}}\right]$	A1	All other terms correct
	When $\frac{dy}{dx} = 0$, $2x-1 = x+2$	M1	equate to zero and attempt to solve
	$x = 3$	A1	
	$y = \sqrt{5}, \frac{5}{\sqrt{5}}, 2.24$	A1	

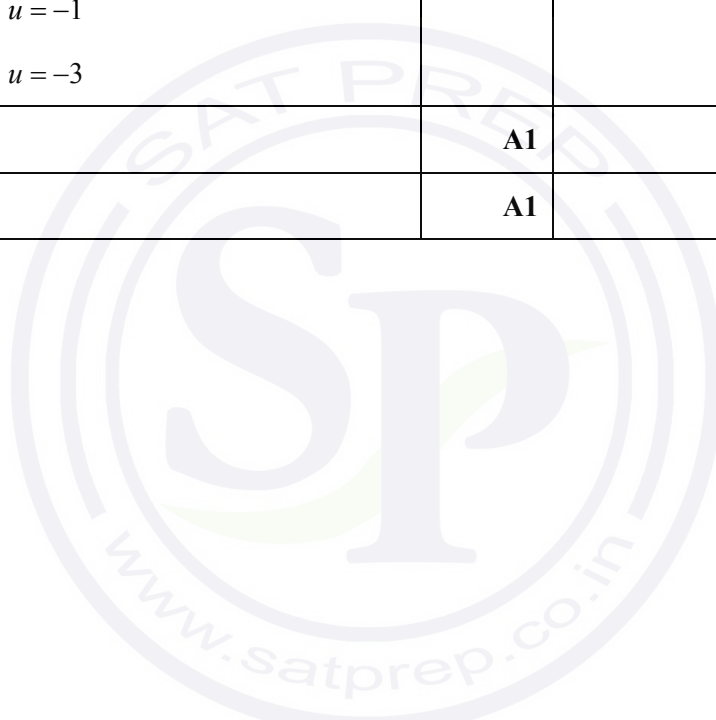
Question	Answer	Marks	Partial Marks
7(i)	1000	B1	
7(ii)	$2000 = 1000e^{\frac{t}{4}}$	B1	
	$t = 4 \ln 2, \ln 16$	M1	For $4 \ln k$ or $\ln k^4, k > 0$
	2.77	A1	
7(iii)	$B = 1000e^2$ $= 7389, 7390$	B1	
8(a)	$3(1 - \sin^2 \theta) + 4 \sin \theta = 4$	M1	use of correct identity
	$(3 \sin \theta - 1)(\sin \theta - 1) = 0$ $\sin \theta = \frac{1}{3}, \sin \theta = 1$	M1	For attempt to solve a 3 term quadratic equation in $\sin \theta$ to obtain $\sin \theta =$
	$\theta = 19.5^\circ, 160.5^\circ$	A1	
	90°	A1	
8(b)	$\tan 2\phi = \sqrt{3}$ $2\phi = \frac{\pi}{3}, -\frac{2\pi}{3}$	M1	obtaining an equation in $\tan 2\phi$ and correct attempt to solve for one solution to reach $2\phi = k$
	for one correct solution $\phi = \frac{\pi}{6}, \text{ or } 0.524$	A1	
	for attempt at a second solution	M1	
	$\phi = -\frac{\pi}{3}, \text{ or } -1.05$	A1	for a correct second solution and no other solutions within the range
9(a)(i)	1000	B1	
9(a)(ii)	for use of power rule	M1	
	for addition or subtraction rule	M1	dep on previous M1
	$\lg \frac{1000a}{b^2}$	A1	Allow $\lg \frac{10^3 a}{b^2}$
9(b)(i)	$x^2 - 5x + 6 = 0$	M1	For attempt to obtain a quadratic equation and solve
	$x = 3, x = 2$	A1	for both

Question	Answer	Marks	Partial Marks
9b(ii)	$(\log_4 a)^2 - 5\log_4 a + 6 = 0$	M1	For the connection with (i) and attempt to deal with at least one logarithm correctly, either $4^{\text{their } 3}$ or $4^{\text{their } 2}$
	$a = 64$	A1	
	$a = 16$	A1	
10(i)	$AC^2 = (4\sqrt{3} - 5)^2 + (4\sqrt{3} + 5)^2$	M1	For attempt to use the cosine rule
	$-2(4\sqrt{3} - 5)(4\sqrt{3} + 5)\cos 60^\circ$	A1	For all correct unsimplified
	$AC^2 = 123$	M1	M1 dep for attempt to evaluate without use of calculator
	$AC = \sqrt{123}$	A1	
	ALTERNATIVE METHOD		
	Taking D as the foot of the perpendicular from A : Find AD , BD , DC $AC^2 = AD^2 + DC^2$	M1	For a complete method to get AC^2
	$AC^2 = \left(\frac{12 - 5\sqrt{3}}{2}\right)^2 + \left(\frac{15 + 4\sqrt{3}}{2}\right)^2$	A1	For all correct unsimplified
	$AC^2 = 123$	M1	M1 dep for attempt to evaluate without use of calculator
	$AC = \sqrt{123}$	A1	

Question	Answer	Marks	Partial Marks
10(ii)	$\frac{AC}{\sin 60^\circ} = \frac{4\sqrt{3}-5}{\sin ACB}$ or $\sin ACB = \frac{AD}{AC}$	M1	For attempt at the sine rule or trigonometry involving right-angled triangles
	For attempt at cosec	M1	dep on first M mark $\operatorname{cosec} ACB = \frac{2\sqrt{123}}{\sqrt{3}(4\sqrt{3}-5)}$ or $\frac{2\sqrt{41}}{(4\sqrt{3}-5)}$ oe
	$\operatorname{cosec} ACB = \frac{2}{\sqrt{3}} \frac{\sqrt{123}}{(4\sqrt{3}-5)} \times \frac{4\sqrt{3}+5}{4\sqrt{3}+5}$	M1	dep on previous M mark for a statement involving rationalisation using $a\sqrt{3}+b$
	$= \frac{2\sqrt{41}}{23} (4\sqrt{3}+5)$	A1	For rationalisation using $\frac{4\sqrt{3}+5}{4\sqrt{3}+5}$ oe and simplification
	ALTERNATIVE METHOD		
	$\frac{1}{2} (4\sqrt{3}-5)(4\sqrt{3}+5) \sin 60 = \frac{23\sqrt{3}}{4}$	M1	Area of ABC
	$\frac{1}{2} \sqrt{123} (4\sqrt{3}+5) \sin ACB = \frac{23\sqrt{3}}{4}$	M1	For attempt at a second area of ABC and equating to first area
	For attempt at cosec	M1	dep on first 2 M marks
	$= \frac{2\sqrt{41}}{23} (4\sqrt{3}+5)$	A1	Need to be convinced no calculator is being used in simplification

Question	Answer	Marks	Partial Marks
11	When $x = 0$, $y = \frac{1}{2}$	B1	For $y = \frac{1}{2}$
	$\frac{dy}{dx} = \frac{1}{2}e^{4x}$	B1	
	$\frac{dy}{dx} = \frac{1}{2}$, Gradient of normal = -2	B1	FT on <i>their</i> $\frac{dy}{dx}$, must be numeric
	either: Normal $y - \frac{1}{2} = -2x$ or: Gradient of normal = $-\frac{OA}{OB}$	M1	For an attempt at a normal equation passing through <i>their</i> $\left(0, \frac{1}{2}\right)$ and a substitution of $y = 0$
	When $y = 0$, $x = \frac{1}{4}$	A1	
	EITHER: $\int_0^{\frac{1}{4}} \frac{1}{8}e^{4x} + \frac{3}{8} dx$	M1	For attempt to integrate to obtain $k_1e^{4x} + \frac{3}{8}x$, $k_1 \neq \frac{1}{8}$, $k_1 \neq \frac{1}{2}$
	$\left[\frac{1}{32}e^{4x} + \frac{3x}{8} \right]_0^{\frac{1}{4}}$	A1	For correct integration
	Use of limits	M1	M1dep
	For area of triangle = $\frac{1}{16}$	B1	FT on <i>their</i> $x = \frac{1}{4}$
	$= \frac{e}{32}$	A1	final answer in correct form
	OR: $\int_0^{\frac{1}{4}} \frac{1}{8}e^{4x} + \frac{3}{8} - \frac{1}{2} + 2x dx$	M1	For attempt at subtraction and attempt to integrate to obtain $k_1e^{4x} + \frac{3}{8}x + k_2x + k_3x^2$, $k_1 \neq \frac{1}{8}$
	$\left[\frac{1}{32}e^{4x} - \frac{1}{8}x + x^2 \right]_0^{\frac{1}{4}}$	A2	-1 for each error for integration
	for use of limits	M1	M1dep
	$= \frac{e}{32}$	A1	final answer in correct form

Question	Answer	Marks	Partial Marks
12(a)	$p = \frac{1}{4}$	B1	
	$p + q - 4q + 6 = 4$	B1	FT on <i>their p</i>
	$q = \frac{3}{4}$	B1	
12(b)	$\left(x^{\frac{1}{3}} + 3\right)\left(x^{\frac{1}{3}} + 1\right) = 0$	M1	For attempt to factorise and solve, or solve using the quadratic formula oe, a quadratic in $x^{\frac{1}{3}}$ or u
	$x^{\frac{1}{3}} = -1$ or $u = -1$ $x^{\frac{1}{3}} = -3$ or $u = -3$	A1	For both
	$x = -1$	A1	
	$x = -27$	A1	





ADDITIONAL MATHEMATICS

0606/13

Paper 1

May/June 2018

MARK SCHEME

Maximum Mark: 80

Published

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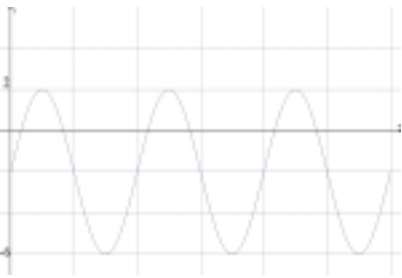
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Question	Answer	Marks	Partial Marks																				
1	Substitution and simplification to obtain a 3 term quadratic in one variable	M1	substitution of $y = x + 4$ or $x = y - 4$ and simplification to 3 terms.																				
	$x^2 - 2x - 8 = 0$ or $2x^2 - 4x - 16 = 0$ or $y^2 - 10y + 16 = 0$ or $y^2 - 10y + 16 = 0$	A1	correct equation of the form $ax^2 + bx + c = 0$ or $ay^2 + by + c = 0$																				
	Solution of quadratic equation	M1	M1 dep																				
	$x = 4, y = 8$ $x = -2, y = 2$	A2	A1 for each pair																				
2	Midpoint $\left(\frac{5}{2}, -1\right)$	B1																					
	Gradient of line $= -\frac{8}{3}$	B1																					
	Gradient of perp $= \frac{3}{8}$	M1																					
	Equation of perp bisector: $y + 1 = \frac{3}{8}\left(x - \frac{5}{2}\right)$	M1	M1 dep Using <i>their</i> perpendicular gradient and <i>their</i> midpoint																				
	$6x - 16y - 31 = 0$ or $-6x + 16y + 31 = 0$	A1																					
3	<table border="1"> <tr> <td>A</td><td>B</td><td>C</td><td>D</td></tr> <tr> <td></td><td>✓</td><td></td><td></td></tr> <tr> <td></td><td></td><td>✓</td><td>✓</td></tr> <tr> <td></td><td></td><td>✓</td><td></td></tr> <tr> <td>✓</td><td></td><td></td><td></td></tr> </table>	A	B	C	D		✓					✓	✓			✓		✓				4	B1 for either each row correct or each column correct – mark to candidate's advantage.
A	B	C	D																				
	✓																						
		✓	✓																				
		✓																					
✓																							
4(i)	$b = 4$	B1																					
	$c = 6$	B1																					
	$2 = a + 4 \sin \frac{\pi}{2}$	M1	Evaluation of a using <i>their</i> b and <i>their</i> c and the given point.																				
	$a = -2$	A1																					

Question	Answer	Marks	Partial Marks
4(ii)		3	B1 for $-6 \leq y \leq 2$ B1 for 3 complete cycles B1 for all correct
5(i)	The number of bacteria at the start of the experiment	B1	
5(ii)	$20\,000 = 800e^{kt}$ so $\frac{20\,000}{800} = e^{2k}$ or $\ln 20\,000 = \ln 800 + \ln(e^{2k})$	M1	use of given equation and attempt to solve for e^{2k} or use logs correctly
	$2k = \ln 25$	M1	correct method to obtain $2k$
	1.61	A1	
5(iii)	$P = 800e^{3\ln 5}$	M1	Substitution of $t = 3$ in formula using <i>their</i> k
	$= 100\,000$	A1	answer in range 99800 to 100200
6(a)	$\left(\frac{\log_3 p}{\log_3 2} \times \log_3 2 \right) + \log_3 q$ or $\log_3 2^{\log_2 p} + \log_3 q$	B1	
	$\log_3 p + \log_3 q$ or $\log_3 (2^{\log_2 p} \times q)$	B1	B1 dep
	$\log_3 pq$	B1	B1 dep
6(b)	$(\log_a 5 - 1)(\log_a 5 - 3) = 0$	M1	solution of quadratic equation
	$\log_a 5 = 1, a = 5$ $\log_a 5 = 3, a = \sqrt[3]{5} \text{ or } 1.71 \text{ or } 5^{\frac{1}{3}}$	A2	A1 for $a = 5$ A1 for $a = \sqrt[3]{5} \text{ or } 1.71 \text{ or } 5^{\frac{1}{3}}$
7(i)	$\frac{1}{2} \begin{pmatrix} 3 & 2 \\ 5 & 4 \end{pmatrix}$	2	B1 for $\frac{1}{2}$ B1 for $\begin{pmatrix} 3 & 2 \\ 5 & 4 \end{pmatrix}$

Question	Answer	Marks	Partial Marks
7(ii)	$4x - 2y = \frac{5}{2}$ $-5x + 3y = \frac{7}{2}$	B1	Relating solution of these equations to matrix in (i) B1 for adapted equation or $\begin{pmatrix} 2.5 \\ 3.5 \end{pmatrix}$ or $2\begin{pmatrix} x \\ y \end{pmatrix}$
	$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 3 & 2 \\ 5 & 4 \end{pmatrix} \begin{pmatrix} 2.5 \\ 3.5 \end{pmatrix}$ or $2\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 3 & 2 \\ 5 & 4 \end{pmatrix} \begin{pmatrix} 5 \\ 7 \end{pmatrix}$	M1	Correct method for pre-multiplication by <i>their</i> inverse matrix.
	$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 7.25 \\ 13.25 \end{pmatrix}$ or $\begin{pmatrix} \frac{29}{4} \\ \frac{53}{4} \end{pmatrix}$ $x = 7.25, y = 13.25$	A2	A1 for each. Condone in matrix form.
8(a)	$3(2\mathbf{i} - 5\mathbf{j}) - 4(\mathbf{i} - 3\mathbf{j})$	M1	For expansion and collection of terms
	$3\mathbf{p} - 4\mathbf{q} = 2\mathbf{i} - 3\mathbf{j}$	A1	
	Magnitude of their $2\mathbf{i} - 3\mathbf{j}$ $\sqrt{2^2 + (-3)^2}$	M1	For method to find magnitude
	Unit vector = $\frac{2\mathbf{i} - 3\mathbf{j}}{\sqrt{13}}$	A1	
8(b)(i)	$v^2 = 2.73^2 + 1.25^2$	B1	Correct use of Pythagoras
	$v = 3.00$	B1	
8(b)(ii)	$\tan \theta = \frac{1.25}{2.73}$ oe	M1	Use of a trig function to obtain a relevant angle
	Angle to $AB = 24.6^\circ$ or 0.429 radians	A1	
9(i)	$256x^8 - 64x^6 + 7x^4$	3	B1 for each term

Question	Answer	Marks	Partial Marks
9(ii)	$\frac{1}{x^4} + \frac{2}{x^2} + 1$	B1	
	$(256x^8 - 64x^6 + 7x^4)\left(\frac{1}{x^4} + \frac{2}{x^2} + 1\right)$ $(256 \times 1 - 64 \times 2 + 7 \times 1)x^4$	M1	M1 for three correctly obtained products leading to terms in x^4 using <i>their</i> $256x^8 - 64x^6 + 7x^4$ and <i>their</i> $\frac{1}{x^4} + \frac{2}{x^2} + 1$
	Coefficient of x^4 is $256 - 128 + 7 = 135$	A1	
10(a)	$\frac{5+6\sqrt{5}}{6+\sqrt{5}} \times \frac{6-\sqrt{5}}{6-\sqrt{5}}$	M1	for rationalisation
	$= \frac{30 - 5\sqrt{5} + 36\sqrt{5} - 30}{31}$	M1	M1dep for expanding the numerator to obtain four terms.
	$= \frac{31\sqrt{5}}{31} = \sqrt{5}$	A1	A1 for $\sqrt{5}$ from correct working
10(b)	$\sqrt{3} \times (\sqrt{2})^6 \times \sqrt{2} = \sqrt{6} \times 2^3$		
	$8\sqrt{6}$	B2	B1 for $\sqrt{6}$ from $\sqrt{3} \times \sqrt{2}$ B1 for 8 from $(\sqrt{2})^6$ or 2^3

Question	Answer	Marks	Partial Marks
10(c)	EITHER: $x^2 + \sqrt{2}x - 4 = 0$	B1	3 term quadratic equation equated to zero
	$x = \frac{-\sqrt{2} \pm \sqrt{18}}{2}$	M1	use of the quadratic formula
	for use of $\sqrt{18} = 3\sqrt{2}$	M1	M1 dep
	$\sqrt{2}, -2\sqrt{2}$	A1	For both from full working
	OR: $x^2 + \sqrt{2}x - 4 = 0$	B1	
	$\left(x + \frac{\sqrt{2}}{2}\right)^2 = 4 + \frac{1}{2}$ $x = \pm \frac{3}{\sqrt{2}} - \frac{\sqrt{2}}{2}$	M1	Correct use of completing the square method
	$x = -\frac{4}{\sqrt{2}}, \frac{2}{\sqrt{2}}$	M1	M1dep for dealing with $\sqrt{2}$ in denominator
	$x = \sqrt{2}, -2\sqrt{2}$	A1	
11(i)	$\frac{dy}{dx} = 16 - \frac{54}{x^3}$	M1	for $\frac{dy}{dx} = 16 \pm \frac{p}{x^3}$
	Equating to zero and obtaining x^3	M1	M1dep
	$x = \frac{3}{2}, y = 36$	A2	A1 for each

Question	Answer	Marks	Partial Marks
11(ii)	EITHER: When $x = 1$, $y = 43$ When $x = 3$, $y = 51$	B1	B1 for both
	$\left(\frac{1}{2}(43+51) \times 2\right) - \int_1^3 16x + \frac{27}{x^2} dx$		
	Area of trapezium $= \left(\frac{1}{2}(43+51) \times 2\right)$ oe	B1	FT from <i>their P</i> and <i>their Q</i>
	Integration to find area under curve	M1	for $\left[px^2 + \frac{q}{x}\right]$
	$= \left[8x^2 - \frac{27}{x}\right]$	A1	Integration correct
	$= \left[8 \times 3^2 - \frac{27}{3}\right] - \left[8 \times 1^2 - \frac{27}{1}\right]$	M1	M1dep for application of limits
	Required area $= 94 - 82$ $= 12$	A1	
	OR: When $x = 1$, $y = 43$ When $x = 3$, $y = 51$	B1	B1 for both
	Equation of PQ : $y = 4x + 39$	B1	Equation of line FT from <i>their P</i> and <i>their Q</i>
	Integration of their $4x + 39 - 16x - \frac{27}{x^2}$	M1	for $\left[px + qx^2 + \frac{r}{x}\right]$
	$= \left[39x - 6x^2 + \frac{27}{x}\right]$	A1	All correct
	$= \left[39 \times 3 - 6 \times 3^2 + \frac{27}{3}\right]$ $- \left[39 \times 1 - 6 \times 1^2 + \frac{27}{1}\right]$	M1	M1dep for application of limits
	Required area $= 72 - 60$ $= 12$	A1	

Question	Answer	Marks	Partial Marks
12	$\frac{dy}{dx} = (2x-5)^{\frac{1}{2}} \quad (+c)$	M1	for $k(2x-5)^{\frac{1}{2}}$,
	for $(2x-5)^{\frac{1}{2}}$	A1	
	Substitution to obtain arbitrary constant	M1	M1 dep Using $\frac{dy}{dx} = 6$ when $x = \frac{9}{2}$
	$\left(\frac{dy}{dx}\right) = (2x-5)^{\frac{1}{2}} + 4$	A1	for correct $\frac{dy}{dx}$
	Integration of <i>their</i> $k(2x-5)^{\frac{1}{2}} + c$	M1	M1 dep on first M1 for integration of $k(2x-5)^{\frac{1}{2}}$ to obtain $m(2x-5)^{\frac{3}{2}}$
	$y = \frac{1}{3}(2x-5)^{\frac{3}{2}} + 4x \quad (+d)$	A1	for $\frac{1}{3}(2x-5)^{\frac{3}{2}} + 4x$ FT <i>their</i> (non -zero) constant
	Finding constant	M1	M1 dep for obtaining arbitrary constant for $m(2x-5)^{\frac{3}{2}} + nx + d$ using $x = \frac{9}{2}, \quad y = \frac{2}{3}$
	$y = \frac{1}{3}(2x-5)^{\frac{3}{2}} + 4x - 20$	A1	for correct equation

ADDITIONAL MATHEMATICS**0606/12**

Paper 12

March 2018

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:

Marks awarded are always **whole marks** (not half marks, or other fractions).

GENERIC MARKING PRINCIPLE 3:

Marks must be awarded **positively**:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:

Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:

Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

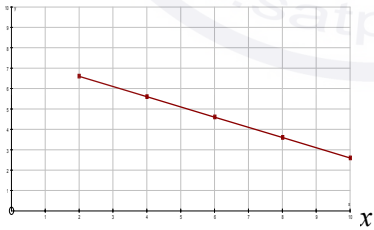
Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	attempt at $p(2)$ or $p(-3)$	M1	
	$2p(2) = p(-3)$	M1	attempt at correct relationship
	$22 = a - b$	A1	may be implied, allow unsimplified
	$p(-1) = 0$ $a + b = -2$	B1	B1 for $a + b = -2$, allow unsimplified
	$a = 10$ $b = -12$	A1	A1 for both
2(i)	$k \cos 3x$	M1	
	$\frac{dy}{dx} = 15 \cos 3x$	A1	A1 all correct
2(ii)	When $x = \frac{\pi}{3}$, $y = 4$	B1	for $y = 4$
	attempt to find the equation of the tangent	M1	
	$\frac{dy}{dx} = -15$ $y - 4 = -15\left(x - \frac{\pi}{3}\right)$ Equation of tangent $\left(y = -15x + 5\pi + 4 \text{ or } \right)$ $\left(y = -15x + 19.7 \right)$	A1	A1FT for correct equation, using <i>their</i> $\frac{dy}{dx}$, allow unsimplified
3(a)	$\frac{18 + 12\sqrt{5} - 6\sqrt{5} - 20}{4 - \sqrt{5}}$	M1	attempt to deal with the numerator
	$\frac{6\sqrt{5} - 2}{4 - \sqrt{5}} \times \frac{4 + \sqrt{5}}{4 + \sqrt{5}}$ $\frac{22\sqrt{5} + 22}{11}$	M1	attempt to rationalise
	$2\sqrt{5} + 2$	A1	must be convinced a calculator has not been used
3(b)	$AC^2 = (6 - 2\sqrt{3})^2 + (6 + 2\sqrt{3})^2$ $-2(6 - 2\sqrt{3})(6 + 2\sqrt{3})\left(-\frac{1}{2}\right)$	M1	application of the cosine rule
	simplification of surds	M1	M1Dep
	$AC = 2\sqrt{30}$	A1	

Question	Answer	Marks	Guidance
4(i)	-2	B1	
	$-\frac{1}{2} \leq x \leq \frac{1}{2}$	B1	
4(ii)	attempt to differentiate a quotient	M1	
	for $\frac{8x}{4x^2 - 1}$	B1	
	$\frac{dy}{dx} = \frac{(x+2) \frac{8x}{(4x^2 - 1)} - \ln(4x^2 - 1)}{(x+2)^2}$	A1	everything else correct
4(iii)	When $x = 2$ $\frac{dy}{dx} = \frac{4}{15} - \frac{\ln 15}{16}$ or 0.0974	M1	attempt to evaluate $\frac{dy}{dx}$ when $x = 2$ and attempt to use method of small changes
	$\partial y = 0.0974h$	A1	cao
5(i)	$n = 10$	B1	
	$10 \times 2^9 \times a = -1280$	M1	attempt to equate second terms
	$a = -\frac{1}{4}$	A1	
	${}^{10}C_2 \times 2^8 \times \left(-\frac{1}{4}\right)^2 = 720$	M1	attempt to equate third terms
	$b = 720$	A1	
5(ii)	$\left[(1024 - 1280x + 720x^2)\right] \left(\frac{1}{x^2} - 2 + x^2\right)$	B1	expansion of $\left(x - \frac{1}{x}\right)^2$
	Independent term = $720 - 2048$	M1	attempt to find independent term, must be considering 2 terms
	= -1328	A1	Must be identified

Question	Answer	Marks	Guidance
6(i)	$\mathbf{c} - \mathbf{a}$	B1	
6(ii)	attempt to use the ratio	M1	
	$\overrightarrow{OM} = \mathbf{a} + \frac{2}{3}(\mathbf{c} - \mathbf{a})$ or $\mathbf{c} - \frac{1}{3}(\mathbf{c} - \mathbf{a})$ $\left(= \frac{2}{3}\mathbf{c} + \frac{1}{3}\mathbf{a} \right)$	A1	allow unsimplified
6(iii)	$\overrightarrow{OM} = \frac{3}{5}\mathbf{b}$	B1	
6(iv)	$\frac{3}{5}\mathbf{b} = \frac{2}{3}\mathbf{c} + \frac{1}{3}\mathbf{a}$	M1	attempt to equate <i>their</i> (ii) and (iii)
	$5\mathbf{a} + 10\mathbf{c} = 9\mathbf{b}$	A1	Must be convinced from simplification
6(v)	$\overrightarrow{AB} = \mathbf{b} - \mathbf{a}$ $= \frac{5}{9}\mathbf{a} + \frac{10}{9}\mathbf{c} - \mathbf{a}$	M1	use of (iv) with $\mathbf{b} - \mathbf{a}$ or $\mathbf{a} - \mathbf{b}$
	$= -\frac{4}{9}\mathbf{a} + \frac{10}{9}\mathbf{c}$	A1	
7(a)	$2a^2 - 4a = 6 - 3a$ $2a^2 - a - 6 = 0$	M1	attempt to use determinant correctly, obtain a 3 term quadratic equation and attempt to solve correctly
	$a = 2$	A1	
	$a = -\frac{3}{2}$	A1	
7(b)(i)	$\frac{1}{5} \begin{pmatrix} 4 & -1 \\ -3 & 2 \end{pmatrix}$	B2	B1 for $\frac{1}{5}$ B1 for $\begin{pmatrix} 4 & -1 \\ -3 & 2 \end{pmatrix}$
7(b)(ii)	$\mathbf{A}^{-1}\mathbf{AC} = \mathbf{A}^{-1}\mathbf{B}$	M1	for pre-multiplying
	$\mathbf{C} = \frac{1}{5} \begin{pmatrix} 4 & -1 \\ -3 & 2 \end{pmatrix} \begin{pmatrix} 2 & 0 \\ -3 & 5 \end{pmatrix}$	M1	M1Dep for attempt at matrix multiplication, at least 2 terms correct, allow with <i>their</i> inverse
	$= \frac{1}{5} \begin{pmatrix} 11 & -5 \\ -12 & 10 \end{pmatrix}$ oe	A1	

Question	Answer	Marks	Guidance
7(c)	$\begin{pmatrix} -\frac{3}{4} & 0 \\ 0 & -\frac{3}{4} \end{pmatrix}$	B1	
8(i)	for attempt to integrate to obtain $k_1 e^{2t} + k_2 t^2$	M1	
	$x = 6e^{2t} - 24t^2 \quad (+c)$	A1	all correct, condone omission of $+c$
	When $t = 0$, $x = 0 \therefore c = -6$	M1	M1Dep for attempt to find c
	$x = 6e^{2t} - 24t^2 - 6$	A1	
8(ii)	$\frac{d^2x}{dt^2} = 24e^{2t} - 48$	M1	attempt to differentiate to obtain $k_1 e^{2t} + k_2$
	When acceleration = 0, $e^{2t} = 2$ oe	M1	equating to zero and attempt to solve
	$t = \frac{1}{2} \ln 2$ or $t = \ln \sqrt{2}$ or 0.347	A1	
8(iii)	substitution of <i>their</i> (ii) into given equation for v	M1	
	$v = 24 - 24 \ln 2$ or $24 - 48 \ln \sqrt{2}$ or 7.36	A1	
9(i)	$\ln y = \ln A + bx$	B1	
9(ii)	$\ln y$ 	M1	attempt to plot $\ln y$ against x Allow $\lg y$ against x Allow $\lg y$ against $\lg e^x$
	straight line with all points joined	A1	

Question	Answer	Marks	Guidance
9(iii)	Gradient = b	M1	M1Dep on (ii) for attempt to find gradient and equate to b or $b \lg e$ if $\lg y$ plotted against x
	$b = -0.5$, allow -0.45 to -0.55	A1	value within the given range
	Intercept = $\ln A$ (= 7.6)	M1	M1Dep on (ii) for attempt to use intercept or coordinates of a point on the curve with <i>their</i> gradient to obtain A
	$A = 2000$ allow $1900 - 2100$	A1	
9(iv)	use of graph or appropriate substitution	M1	
	When $y = 500$, $x = 2.77$ allow $2.2 - 3.0$	A1	
9(v)	use of graph or appropriate substitution	M1	
	When $x = 5$, $\ln y = 5.1$ $y = 164$ allow $155 - 175$	A1	

Question	Answer	Marks	Guidance
10(i)	$y = -3x^3 - 11x^2 - 8x + 4$	M1	attempt to differentiate
	$\frac{dy}{dx} = -9x^2 - 22x - 8$	A1	all correct
	When $\frac{dy}{dx} = 0$, $9x^2 + 22x + 8 = 0$	M1	M1Dep for equating to zero and correct attempt to solve
	$x = -2$	A1	SC Allow B1 for $x = -2$ if A1 not obtained from differentiation
	$x = -\frac{4}{9}$	A1	
	10(i) Alternate scheme		
	$\frac{dy}{dx} = (x+2)^2(-3) + (1-3x)2(x+2)$	M1	attempt to differentiate
	all correct	A1	
	When $\frac{dy}{dx} = 0$, $(x+2)(-4-9x) = 0$ oe	M1	M1Dep for equating to zero and correct attempt to solve
	$x = -2$	A1	SC Allow B1 for $x = -2$ if A1 not obtained from differentiation
	$x = -\frac{4}{9}$	A1	
10(ii)	$D\left(\frac{1}{3}, 0\right)$	B1	Allow mismatch of letters
	$C(0, 4)$	B1	Allow mismatch of letters
10(iii)	Area $= \int_0^{\frac{1}{3}} -3x^3 - 11x^2 - 8x + 4 \, dx$	M1	correct attempt to integrate a cubic equation
	$= \left[-\frac{3}{4}x^4 - \frac{11}{3}x^3 - 4x^2 + 4x \right]_0^{\frac{1}{3}}$	A2	A1 for 3 terms correct A1 for all correct
	$-\frac{3}{4}\left(\frac{1}{81}\right) - \frac{11}{3}\left(\frac{1}{27}\right) - \frac{4}{9} + \frac{4}{3}$	M1	M1Dep for application of limits
	$= \frac{241}{324}$ or 0.744	A1	

ADDITIONAL MATHEMATICS**0606/11**

Paper 1

October/November 2017

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(i)	$A' \cap B$	B1	
1(ii)	$A \cap B \cap C$	B1	
1(iii)	$A \cup B$	B1	
2(i)	$p\left(\frac{1}{2}\right) = \frac{a}{8} + \frac{b}{4} - \frac{13}{2} + 4$	M1	attempt at $p\left(\frac{1}{2}\right)$
	$p'(x) = 3ax^2 + 2bx - 13$ $p'\left(\frac{1}{2}\right) = \frac{3a}{4} + b - 13$	M1	attempt at $p'\left(\frac{1}{2}\right)$
	leading to $a + 2b = 20$ and $3a + 4b - 52 = 0$	A1	at least one correct equation
	solution of simultaneous equations	DM1	
	$a = 12, b = 4$	A1	for both
2(ii)	$p(-1) = -12 + 4 + 13 + 4$	M1	
	9	A1	FT on <i>their</i> integer values of a and b
3(a)	$Tg^{\frac{1}{2}} = 2\pi l^{\frac{1}{2}}$ $T^2g = 4\pi^2l$	B1	multiplication/dealing with power of $\frac{1}{2}$ or squaring
	$l = \frac{T^2g}{4\pi^2}$ or $\left(\frac{Tg^{\frac{1}{2}}}{2\pi}\right)^2$	B1	for either
3(b)	$y^2 - 4y + 3 = 0$ leading to $y = 1, y = 3$	M1	reduction to quadratic equation and attempt to solve
	$\frac{1}{x^3} = 1, \frac{1}{x^3} = 3$	DM1	attempt to solve $x^{\frac{1}{3}} = k$ (positive k)
	$x = 1, x = 27$	A2	A1 for each

Question	Answer	Marks	Guidance
4(i)	$\frac{1}{2}$	B1	
4(ii)	$\lg y = mx^2 + c$ $\lg y = \frac{1}{2}x^2 + 1$	B2	–1 for each error
4(iii)	$y = 10^{\left(\frac{x^2}{2} + 1\right)}$	B1	dealing with lg on <i>their</i> (ii)
	$y = 10^{\left(10^{\frac{x^2}{2}}\right)}$	B2	B1 for each, dependent on first B1
5(i)	(0, 20)	B1	
5(ii)	31.7	B1	
5(iii)	$2e^{2x} - 8e^{-2x} \quad (+c)$	B2	B1 for each correct term
5(iv)	Area of trapezium = $\frac{1}{2}(20 + 31.7)$ = 25.86 or 25.85	B1	
	$\left[2e^{2x} - 8e^{-2x}\right]_0^1 = (2e^2 - 8e^{-2}) - (-6)$	M1	substitution of both limits, must have come from integration of the form $ae^{2x} + be^{-2x}$.
	19.7	A1	
	Required area = 6.15, 6.16, 6.17	A1	
6(a)(i)	$f \geq 3$	B1	must be using a correct notation
6(a)(ii)	$(4x - 1)^2 + 3 = 4$	M1	correct order
	solution of resulting quadratic equation	DM1	
	$x = 0, x = \frac{1}{2}$	A1	both required

Question	Answer	Marks	Guidance
6(b)(i)	$xy - 4y = 2x + 1$	M1	‘multiplying out’
	$x(y - 2) = 4y + 1$ $x = \frac{4y + 1}{y - 2}$	M1	collecting together like terms
	$h^{-1}(x) = \frac{4x + 1}{x - 2}$	A1	correct answer with correct notation
	Range $h^{-1} \neq 4$	B1	must be using a correct notation
6(b)(ii)	$h^2(x) = h\left(\frac{2x + 1}{x - 4}\right)$ $= \frac{2\left(\frac{2x + 1}{x - 4}\right) + 1}{\left(\frac{2x + 1}{x - 4}\right) - 4}$	M1	dealing with h^2 correctly
	dealing with fractions within fractions	M1	
	$= \frac{5x - 2}{17 - 2x}$ oe	A1	
7(i)	$\ln(2x + 1) - \ln(2x - 1)$	B1	
7(ii)	attempt to differentiate	M1	
	$\frac{dy}{dx} = \frac{2}{2x + 1} - \frac{2}{2x - 1} + 4$	A1	all correct
	attempt to obtain in required form	DM1	
	$= \frac{16x^2 - 8}{4x^2 - 1}$	A1	A1 all correct
7(iii)	When $\frac{dy}{dx} = 0$, $16x^2 - 8 = 0$	M1	setting $\frac{dy}{dx} = 0$ and attempt to solve
	$x = \frac{1}{\sqrt{2}}$ only	A1	

Question	Answer	Marks	Guidance
7(iv)	$\frac{d^2y}{dx^2} = \frac{32x(4x^2 - 1) - 8x(16x^2 - 8)}{(4x^2 - 1)^2}$	M1	attempt at second derivative and conclusion or equivalent method
	When $x = \frac{1}{\sqrt{2}}$ $\frac{d^2y}{dx^2}$ is + ve, so minimum	A1	
8(a)(i)	${}^8C_6 \times {}^6C_4$	B1	either 8C_6 or 6C_4
	420	B1	
8(a)(ii)	${}^{12}C_8 + {}^{12}C_{10}$	B2	B1 for each
	= 561	B1	
	Alternate scheme: $1001 - (2 \times {}^{12}C_9)$	B1 B1	
	= 561	B1	
8(b)(i)	136 080	B1	
8(b)(ii)	No of ways ending with 0 - 15 120	B1	
	No of ways ending with 5 - 13 440	B1	
	Total 28 560	B1	
8(b)(iii)	Starting with 6 or 8 - 13 440	B1	
	Starting with 7 or 9 - 16 800	B1	
	Total = 30 240	B1	
9(i)	$\tan\left(\frac{PAQ}{2}\right) = 2.4$	M1	valid method
	$PAQ = 2.352(01....)$ $PAQ = 2.35$ correct to 3 sf	A1	must see greater than 3 sf then rounding
9(ii)	$PBQ = 0.790$ or 0.792	B1	
9(iii)	$(2.352 \times 10) + (0.790 \times 24)$	M1, A1	M1 for correct attempt at an arc length A1 for one correct arc length
	= awrt 42.5	A1	

Question	Answer	Marks	Guidance
9(iv)	$\left(\left(\frac{1}{2} \times 24^2 \times 0.790 \right) - \left(\frac{1}{2} \times 24^2 \times \sin 0.790 \right) \right)$	B1,B1	B1 for a correct sector area allow, unsimplified B1 for a correct area of a triangle, allow unsimplified
	$+ \left(\left(\frac{1}{2} \times 10^2 \times 2.352 \right) - \left(\frac{1}{2} \times 10^2 \times \sin 2.352 \right) \right)$	B1	correct plan, dependent on both previous B marks
	$= 22.94 + 82.1$ $= 105$	B1	
10(a)	$\frac{3}{4} = \sin^2 2x$	B1	dealing correctly with cosec
	$\sin 2x = \pm \frac{\sqrt{3}}{2}$ $2x = 60, 120, 240, 300$	M1	correct method of solution including dealing with $2x$ correctly, may be implied by one correct solution.
	$x = 30, 60, 120, 150$	A2	A1 for each correct pair
10(b)	$\tan \left(y - \frac{\pi}{4} \right) = \frac{1}{\sqrt{3}}$	M1	dealing with order of operations to obtain a first solution
	$y - \frac{\pi}{4} = \frac{\pi}{6}, \frac{7\pi}{6}$	M1	M1 for attempt to obtain a second solution
	$y = \frac{5\pi}{12}, \frac{17\pi}{12}$	A2	A1 for each

ADDITIONAL MATHEMATICS**0606/12**

Paper 1

October/November 2017

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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MARK SCHEME NOTES

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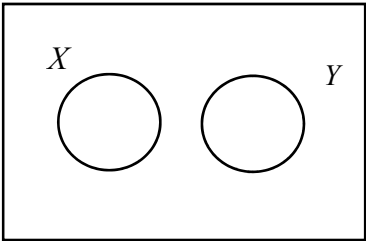
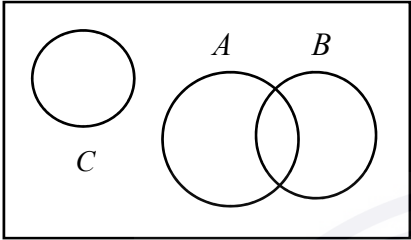
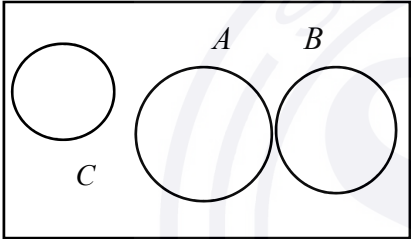
Types of mark

- M** Method marks, awarded for a valid method applied to the problem.
- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

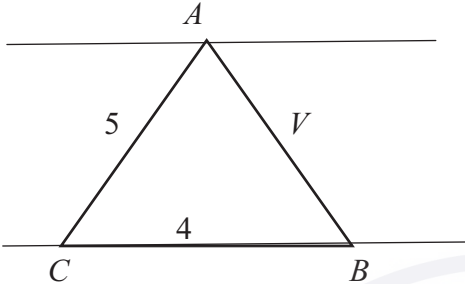
Abbreviations

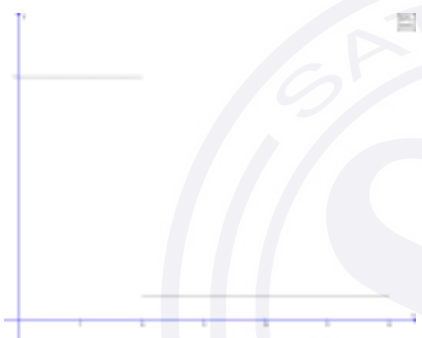
awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(i)		1	
1(ii)	<p>Either</p>  <p>Or</p> 	2	<p>B1 for C with no intersection with either A or B (allow if C is not represented by a circle)</p> <p>B1 for all correct, C must be represented by a circle</p>
2	$a = 4$	B1	
	$b = 6$	B1	
	$c = -2$	M1, A1	M1 for use of $\left(\frac{\pi}{12}, 2\right)$ to obtain c , using <i>their</i> values of a and of b
3(i)	$32 - 20x^2 + 5x^4$	B3	B1 for each correct term
3(ii)	$(32 - 20x^2 + 5x^4)\left(\frac{1}{x^2} + \frac{9}{x^4}\right)$	B1	$\frac{1}{x^2}$ and $\frac{9}{x^4}$
	Independent of x : $-20 + 45$	M1	attempt to deal with 2 terms independent of x , must be looking at terms in x^2 and $\frac{1}{x^2}$ and terms in x^4 and $\frac{1}{x^4}$
	$= 25$	A1	FT <i>their</i> answers from (i) (<i>their</i> -20×1) + (<i>their</i> 5×9)

Question	Answer	Marks	Guidance
4	correct differentiation of $\ln(3x^2 + 2)$	B1	
	attempt to differentiate a quotient or a product	M1	
	$\frac{dy}{dx} = \frac{(x^2 + 1)\left(\frac{6x}{3x^2 + 2}\right) - 2x \ln(3x^2 + 2)}{(x^2 + 1)^2}$	A1	all other terms correct.
	When $x = 2$, $\frac{dy}{dx} = \frac{5\left(\frac{12}{14}\right) - 4 \ln 14}{25}$	M1	M1dep for substitution and attempt to simplify
	$= \frac{6}{35} - \frac{4}{25} \ln 14$	A2	A1 for each correct term, must be in simplest form
5(i)	Either Gradient = -0.2	B1	
	$\lg y = -0.2x + c$	B1	$\lg y = mx + c$ soi
	correct attempt to find c	M1	must have previous B1
	$\lg y = 0.42 - 0.2x$ or $\lg y = \frac{21}{50} - \frac{x}{5}$	A1	line in either form, allow equivalent fractions
	Or $0.3 = 0.6m + c$	B1	
	$0.2 = 1.1m + c$	B1	
	attempt to solve for both m and c	M1	must have at least one of the previous B marks
	Leading to $\lg y = 0.42 - 0.2x$ or $\lg y = \frac{21}{50} - \frac{x}{5}$	A1	line in either form, allow equivalent fractions

Question	Answer	Marks	Guidance
5(ii)	Either $y = 10^{(0.42-0.2x)}$	M1	dealing with the index, using their answer to (i)
	$y = 10^{0.42} (10^{-0.2x})$ $y = 2.63(10^{-0.2x})$	A2	A1 for each
	Or $y = A(10^{bx})$ leads to $\lg y = \lg A + bx$ Compare this form with their equation from (i)	M1	comparing their answer to (i) with $\lg y = \lg A + bx$ may be implied by one correct term from correct work
	$\lg A = 0.42$ so $A = 2.63$	A1	
	$b = -0.2$	A1	A1 for each
6(i)	$y \in \mathbb{R}$ oe	B1	Must have correct notation i.e. no use of x
6(ii)	$y > 3$ oe	B1	Must have correct notation i.e. no use of x
6(iii)	$f^{-1}(x) = e^x$ or $g(4) = 35$	B1	First B1 may be implied by correct answer or by use of 35
	$f^{-1}g(4) = e^{35}$	B1	
6(iv)	$\frac{y-3}{2} = x^2$ or $\frac{x-3}{2} = y^2$	M1	valid attempt to obtain the inverse
	$g^{-1}(x) = \sqrt{\frac{x-3}{2}}$	A1	correct form, must be $g^{-1}(x) =$ or $y =$
	Domain $x > 3$	B1	Must have correct notation
7(i)	$p\left(\frac{1}{2}\right): \frac{a}{8} + 2 + \frac{b}{2} + 5 = 0$	M1	substitution of $x = \frac{1}{2}$ and equating to zero (allow unsimplified)
	$p(-2): -8a + 32 - 2b + 5 = -25$	M1	substitution of $x = -2$ and equating to -25 (allow unsimplified)
	leading to $a + 4b + 56 = 0$ $4a + b - 31 = 0$ oe	M1	M1dep for solution of simultaneous equations to obtain a and b
	$a = 12, b = -17$	A2	A1 for each

Question	Answer	Marks	Guidance
7(ii)	$12x^3 + 8x^2 - 17x = 0$ $x = 0$	B1	for $x = 0$
	$x = -\frac{1}{3} \pm \frac{\sqrt{55}}{6}$ oe	B1	
8			
8(i)	$\angle ABC = 67.4^\circ$	B1	
	$\frac{4}{\sin BAC} = \frac{5}{\sin 67.4^\circ}$	M1	attempt at the sine rule, using 4 and 5 (or e.g. use of cosine rule followed by sine rule on triangle shown)
	$\angle BAC = 47.6^\circ$	A1	may be implied by later work
	Angle required = $180^\circ - 47.6^\circ - 67.4^\circ = 65^\circ$	A1	Answer Given
8(ii)	$V^2 = 5^2 + 4^2 - (2 \times 5 \times 4 \times \cos 65^\circ)$	M1	attempt at the cosine rule or sine rule to obtain V – allow if seen in (i)
	$V = 4.91$ or $\frac{4}{\sin BAC} = \frac{V}{\sin 65^\circ}$	A1	
	Distance to travel: $\frac{120}{\sin 67.4^\circ}$	M1	distance to travel – allow if seen in (i)
	130 or $\sqrt{120^2 + 50^2}$	A1	
	Time taken: $\frac{130}{4.91}$	M1	M1dep for correct method to find the time, must have both of the previous M marks
	26.5	A1	

Question	Answer	Marks	Guidance
	<u>Alternative method</u> $AC = \frac{120}{\cos 25}$ oe	M1	correct attempt at AC
	$= 132.4$	A1	Allow 132
	Speed for this distance = 5	M1A1	M1dep A1 for speed, it must be 5 exactly for A1, must have first M mark
	Time taken $= \frac{132.4}{5}$	M1	M1dep for a correct method to find the time, must have both of the previous M marks
	$= 26.5$	A1	
9(a)		B3	B1 for line joining (0,5) and (10,5) B1 for a line joining (10,0.5) and (30,0.5) B1 all correct with no solid line joining (10,5) to (10,0.5)
9(b)(i)	3	B1	
9(b)(ii)	$\frac{dv}{dt} = -15e^{-5t} + \frac{3}{2}$	M1	attempt to differentiate, must be in the form $ae^{-5t} + b$
	When $\frac{dv}{dt} = 0$, $e^{-5t} = 0.1$	M1	M1dep for equating to zero and attempt to solve, must be of the form $ae^{-5t} = b$, $b > 0$ to obtain an equation in the form $-5t = k$ where k is a logarithm or < 0
	$t = 0.461$	A1	

Question	Answer	Marks	Guidance
9(b)(iii)	Either attempt to integrate, must be in the form $ce^{-5t} + dt^2$	M1	
	$s = -\frac{3}{5}e^{-5t} + \frac{3}{4}t^2 \quad (+c)$	A1	
	When $t = 0, s = 0$ so $c = \frac{3}{5}$	M1	M1dep for attempt to find c and substitute $t = 0.5$
	$s = 0.738$	A1	
	Or attempt to integrate, must be in the form $ce^{-5t} + dt^2$	M1	
	$\left[-\frac{3}{5}e^{-5t} + \frac{3}{4}t^2\right]_0^{0.5}$	A1	
	correct use of limits	M1	M1dep
	leading to $s = 0.738$	A1	
10(i)	$5\angle BAC = 6.2, \angle BAC = 1.24$	B1	
10(ii)	$\sin 0.62 = \frac{BD}{5}, BD = 2.905, 2.91$	B1	valid method to find BD
	Arc $BFC: \pi \times BD (= 9.13)$	M1	attempt to find arc length BFC , using <i>their</i> BD
	Perimeter: $9.13 + 6.2 = 15.3$	A1	
10(iii)	Area: $\left(\frac{1}{2} \times \pi \times 2.91^2\right) - \left(\left(\frac{1}{2} \times 5^2 \times 1.24\right) - \left(\frac{1}{2} \times 5^2 \times \sin 1.24\right)\right)$	B3	B1 for area of semi circle (= 13.3) B1 for area of sector (= 15.5) B1 for area of triangle (= 11.8)
	$9.58 \leq \text{Area} \leq 9.62$	B1	final answer

Question	Answer	Marks	Guidance
11(a)	$\tan(\phi + 35^\circ) = \frac{2}{5}$	M1	dealing correctly with cot and an attempt at solution of $\tan(\phi + 35) = c$, order must be correct, to obtain a value for $\phi + 35$
	$\phi + 35^\circ = 21.8^\circ, 201.8^\circ, 381.8^\circ$	M1	M1dep for an attempt at a second solution in the range, $(180^\circ + \text{their first solution in the range oe})$
	$\phi = 166.8^\circ, 346.8^\circ$	A2	A1 for each
11(b)(i)	Either $\frac{\frac{1}{\cos \theta}}{\frac{\cos \theta}{\sin \theta} + \frac{\sin \theta}{\cos \theta}}$	M1	expressing all terms in terms of $\sin \theta$ and $\cos \theta$ where necessary
	$= \frac{1}{\cos \theta} \left(\frac{\sin \theta \cos \theta}{\cos^2 \theta + \sin^2 \theta} \right)$	M1	dealing with the fractions correctly to get $\frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta \cos \theta}$ in denominator or as in left hand column
	$= \frac{\sin \theta}{(1)}$	A1	use of identity, together with a complete and correct solution, withhold A1 for incorrect use of brackets
	Or $\frac{\sec \theta}{\frac{1}{\tan \theta} + \tan \theta} = \frac{\sec \theta}{\frac{1 + \tan^2 \theta}{\tan \theta}}$	M1	dealing with fractions in the denominator correctly to get $\frac{1 + \tan^2 \theta}{\tan \theta}$ in the denominator, allow $\tan \theta$ taken to the numerator
	$= \frac{\sec \theta \tan \theta}{\sec^2 \theta}$	M1	use of the identity to get $\sec^2 \theta$
	$= \frac{\tan \theta}{\sec \theta} = \frac{\sin \theta}{\cos \theta} \times \cos \theta = \sin \theta$	A1	expressing all terms in terms of $\sin \theta$ and $\cos \theta$ and simplification to the given answer, withhold A1 for incorrect use of brackets

Question	Answer	Marks	Guidance
11(b)(ii)	$\sin 3\theta = -\frac{\sqrt{3}}{2}$	M1	correct attempt to solve for θ , order must be correct, may be implied by one correct solution
	$3\theta = -\frac{2\pi}{3}, -\frac{\pi}{3}, \frac{4\pi}{3}$ $\theta = -\frac{2\pi}{9}, -\frac{\pi}{9}, \frac{4\pi}{9}$	A3	A1 for each



ADDITIONAL MATHEMATICS**0606/13**

Paper 1

October/November 2017

MARK SCHEME

Maximum Mark: 80

Published

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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1	Using $\tan^2 \theta + 1 = \sec^2 \theta$ to obtain $y = 2(\tan^2 \theta + 1)$ or $(x+5)^2 = \sec^2 \theta - 1$ $(x+5)^2 + 1 = \frac{y}{2}$	M1	use of correct identity
	$y = 2((x+5)^2 + 1)$ oe	A1	
2	$\frac{dy}{dx} = 10e^{5x} + 3$ an attempt at integration in form $ae^{5x} + bx$	M1	
	$y = \frac{10}{5}e^{5x} + 3x (+c)$	A1	condone omission of c
	attempt to find c using $x = 0, y = 9$	M1	M1dep
	$y = 2e^{5x} + 3x + 7$	A1	
3	$9 < 4k(k-4)$ $4k^2 - 16k - 9$	M1	use of the discriminant with correct values
	$(2k-9)(2k+1)$	M1	M1dep for solution of <i>their</i> quadratic to obtain critical values
	Critical values $\frac{9}{2}, -\frac{1}{2}$	A1	
	$k < -\frac{1}{2}, k > \frac{9}{2}$	A1	
4	$a = 3$	B1	
	$b = 8$	B1	
	$\frac{5}{2} = 3\cos\left(8 \times \frac{\pi}{12}\right) + c$	M1	substitution of $x = \frac{\pi}{12}$ and $y = \frac{5}{2}$ to find c
	$c = 4$	A1	
5(i)	$\frac{5}{14}(7x-10)^{\frac{2}{5}}$	B2	B1 for $k(7x-10)^{\frac{2}{5}}$

Question	Answer	Marks	Guidance
5(ii)	$\frac{5}{14} \left[(7x-10)^{\frac{2}{5}} \right]_6^a = \frac{25}{14}$ $\frac{5}{14} (7a-10)^{\frac{2}{5}} - \frac{5}{14} (7 \times 6 - 10)^{\frac{2}{5}} = \frac{25}{14}$ $(7a-10)^{\frac{2}{5}} - 4 = 5$	M1	correct application of limits for $k(7x-10)^{\frac{2}{5}}$
	$a = \frac{9^{\frac{5}{2}} + 10}{7}$	M1	M1dep for evaluation of $(7 \times 6 - 10)^{\frac{2}{5}}$ and correct order of operations to find a , including dealing with power.
	$a = \frac{253}{7} \text{ or } 36\frac{1}{7}$	A1	
6(i)	Gradient = $\frac{2.4-0.9}{0.2-0.8} (= -2.5)$	B1	
	$\ln y = -\frac{5}{2}x^2 + c$	M1	straight line form and correct substitutions to find c
	$\ln y = -\frac{5}{2}x^2 + 2.9 \text{ oe}$	A1	
	<u>Alternative method</u> $2.4 = p(0.2) + q$ $0.9 = p(0.8) + q$	B1	
	Correct method of solution to find p and q from two correct equations	M1	M1dep
	$\ln y = -\frac{5}{2}x^2 + 2.9$	A1	
6(ii)	$y = e^{\left(-\frac{5}{2}x^2 + 2.9\right)}$	M1	dealing with \ln
	$y = e^{-\frac{5}{2}x^2} \times e^{2.9}$	M1	M1dep for dealing with the index
	$y = 18.2z^{-\frac{5}{2}}$	A1	

Question	Answer	Marks	Guidance
7(i)	$64 - 48x^2 + 15x^4$	B3	B1 for each correct term in final line of response
7(ii)	$(64 - 48x^2 + 15x^4) \left(\frac{1}{x^2} + 2 + x^2 \right)$	B1	B1 for $\frac{1}{x^2} + 2 + x^2$ oe
	at least two correctly obtained products leading to terms in x^2	M1	
	Term in x^2 : $64 + 15 - 96$	A1	FT for correct evaluation of <i>their</i> $64 + (2 \times \text{their} - 48) + \text{their } 15$
	$= -17$	A1	
8(i)	attempt to differentiate a product	M1	
	$\frac{dy}{dx} = \left((x-4) \times \frac{5}{3} \times 3(3x-1)^{\frac{2}{3}} \right) + (3x-1)^{\frac{5}{3}}$	A2	A1 for $(+)$ $\left((x-4) \times \frac{5}{3} \times 3(3x-1)^{\frac{2}{3}} \right)$ A1 for $(+)(3x-1)^{\frac{5}{3}}$
	$= (3x-1)^{\frac{2}{3}} ((5x-20) + (3x-1))$	M1	use of $(3x-1)^{\frac{5}{3}} = (3x-1)^{\frac{2}{3}} (3x-1)$
	$= (3x-1)^{\frac{2}{3}} (8x-21)$	A1	
8(ii)	When $x = 3$, $\frac{dy}{dx} = 8^{\frac{2}{3}} \times 3$	M1	$(3 \times 3 - 1)^{\frac{2}{3}} \times k$ or $(9 - 1)^{\frac{2}{3}} \times k$ or $4 \times k$ (where k is any number)
	$\partial y = 8^{\frac{2}{3}} \times 3 \times h$	M1	M1dep for <i>their</i> $\left((9 - 1)^{\frac{2}{3}} \times k \right) \times h$
	$\partial y = 12h$	A1	
9(a)(i)	720	B1	
9(a)(ii)	240	B1	
9(a)(iii)	$k \times 4! \times 2$ or $240 - k \times 4! \times 2$ or correct equivalents with no extra terms added or subtracted	B1	
	$4 \times 4! \times p$ or correct equivalents with no extra terms added or subtracted	B1	
	192	B1	

Question	Answer	Marks	Guidance
9(b)(i)	6435	B1	
9(b)(ii)	With twins: ${}^{13}C_6$ or 1716 Without twins: ${}^{13}C_8$ or 1287	B2	B1 for ${}^{13}C_6$ or 1716 or ${}^{13}C_8$ or 1287 B1 for (${}^{13}C_6$ and ${}^{13}C_8$) or (1716 and 1287) with no multiples and no extra terms
	Total: $1716 + 1287 = 3003$	B1	3003 from a correct method
10(a)	matrix multiplication, must have at least 2 correct elements	M1	
	$\mathbf{AB} = \begin{pmatrix} 13 & 8 \\ 2a-5b & 3a+4b \end{pmatrix}$	A1	
	$2a-5b=18$ $3a+4b=4$	M1	formation and solution of simultaneous equations
	leading to $a=4, b=-2$	A1	
	<u>Alternate scheme</u> $\mathbf{AB} = \begin{pmatrix} 13 & 8 \\ 18 & 4 \end{pmatrix}$ $\mathbf{ABB}^{-1} = \begin{pmatrix} 13 & 8 \\ 18 & 4 \end{pmatrix} \mathbf{B}^{-1}$	M1	Correct plan
	Correct inverse	B1	
	$\mathbf{A} = \begin{pmatrix} 4 & -1 \\ a & b \end{pmatrix} = \frac{1}{23} \begin{pmatrix} 13 & 8 \\ 18 & 4 \end{pmatrix} \begin{pmatrix} 4 & -3 \\ 5 & 2 \end{pmatrix}$	M1	Correct order and method of multiplication with at least two correct elements
	leading to $a=4, b=-2$	A1	
10(b)(i)	$-\frac{1}{17} \begin{pmatrix} 1 & 5 \\ 4 & 3 \end{pmatrix}$ oe	B2	B1 for $-\frac{1}{17}$ B1 for $\begin{pmatrix} 1 & 5 \\ 4 & 3 \end{pmatrix}$
10(b)(ii)	$\mathbf{Z} = -\frac{1}{17} \begin{pmatrix} 1 & 5 \\ 4 & 3 \end{pmatrix} \begin{pmatrix} -1 & 2 \\ 4 & 0 \end{pmatrix}$	M1	pre-multiplication with two elements correct
	$= -\frac{1}{17} \begin{pmatrix} 19 & 2 \\ 8 & 8 \end{pmatrix}$ oe	A2	A1 for four correct of $-\frac{1}{17}, 19, 2, 8, 8$

Question	Answer	Marks	Guidance
11(i)	1.48	B1	
11(ii)	$\frac{1}{2} \times 10^2 \times \theta = 21.8$	M1	correct use of sector area
	$\theta = 0.436$	A1	
11(iii)	$\angle BOC = \frac{2\pi - 1.48 - 0.436}{2} \quad (= 2.18(4))$	B1	2.18(4) or unsimplified
	$BC = 20 \sin\left(\frac{1}{2} \angle BOC\right)$ or $BC = \frac{10 \times \sin BOC}{\sin\left(\frac{\pi - BOC}{2}\right)}$ or $BC = \sqrt{(200 - 200 \cos BOC)}$ $BC = 17.7(5)$	M2	M1 for a complete correct method to find BC using <i>their</i> angle BOC M1 for a correct plan using 14.8, <i>their</i> BC and $10 \times$ <i>their</i> answer to (ii)
	Perimeter = $14.8 + (2 \times 17.7(5)) + 4.36$ = 54.7 or 54.6	A1	awrt 54.7 or awrt 54.6

Question	Answer	Marks	Guidance
11(iv)	Area = $\left(\frac{1}{2} \times 10^2 \times 1.48\right) + 21.8 + 2\left(\frac{1}{2} \times 10^2 \sin 2.18(4)\right)$	B2	B1 for $\left(\frac{1}{2} \times 10^2 \times 1.48\right) + 21.8$ B1 for $2\left(\frac{1}{2} \times 10^2 \sin 2.18(4)\right)$
	= 178	B1	awrt 178 from correct working
	<u>Alternative method 1</u> Segment area = $\frac{1}{2}(10^2(2.18 - \sin 2.18))$	B1	B1 for $2 \times \frac{1}{2}(10^2(2.18(4) - \sin 2.18(4)))$
	Area required = $100\pi - 2 \times \frac{1}{2}(10^2(2.18(4) - \sin 2.18(4)))$	B1	
	= 178	B1	awrt 178 from correct working
	<u>Alternative method 2</u> Area of trapezium = $\frac{1}{2}((13.5 + 4.33)(17.1))$	B1	correct area of trapezium <i>ABCD</i> (allow unsimplified)
	Area of segments = $\frac{1}{2}(10^2(1.48 - \sin 1.48)) + \frac{1}{2}(10^2(0.436 - \sin 0.436))$	B1	correct area of both segments (allow unsimplified)
	= 178	B1	awrt 178 from correct working

Question	Answer	Marks	Guidance
12(i)	$2x^2 + 5x - 12 = 0$ or $y^2 + 3y - 28 = 0$	M1	attempt to get in terms of one variable
	$(2x - 3)(x + 4) = 0$ or $(y + 7)(y - 4) = 0$	M1	M1dep for solution of a three term quadratic
	leading to $x = -4$, $y = -7$ and $x = \frac{3}{2}$, $y = 4$	A2	A1 for each 'pair'
	Midpoint $M \left(\frac{\frac{3}{2} - 4}{2}, \frac{4 + (-7)}{2} \right) \left(= \left(-\frac{5}{4}, -\frac{3}{2} \right) \right)$	A1	correctly obtained midpoint
	Gradient of $PQ = 2$	B1	may be implied
	Perp gradient = $-\frac{1}{2}$	M1	$\frac{-1}{\text{their gradient of } PQ}$
	Perp bisector: $y + \frac{3}{2} = -\frac{1}{2} \left(x + \frac{5}{4} \right)$	M1	M1dep for equation of perp bisector using <i>their</i> perp gradient and <i>their</i> midpoint. (unsimplified)
	$y = -\frac{1}{2}(-10) - \frac{17}{8} = \frac{23}{8}$ or $\frac{23}{8} = -\frac{1}{2}x - \frac{17}{8} \rightarrow x = -10$	A1	all correct so far and for verification using a correct equation

Question	Answer	Marks	Guidance
12(ii)	$\text{Area} = \frac{1}{2} \times \left(\frac{17}{8} + 1 \right) \times \frac{5}{4}$	M1	finding R , S and RS
	correct method for finding area	M1	M1dep
	$= \frac{125}{64}$ or 1.95 or $1\frac{61}{64}$	A1	
	<u>Alternative method 1</u> $\text{Area} = \frac{1}{2} \times \frac{\sqrt{125}}{4} \times \frac{\sqrt{125}}{8}$	M1	finding R , S , RM and MS
	correct method for finding area	M1	M1dep
	$= \frac{125}{64}$ or 1.95 or $1\frac{61}{64}$	A1	
	<u>Alternative method 2</u> $\text{Area} = \frac{1}{2} \begin{vmatrix} 0 & 0 & \frac{-5}{4} & 0 \\ 1 & \frac{-17}{8} & \frac{-3}{2} & 1 \end{vmatrix}$	M1	finding R and S to obtain their $\frac{1}{2} \begin{vmatrix} 0 & 0 & \frac{-5}{4} & 0 \\ 1 & \frac{-17}{8} & \frac{-3}{2} & 1 \end{vmatrix}$
	$= \frac{1}{2} \left -\frac{5}{4} - \frac{85}{32} \right $ oe	M1	M1dep for correct method of evaluation
	$= \frac{125}{64}$ or 1.95 or $1\frac{61}{64}$	A1	

ADDITIONAL MATHEMATICS**0606/11**

Paper 1

May/June 2017

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

Types of mark

- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
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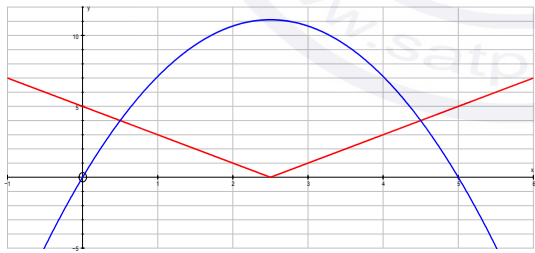
Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied

Question	Answer	Marks	Guidance
1(i)	$kx - 5 = x^2 + 4x$ $x^2 + (4 - k)x + 5 = 0$	M1	equating line and curve equation and collecting terms to form an equation of the form $ax^2 + bx + c = 0$ x terms must be gathered together, maybe implied by later work
	For a tangent $(4 - k)^2 = 20$	DM1	correct use of discriminant
	$k = 4 + 2\sqrt{5}$	A1	Accept $k = 4 + \sqrt{20}$
	Alternative Gradient of line = k Gradient of curve = $\frac{dy}{dx} = 2x + 4$ Equating: $k = 2x + 4$	M1	
	substitution of $k = 2x + 4$ or $x = \frac{k - 4}{2}$ in $kx - 5 = x^2 + 4$ and simplify to a quadratic equation in k or x	DM1	
	$k = 4 + 2\sqrt{5}$	A1	Accept $k = 4 + \sqrt{20}$
1(ii)	Normal gradient = $-\frac{1}{4 + 2\sqrt{5}} \times \frac{4 - 2\sqrt{5}}{4 - 2\sqrt{5}}$	M1	use of negative reciprocal and attempt to rationalise using a form of $a - b\sqrt{5}$ or $a - \sqrt{20}$ or <i>their</i> equivalent from (i)
	$= -\frac{4 - 2\sqrt{5}}{-4}$ oe $= 1 - \frac{\sqrt{5}}{2}$	A1	$-\frac{4 - 2\sqrt{5}}{-4}$ oe leading to $1 - \frac{\sqrt{5}}{2}$
2	$p(3) = 27 + 9a + 3b - 48$	M1	attempt to find $p(3)$
	$3a + b = 9$ oe	A1	
	$p'(x) = 3x^2 + 2ax + b$ $p'(1) = 3 + 2a + b$	M1	attempt to differentiate and find $p'(1)$ must have 2 terms correct
	$2a + b = -3$ oe	A1	
	$a = 12, b = -27$	A1	for both
3(a)	$x^3 y^7$	B2	B1 for each term

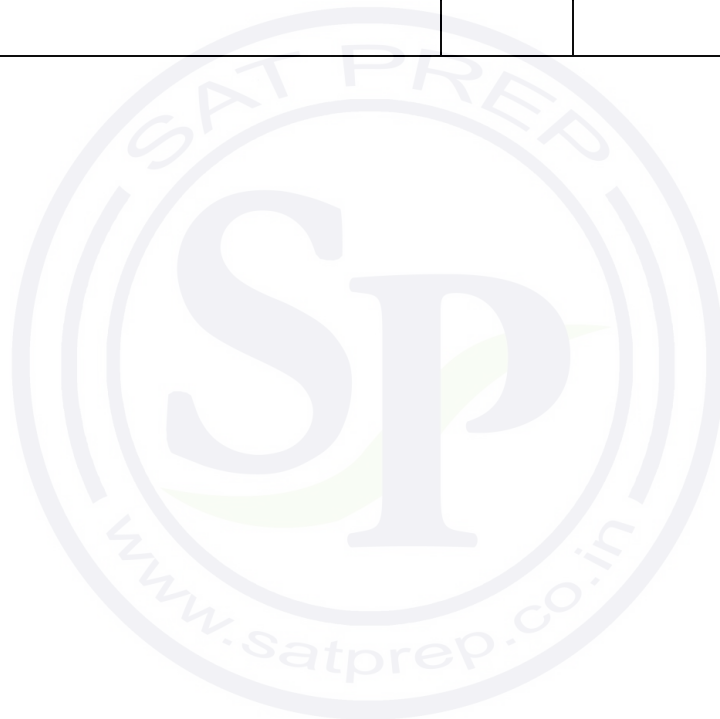
Question	Answer	Marks	Guidance
3(b)(i)	for $(t-2)^{\frac{3}{2}} = (t-2)^{\frac{1}{2}}(t-2)$ soi	M1	
	$(t-2)^{\frac{1}{2}}(4+5(t-2))$	A1	
	$(t-2)^{\frac{1}{2}}(5t-6)$	A1	
3(b)(ii)	2 and $\frac{6}{5}$	B1	FT on <i>their</i> $(t-2)^{\frac{1}{2}}(5t-6)$, must have 2
4(a)(i)	$f > 5$, $f(x) > 5$	B1	
4(a)(ii)	$\frac{y-5}{3} = e^{-4x}$ or $\frac{x-5}{3} = e^{-4y}$	B1	
	$-4x = \ln\left(\frac{y-5}{3}\right)$ or $-4y = \ln\left(\frac{x-5}{3}\right)$	B1	
	leading to $f^{-1}(x) = -\frac{1}{4}\ln\left(\frac{x-5}{3}\right)$ or $f^{-1}(x) = \frac{1}{4}\ln\left(\frac{3}{x-5}\right)$ or $f^{-1}(x) = \frac{1}{4}(\ln 3 - \ln(x-5))$ or $f^{-1}(x) = -\frac{1}{4}(\ln(x-5) - \ln 3)$	B1	
	Domain $x > 5$	B1	
4(b)	$\ln(x^2 + 5) = 2$	B1	
	$x^2 + 5 = e^2$	B1	
	$x = 1.55$ or better or $\sqrt{e^2 - 5}$	B1	
5(a)(i)	$\overrightarrow{OM} = \overrightarrow{OC} + \frac{1}{2}(\overrightarrow{OA} - \overrightarrow{OC})$ oe	M1	may be implied by correct answer.
	$\frac{1}{2}(\mathbf{a} + \mathbf{c})$	A1	

Question	Answer	Marks	Guidance
5(a)(ii)	$\mathbf{b} = \frac{5}{2}\overline{OM}$ oe, $\frac{5}{2}$ (their (i)) or $\overline{OM} = \frac{2}{3}(\mathbf{b} - \overline{OM})$	M1	dealing with ratio correctly to relate \mathbf{b} or \overline{OB} to \overline{OM}
	$= \frac{5}{4}(\mathbf{a} + \mathbf{c})$	A1	
5(b)(i)	$ -10\mathbf{i} + 24\mathbf{j} = 26$ $\mathbf{p} = \frac{39}{26}(-10\mathbf{i} + 24\mathbf{j})$	M1	magnitude of $-10\mathbf{i} + 24\mathbf{j}$ and use with 39
	$\mathbf{p} = -15\mathbf{i} + 36\mathbf{j}$	A1	
5(b)(ii)	If parallel to the y -axis, \mathbf{i} component is zero	M1	realising \mathbf{i} component is zero
	so $2\mathbf{p} + \mathbf{q} = 12\mathbf{j}$	DM1	use of 12
	$\mathbf{q} = 30\mathbf{i} - 60\mathbf{j}$	A1	
5(b)(iii)	$ \mathbf{q} = 30\sqrt{1^2 + (-2)^2}$ or $\sqrt{900} \times \sqrt{5}$	M1	attempt at magnitude of <i>their</i> \mathbf{q}
	$ \mathbf{q} = 30\sqrt{5}$	A1	Answer Given: must have full and correct working
6(i)	$\frac{1}{2} \times 12^2 \times \theta = 150$	M1	use of sector area
	$\theta = 2.083$, so $\theta = 2.08$ to 2dp	A1	
6(ii)	Area of triangle $AOB = \frac{1}{2} \times 12^2 \sin 2.08$	M1	correct method for area of triangle
	Area of segment $= 150 - \frac{1}{2} \times 12^2 \times \sin 2.08$	A1	allow unsimplified, using $\theta = 2.08, 2.083$ or $\frac{150}{72}$
	$\sin 1.04 = \frac{AB}{12}$	M1	correct trigonometric statement using $\theta = 2.08, 2.083$ or $\frac{150}{72}$ with attempt to obtain AB
	$AB = \text{awrt } 20.7$	A1	
	Shaded area $= \text{their } AB \times 8 - \text{their segment area}$	M1	execution of a correct 'plan' (rectangle – segment)
	awrt 78.4 or 78.5	A1	

Question	Answer	Marks	Guidance
6(iii)	Arc $AB = 25$ or 24.96	B1	
	Perimeter = $25 + \text{their } AB + 16$	M1	correct 'plan' (arc + <i>their</i> $AB + 2 \times 8$)
	awrt 61.7	A1	
7	differentiation to obtain answer in the form $p(3x^2 + 8)^{\frac{2}{3}}$ or $qx(3x^2 + 8)^{\frac{2}{3}}$	M1	
	$6x(3x^2 + 8)^{\frac{2}{3}}$	B1	
	$\frac{dy}{dx} = \frac{5}{3} \times 6x(3x^2 + 8)^{\frac{2}{3}}$	A1	all correct
	When $\frac{dy}{dx} = 0$ only solution is $x = 0$	DM1	$qx(3x^2 + 8)^{\frac{2}{3}} = 0$ and attempt to solve
	$x = 0$ and $3x^2 + 8 = 0$ has no solutions	A1	
	Stationary point at $(0, 32)$	A1	
	correct gradient method with substitution of x values either side of zero or equivalent valid method	M1	
	correct conclusion from correct work using a correct $\frac{dy}{dx}$	A1	
8(i)		B5	B1 for shape of modulus function B1 for y intercept = 5 (for modulus graph only) B1 for x intercept = 2.5 at the V of a modulus graph B1 for shape of quadratic function for $-1 \leq x \leq 6$ B1 for intercepts at $x = 0$ and $x = 5$ for a quadratic graph
8(ii)	$2x - 5 = \pm 4$	B1	one correct answer
	$x = \frac{9}{2}$	M1	solution of two different correct linear equations or solution of an equation obtained from squaring both sides or use of symmetry from first solution.
	$x = \frac{1}{2}$	A1	second correct solution

Question	Answer	Marks	Guidance
8(iii)	$16\left(\frac{1}{2}\right)^2 - 80\left(\frac{1}{2}\right) + 36 = 4$ and $16\left(\frac{9}{2}\right)^2 - 80\left(\frac{9}{2}\right) + 36 = 4$	B1	verification using both x values or for forming and solving $16x^2 - 80x + 36 = 0$
8(iv)	using <i>their</i> values from (ii) in an equality of the form $a \leq x \leq b$ or $a < x < b$	M1	
	$\frac{1}{2} \leq x \leq \frac{9}{2}$ cao	A1	
9(i)	$5 + 4\left(\sec^2\left(\frac{x}{3}\right) - 1\right)$ leading to given answer	B1	use of correct identity
9(ii)	$3 \tan\left(\frac{x}{3}\right) (+c)$	B1	
9(iii)	attempt to integrate using (i) and/or (ii)	M1	
	$\text{Area} = \int_{\frac{\pi}{2}}^{\pi} 4 \sec^2\left(\frac{x}{3}\right) + 1 \, dx$	A1	all correct
	$\left[12 \tan\left(\frac{x}{3}\right) + x\right]_{\frac{\pi}{2}}^{\pi}$	DM1	correct method for evaluation using limits in correct order
	$= \left(12 \tan \frac{\pi}{3} + \pi\right) - \left(12 \tan \frac{\pi}{6} + \frac{\pi}{2}\right)$	A1	
	$= 8\sqrt{3} + \frac{\pi}{2}$	A1	
10(a)	differentiation of a quotient or equivalent product	M1	
	correct differentiation of e^{3x}	B1	
	$\frac{dy}{dx} = \frac{3e^{3x}(4x^2 + 1) - 8xe^{3x}}{(4x^2 + 1)^2}$ or $\frac{dy}{dx} = \frac{3e^{3x}}{4x^2 + 1} - \frac{8xe^{3x}}{(4x^2 + 1)^2}$	A1	everything else correct including brackets where needed, allow unsimplified

Question	Answer	Marks	Guidance
10(b)(i)	one term differentiated correctly	M1	
	$\frac{dy}{dx} = -4\sin\left(x + \frac{\pi}{3}\right) + 2\sqrt{3}\cos\left(x + \frac{\pi}{3}\right)$	A1	all correct
	When $x = \frac{\pi}{2}$, $\frac{dy}{dx} = -5$	A1	
10(b)(ii)	$\frac{dy}{dx} \times \frac{dx}{dt} = \frac{dy}{dt}$ $-5 \times \frac{dx}{dt} = 10$ oe	M1	correct use of rates of change
	$\frac{dy}{dt} = -2$	A1	FT answer to (i)



ADDITIONAL MATHEMATICS**0606/12**

Paper 1

May/June 2017

MARK SCHEME

Maximum Mark: 80

Published

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MARK SCHEME NOTES

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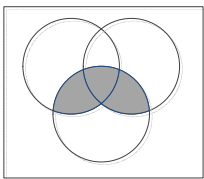
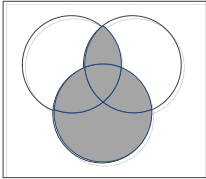
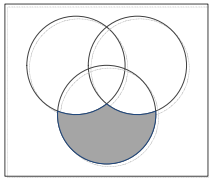
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soi	seen or implied

Question	Answer	Marks	Partial Marks
1	 $(A \cup B) \cap C$  $(A \cap B) \cup C$  $(A' \cap B') \cap C$	B3	B1 for each
2	attempt at differentiating a quotient, must have minus sign and $(x+1)^2$ in the denominator	M1	
	for $(5x^2 + 4)^{-\frac{1}{2}}$	B1	
	for $\frac{1}{2}(10x)(5x^2 + 4)^{-\frac{1}{2}}$	DB1	
	$\frac{dy}{dx} = \frac{(x+1)\frac{1}{2}(10x)(5x^2 + 4)^{-\frac{1}{2}} - (5x^2 + 4)^{\frac{1}{2}}}{(x+1)^2}$	A1	all else correct
	When $x = 3$, $\frac{dy}{dx} = \frac{11}{112}$	A1	must be exact
	Alternative $y = (5x^2 + 4)^{\frac{1}{2}}(x+1)^{-1}$	M1	attempt to differentiate a product
	for $(5x^2 + 4)^{-\frac{1}{2}}$	B1	
	for $\frac{1}{2}(10x)(5x^2 + 4)^{-\frac{1}{2}}$	DB1	
	$\frac{dy}{dx} = \frac{1}{2}10x(5x^2 + 4)^{-\frac{1}{2}}(x+1)^{-1} + (5x^2 + 4)^{\frac{1}{2}}(-(x+1)^{-2})$	A1	all else correct
	When $x = 3$, $\frac{dy}{dx} = \frac{11}{112}$	A1	A1 must be exact

Question	Answer	Marks	Partial Marks
3(a)	$\mathbf{v} = 3\sqrt{5} \times \frac{1}{\sqrt{5}}(\mathbf{i} - 2\mathbf{j})$	M1	attempt to find the magnitude of $(\mathbf{i} - 2\mathbf{j})$ and use
	$= 3\mathbf{i} - 6\mathbf{j}$	A1	for $3\mathbf{i} - 6\mathbf{j}$ only
3(b)	$\mathbf{w} = 2 \cos 30^\circ \mathbf{i} + 2 \sin 30^\circ \mathbf{j}$	M1	attempt to use trigonometry correctly to obtain components
	$= \sqrt{3}\mathbf{i} + \mathbf{j}$	A1	
4	$3^n - n3^{n-1}\left(\frac{x}{6}\right) + n(n-1)3^{n-2}\left(\frac{x}{6}\right)^2$ $3^n = 81$, so $n = 4$	B1	
	$4 \times 3^3 \times -\frac{1}{6} = a$	M1	for $-n3^{n-1}\left(\frac{x}{6}\right)$, ${}^nC_1 3^{n-1}\left(-\frac{x}{6}\right)$ or $\binom{n}{1} 3^{n-1}\left(-\frac{x}{6}\right)$, with/without <i>their n</i>
	$a = -18$	A1	using <i>their n</i> and equating to a to obtain $a = -18$
	$\frac{4 \times 3}{2} \times 3^2 \times \frac{1}{36} = b$	M1	for $n(n-1)3^{n-2}\left(\frac{x}{6}\right)^2$, ${}^nC_2 3^{n-2}\left(\frac{x}{6}\right)^2$ or $\binom{n}{2} 3^{n-2}\left(\frac{x}{6}\right)^2$, with/without <i>their n</i>
	$b = \frac{3}{2}$	A1	using <i>their n</i> and equating to b to obtain $b = \frac{3}{2}$
5(i)	$v = -12 \sin 3t$	B1	
5(ii)	12	B1	FT on <i>their</i> (i) of the form $k \sin 3t$, must be $ k $
5(iii)	$a = -36 \cos 3t$	B1	allow unsimplified
	$3t = \frac{\pi}{2}$, 1.57 or better	B1	
	$t = \frac{\pi}{6}$ or 0.524	B1	
5(iv)	4 cao	B1	may be obtained from knowledge of cosine curve

Question	Answer	Marks	Partial Marks
6(i)	$\frac{1}{\sin \theta} \times \frac{1}{\frac{\cos \theta}{\sin \theta} + \frac{\sin \theta}{\cos \theta}}$	M1	for $\cot \theta = \frac{\cos \theta}{\sin \theta}$, $\tan \theta = \frac{\sin \theta}{\cos \theta}$, $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$
	dealing with the fractions correctly	M1	
	$\frac{1}{\sin \theta} \times \frac{\sin \theta \cos \theta}{\cos^2 \theta + \sin^2 \theta}$	M1	use of identity
	$= \cos \theta$	A1	correct simplification, with all correct
	Alternative 1 $\frac{\operatorname{cosec} \theta}{\frac{1}{\tan \theta} (1 + \tan^2 \theta)}$	M1	dealing with fractions
	$= \frac{\tan \theta \operatorname{cosec} \theta}{\sec^2 \theta}$	M1	use of appropriate identity
	$= \frac{\sin \theta}{\cos \theta} \times \frac{1}{\sin \theta} \times \cos^2 \theta$	M1	for $\cot \theta = \frac{1}{\tan \theta}$, $\tan \theta = \frac{\sin \theta}{\cos \theta}$, $\sec \theta = \frac{1}{\cos \theta}$, $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$
	$= \cos \theta$	A1	correct simplification, with all correct
	Alternative 2 $\frac{\operatorname{cosec} \theta}{\frac{1}{\cot \theta} (\cot^2 \theta + 1)}$	M1	dealing with fractions
	$= \frac{\cot \theta \operatorname{cosec} \theta}{\operatorname{cosec}^2 \theta}$	M1	use of appropriate identity
	$= \frac{\cot \theta}{\operatorname{cosec} \theta}$ $= \frac{\cos \theta}{\sin \theta} \times \sin \theta$	M1	for $\cot \theta = \frac{\cos \theta}{\sin \theta}$, $\tan \theta = \frac{\sin \theta}{\cos \theta}$, $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$
	$= \cos \theta$	A1	correct simplification, with all correct

Question	Answer	Marks	Partial Marks
6(ii)	$\int_0^a \cos 2\theta \, d\theta = \left[\frac{1}{2} \sin 2\theta \right]_0^a$	B1	
	$\frac{1}{2} \sin 2a = \frac{\sqrt{3}}{4}$	M1	use of $\left[k \sin 2\theta \right]_0^a = \frac{\sqrt{3}}{4}$ to obtain $k \sin 2a = \frac{\sqrt{3}}{4}$
	$2a = \frac{\pi}{3}$	DM1	attempt to solve equation of the form $k \sin 2a = \frac{\sqrt{3}}{4}$, with $-1 \leq \frac{\sqrt{3}}{4k} \leq 1$, must have a correct order of operations dealing with the double angle
	$a = \frac{\pi}{6}$, 0.167π or better	A1	
7(i)	$\lg y = \lg A + bx$	B1	straight line form, may be implied by correct values of both A and b later
	Gradient = b ,	M1	equating gradient to b
	$b = 3$	A1	
	Use of substitution into one of the following $2.2 = \lg A + 0.5b$ $3.7 = \lg A + b$ $158.489 = A \times 10^{0.5b}$ $5011.872 = A \times 10^b$ or equivalent valid method leads to $\lg A = 0.7$	M1	
	$A = 5$, 5.01 or $10^{0.7}$	A1	
	Alternative 1 $\lg y = \lg A + bx$	B1	straight line form, may be implied by correct work later
	$2.2 = \lg A + 0.5b$	M1	one correct equation
	$3.7 = \lg A + b$	A1	both equations correct
	attempt to solve 2 correct equations	M1	
	leading to $b = 3$ and $A = 5$, 5.01 or $10^{0.7}$	A1	

Question	Answer	Marks	Partial Marks
7(i)	Alternative 2 $y = A(10^{bx})$ $158.489 = A \times 10^{0.5b}$	M1	one correct equation
	$5011.872 = A \times 10^b$	A1	both correct
	$\frac{5011.872}{158.489} = 10^{0.5b}$	M1	attempt to solve 2 correct equations
	leading to $b = 3$	A1	correct b
	Use of substitution leads to $A = 5, 5.01$ or $10^{0.7}$	A1	correct A
7(ii)	Substitute A and b correctly into either $y = A(10^{0.6b})$, $\lg y = \lg A + 0.6b$ or $\lg y = \lg A + 0.6 \lg 10^b$ or using $\lg y = 1.8 + 0.7$	M1	correct statement using <i>their</i> A and b correctly in either equation or using $\lg y = 3x + 0.7$
	$y = 316, 315$ or $10^{2.5}$	A1	
7(iii)	Substitute A and b correctly into either $600 = A(10^{bx})$, $\lg 600 = \lg A + bx$ or $\lg 600 = \lg A + x \lg 10^b$ or using $\lg 600 = 3x + 0.7$	M1	correct statement using <i>their</i> A and b correctly in either equation or using $\lg y = 3x + 0.7$
	$x = 0.693$	A1	
8(a)(i)	2520	B1	
8(a)(ii)	360	B1	
8(a)(iii)	1080	B1	
8(a)(iv)	6 or 8 to start with No of ways = $2 \times 5 \times 4 \times 3 \times 2$ = 240	B1	
	9 to start with No of ways = $1 \times 5 \times 4 \times 3 \times 3$ = 180	B1	
	Total number of ways = 420	DB1	Dependent on both previous B marks

Question	Answer	Marks	Partial Marks
8(a)(iv)	Alternative 1 All numbers > 6000 – all odd numbers > 6000	B1	plan and attempt to use, must be using 1080
	1080 – 180 – 480	B1	for 180 and 480
	Total number of ways = 420	DB1	Dependent on both previous B marks
	Alternative 2 Even numbers > 60000 : Odd numbers > 60000 7 : 11	B1	correct ratio
	Total number of ways = $\frac{7}{18} \times 1080$	B1	
	= 420	DB1	Dependent on both previous B marks
8(b)(i)	480700	B1	
8(b)(ii)	26460	B1	
8(b)(iii)	With brother and sister ${}^{23}C_5 = 33649$	B1	for ${}^{23}C_5$ or ${}^{23}C_5 \times {}^kC_k$
	Without brother and sister ${}^{23}C_7 = 245157$	B1	for ${}^{23}C_7$ or ${}^{23}C_7 \times {}^kC_k$
	Total number of ways = 278806	B1	for ${}^{23}C_5 + {}^{23}C_7$ and evaluation
9(a)(i)	3×2	B1	
9(a)(ii)	correct attempt to multiply the 2 matrices	M1	
	$C = \begin{pmatrix} 6 & -6 \\ 5 & 2 \\ 19 & -8 \end{pmatrix}$	A2	–1 for each incorrect element
9(b)(i)	$X^{-1} = \frac{1}{13} \begin{pmatrix} -7 & 12 \\ -4 & 5 \end{pmatrix}$	B2	B1 for correct use of determinant B1 for correct matrix
9(b)(ii)	$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{13} \begin{pmatrix} -7 & 12 \\ -4 & 5 \end{pmatrix} \begin{pmatrix} 26 \\ 52 \end{pmatrix}$	B1	
	attempt to evaluate using inverse from (i) together with pre-multiplication to obtain a 2×1 matrix	M1	
	$x = 34, y = 12$	A2	A1 for each
10(i)	0.5	B1	for 0.5 from correct work only

Question	Answer	Marks	Partial Marks
10(ii)	$15^2 = 8^2 + 8^2 - (2 \times 8 \times 8 \times \cos AOB)$ $AOB = 2.43075$ rads	M1	use of cosine rule (or equivalent) to obtain angle AOB .
	$DOC = AOB - 2(\text{their } AOD)$	M1	use of angle AOD and symmetry
	$DOC = 1.43$ to 2 dp	A1	Answer Given: need to have seen either 2.431 or better, or 1.431 or better in previous calculations
	Alternative 1 $15 = 2 \times 8 \times \sin\left(\frac{1 + DOC}{2}\right)$	M1	use of basic trigonometry
	use of $\frac{1 + 0.5DOC}{2}$	M1	may be implied
	$DOC = 1.43$ to 2 dp	A1	Answer Given: need to have seen either 2.431 or better, or 1.431 or better or 1.215 or better in previous calculations
	Alternative 2 $15^2 = 8^2 + 8^2 - (2 \times 8 \times 8 \times \cos AOB)$ $AOB = 2.43075$ rads $\angle AOB \times 8 = \text{arc } AB$	M1	use of cosine rule (or equivalent) to obtain angle AOB .
	$\frac{\text{arc } AB - 8}{8} = \angle DOC$	M1	attempt at DOC , must be a complete method with AOB found
	$DOC = 1.43$ to 2 dp	A1	Answer Given: need to have seen either 2.431 or better, or 1.431 or better or 1.215 or better in previous calculations
	Alternative 3 Equating 2 different forms for the area of triangle AOB $\frac{15\sqrt{31}}{4} = \frac{1}{2} \times 8^2 \sin AOB$, $AOB = 2.43075$ rads	M1	using both different forms of the area of triangle AOB
	$DOC = AOB - 2(\text{their } AOD)$	M1	use of angle AOD and symmetry
	$DOC = 1.43$ to 2 dp	A1	Answer Given: need to have seen either 2.431 or better, or 1.431 or better in previous calculations

Question	Answer	Marks	Partial Marks
10(iii)	$\sin\left(\frac{1.43}{2}\right) = \frac{DC}{8} \text{ or}$ $DC^2 = 8^2 + 8^2 - (2 \times 8 \times 8 \times \cos 1.43)$	M1	use of cosine rule or basic trigonometry to obtain DC
	$DC = 10.49$	A1	awrt 10.5, may be implied
	Perimeter = $10.49 + 4 + 4 + 15$ = 33.5	A1	awrt 33.5
10(iv)	$\frac{1}{2} \times 8^2 (2.43 - \sin 2.43) - \frac{1}{2} \times 8^2 (1.431 - \sin 1.431)$	B1	area of one appropriate sector; allow unsimplified; may be implied by a correct segment
	area of one appropriate triangle, allow unsimplified	B1	
	an appropriate segment, allow unsimplified	B1	
	= 42.8 (allow awrt 42.8)	B1	final answer
	Alternative 1 Area of a trapezium + 2 small segments	B1	one appropriate small sector, allow unsimplified (could be doubled)
	Each small segment = $\frac{1}{2} \times 8^2 (0.5 - \sin 0.5)$	B1	an appropriate triangle, allow unsimplified (could be doubled)
	Area of trapezium = $\frac{1}{2} (15 + 10.5) \times (6.041 - 2.784)$	B1	attempt at trapezium, must have a correct attempt at finding the distance between the parallel sides – allow unsimplified
	Total area = 42.8 (allow awrt 42.8)	B1	final answer
	Alternative 2 Area of 2 small sectors + area of triangle ODC – the area of triangle OAB Area of a small sector = $\frac{1}{2} \times 8^2 \times \frac{1}{2}$	B1	area of small sector, allow unsimplified, (could be doubled)
	Area of triangle ODC = $\frac{1}{2} \times 8^2 \times \sin 1.43$	B1	area of triangle ODC , allow unsimplified
	Area of triangle OAB = $\frac{1}{2} \times 8^2 \times \sin 2.43$	B1	area of triangle OAB , allow unsimplified
	Total area = 42.8 (allow awrt 42.8)	B1	final answer

Question	Answer	Marks	Partial Marks
10(iv)	Alternative 3 Area of rectangle + 2 small triangles + 2 small segments Each small segment = $\frac{1}{2} \times 8^2 (0.5 - \sin 0.5)$	B1	area of a small segment, allow unsimplified, could be doubled
	$\frac{1}{2} \times \frac{(15 - 10.49)}{2} (6.041 - 2.784)$	B1	area of a small triangle, allow unsimplified, could be doubled
	Area of rectangle = $10.49 \times (6.041 - 2.784)$	B1	allow unsimplified, could be doubled
	Total area = 42.8 (allow awrt 42.8)	B1	final answer
	Alternative 4 Sector AOB – sector AOD – sector COB – triangle DOC	B1	area of one appropriate sector; allow unsimplified; may be implied by a correct segment
	$\left(\frac{1}{2} \times 8^2 \times 2.43 \right) - 2 \left(\frac{1}{2} \times 8^2 \times 0.5 \right) - \left(\frac{1}{2} \times 8^2 \sin 1.43 \right)$ Area = sector AOB – segment DC – triangle AOB	B1	area of one appropriate triangle, allow unsimplified
	$\left(\frac{1}{2} \times 8^2 \times 2.43 \right) - (\text{their segment}) - \left(\frac{1}{2} \times 8^2 \sin 2.43 \right)$	B1	an appropriate segment, allow unsimplified
	Total area = 42.8 (allow awrt 42.8)	B1	final answer
11(i)	me^{2x-1} where m is numeric constant	M1	
	$f(x) = \frac{1}{2}e^{2x-1} (+c)$	A1	condone omission of +c
	$\frac{7}{2} = \frac{1}{2} + c$	DM1	correct attempt to find arbitrary constant
	$f(x) = \frac{1}{2}e^{2x-1} + 3$	A1	must be an equation
11(ii)	ke^{2x-1} where k is a numeric constant	M1	
	$f''(x) = 2e^{2x-1}$	A1	
	$2x - 1 = \ln\left(\frac{4}{k}\right)$	DM1	attempt to equate to 4 and use logarithms
	$x = \frac{1}{2} + \ln\sqrt{2}$	A1	



Cambridge International Examinations
Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS

0606/13

Paper 1

May/June 2017

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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Cambridge is publishing the mark schemes for the May/June 2017 series for most Cambridge IGCSE[®], Cambridge International A and AS Level and Cambridge Pre-U components, and some Cambridge O Level components.

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This document consists of **8** printed pages.

MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

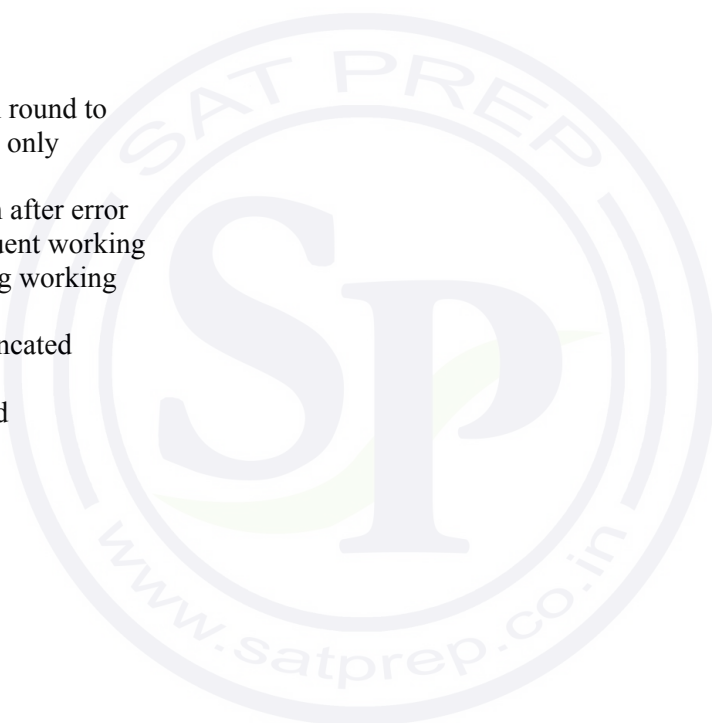
Types of mark

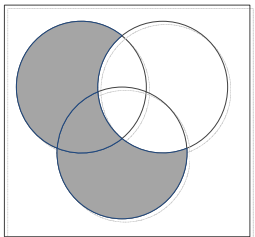
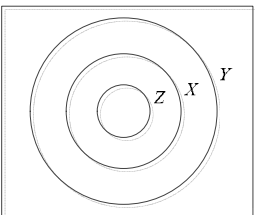
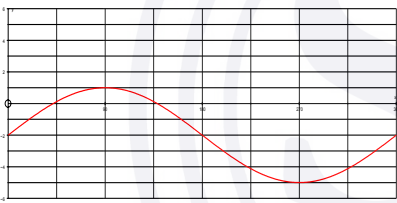
- M Method marks, awarded for a valid method applied to the problem.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B Mark for a correct result or statement independent of Method marks.

When a part of a question has two or more ‘method’ steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation ‘**dep**’ is used to indicate that a particular M or B mark is dependent on an earlier mark in the scheme.

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied



Question	Answer	Marks	Partial Marks
1(a)		1	
1(b)		1	
2(i)	4	1	
2(ii)	40° or $\frac{2\pi}{9}$ or 0.698 rad	1	
3(i)		3	B1 for a complete cycle starting and ending at -2 B1 for max at $y = 1$ and min at $y = -5$ B1 for a completely correct graph
3(ii)	5	1	FT their min value for y
4(i)	$\text{Area} = \frac{1}{2}(3 + 2\sqrt{5})(4 + 6\sqrt{5})$ $= \frac{1}{2}(12 + 26\sqrt{5} + 60)$	M1	use of correct formula and attempt to expand out the brackets
	$= 36 + 13\sqrt{5}$	A1	
4(ii)	$\frac{3 + 2\sqrt{5}}{2 + 3\sqrt{5}}$	B1	
	$= \frac{3 + 2\sqrt{5}}{2 + 3\sqrt{5}} \times \frac{2 - 3\sqrt{5}}{2 - 3\sqrt{5}}$	M1	
	$= \frac{6 - 5\sqrt{5} - 30}{4 - 45}$ $= \frac{24 + 5\sqrt{5}}{41}$	A1	for answer

Question	Answer	Marks	Partial Marks
5	When $x = 4$, $y = 5$	B1	for y
	$\frac{dy}{dx} = \frac{1}{2} \times 4(4x + 9)^{-\frac{1}{2}}$	B1	for $2(4x + 9)^{-\frac{1}{2}}$, allow unsimplified
	When $x = 4$, $\frac{dy}{dx} = \frac{2}{5}$, so perp grad = $-\frac{5}{2}$	M1	obtaining numerical gradient for normal
	Equation of normal $y - 5 = -\frac{5}{2}(x - 4)$ $(2y = 30 - 5x)$	M1	for equation of normal
	$A(6, 0)$, $B(0, 15)$	A2	A1 for each
	Midpoint $\left(3, \frac{15}{2}\right)$	B1	FT on <i>their</i> x/y intercepts
6(a)(i)	dealing with multiplication and addition	M1	implied by 2 correct elements
	$A + 3C = \begin{pmatrix} -12 & 7 \\ 11 & 7 \end{pmatrix}$	A1	
6(a)(ii)	correct attempt to multiply	M1	implied by 2 correct elements
	$BA = \begin{pmatrix} 17 & 9 \\ 14 & 18 \\ -3 & -1 \end{pmatrix}$	A1	
6(b)(i)	$X^{-1} = \frac{1}{10} \begin{pmatrix} -2 & 3 \\ -4 & 1 \end{pmatrix}$	B2	B1 for $\frac{1}{10}$, B1 for $\begin{pmatrix} -2 & 3 \\ -4 & 1 \end{pmatrix}$
6(b)(ii)	$\begin{pmatrix} a & b \\ c & d \end{pmatrix} = \frac{1}{10} \begin{pmatrix} -2 & 3 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} 5 & -10 \\ 15 & 20 \end{pmatrix}$	M1	pre-multiplication using matrix from (b)(i)
	$= \begin{pmatrix} 3.5 & 8 \\ -0.5 & 6 \end{pmatrix}$	A2	-1 for each incorrect element

Question	Answer	Marks	Partial Marks
7(a)	$\text{LHS} = \frac{\frac{\sin^2 \theta}{\cos^2 \theta} + \sin^2 \theta}{\cos \theta + \frac{1}{\cos \theta}}$	M1	for obtaining all in terms of $\sin \theta$ and $\cos \theta$
	$= \frac{\frac{\sin^2 \theta + \sin^2 \theta \cos^2 \theta}{\cos^2 \theta}}{\frac{\cos^2 \theta + 1}{\cos \theta}}$	M1	for simplification using addition of fractions
	$= \frac{\sin^2 \theta (1 + \cos^2 \theta)}{\cos \theta (\cos^2 \theta + 1)}$ $= \frac{\sin^2 \theta}{\cos \theta}$	M1	for factorisation and subsequent cancelling of common term
	$\tan \theta \sin \theta = \text{RHS}$	A1	correct final simplification
	Alternative $\frac{\sec^2 \theta - 1 - \cos^2 \theta + 1}{\cos \theta + \sec \theta}$	M1	use of correct identities
	$= \frac{(\sec \theta - \cos \theta)(\sec \theta + \cos \theta)}{(\sec \theta - \cos \theta)}$ $= \sec \theta - \cos \theta$	M1	attempt to factorise and simplify
	$= \frac{1 - \cos^2 \theta}{\cos \theta}$	M1	simplification to obtain terms in $\sin \theta$ and $\cos \theta$ only
	$= \frac{\sin^2 \theta}{\cos \theta}$ $= \tan \theta \sin \theta$	A1	for final simplification
7(b)	$\sin \phi = \frac{x}{3}, \cos \phi = \frac{3}{y}$	M1	for obtaining $\sin \phi$ and $\cos \phi$ in terms of x and y and attempt to use correct identity
	Using $\sin^2 \phi + \cos^2 \phi = 1$ leads to $\frac{x^2}{9} + \frac{9}{y^2} = 1$ and hence $x^2 y^2 + 81 = 9y^2$	M1	attempt at simplification
	81	A1	

Question	Answer	Marks	Partial Marks
	Alternative method using substitution $\left(9 \times \frac{9}{\cos^2 \phi}\right) - \left(\frac{9}{\cos^2 \phi} \times 9 \sin^2 \phi\right)$	M1	attempt to substitute in for x and y
	$= \left(\frac{81}{\cos^2 \phi}\right) - \left(\frac{81 \sin^2 \phi}{\cos^2 \phi}\right)$	M1	simplification of fractions
	$= \frac{81(1 - \sin^2 \phi)}{\cos^2 \phi} \text{ or } 81(\sec^2 \phi - \tan^2 \phi)$ leading to 81	A1	use of correct identity to obtain 81
8(i)	$p\left(-\frac{1}{2}\right) = -\frac{2}{8} + \frac{a}{4} - 2 + b$	M1	for attempt at $p\left(-\frac{1}{2}\right)$
	leading to $a + 4b = 9$ oe	A1	
	$p(1) = 2 + a + 4 + b$ leading to $a + b = -18$ oe	B1	
	solution of simultaneous equations	M1	
	$a = -27, b = 9$	A1	for both
8(ii)	attempt at factorisation using either long division or observation	M1	
	$(2x + 1)(x^2 - 14x + 9)$	A1	
8(iii)	attempt to solve $q(x) = 0$	M1	
	$x = 7 \pm 2\sqrt{10}, -\frac{1}{2}$	A1	for all 3 solutions
9(i)	$\left[3e^{5x} + e^{-5x}\right]_{-k}^k = 6$	B2	B1 for each term integrated correctly
	$(3e^{5k} + e^{-5k}) - (3e^{-5k} + e^{5k}) = 6$	M1	for use of limits with $ae^{5x} + be^{-5x}$
	$2e^{5k} - 2e^{-5k} = 6$	A1	correct unsimplified
	$e^{5k} - e^{-5k} = 3$	A1	correct simplification to obtain given answer

Question	Answer	Marks	Partial Marks
9(ii)	$y^2 - 3y - 1 = 0$	M1	for correct attempt to obtain a quadratic equation in terms of y or e^{5x}
	$y = \frac{3 \pm \sqrt{9+4}}{2}$, $y = e^{5k} = 3.303$ only	DM1	for attempt to solve quadratic equation and solve for k
	$k = 0.239$	A1	A0 if more than one solution is given
10(i)	for attempt to differentiate a product	M1	
	$\frac{5}{5x+1}$	B2	B1 for $\frac{1}{5x+1}$
	$\frac{dy}{dx} = (10x+2) \times \frac{5}{5x+1} + 10 \ln(5x+1)$	A1	all else correct
10(ii)	$(10x+2) \times \frac{5}{5x+1} = 10$	B1	simplification to obtain 10, allow if seen in (i)
	$10 \int \ln(5x+1) dx$ $= (10x+2) \ln(5x+1) - 10x$	M1	use of result from part (i)
	$\int \ln(5x+1) dx$ $= \frac{(5x+1)}{5} \ln(5x+1) - x$	A1	
10(iii)	$\left[(x+0.2) \ln(5x+1) - x \right]_0^{\frac{1}{5}}$	M1	use of limits in result from (ii)
	$= -\frac{1}{5} + \frac{2}{5} \ln 2 = \frac{-1 + \ln 4}{5}$ cao	A1	
11(i)	attempt to differentiate	M1	
	$\frac{dy}{dx} = 6 - \frac{3}{2}x^{\frac{1}{2}}$	A1	
	When $\frac{dy}{dx} = 0$	M1	equating to zero and attempt to solve
	$x = 16$, $y = 32$	A1	both correct

Question	Answer	Marks	Partial Marks
11(ii)	$\frac{d^2y}{dx^2} = -\frac{3}{4}x^{-\frac{1}{2}}$	B1	correct differentiation
	This is negative so a maximum point	DB1	correct conclusion
11(iii)	When $x = 4$, $\frac{dy}{dx} = 3$	B1	
	$\partial y \approx \frac{dy}{dx} \times h$	M1	use of small increases
	$\approx 3h$	A1	FT their (iii)
12(i)	attempt to differentiate	M1	
	$6 \cos 2t + 6$	A1	
12(ii)	$\cos 2t = -1$	M1	attempt to equate (i) to zero and solve
	$t = \frac{\pi}{2}$	A1	
12(iii)	attempt to integrate	M1	
	$x = -\frac{3}{2} \cos 2t + 3t^2 + 2t \quad (+c)$	A2	-1 for each error
	When $t = 0$, $x = 0$, so $c = \frac{3}{2}$	M1	attempt to find c
	$x = \frac{3}{2} - \frac{3}{2} \cos 2t + 3t^2 + 2t$	A1	

ADDITIONAL MATHEMATICS**0606/12**

Paper 12

March 2017

MARK SCHEME

Maximum Mark: 80

Published

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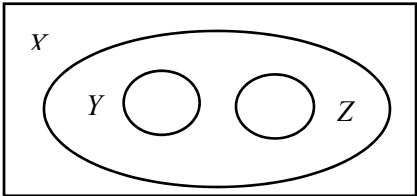
Types of mark

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- A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.
- B** Mark for a correct result or statement independent of Method marks.

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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
nfw	not from wrong working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question	Answer	Marks	Part Marks
1 (a) (i)	0	B1	
	(ii) 10	B1	
		B1	either $X \cap Y = Y$ or $X \cap Z = Z$
		B1	$Y \cap Z = \emptyset$
		B1	completely correct Venn diagram.

Question	Answer	Marks	Part Marks
2 (i)		B1 B1 B1	2 complete cycles having a maximum at $y = 4$ and a minimum at $y = -2$ completely correct curve
(ii)	$(90^\circ, -2)$	B1	
3	$a^5 + 5a^4\left(\frac{x}{4}\right) + 10a^3\left(\frac{x}{4}\right)^2$ $a^5 = 32$, so $a = 2$ $b = 5 \times \frac{1}{4} \times (\text{their } a)^4$, leading to $b = 20$ $c = 10 \times \frac{1}{16} \times (\text{their } a)^3$ leading to $c = 5$	B1 M1 A1 M1 A1	correct attempt to obtain b
4 (a) (i)	$\frac{1}{10} \begin{pmatrix} 4 & 3 \\ -2 & 1 \end{pmatrix}$	B1 B1	for $\frac{1}{\text{determinant}}$ for matrix
(ii)	$M = \frac{1}{10} \begin{pmatrix} 4 & 3 \\ -2 & 1 \end{pmatrix} \begin{pmatrix} -1 & -5 \\ 4 & 2 \end{pmatrix}$ $M = \frac{1}{5} \begin{pmatrix} 4 & -7 \\ 3 & 6 \end{pmatrix}$ oe	M1 A2,1,0	pre-multiplication by the matrix from part (i) -1 each element error
(b)	$-3a + 2 = 4(6a - 4)$ $a = \frac{2}{3}$	M1 A1	correct use of a determinant

Question	Answer	Marks	Part Marks
5 (i)	$\begin{aligned} \text{LHS} &= \frac{1}{\sin \theta} - \sin \theta \\ &= \frac{1 - \sin^2 \theta}{\sin \theta} \\ &= \frac{\cos^2 \theta}{\sin \theta} \\ &= \cot \theta \cos \theta \end{aligned}$	M1 M1 A1	dealing with $\operatorname{cosec} \theta$ and attempt at dealing with fractions correct use of identity completely correct proof
(ii)	$\begin{aligned} \cot \theta \cos \theta &= \frac{1}{3} \cos \theta \\ 3 \cot \theta \cos \theta - \cos \theta &= 0 \\ \cos \theta (3 \cot \theta - 1) &= 0 \\ \cos \theta &= 0 \quad \cot \theta = \frac{1}{3}, \text{ so } \tan \theta = 3 \\ \theta &= \frac{\pi}{2}, \frac{3\pi}{2}, \theta = 1.25, 4.39 \end{aligned}$	M1 M1 A1,A1	use of part (i), manipulation and factorisation dealing with $\cot \theta$ and attempt to solve A1 for each pair of solutions (allow 1.57 and 4.71)
6 (a) (i)	40 320	B1	
(ii)	720	B1	
(iii)	5040	B1	
(b) (i)	35	B1	
(ii)	1	B1	
(iii)	Twins in team of 4 ${}^5C_2 = 10$ Twins in team of 3 $= 5$ Total = 15 www	B1 B1 B1	

Question	Answer	Marks	Part Marks
7 (a)	$\frac{102}{17} \begin{pmatrix} 8 \\ -15 \end{pmatrix}$	M1	attempt to obtain magnitude of $\begin{pmatrix} 8 \\ -15 \end{pmatrix}$ and use it
	$\begin{pmatrix} 48 \\ -90 \end{pmatrix}$	A1	
	(b) $\begin{pmatrix} 2p-2q+4 \\ 10p+2q+3 \end{pmatrix} = \begin{pmatrix} p^2 \\ 27 \end{pmatrix}$	M1	dealing with the scalar and with addition
	$2p-2q+4 = p^2$ $10p+2q+3 = 27$	M1 A1	equating like vectors and simplifying both equations correct
	leading to $p^2 - 12p + 20 = 0$	M1	elimination of q and subsequent solution of quadratic
	$p = 2, q = 2$ $p = 10, q = -38$	A1 A1	
8 (i)	$\frac{dy}{dx} = -2\cos 2x (+c)$	M1 A1	integration to obtain the form $a \cos 2x$ correct, condone omission of c
	$5 = -2\cos \pi + c$	M1	attempt to find c
	$\frac{dy}{dx} = 3 - 2\cos 2x$	A1	May be implied by a correct c
	(ii) $y = 3x - \sin 2x (+c)$	M1 A1	integration to obtain the form $a \sin 2x$ correct, condone omission of c
	$-\frac{1}{2} = \frac{\pi}{4} - \frac{1}{2} + c$	M1	attempt to find c
	$y = 3x - \sin 2x - \frac{\pi}{4}$ oe	A1	
	(iii) When $x = \frac{\pi}{12}$, $\frac{dy}{dx} = 3 - \sqrt{3}$		
	Normal equation: $y + \frac{1}{2} = \frac{1}{\sqrt{3}-3} \left(x - \frac{\pi}{12} \right)$	M1 A1FT	attempt to obtain perpendicular gradient and normal equation FT on their $\frac{dy}{dx}$ from (i). Allow unsimplified
	$y = -0.789x - 0.294$ cao	A1	

Question	Answer	Marks	Part Marks	
9	(i)	$\frac{1}{2} \times 10^2 \times \theta = 20\pi$	M1	use of sector area to obtain θ
		$\theta = \frac{2\pi}{5}$	A1	
	(ii)	Arc length $AB = 4\pi$	B1FT	FT <i>their</i> θ
		$BC^2 = 10^2 + 10^2 - (2 \times 10 \times 10 \times \cos 2\theta)$		
		or $\frac{BC}{\sin \frac{4\pi}{5}} = \frac{10}{\sin \frac{\pi}{10}}$	M1	valid attempt to obtain BC
		$BC = 19.02$	A1	
		Perimeter = 50.6	A1	
	(iii)	Area =		
		Either		
		$\left(\frac{1}{2} \times 19.02^2 \sin \frac{\pi}{5}\right)$	M1	area of triangle ACB
	$+ \left(20\pi - \left(\frac{1}{2} \times 10^2 \sin \frac{2\pi}{5}\right)\right)$	M1	area of relevant segment	
	= 121.6 allow awrt 122	A1		
	Or			
	$20\pi + 2\left(\frac{1}{2} \times 10 \times 10 \sin \frac{4\pi}{5}\right)$	M1,M1	M1 for area of triangle AOB or AOC	
	= 121.6 allow awrt 122	A1	M1 for a complete method	

Question	Answer	Marks	Part Marks
10	$(2x-5)^{\frac{3}{2}} = 3\sqrt{3}$ $x = 4$ <p>At A $x = 2.5$ Either</p> $\text{Area} = \frac{1}{2} \times \frac{3}{2} \times 3\sqrt{3} - \int_{2.5}^4 (2x-5)^{\frac{3}{2}} dx$ $= \frac{9\sqrt{3}}{4} - \left[\frac{1}{5} (2x-5)^{2.5} \right]_{2.5}^4$ $= \frac{9\sqrt{3}}{4} - \left(\frac{1}{5} (3)^{2.5} - 0 \right)$ $= \frac{9\sqrt{3}}{20}$ <p>Or</p> <p>line AB: $y = 2\sqrt{3}x - 5\sqrt{3}$</p> $\text{Area} = \int_{2.5}^4 2\sqrt{3}x - 5\sqrt{3} - (2x-5)^{\frac{3}{2}} dx$ $= \left[\sqrt{3}x^2 - 5\sqrt{3}x - \frac{(2x-5)^{\frac{5}{2}}}{5} \right]_{2.5}^4$ $= \frac{9\sqrt{3}}{4} - \frac{9\sqrt{3}}{5}$ $= \frac{9\sqrt{3}}{20}$	M1 A1 B1 M1 M1 A1 DM1 A1 M1 M1 A1 DM1 A1	<p>attempt to find x-coordinate of B</p> <p>x-coordinate of B</p> <p>x-coordinate of A</p> <p>plan and attempt to find the area of the triangle. Allow unsimplified</p> <p>attempt at integration, must be in the form $(2x-5)^{2.5}$</p> <p>correct integration</p> <p>attempt to use limits correctly</p> <p>equation of AB and attempt to integrate</p> <p>attempt at integration, must contain the form $(2x-5)^{2.5}$</p> <p>correct integration</p> <p>attempt to use correct limits correctly</p>
11 (i)	$\ln y = \ln A + bx$ $0.7 = \ln A + b$ $3.7 = \ln A + 2.5b$ <p>leading to $b = 2$ and $\ln A = -1.3$, so $A = 0.273$ or $e^{-1.3}$</p>	B1 M1 A1 A1 M1,A1	<p>may be implied by later work use of either point correctly in above equation or equivalent</p> <p>one correct equation</p> <p>M1 for dealing with \ln correctly to obtain A.</p>
(ii)	$\ln y = -1.3 + 2x$ $\ln y = 2.7$ $y = 14.9$	 M1 A1	 <p>valid attempt to find y. Must include correct substitution and dealing with \ln correctly.</p>



Cambridge International Examinations
Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS

0606/11

Paper 1

October/November 2016

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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This document consists of **6** printed pages.

Page 2	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2016	0606	11

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question	Answer	Marks	Part Marks
1 (a) (i)	10	B1	
(ii)	22	B1	
(iii)	4	B1	
(b) (i)	$Q \subset R$	B1	
(ii)	$P \cap Q = \emptyset$, or $\{ \}$	B1	
2	$a=1, b=-3, c=-1$	B3	B1 for each
3	$3y^2 + 5y - 2 = 0$ $y = \frac{1}{3}, y = -2$ $x = 3^{\frac{1}{3}}, x = 3^{-2}$ $x = 1.44, x = \frac{1}{9}$	B1, B1 M1 M1 A1, A1	B1 for $5y$ or $5\log_3 x$, B1 for -2 for correct attempt at the solution of <i>their</i> quadratic equation for dealing with one base 3 logarithm correctly A1 for each
4 (i)	$32x^{10} - \frac{80}{3}x^7 + \frac{80}{9}x^4$	B3	B1 for each term, powers of x must be simplified
(ii)	Coefficients needed: $\left(3 \times \text{their} - \frac{80}{3} \right) + (1 \times \text{their } 32)$ $= -48$	M1 A1	for dealing with 2 terms Allow A1 for $-48x^7$

Page 3	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2016	0606	11

Question	Answer	Marks	Part Marks
5 (i)	$\frac{dy}{dx} = \frac{3}{2(3x+2)}$	B1	for correct derivative of log function
	When $x = -\frac{1}{3}$, $y = 0$, $\frac{dy}{dx} = \frac{3}{2}$	B1	for $y = 0$
	Equation of normal: $y = -\frac{2}{3}\left(x + \frac{1}{3}\right)$	M1 A1	M1 for attempt at a gradient of a perpendicular from differentiation and the equation of the normal
(ii)	$Q\left(0, -\frac{2}{9}\right)$ or $(0, 0.22)$ or better	B1 ft	Follow through on <i>their c</i> from part (i)
	$R\left(0, \frac{1}{2}\ln 2\right)$ or $(0, 0.35)$ or better	B1	
	Area of $PQR = \frac{1}{2}\left(\frac{1}{2}\ln 2 + \frac{2}{9}\right) \times \frac{1}{3}$		
	$= 0.0948$	B1	Allow 0.095
6 (a)	YX, XZ	B2	B2 for both with no extras B1 for 1 correct with or without extras B1 for both correct with extras B0 for anything else
(b) (i)	$\frac{1}{18}\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}$	B1, B1	B1 for $\frac{1}{18}$, B1 for $\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}$
(ii)	C = A⁻¹B		
	$= \frac{1}{18}\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}\begin{pmatrix} -4 & 2 \\ 10 & 4 \end{pmatrix}$	M1	for pre-multiplication
	$= \begin{pmatrix} -1 & 1 \\ 2 & 0 \end{pmatrix}$	A1, A1	A1 for any correct pair of elements, but must be from correct matrices

Page 4	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2016	0606	11

Question	Answer	Marks	Part Marks
7 (i)	$(0, \sqrt{3})$ or $(0, 1.73)$ or better	B1	
(ii)	$\left(\frac{\pi}{6}, 2\right)$ or $(0.524, 2)$ or better	B1, B1	B1 for each
(iii)	$\cos\left(x - \frac{\pi}{6}\right) = 0$ $x = \frac{2\pi}{3}$ oe or 2.09 or better	M1 A1	for correct attempt to solve trigonometric equation
(iv)	$2\sin\left(x - \frac{\pi}{6}\right)$ (+c)	B1	
(v)	Area = $\left[2\sin\left(x - \frac{\pi}{6}\right)\right]_0^{\frac{2\pi}{3}}$ = 2 + 1 = 3	M1 A1	for correct use of their limits, in radians, into $k\sin\left(x - \frac{\pi}{6}\right)$.
8 (i)	$47 - 24 = 12\theta$ $\theta = \frac{23}{12}$, so $\theta = 1.917$ or better $\theta = 1.92$ to 2dp	M1 A1	for complete correct method to get $\theta =$ must have evidence of working to more than 2 dp, allow if 1.916 seen (truncated)
(ii)	$\sin\frac{\theta}{2} = \frac{CD/2}{12}$ $CD = \text{awrt } 19.6 \text{ or } 19.7$	M1 A1	for a complete method, may use cosine rule to get CD
(iii)	Area of sector = awrt 138 Area of triangle AOB = awrt 67 or 68 Area of segment = awrt 70 or 71 $AD \times AB + \text{segment area} = 425$ leading to $AD = \text{awrt } 18.1 \text{ or } 18.0$ Alternative method: Area of sector = awrt 138 Difference in length between BC (or AD) and OM where M is the midpoint of $CD = 6.88$, allow awrt 6.9 Remaining area consists of two trapezia each of width 9.85 and each of area 143.4 $\frac{1}{2}(2BC - 6.88) \times 9.85 = 143.4$ oe leading to $AD = \text{awrt } 18.1 \text{ or } 18.0$	B1 M1 M1 M1 A1 B1 M1 M1 M1 A1	for sector area, allow unsimplified for a correct attempt at area for segment area (<i>their</i> sector area – <i>their</i> triangle area) for complete method to find AD Allow A1 for 18 for sector area for attempt to find difference between parallel sides for area of one trapezium $\frac{1}{2}(2BC - \text{their } 6.88) \times \text{their } 9.85$ oe for attempt to find either BC or AD

Page 5	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2016	0606	11

Question	Answer	Marks	Part Marks
9 (i)	$p\left(\frac{3}{2}\right): \frac{27a}{8} - \left(4 \times \frac{9}{4}\right) + \frac{3b}{2} + 18 (=0)$	M1	for attempt at $p\left(\frac{3}{2}\right)$
	$p'\left(\frac{3}{2}\right) = \left(3a \times \frac{9}{4}\right) - \left(8 \times \frac{3}{2}\right) + b (=0)$	M1	for differentiation and attempt at $p'\left(\frac{3}{2}\right)$
	leading to $9a + 4b + 24 = 0$ oe	M1	for solution of simultaneous equations, to get either a or b
	and $27a + 4b - 48 = 0$ oe	A1	for both
	leading to $a = 4, b = -15$		
(ii)	$(x+2)(2x-3)^2$ oe	M1, A1	M1 for attempt at long division or factorisation
(iii)	$(x+2)(2x-3)^2 = x+2$		
	$x+2=0, x=-2$	B1	Must be using $(x+2)$ correctly using part (ii) to get $x=-2$
	$(2x-3)^2 = 1$	M1	for solution of the quadratic equation
	leading to $x=1, x=2$	A1	
10 (a) (i)	$20U + \frac{1}{2}\left(U + \frac{U}{2}\right)10 = 165$	M1	for realising that area under the graph is needed and attempt to find an area
		DM1	for equating their area to 165 and attempt to solve
	leading to $U = 6$	A1	
	(ii) Gradient of line: -0.3	M1, A1	M1 for use of the gradient, must be negative
	(b) (i) 27	B1	
	(ii) $t^2 = 8 \ln 4$	M1	for a correct attempt to solve $e^{\frac{t^2}{8}} = 4$
	$t = 3.33$ or better	A1	
	(iii) acceleration $= 3 \frac{2t}{8} e^{\frac{t^2}{8}} \left(e^{\frac{t^2}{8}} - 4 \right)^2$	M1, A1	M1 for a correct attempt to differentiate using the chain rule
	When $t = 1, a = 6.98$	M1, A1	M1 for use of $t = 1$ in their acceleration

Page 6	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2016	0606	11

Question	Answer	Marks	Part Marks
11 (i)	$\ln y = \ln A + x \ln b$	B1	may be implied, if equation not seen specifically, by correct values for A and b for use of gradient to obtain $\ln b$
	Gradient: $\ln b = -\frac{0.12}{8}, = -0.015$	M1	
	$b = 0.985$	A1	Allow A1 for $e^{-0.015}$
	Intercept: $\ln A = 0.26$	DM1	for use of one of the given points correctly
	$A = 1.30$	A1	Allow A1 for $e^{0.26}$ or 1.3
	Alternative 1		
	$\ln y = \ln A + x \ln b$	B1	
	$0.2 = 4 \ln b + \ln A$	M1	for one correct equation
	$0.08 = 12 \ln b + \ln A$	DM1	for attempt to obtain either $\ln A$ or $\ln b$ from simultaneous equations
	$A = 1.30$ and $b = 0.985$	A1, A1	Allow A1 for $b = e^{-0.015}$ and $a = e^{0.26}$ or 1.3
(ii)	Alternative 2		
	$1.22 = Ab^4$	B1	
	$1.08 = Ab^{12}$	B1	
		M1	for correct attempt to obtain b or A , must already have B2
	$A = 1.30$ and $b = 0.985$	A1, A1	Allow A1 for $b = e^{-0.015}$ and $a = e^{0.26}$ or 1.3
	When $x = 6$, $\ln y = 0.17$	M1	for $\ln y = \text{their } \ln A + 6 \text{ their } \ln b$ or $y = \text{their } A \times (\text{their } b)^6$
	$y = 1.19$	A1	allow awrt 1.18 to 1.20
	When $y = 1.1$, $\ln y = 0.095$	M1	for $\ln 1.1 = \text{their } \ln A + x \text{ their } \ln b$ or $1.1 = \text{their } A \times (\text{their } b)^x$
	$x = 11$	A1	allow 10.5 to 11.5



Cambridge International Examinations
Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS

0606/12

Paper 1

October/November 2016

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

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Page 2	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2016	0606	12

Abbreviations

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isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question	Answer	Marks	Part Marks
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(ii)	22	B1	
(iii)	4	B1	
(b) (i)	$Q \subset R$	B1	
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3	$3y^2 + 5y - 2 = 0$ $y = \frac{1}{3}, y = -2$ $x = 3^{\frac{1}{3}}, x = 3^{-2}$ $x = 1.44, x = \frac{1}{9}$	B1, B1 M1 M1 A1, A1	B1 for $5y$ or $5\log_3 x$, B1 for -2 for correct attempt at the solution of <i>their</i> quadratic equation for dealing with one base 3 logarithm correctly A1 for each
4 (i)	$32x^{10} - \frac{80}{3}x^7 + \frac{80}{9}x^4$	B3	B1 for each term, powers of x must be simplified
(ii)	Coefficients needed: $\left(3 \times \text{their} - \frac{80}{3} \right) + (1 \times \text{their } 32)$ $= -48$	M1 A1	for dealing with 2 terms Allow A1 for $-48x^7$

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	Cambridge IGCSE – October/November 2016	0606	12

Question	Answer	Marks	Part Marks
5 (i)	$\frac{dy}{dx} = \frac{3}{2(3x+2)}$	B1	for correct derivative of log function
	When $x = -\frac{1}{3}$, $y = 0$, $\frac{dy}{dx} = \frac{3}{2}$	B1	for $y = 0$
	Equation of normal: $y = -\frac{2}{3}\left(x + \frac{1}{3}\right)$	M1 A1	M1 for attempt at a gradient of a perpendicular from differentiation and the equation of the normal
(ii)	$Q\left(0, -\frac{2}{9}\right)$ or $(0, 0.22)$ or better	B1 ft	Follow through on <i>their c</i> from part (i)
	$R\left(0, \frac{1}{2}\ln 2\right)$ or $(0, 0.35)$ or better	B1	
	Area of $PQR = \frac{1}{2}\left(\frac{1}{2}\ln 2 + \frac{2}{9}\right) \times \frac{1}{3}$		
	$= 0.0948$	B1	Allow 0.095
6 (a)	YX, XZ	B2	B2 for both with no extras B1 for 1 correct with or without extras B1 for both correct with extras B0 for anything else
(b) (i)	$\frac{1}{18}\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}$	B1, B1	B1 for $\frac{1}{18}$, B1 for $\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}$
(ii)	$C = A^{-1}B$ $= \frac{1}{18}\begin{pmatrix} 7 & 1 \\ -4 & 2 \end{pmatrix}\begin{pmatrix} -4 & 2 \\ 10 & 4 \end{pmatrix}$ $= \begin{pmatrix} -1 & 1 \\ 2 & 0 \end{pmatrix}$	M1 A1, A1	for pre-multiplication A1 for any correct pair of elements, but must be from correct matrices

Page 4	Mark Scheme	Syllabus	Paper
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7 (i)	$(0, \sqrt{3})$ or $(0, 1.73)$ or better	B1	
(ii)	$\left(\frac{\pi}{6}, 2\right)$ or $(0.524, 2)$ or better	B1, B1	B1 for each
(iii)	$\cos\left(x - \frac{\pi}{6}\right) = 0$ $x = \frac{2\pi}{3}$ oe or 2.09 or better	M1 A1	for correct attempt to solve trigonometric equation
(iv)	$2\sin\left(x - \frac{\pi}{6}\right)$ (+c)	B1	
(v)	Area = $\left[2\sin\left(x - \frac{\pi}{6}\right)\right]_0^{\frac{2\pi}{3}}$ = 2 + 1 = 3	M1 A1	for correct use of their limits, in radians, into $k\sin\left(x - \frac{\pi}{6}\right)$.
8 (i)	$47 - 24 = 12\theta$ $\theta = \frac{23}{12}$, so $\theta = 1.917$ or better $\theta = 1.92$ to 2dp	M1 A1	for complete correct method to get $\theta =$ must have evidence of working to more than 2 dp, allow if 1.916 seen (truncated)
(ii)	$\sin\frac{\theta}{2} = \frac{CD/2}{12}$ $CD = \text{awrt } 19.6 \text{ or } 19.7$	M1 A1	for a complete method, may use cosine rule to get CD
(iii)	Area of sector = awrt 138 Area of triangle AOB = awrt 67 or 68 Area of segment = awrt 70 or 71 $AD \times AB + \text{segment area} = 425$ leading to $AD = \text{awrt } 18.1 \text{ or } 18.0$ Alternative method: Area of sector = awrt 138 Difference in length between BC (or AD) and OM where M is the midpoint of $CD = 6.88$, allow awrt 6.9 Remaining area consists of two trapezia each of width 9.85 and each of area 143.4 $\frac{1}{2}(2BC - 6.88) \times 9.85 = 143.4$ oe leading to $AD = \text{awrt } 18.1 \text{ or } 18.0$	B1 M1 M1 M1 A1 B1 M1 M1 M1 A1	for sector area, allow unsimplified for a correct attempt at area for segment area (<i>their</i> sector area – <i>their</i> triangle area) for complete method to find AD Allow A1 for 18 for sector area for attempt to find difference between parallel sides for area of one trapezium $\frac{1}{2}(2BC - \text{their } 6.88) \times \text{their } 9.85$ oe for attempt to find either BC or AD

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9 (i)	$p\left(\frac{3}{2}\right): \frac{27a}{8} - \left(4 \times \frac{9}{4}\right) + \frac{3b}{2} + 18 (=0)$	M1	for attempt at $p\left(\frac{3}{2}\right)$
	$p'\left(\frac{3}{2}\right) = \left(3a \times \frac{9}{4}\right) - \left(8 \times \frac{3}{2}\right) + b (=0)$	M1	for differentiation and attempt at $p'\left(\frac{3}{2}\right)$
	leading to $9a + 4b + 24 = 0$ oe	M1	for solution of simultaneous equations, to get either a or b
	and $27a + 4b - 48 = 0$ oe	A1	for both
	leading to $a = 4, b = -15$		
(ii)	$(x+2)(2x-3)^2$ oe	M1, A1	M1 for attempt at long division or factorisation
(iii)	$(x+2)(2x-3)^2 = x+2$		
	$x+2=0, x=-2$	B1	Must be using $(x+2)$ correctly using part (ii) to get $x=-2$
	$(2x-3)^2 = 1$	M1	for solution of the quadratic equation
	leading to $x=1, x=2$	A1	
10 (a) (i)	$20U + \frac{1}{2}\left(U + \frac{U}{2}\right)10 = 165$	M1	for realising that area under the graph is needed and attempt to find an area
		DM1	for equating their area to 165 and attempt to solve
	leading to $U = 6$	A1	
	(ii) Gradient of line: -0.3	M1, A1	M1 for use of the gradient, must be negative
	(b) (i) 27	B1	
(ii)	$t^2 = 8 \ln 4$	M1	for a correct attempt to solve $e^{\frac{t^2}{8}} = 4$
	$t = 3.33$ or better	A1	
(iii)	acceleration $= 3 \frac{2t}{8} e^{\frac{t^2}{8}} \left(e^{\frac{t^2}{8}} - 4 \right)^2$	M1, A1	M1 for a correct attempt to differentiate using the chain rule
	When $t = 1, a = 6.98$	M1, A1	M1 for use of $t = 1$ in their acceleration

Page 6	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks
11 (i)	$\ln y = \ln A + x \ln b$	B1	may be implied, if equation not seen specifically, by correct values for A and b for use of gradient to obtain $\ln b$
	Gradient: $\ln b = -\frac{0.12}{8}, = -0.015$	M1	
	$b = 0.985$	A1	Allow A1 for $e^{-0.015}$
	Intercept: $\ln A = 0.26$	DM1	for use of one of the given points correctly
	$A = 1.30$	A1	Allow A1 for $e^{0.26}$ or 1.3
	Alternative 1		
	$\ln y = \ln A + x \ln b$	B1	
	$0.2 = 4 \ln b + \ln A$	M1	for one correct equation
	$0.08 = 12 \ln b + \ln A$	DM1	for attempt to obtain either $\ln A$ or $\ln b$ from simultaneous equations
	$A = 1.30$ and $b = 0.985$	A1, A1	Allow A1 for $b = e^{-0.015}$ and $a = e^{0.26}$ or 1.3
(ii)	Alternative 2		
	$1.22 = Ab^4$	B1	
	$1.08 = Ab^{12}$	B1	
		M1	for correct attempt to obtain b or A , must already have B2
	$A = 1.30$ and $b = 0.985$	A1, A1	Allow A1 for $b = e^{-0.015}$ and $a = e^{0.26}$ or 1.3
	When $x = 6$, $\ln y = 0.17$	M1	for $\ln y = \text{their } \ln A + 6 \text{ their } \ln b$ or $y = \text{their } A \times (\text{their } b)^6$
	$y = 1.19$	A1	allow awrt 1.18 to 1.20
	When $y = 1.1$, $\ln y = 0.095$	M1	for $\ln 1.1 = \text{their } \ln A + x \text{ their } \ln b$ or $1.1 = \text{their } A \times (\text{their } b)^x$
	$x = 11$	A1	allow 10.5 to 11.5



Cambridge International Examinations
Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS

0606/13

Paper 1

October/November 2016

MARK SCHEME

Maximum Mark: 80

<p>Published</p>

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

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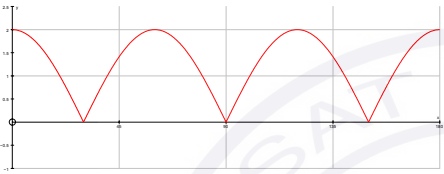
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This document consists of **8** printed pages.

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Abbreviations

awrt answers which round to
 cao correct answer only
 dep dependent
 FT follow through after error
 isw ignore subsequent working
 oe or equivalent
 rot rounded or truncated
 SC Special Case
 soi seen or implied
 www without wrong working

Question	Answer	Marks	Part Marks
1		B1 B1 B1	for symmetrical shape as in the diagram with curved maxima of equal height and cusps on the x-axis for a complete 'curve' with all low points on the x-axis and all high points on $y = 2$ for a complete 'curve' meeting the x-axis at $x = 30^\circ, 90^\circ, 150^\circ$ only.
2	$= \frac{4m^2 - 9}{2m + 3}$ $= \frac{(2m - 3)(2m + 3)}{2m + 3}$ $= 2m - 3$ <p>Alternative Method</p> $(4m\sqrt{m} - \frac{9}{\sqrt{m}})$ $= (2\sqrt{m} + \frac{3}{\sqrt{m}})(Am + B)$ <p>Comparing coefficients $2A = 4, 3A + 2B = 0, 3B = -9$</p>	M1 A1 A1 M1 A1 A1	for multiplying each term by \sqrt{m} , using a common denominator of \sqrt{m} or for multiplying numerator and denominator by $2\sqrt{m} - \frac{3}{\sqrt{m}}$ for a correct expression that will cancel $\frac{(2m - 3)(2m + 3)}{2m + 3}, \frac{(4m^2 - 9)(2m - 3)}{(4m^2 - 9)}$ $\frac{(2m - 3)(2m + 3)(2m - 3)}{(2m + 3)(2m - 3)}$, or equivalents for $2m - 3$ or $A = 2, B = -3$ for correct expansion for correct comparisons to obtain A and B for $2m - 3$ or $A = 2, B = -3$

Page 3	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks
3 (i)	$3x^2 - 2xp + (p+3) = 0$ $(-2p)^2 - 4 \times 3 \times (p+3) \geq 0$ oe $p^2 \geq 3(p+3)$ or $4p^2 - 12p - 36 \geq 0$ $p^2 - 3p - 9 \geq 0$	M1 DM1 A1	for obtaining a 3-term quadratic in the form $ax^2 + bx + c (= 0)$ for correct substitution of <i>their</i> a , b and c into ' $b^2 - 4ac$ ' and use of discriminant. for full correct working, \geq the only sign used, \geq used before division by 4 and \geq used in answer line and penultimate line.
3 (ii)	Correct method of solution $p^2 - 3p - 9 = 0$ leading to critical values $p = \frac{3 \pm 3\sqrt{5}}{2}$ $p \leq \frac{3 - 3\sqrt{5}}{2}$, $p \geq \frac{3 + 3\sqrt{5}}{2}$	M1 A1 A1	for correct substitution in the quadratic formula or for correct attempt to complete the square. (allow 1 sign error in either method) for both correct critical values for correct range
4 (i)	$64 - 48x + 15x^2$	B3	for each correct term
4 (ii)	$(4 \times '64') + (2 \times '-48') + (3 \times '15')$ = 205 cao	M1 A1 A1	for correctly obtaining three products using <i>their</i> coefficients in (i) for two correct out of three products (unsimplified) cao for 205 selected as final answer
5 (i)	$\log_9 xy = \log_9 x + \log_9 y$ $= \frac{\log_3 x}{\log_3 9} + \frac{\log_3 y}{\log_3 9}$ $= \frac{\log_3 x}{2} + \frac{\log_3 y}{2} = \frac{5}{2}$ $\log_3 x + \log_3 y = 5$ Alternative method $\log_9 xy = \frac{5}{2}$ $xy = 9^{\frac{5}{2}} = 3^5$ $\log_3 xy = 5$ $\log_3 x + \log_3 y = 5$	M1 M1 A1 M1 M1 A1	for use of $\log AB = \log A + \log B$ for correct method for change of base. Division by $\log_3 9$ should be seen and not implied. for dealing with 2 correctly and 'finishing off' for obtaining xy as a power of 3 for correct use of \log_3 for using law for logs and arriving at correct answer

Page 4	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks
(ii)	$\log_3 x(5 - \log_3 x) = -6$ $-(\log_3 x)^2 + 5\log_3 x = -6$ $(\log_3 x)^2 - 5\log_3 x - 6 = 0$ leading to $\log_3 x = 6, \log_3 x = -1$ $x = 729, x = \frac{1}{3}$ $y = \frac{1}{3}, y = 729$	M1 A1 A1 DM1 A1	for substitution, correct expansion of brackets and manipulation to get a 3 term quadratic for a correct quadratic equation in the form $ax^2 + bx + c = 0$ for both solutions for method of solution of $\log_3 x = k$ or $\log_3 y = k$ for all x and y correct
6 (i)	$\frac{6x}{3x^2 - 11}$	M1 A1	M1 for $\frac{mx}{3x^2 - 11}$
(ii)	$p = \frac{1}{6}$	B1	FT for $p = \frac{1}{m}$
(iii)	$\frac{1}{6}\ln(3a^2 - 11) - \frac{1}{6}\ln 1 = \ln 2$ $\ln(3a^2 - 11) = \ln 2^6$ $3a^2 - 11 = 64$ $a = 5$ only	M1 DM1 DM1 A1	for correct use of limits in $p \ln(3x^2 - 11)$ May be implied by following equation for dealing with logs correctly for solution of $3a^2 - 11 = k$ for 5 obtained from an exact method

Page 5	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks
7 (i)	$\ln y = \ln A + \frac{b}{x}$ Gradient: $b = -0.8$ Intercept or use of equation: $\ln A = 4.7$ $A = 110$ Alternative Method $3.5 = \ln A + 1.5b$ and $1.5 = \ln A + 4b$ leading to $b = -0.8$ $\ln A = 4.7$ and $A = 110$ Alternative Method $e^{1.5} = Ae^{4b}$ $e^{3.5} = Ae^{1.5b}$ leading to $b = -0.8$ and $A = 110$	B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1 B1	for equation, may be implied, must be using \ln unless recovered for $b = -0.8$ oe for $\ln A = 4.7$ oe, allow 4.65 to 4.75 for $A = 110$, allow 105 to 116 Allow A in terms of e for one equation for $b = -0.8$ for $\ln A = 4.7$ for $A = 110$ or $e^{4.7}$ for $e^{1.5} = Ae^{4b}$ or $4.48 = Ae^{4b}$ for $e^{3.5} = Ae^{1.5b}$ or $33.1 = Ae^{1.5b}$ for $b = -0.8$ for $A = 110$ or $e^{4.7}$
(ii)	When $x = 0.32$, $\frac{1}{x} = 3.125$, $\ln y = 2.2$ $y = 9$ (allow 8.5 to 9.5) or $e^{2.2}$	M1 A1	for a complete method to obtain y , using either the graph, using <i>their</i> values in the equation for $\ln y$ or using <i>their</i> values in the equation for y .
(iii)	When $y = 20$, $\ln y = 3$, $\frac{1}{x} = 2.125$ so $x = 0.47$ (allow 0.45 to 0.49)	M1 A1	for a complete method to obtain x , using either the graph, using <i>their</i> values in the equation for $\ln y$ or using <i>their</i> values in the equation for y .

Page 6	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks
8 (a) (i)	$\frac{\operatorname{cosec} \theta}{\operatorname{cosec} \theta - \sin \theta} = \frac{\frac{1}{\sin \theta}}{\frac{1}{\sin \theta} - \sin \theta}$ $= \frac{1}{1 - \sin^2 \theta} \text{ or } = \frac{\frac{1}{\sin \theta}}{\frac{(1 - \sin^2 \theta)}{\sin \theta}}$ $= \frac{1}{\cos^2 \theta}$ $= \sec^2 \theta$ <p>Alternative Method using cosec</p> $\frac{\operatorname{cosec} \theta}{\operatorname{cosec} \theta - \sin \theta} = \frac{\operatorname{cosec} \theta}{\operatorname{cosec} \theta - \frac{1}{\operatorname{cosec} \theta}}$ $= \frac{\operatorname{cosec}^2 \theta}{\operatorname{cosec}^2 \theta - 1}$ $= \frac{1 + \cot^2 \theta}{\cot^2 \theta}$ $= \tan^2 \theta + 1 = \sec^2 \theta$	<p>M1</p> <p>DM1</p> <p>A1</p>	<p>for using $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$ and either attempt to multiply top and bottom by $\sin \theta$ or an attempt to combine terms in denominator.</p> <p>for correct use of $1 - \sin^2 \theta = \cos^2 \theta$</p> <p>for completing the proof</p>
(ii)	$\cos^2 \theta = \frac{1}{4}, \quad \cos \theta = \pm \frac{1}{2}$ $\text{or } \tan^2 \theta = 3, \quad \tan \theta = \pm \sqrt{3}$ $\text{or } \sin^2 \theta = \frac{3}{4}, \quad \sin \theta = \pm \frac{\sqrt{3}}{2}$ $\theta = 60^\circ, 120^\circ, 240^\circ, 300^\circ$	<p>M1</p> <p>DM1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>for using $\sin \theta = \frac{1}{\operatorname{cosec} \theta}$ and an attempt to combine terms in denominator.</p> <p>for use of $1 + \cot^2 \theta = \operatorname{cosec}^2 \theta$</p> <p>for completing the proof</p> <p>for using (i) to obtain a value for $\cos^2 \theta$, $\tan^2 \theta$ or $\sin^2 \theta$ and then taking the square root.</p> <p>for two correct values</p> <p>for two further correct values and no extras in range.</p>
(b)	$\tan \left(x + \frac{\pi}{4} \right) = \frac{1}{\sqrt{3}}$ $x = \frac{\pi}{6} - \frac{\pi}{4}, \frac{7\pi}{6} - \frac{\pi}{4}, \frac{13\pi}{6} - \frac{\pi}{4}$ $x = \left(-\frac{\pi}{12} \right), \frac{11\pi}{12}, \frac{23\pi}{12}$	<p>M1</p> <p>A1,A1</p>	<p>for correct order of operations, can be implied by $x = -\frac{\pi}{12}$</p> <p>A1 for $x = \frac{11\pi}{12}$</p> <p>A1 for $x = \frac{23\pi}{12}$</p> <p>If there are extra solutions in range in addition to the two correct ones then A1A0</p>

Page 7	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks
9	(a) (i) ${}^{18}C_5 = 8568$ mmm	B1	
	(ii) Either		
	${}^{10}C_4 \times {}^8C_1 = 1680$	B1	for a correct plan
	${}^{10}C_3 \times {}^8C_2 = 3360$	B2,1,0	B2 4 correct numbers with no extras B1 3 correct numbers (out of 3 or 4)
	${}^{10}C_2 \times {}^8C_3 = 2520$		
	${}^{10}C_1 \times {}^8C_4 = 700$		
	Total = 8260	B1	for correct total
	Or		
	their ${}^{18}C_5 - ({}^{10}C_5 + {}^8C_5)$	B1	for correct plan
	$8568 - (252 + 56)$	B1	for 252 subtracted
(b)	(i) ${}^{10}P_6 = 151200$	B1	
	(ii) $4 \times {}^8P_4 \times 3$	M1	for correct unsimplified
	= 20160	A1	for correct numerical answer
	(iii) Answer to (i) - 7P_6	M1	for correct plan
	= 146160	A1	for correct unsimplified
		A1	for correct numerical answer
	Alternative:		
	1 symbol: 45360	B2,1,0	B2 for all 3 correct
	2 symbols: 75600		B1 for 2 correct (out of 2 or 3)
	3 symbols: 25200		
	Total: 146160	B1	for correct sum

Page 8	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Part Marks
10 (i)	$f(x) = 3x^2 - 4e^{2x} (+c)$	M1	for one correct term
	passing through $(0, -3)$ $-3 = 3 \times 0 - 4e^0 + c$ $f(x) = 3x^2 - 4e^{2x} + 1$	A1 A1 DM1	for one correct term $3x^2$ or $-4e^{2x}$ for a second correct term with no extras for correct method to find c .
(ii)	$f'(0) = -8$	A1	for correct equation
	Normal: $y + 3 = \frac{1}{8}x$ $8y + 24 = x$ $y = 2 - 3x$	B1 M1 DM1	for $m = \frac{1}{8}$ for equation of normal using $m = \frac{1}{8}$ for solving normal equation simultaneously with $y = 2 - 3x$ to get a value of x
	leads to $x = \frac{8}{5}$ oe Area = $= \frac{1}{2} \times 3 \times \frac{8}{5} = 2.4$ oe	A1 B1	for $x = \frac{8}{5}$, 1.6 oe FT for a numerical answer equal to $\left \frac{1}{2} \times 3 \times \text{their } x \right $
11 (i)	$a = 8t - 8$ When $t = 3$, $a = 16$	B1 B1	for $8t - 8$ for 16
(ii)	0.5, 1.5	B1, B1	B1 for each
(iii)	$s = \frac{4}{3}t^3 - 4t^2 + 3t$	M1 A1	for at least two terms correct all correct
	when $t = \frac{1}{2}$, $s = \frac{2}{3}$	DM1	for calculating displacement when either $t = \frac{1}{2}$ or $t = \frac{3}{2}$
	when $t = \frac{3}{2}$, $s = 0$	DM1	for calculating displacement at $t = \frac{1}{2}$ and doubling.
	total distance travelled = $\frac{4}{3}$	A1	for $\frac{4}{3}$ oe allow 1.33
	Alternative method	M1A1 DM1	As before DM1 for calculating displacement when $t = 0.5$ or for calculating distance travelled between $t = 0.5$ and $t = 1.5$
		DM1	DM1 for doubling distance travelled between $t = 0.5$ and $t = 1.5$ or for adding that distance to displacement at $t = 0.5$
		A1	A1 for $\frac{4}{3}$ oe allow 1.33



Cambridge International Examinations
Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS

0606/11

Paper 1

May/June 2016

MARK SCHEME

Maximum Mark: 80

Published

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This document consists of 7 printed pages.

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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question	Answer	Marks	Guidance
1 (i)	-27	B1	
(ii)	$9 - 8k = 0$ $k = \frac{9}{8}$ Or $\frac{dy}{dx} = 4x - 3$ when $\frac{dy}{dx} = 0$, $x = \frac{3}{4}$ so $k = \frac{9}{8}$ Or completing the square $y = 2\left(x - \frac{3}{4}\right)^2 + k - \frac{9}{8}$ $k = \frac{9}{8}$	M1 A1 M1 A1 M1 A1	for use of discriminant with a complete method to get to $k =$ for a complete method to get to $k =$ for a complete method to get to $k =$
2 (a)	$2^{4(3x-1)} = 2^{3(x+2)}$ or $4^{2(3x-1)} = 4^{\frac{3}{2}(x+2)}$ or $8^{\frac{4}{3}(3x-1)} = 8^{x+2}$ or $16^{3x-1} = 16^{\frac{3}{4}(x+2)}$ leading to $x = \frac{10}{9}$ cao	B1 M1 A1	B1 for a correct statement for equating indices
(b)	$p = \frac{5}{3}$ $q = -2$	B1 B1	

Page 3	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Guidance
3	<p>On x-axis, $2x^2 - 7 = 1$ $x = 2$</p> $\frac{dy}{dx} = \frac{4x}{2x^2 - 7}$ <p>When $x = 2$, $\frac{dy}{dx} = 8$</p> <p>Gradient of normal $= -\frac{1}{8}$</p> <p>Equation of normal $y = -\frac{1}{8}(x - 2)$</p> <p>Required form $x + 8y - 2 = 0$</p>	<p>M1 A1 B1</p> <p>M1 A1</p>	<p>for equating to 1</p> <p>for attempt at perpendicular through <i>their</i> (2, 0), must be using $y = 0$ must be equated to zero with integer coefficients</p>
4 (a)	$\mathbf{A}^2 = \begin{pmatrix} 7 & -2 \\ -3 & 6 \end{pmatrix}$ $\mathbf{A}^2 - 2\mathbf{B} = \begin{pmatrix} 1 & -2 \\ -5 & 2 \end{pmatrix}$	<p>B1 M1 A1</p>	<p>for their $\mathbf{A}^2 - 2\mathbf{B}$</p>
(b)	$\begin{pmatrix} 4 & 1 \\ 10 & 3 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$ <p>so $\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 3 & -1 \\ -10 & 4 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$</p> <p>leading to $\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 1 \\ -3 \end{pmatrix}$</p> <p>$x = 1$ $y = -3$</p>	<p>M1 DM1 A1 A1</p>	<p>for pre-multiplication by <i>their</i> inverse matrix DM1 for attempt at matrix multiplication Allow in matrix form</p>
5 (i)	$\frac{d}{dx} \left(\frac{e^{4x}}{4} - xe^{4x} \right) = e^{4x} - ((x \times 4e^{4x}) + e^{4x})$ $= -4xe^{4x}$	<p>B1 M1 A1 A1</p>	<p>for $\frac{d}{dx} \left(\frac{e^{4x}}{4} \right) = e^{4x}$ for attempt to differentiate a product for a correct product for correct final answer</p>
(ii)	$\int_0^{\ln 2} xe^{4x} dx = -\frac{1}{4} \left[\frac{e^{4x}}{4} - xe^{4x} \right]_0^{\ln 2}$ $= -\frac{1}{4} \left(\left(\frac{16}{4} - 16 \ln 2 \right) - \frac{1}{4} \right)$ $= 4 \ln 2 - \frac{15}{16}$	<p>B1FT B1 M1 A1</p>	<p>FT for use of <i>their</i> $\frac{1}{p} \times \left(\frac{e^{4x}}{4} - xe^{4x} \right)$, must be numerical p, but $\neq 0$ for $e^{4 \ln 2} = 16$ for correct use of limits, must be an integral of the correct form</p>

Page 4	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Guidance
6 (i)	$2 - \sqrt{5} < f(x) \leq 2$	B2	B1 for ≤ 2 B1 for $2 - \sqrt{5} <$ or awrt -0.24 Must be using f , $f(x)$ or y , $2 - \sqrt{5} <$, if not then B1 max
(ii)	$f^{-1}(x) = (2 - x)^2 - 5$ Domain $2 - \sqrt{5} < x \leq 2$ Range y or $-5 \leq f^{-1}(x) < 0$	M1 A1 B1 B1	for a correct method to find the inverse Must be using the correct variables for the B marks
(iii)	$fg(x) = f\left(\frac{4}{x}\right)$ $= 2 - \sqrt{\frac{4}{x}} + 5$ leading to $x = -4$	M1 DM1 A1	for correct order of functions for solution of equation
7 (i)	Finding an angle of 68.2° or 21.8° $\frac{4.5}{\sin 68.2} = \frac{2.4}{\sin \alpha}$ leading to $\alpha = 29.7^\circ$ (allow ± 0.1) Direction is 82.1° to the bank, upstream (allow $\pm 0.1^\circ$)	B1 B1 B1 B1	for the sine rule
(ii)	$\frac{4.5}{\sin 68.2} = \frac{2.4}{\sin 29.7} = \frac{v_r}{\sin 82.1}$ leading to $v_r = 4.8$ time taken = $\frac{80.78}{4.8} = 16.8$ Alternative method: Finding an angle of 68.2° or 21.8° $4.5^2 = 2.4^2 + v_r^2 - (2 \times 2.4 \times v_r \cos 68.2)$ leading to $v_r = 4.8$ Use of sine rule to obtain angle and direction to obtain direction is 82.1° to the bank, upstream Use of time taken = $\frac{80.78}{4.8} = 16.8$	B1 B1 M1 A1 B1 B1 B1 B1 B1 M1 A1	for the sine rule for resultant velocity for attempt to find AB and hence the time taken for correct use of the cosine rule for resultant velocity for use of the sine rule for $\alpha = 29.7^\circ$ for 82.1° for attempt to find AB and hence the time taken

Page 5	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Guidance
8	(i) $y - 6 = -\frac{4}{12}(x + 8)$ ($3y + x = 10$)	M1 A1	for a correct method allow unsimplified
	(ii) $y - 7 = 3(x + 1)$ ($y = 3x + 10$)	DM1 A1	for attempt at a perpendicular line using (-1, 7) allow unsimplified
	(iii) point of intersection $(-2, 4)$ which is the midpoint of AB	M1 M1 A1	for attempt to find the point of intersection using simultaneous equations for attempt to find midpoint for all correct
	Alternative method: Midpoint $(-2, 4)$ Verification that this point lies on CP .	M1 M1 A1	for attempt to find midpoint for full verification for all correct
	(iv) $CP = \sqrt{10}$ or 3.16	B1	
(v)	Area = $\frac{1}{2} \times \sqrt{10} \times 4\sqrt{10}$ = 20	M1	for correct method using CP
		A1	for 19.9 – 20.1

Page 6	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	11

Question	Answer	Marks	Guidance
9 (i)	$2 \cos x \cot x = \cot x + 2 \cos x$ $2 \cos x \frac{\cos x}{\sin x} + 1 = \frac{\cos x}{\sin x} + 2 \cos x$	M1	for use of $\cot x = \frac{\cos x}{\sin x}$ for both terms
	$2 \cos^2 x + \sin x = \cos x + 2 \cos x \sin x$ $2 \cos^2 x - 2 \cos x \sin x = \cos x - \sin x$ $2 \cos x (\cos x - \sin x) = \cos x - \sin x$ $(2 \cos x - 1)(\cos x - \sin x) = 0$	DM1 DM1 A1	for multiplication throughout by $\sin x$ for attempt to factorise for completely correct solution www
(ii)	<p>Alternative method:</p> $a \cos^2 x - a \cos x \sin x - b \cos x + b \sin x = 0$ $a \cos x \cot x - a \cos x - b \cot x + b = 0$ $a = 2, b = 1$	M1 DM1 DM1 A1	for expansion of RHS for division by $\sin x$ for comparing like terms to obtain both a and b for both correct www
	$(2 \cos x - 1)(\cos x - \sin x) = 0$ $\cos x = \frac{1}{2}, \tan x = 1$ $x = \frac{\pi}{3}, x = \frac{\pi}{4}$	M1 A1,A1	for either A1 for each, penalise extra solutions within the range by withholding the last A mark
10 (i)	<p>Alternative method:</p> $(2 \cos x - 1)(\cot x - 1) = 0$ Leading to $\cos x = \frac{1}{2}, \tan x = 1$ $x = \frac{\pi}{3}, x = \frac{\pi}{4}$	M1 A1,A1	for attempt to factorise the original equation and attempt to solve A1 for each, penalise extra solutions within the range by withholding the last A mark
10 (i)	$f(-2) = -32 - 2k + p = 0$ $f'\left(\frac{1}{2}\right) = \frac{12}{4} + k = 0$ leading to $k = -3$ and $p = 26$	M1 M1 A1,A1	for attempt at $f(-2)$ for attempt at $f'\left(\frac{1}{2}\right)$ A1 for each
(ii)	$(x+2)(4x^2 - 8x + 13)$	B1FT B1	FT for <i>their</i> $\frac{p}{2}$ all correct
(iii)	Showing that $4x^2 - 8x + 13 = 0$ has no real roots so $x = -2$ only www	M1, A1	M1 for a valid attempt at solution of equation leading to no solution or consideration of the discriminant

Page 7	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	11

Question	Answer	Marks	Guidance
11 (i)	$AB = 2r \sin \theta$ or $\sqrt{r^2 + r^2 - 2r^2 \cos 2\theta}$ or $\frac{r \sin 2\theta}{\sin\left(\frac{\pi}{2} - \theta\right)}$ or $\frac{r \sin 2\theta}{\cos \theta}$	B1	
(ii)	$2r \sin \theta + 2r\theta = 20$ $r = \frac{10}{\theta + \sin \theta}$	M1 A1	for use of (i) + arc length = 20, oe must be convinced
(iii)	$\frac{dr}{d\theta} = -\frac{10(1 + \cos \theta)}{(\theta + \sin \theta)^2}$ When $\theta = \frac{\pi}{6}$, $\frac{dr}{d\theta} = -17.8$	M1 A2,1,0 A1	for a correct attempt to differentiate –1 each error allow awrt –17.8
(iv)	$\frac{dr}{dt} = 15$ $\frac{d\theta}{dt} = \frac{dr}{dt} \div \frac{dr}{d\theta}$ $\frac{d\theta}{dt} = -0.842$	B1 M1 A1	may be implied for use of $\frac{15}{\text{their (iii)}}$ allow –0.84 or –0.843



Cambridge International Examinations
Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS

0606/12

Paper 1

May/June 2016

MARK SCHEME

Maximum Mark: 80

Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

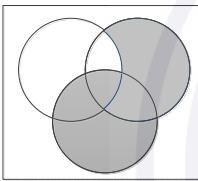
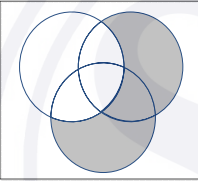
Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2016 series for most Cambridge IGCSE®, Cambridge International A and AS Level components and some Cambridge O Level components.

Page 2	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	12

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question	Answer	Marks	Guidance
1 (a)	$Y \subset X$ or $Y \subseteq X$ only $Y \cap Z = \emptyset$ or $\{ \}$ only	B1 B1	
(b)	(i)  (ii) 	B1 B1	
2 (i)	$32 - \frac{20}{x} + \frac{5}{x^2}$	B3	B1 for each correct term – must be integers
(ii)	$(3 \times 32) + \left(-\frac{20}{x} \times 4x \right) = 16$ Accept $16x^0$	M1 A1	for $(3 \times \text{their } 32) + \left(\frac{\text{their } (-20)}{x} \times 4x \right)$
3 (i)	$\mathbf{b} - \mathbf{c} = \begin{pmatrix} 6 \\ -2 \end{pmatrix}$ $4 + y^2 = 36 + 4$ $y = \pm 6$	B1 M1 A1	may be implied by further correct working for one correct attempt at using the modulus
(ii)	$\mu + 4 = 2\lambda$ or $-4\mu + 24 = 7\lambda$ $\mu - 4 = -\lambda$ or $8\mu - 8 = \lambda$ leading to $\mu = \frac{4}{3}$, $\lambda = \frac{8}{3}$ oe allow 1.33 and 2.67 or better	B1 B1 DB1	for one correct equation in μ and λ for a second correct equation in μ and λ for both, must have both previous B marks

Page 3	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	12

Question	Answer	Marks	Guidance
4	$(4 + \sqrt{5})x^2 + (2 - \sqrt{5})x - 1 = 0$ $x = \frac{-(2 - \sqrt{5}) \pm \sqrt{(2 - \sqrt{5})^2 - 4(4 + \sqrt{5})(-1)}}{2(4 + \sqrt{5})}$ $x = \frac{-(2 - \sqrt{5}) \pm \sqrt{9 - 4\sqrt{5} + 16 + 4\sqrt{5}}}{2(4 + \sqrt{5})}$ $= \frac{-(2 - \sqrt{5}) + 5}{2(4 + \sqrt{5})}$ $= \frac{3 + \sqrt{5}}{2(4 + \sqrt{5})}$ $= \frac{(3 + \sqrt{5})(4 - \sqrt{5})}{2(4 + \sqrt{5})(4 - \sqrt{5})}$ $= \frac{7 + \sqrt{5}}{22}$	<p>M1</p> <p>A1</p> <p>DM1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>You must be convinced that a calculator is not being used.</p> <p>for use of quadratic formula (allow one sign error), allow $b^2 = 9 - 4\sqrt{5}$ all correct</p> <p>for attempt to simplify the discriminant (minimum of 4 terms must be seen in discriminant, 2 terms involving $\sqrt{5}$ and 2 constant terms)</p> <p>for $\frac{3 + \sqrt{5}}{2(4 + \sqrt{5})}$ or $\frac{3 + \sqrt{5}}{8 + 2\sqrt{5}}$, ignore negative solution if included</p> <p>for attempt to rationalise an expression of the form $\frac{a \pm b\sqrt{5}}{c \pm d\sqrt{5}}$ as part of their solution of the quadratic Must obtain an integer denominator</p> <p>Final A1 can only be awarded if all previous marks have been obtained</p>
5 (i)	$(1 - \cos \theta)(1 + \sec \theta)$ $= 1 - \cos \theta + \frac{1}{\cos \theta} - \frac{\cos \theta}{\cos \theta}$ $= \sec \theta - \cos \theta$ $= \frac{1}{\cos \theta} - \cos \theta$ $= \frac{1 - \cos^2 \theta}{\cos \theta}$ $= \frac{\sin^2 \theta}{\cos \theta}$ $= \sin \theta \tan \theta$	<p>M1</p> <p>DM1</p> <p>A1</p> <p>A1</p>	<p>M1 for expansion and use of $\sec \theta = \frac{1}{\cos \theta}$ consistently, allow one sign error</p> <p>for attempt at a single fraction, dependent on first M1</p>

Page 4	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	12

Question	Answer	Marks	Guidance
(ii)	<p>Alternative method:</p> $(1 - \cos \theta) \left(\frac{\cos \theta + 1}{\cos \theta} \right)$ $= \frac{1 - \cos^2 \theta}{\cos \theta}$ $= \frac{\sin^2 \theta}{\cos \theta}$ $= \sin \theta \tan \theta \quad \text{www}$ <p>$\sin \theta \tan \theta = \sin \theta$ $\sin \theta (\tan \theta - 1) = 0$</p> <p>$\tan \theta = 1, \theta = \frac{\pi}{4},$ allow 0.785 or better $\sin \theta = 0, \theta = 0, \pi$ or 3.14 or better</p>	<p>M1</p> <p>DM1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>B1</p>	<p>for attempt at a single fraction for second factor and use of $\sec \theta = \frac{1}{\cos \theta}$ for expansion</p> <p>for $\theta = \frac{\pi}{4}$ from $\tan \theta = 1$</p> <p>for $\theta = 0$ from $\sin \theta = 0$</p> <p>for $\theta = \pi$ from $\sin \theta = 0$</p>
6	$\frac{d}{dx} \left(e^{3x} (4x+1)^{\frac{1}{2}} \right)$ $= e^{3x} \frac{1}{2} \times 4 (4x+1)^{-\frac{1}{2}} + 3e^{3x} (4x+1)^{\frac{1}{2}}$ $= \frac{2e^{3x}}{(4x+1)^{\frac{1}{2}}} + 3e^{3x} (4x+1)^{\frac{1}{2}}$ $= \frac{e^{3x}}{(4x+1)^{\frac{1}{2}}} (2 + 12x + 3)$ $= \frac{e^{3x}}{(4x+1)^{\frac{1}{2}}} (12x + 5)$	<p>B1</p> <p>B1</p> <p>B1</p> <p>DM1</p> <p>A1</p>	<p>for $re^{3x} (4x+1)^{-\frac{1}{2}}$ must be part of a sum, $r = \frac{1}{2}$ or 2 or $\frac{1}{2} \times 4$</p> <p>for $se^{3x} (4x+1)^{\frac{1}{2}}$ must be part of a sum, s is 1 or 3</p> <p>for all correct, allow unsimplified</p> <p>for $\frac{e^{3x}}{(4x+1)^{\frac{1}{2}}} (a + bx)$, dependent on first 2 B marks, must be using a correct method, collecting terms in the numerator correctly</p>
7 (i)	$\cos 3x = \frac{1}{2}, \quad x = \frac{\pi}{9} \quad \text{or} \quad 0.349, 20^\circ,$ allow 0.35	<p>M1</p> <p>A1</p>	<p>for correct attempt to solve the trigonometric equation</p>
(ii)	$B \left(\frac{\pi}{3}, 3 \right) \text{ or } (1.05, 3), (60^\circ, 3)$	<p>B1B1</p>	<p>B1 for each, must be in correct position or in terms of $x =$ and $y =$</p>

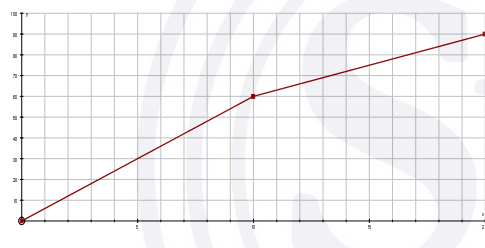
Page 5	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	12

Question	Answer	Marks	Guidance
(iii)	$\int_{\frac{\pi}{9}}^{\frac{\pi}{3}} 1 - 2 \cos 3x \, dx = \left[x - \frac{2}{3} \sin 3x \right]_{\frac{\pi}{9}}^{\frac{\pi}{3}}$ $= \frac{\pi}{3} - \left(\frac{\pi}{9} - \left(\frac{2}{3} \times \frac{\sqrt{3}}{2} \right) \right)$ $= \frac{2\pi}{9} + \frac{\sqrt{3}}{3} \text{ oe or } 1.28$	<p>M1</p> <p>A1</p> <p>DM1</p> <p>A1</p>	<p>for $x \pm a \sin 3x$ attempt to integrate at least one term</p> <p>for correct integration</p> <p>for correct use of limits from (i) and (ii), must be in radians</p>
8 (i)	$\lg y = x^2 \lg b + \lg A$ $\lg b = \pm 0.21$ $b = 0.617$ allow 0.62, $10^{-0.21}$ $\lg A = 0.94$ allow 0.93 to 0.95 $A = 8.71$ allow awrt 8.5 to 8.9 Alternative method 5.37 or $10^{0.73} = Ab$ 1.259 or $10^{0.1} = Ab^4$ $b^3 = 10^{-0.63}$ $b = 0.617$ allow 0.62, $10^{-0.21}$ $A = 8.71$ allow awrt 8.5 to 8.9	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p>	<p>for $\lg b = \pm 0.21$ may be implied</p> <p>for both equations, allow correct to 2 sf</p>
(ii)	$x = 1.5, x^2 = 2.25$ $y = 2.93$, allow awrt 2.9 or 3.0	<p>M1</p> <p>A1</p>	<p>for correct use of graph $y = \text{their} A \times \text{their} b^{1.5^2}$</p> <p>or $\lg y = \lg \text{their} A + (1.5^2 \lg \text{their} b)$</p>
(iii)	$\lg y = 0.301, \text{ or } 2 = '8.71(0.617)^{x^2}'$ $x = 1.74$, allow $\sqrt{3}$ or awrt 1.7, 1.8	<p>M1</p> <p>A1</p>	<p>for correct use of graph to read off x^2</p> <p>$2 = \text{their} A (\text{their} b)^{x^2}$ or</p> <p>$\lg 2 = (\lg \text{their} b) x^2 + \lg (\text{their} A)$</p>
9 (i)	$y = \frac{2}{3}(3x+10)^{\frac{1}{2}} (+c)$ passes through $\left(2, -\frac{4}{3} \right)$, so $c = -4$ $y = \frac{2}{3}(3x+10)^{\frac{1}{2}} - 4$ oe	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>for $p(3x+10)^{\frac{1}{2}}$ where p is a constant</p> <p>for $\frac{2}{3}(3x+10)^{\frac{1}{2}}$ oe unsimplified</p> <p>for attempt to find c, must have attempt to integrate, must have the first B1</p>

Page 6	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	12

Question	Answer	Marks	Guidance
(ii)	<p>When $x = 5$,</p> $y = -\frac{2}{3}$ <p>perpendicular gradient $= -5$</p> <p>Equation of normal: $y + \frac{2}{3} = -5(x - 5)$</p> <p>When $y = -\frac{5}{3}$,</p> $x = 5.2 \text{ oe}$	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>DM1</p> <p>A1</p>	<p>for attempt at the normal using <i>their</i> perpendicular gradient and <i>their</i> y value (but not $y = -\frac{4}{3}$ or $-\frac{5}{3}$).</p> <p>for use of $y = -\frac{5}{3}$ in their normal equation to get as far as $x = \dots$</p>
10 (i)	<p>Area: $20 = \pi x^2 + xy$</p> $y = \frac{20 - \pi x^2}{x}$ $P = 2\pi x + 2x + 2y$ $= 2\pi x + 2x + 2\left(\frac{20 - \pi x^2}{x} - \pi x\right)$ $= 2x + \frac{40}{x}$ <p>Alternative method:</p> $20 = \pi x^2 + xy$ $P = 2\pi x + 2y + 2x$ $= \frac{2}{x}(\pi x^2 + xy) + 2x$ $= \frac{2}{x}(20) + 2x$ $= 2x + \frac{40}{x}$	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>B1</p> <p>A1</p>	<p>for attempt to use perimeter and obtain in terms of x only</p> <p>all steps seen, www AG</p> <p>for attempt to use perimeter and write in $\frac{\pi x^2 + xy}{x}$</p> <p>for replacing $\pi x^2 + xy$ with 20</p> <p>all steps seen, www AG</p>

Page 7	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	12

Question	Answer	Marks	Guidance
(ii)	$\frac{dP}{dx} = 2 - \frac{40}{x^2}$ When $\frac{dP}{dx} = 0$, $x = 2\sqrt{5}$ allow 4.47, $\sqrt{20}$ leading to $P = 8\sqrt{5}$, allow 17.9 $\frac{d^2P}{dx^2} = \frac{80}{x^3}$, always positive so a minimum	M1 DM1 A1 A1 A1	for attempt to differentiate for equating to zero and attempt to solve at least as far as $x^2 =$ for this statement or use of gradient inspection either side of correct x
11 (a) (i)	Distance = area under graph = 1275	M1 A1	for attempt to find the area, one correct area seen (triangle, rectangle or trapezium) as part of a sum.
(ii)	deceleration is 1.5 oe	B1	
(b)		B1 B1FT	for a straight line between (0,0) and (10,60) FT a straight line between (10, 60) and (20, 90), a displacement vector $\begin{pmatrix} 10 \\ 30 \end{pmatrix}$ from <i>their</i> (10, <i>their</i> 60)
(c) (i)	e^{2t} is always positive or oe	B1	
(ii)	$a = 8e^{2t}$ $e^{2t} = \frac{3}{2}$ $t = \frac{1}{2} \ln \frac{3}{2}$, $\ln \sqrt{\frac{3}{2}}$ or $\frac{1}{2} \ln 1.5$	M1 A1	for attempt to differentiate, must be of the form pe^{2t} , equate to 12 and solve. Allow fractions equivalent to $\frac{3}{2}$
(iii)	$s = \left[2e^{2t} + 6t \right]_{0.4}^{0.5}$ $= (2e + 3) - (2e^{0.8} + 2.4)$ $(= 8.436 - 6.851)$ $= 1.59$, allow 1.58	M1 A1 DM1 A1	for attempt to integrate to get $qe^{2t} + 6t$ all correct for correct use of limits or considering distances separately, ignore attempts at c



Cambridge International Examinations
Cambridge International General Certificate of Secondary Education

ADDITIONAL MATHEMATICS

0606/13

Paper 1

May/June 2016

MARK SCHEME

Maximum Mark: 80

Published

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This document consists of 7 printed pages.

Page 2	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	13

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question	Answer	Marks	Guidance
1 (i)	-27	B1	
(ii)	$9 - 8k = 0$ $k = \frac{9}{8}$ Or $\frac{dy}{dx} = 4x - 3$ when $\frac{dy}{dx} = 0$, $x = \frac{3}{4}$ so $k = \frac{9}{8}$ Or completing the square $y = 2\left(x - \frac{3}{4}\right)^2 + k - \frac{9}{8}$ $k = \frac{9}{8}$	M1 A1 M1 A1 M1 A1	for use of discriminant with a complete method to get to $k =$ for a complete method to get to $k =$ for a complete method to get to $k =$
2 (a)	$2^{4(3x-1)} = 2^{3(x+2)}$ or $4^{2(3x-1)} = 4^{\frac{3}{2}(x+2)}$ or $8^{\frac{4}{3}(3x-1)} = 8^{x+2}$ or $16^{3x-1} = 16^{\frac{3}{4}(x+2)}$ leading to $x = \frac{10}{9}$ cao	B1 M1 A1	B1 for a correct statement for equating indices
(b)	$p = \frac{5}{3}$ $q = -2$	B1 B1	

Page 3	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	13

Question	Answer	Marks	Guidance
3	<p>On x-axis, $2x^2 - 7 = 1$ $x = 2$</p> $\frac{dy}{dx} = \frac{4x}{2x^2 - 7}$ <p>When $x = 2$, $\frac{dy}{dx} = 8$</p> <p>Gradient of normal $= -\frac{1}{8}$</p> <p>Equation of normal $y = -\frac{1}{8}(x - 2)$</p> <p>Required form $x + 8y - 2 = 0$</p>	<p>M1 A1 B1</p> <p>M1 A1</p>	<p>for equating to 1</p> <p>for attempt at perpendicular through <i>their</i> (2, 0), must be using $y = 0$ must be equated to zero with integer coefficients</p>
4 (a)	$\mathbf{A}^2 = \begin{pmatrix} 7 & -2 \\ -3 & 6 \end{pmatrix}$ $\mathbf{A}^2 - 2\mathbf{B} = \begin{pmatrix} 1 & -2 \\ -5 & 2 \end{pmatrix}$	<p>B1 M1 A1</p>	<p>for their $\mathbf{A}^2 - 2\mathbf{B}$</p>
(b)	$\begin{pmatrix} 4 & 1 \\ 10 & 3 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \end{pmatrix}$ <p>so $\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 3 & -1 \\ -10 & 4 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$</p> <p>leading to $\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 1 \\ -3 \end{pmatrix}$</p> <p>$x = 1$ $y = -3$</p>	<p>M1 DM1 A1 A1</p>	<p>for pre-multiplication by <i>their</i> inverse matrix DM1 for attempt at matrix multiplication Allow in matrix form</p>
5 (i)	$\frac{d}{dx} \left(\frac{e^{4x}}{4} - xe^{4x} \right) = e^{4x} - ((x \times 4e^{4x}) + e^{4x})$ $= -4xe^{4x}$	<p>B1 M1 A1 A1</p>	<p>for $\frac{d}{dx} \left(\frac{e^{4x}}{4} \right) = e^{4x}$ for attempt to differentiate a product for a correct product for correct final answer</p>
(ii)	$\int_0^{\ln 2} xe^{4x} dx = -\frac{1}{4} \left[\frac{e^{4x}}{4} - xe^{4x} \right]_0^{\ln 2}$ $= -\frac{1}{4} \left(\left(\frac{16}{4} - 16 \ln 2 \right) - \frac{1}{4} \right)$ $= 4 \ln 2 - \frac{15}{16}$	<p>B1FT B1 M1 A1</p>	<p>FT for use of <i>their</i> $\frac{1}{p} \times \left(\frac{e^{4x}}{4} - xe^{4x} \right)$, must be numerical p, but $\neq 0$ for $e^{4 \ln 2} = 16$ for correct use of limits, must be an integral of the correct form</p>

Page 4	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	13

Question	Answer	Marks	Guidance
6 (i)	$2 - \sqrt{5} < f(x) \leq 2$	B2	B1 for ≤ 2 B1 for $2 - \sqrt{5} <$ or awrt -0.24 Must be using f , $f(x)$ or y , $2 - \sqrt{5} <$, if not then B1 max
(ii)	$f^{-1}(x) = (2 - x)^2 - 5$ Domain $2 - \sqrt{5} < x \leq 2$ Range y or $-5 \leq f^{-1}(x) < 0$	M1 A1 B1 B1	for a correct method to find the inverse Must be using the correct variables for the B marks
(iii)	$fg(x) = f\left(\frac{4}{x}\right)$ $= 2 - \sqrt{\frac{4}{x}} + 5$ leading to $x = -4$	M1 DM1 A1	for correct order of functions for solution of equation
7 (i)	Finding an angle of 68.2° or 21.8° $\frac{4.5}{\sin 68.2} = \frac{2.4}{\sin \alpha}$ leading to $\alpha = 29.7^\circ$ (allow ± 0.1) Direction is 82.1° to the bank, upstream (allow $\pm 0.1^\circ$)	B1 B1 B1 B1	for the sine rule
(ii)	$\frac{4.5}{\sin 68.2} = \frac{2.4}{\sin 29.7} = \frac{v_r}{\sin 82.1}$ leading to $v_r = 4.8$ time taken = $\frac{80.78}{4.8} = 16.8$ Alternative method: Finding an angle of 68.2° or 21.8° $4.5^2 = 2.4^2 + v_r^2 - (2 \times 2.4 \times v_r \cos 68.2)$ leading to $v_r = 4.8$ Use of sine rule to obtain angle and direction to obtain direction is 82.1° to the bank, upstream Use of time taken = $\frac{80.78}{4.8} = 16.8$	B1 B1 M1 A1 B1 B1 B1 B1 B1 M1 A1	for the sine rule for resultant velocity for attempt to find AB and hence the time taken for correct use of the cosine rule for resultant velocity for use of the sine rule for $\alpha = 29.7^\circ$ for 82.1° for attempt to find AB and hence the time taken

Page 5	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Guidance
8	(i) $y - 6 = -\frac{4}{12}(x + 8)$ ($3y + x = 10$)	M1 A1	for a correct method allow unsimplified
	(ii) $y - 7 = 3(x + 1)$ ($y = 3x + 10$)	DM1 A1	for attempt at a perpendicular line using (-1, 7) allow unsimplified
	(iii) point of intersection $(-2, 4)$ which is the midpoint of AB	M1 M1 A1	for attempt to find the point of intersection using simultaneous equations for attempt to find midpoint for all correct
	Alternative method: Midpoint $(-2, 4)$ Verification that this point lies on CP .	M1 M1 A1	for attempt to find midpoint for full verification for all correct
	(iv) $CP = \sqrt{10}$ or 3.16	B1	
(v)	$\text{Area} = \frac{1}{2} \times \sqrt{10} \times 4\sqrt{10}$ $= 20$	M1	for correct method using CP
		A1	for 19.9 – 20.1

Page 6	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – May/June 2016	0606	13

Question	Answer	Marks	Guidance
9 (i)	$2 \cos x \cot x = \cot x + 2 \cos x$ $2 \cos x \frac{\cos x}{\sin x} + 1 = \frac{\cos x}{\sin x} + 2 \cos x$	M1	for use of $\cot x = \frac{\cos x}{\sin x}$ for both terms
	$2 \cos^2 x + \sin x = \cos x + 2 \cos x \sin x$ $2 \cos^2 x - 2 \cos x \sin x = \cos x - \sin x$ $2 \cos x (\cos x - \sin x) = \cos x - \sin x$ $(2 \cos x - 1)(\cos x - \sin x) = 0$	DM1 DM1 A1	for multiplication throughout by $\sin x$ for attempt to factorise for completely correct solution www
(ii)	<p>Alternative method:</p> $a \cos^2 x - a \cos x \sin x - b \cos x + b \sin x = 0$ $a \cos x \cot x - a \cos x - b \cot x + b = 0$ $a = 2, b = 1$	M1 DM1 DM1 A1	for expansion of RHS for division by $\sin x$ for comparing like terms to obtain both a and b for both correct www
	$(2 \cos x - 1)(\cos x - \sin x) = 0$ $\cos x = \frac{1}{2}, \tan x = 1$ $x = \frac{\pi}{3}, x = \frac{\pi}{4}$	M1 A1,A1	for either A1 for each, penalise extra solutions within the range by withholding the last A mark
10 (i)	<p>Alternative method:</p> $(2 \cos x - 1)(\cot x - 1) = 0$ Leading to $\cos x = \frac{1}{2}, \tan x = 1$ $x = \frac{\pi}{3}, x = \frac{\pi}{4}$	M1 A1,A1	for attempt to factorise the original equation and attempt to solve A1 for each, penalise extra solutions within the range by withholding the last A mark
10 (i)	$f(-2) = -32 - 2k + p = 0$ $f'\left(\frac{1}{2}\right) = \frac{12}{4} + k = 0$ leading to $k = -3$ and $p = 26$	M1 M1 A1,A1	for attempt at $f(-2)$ for attempt at $f'\left(\frac{1}{2}\right)$ A1 for each
(ii)	$(x+2)(4x^2 - 8x + 13)$	B1FT B1	FT for <i>their</i> $\frac{p}{2}$ all correct
(iii)	Showing that $4x^2 - 8x + 13 = 0$ has no real roots so $x = -2$ only www	M1, A1	M1 for a valid attempt at solution of equation leading to no solution or consideration of the discriminant

Page 7	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Guidance
11 (i)	$AB = 2r \sin \theta$ or $\sqrt{r^2 + r^2 - 2r^2 \cos 2\theta}$ or $\frac{r \sin 2\theta}{\sin\left(\frac{\pi}{2} - \theta\right)}$ or $\frac{r \sin 2\theta}{\cos \theta}$	B1	
(ii)	$2r \sin \theta + 2r\theta = 20$ $r = \frac{10}{\theta + \sin \theta}$	M1 A1	for use of (i) + arc length = 20, oe must be convinced
(iii)	$\frac{dr}{d\theta} = -\frac{10(1 + \cos \theta)}{(\theta + \sin \theta)^2}$ When $\theta = \frac{\pi}{6}$, $\frac{dr}{d\theta} = -17.8$	M1 A2,1,0 A1	for a correct attempt to differentiate –1 each error allow awrt –17.8
(iv)	$\frac{dr}{dt} = 15$ $\frac{d\theta}{dt} = \frac{dr}{dt} \div \frac{dr}{d\theta}$ $\frac{d\theta}{dt} = -0.842$	B1 M1 A1	may be implied for use of $\frac{15}{\text{their (iii)}}$ allow –0.84 or –0.843

CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International General Certificate of Secondary Education

MARK SCHEME for the March 2016 series

0606 ADDITIONAL MATHEMATICS

0606/12

Paper 12, maximum raw mark 80

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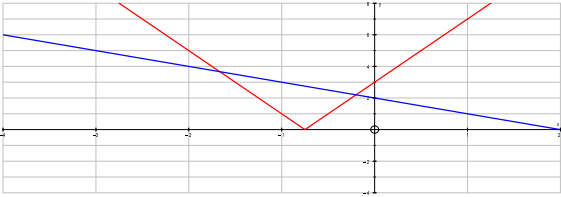
Page 2	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – March 2016	0606	12

Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

Question	Answer	Marks	Guidance
1	$ax + 9 = -2x^2 + 3x + 1$ $2x^2 + (a - 3)x + 8 = 0$ For 2 distinct roots, $(a - 3)^2 > 64$ Critical values -5 and 11 $a > 11$, $a < -5$	M1 M1 A1 A1	for attempt to equate the line and the curve and obtain a 3 term quadratic equation for use of the discriminant for critical values for correct range
2	$a = -\frac{13}{6}$, $b = 0$, $c = 1$	B3	B1 for each
3	$\log_5 \sqrt{x} + \log_{25} x = 3$ $\frac{1}{2} \log_5 x + \frac{\log_5 x}{\log_5 25} = 3$ $\log_5 x = 3$ $x = 125$ cao Alternative scheme: $\frac{\log_{25} \sqrt{x}}{\log_{25} 5} + \log_{25} x = 3$ $\frac{\frac{1}{2} \log_{25} x}{\log_{25} 5} + \log_{25} x = 3$ $\log_{25} x = \frac{3}{2}$ $x = 125$ cao	B1,B1 B1 B1 B1	B1 for $\frac{1}{2} \log_5 x$ B1 for $\frac{\log_5 x}{\log_5 25}$ for final answer for change of base for $\frac{1}{2} \log_{25} x$ (must be from correct work) for final answer

Page 3	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Guidance
4 (i)		B1 B1 B1 B1	for a line in correct position for (0, 2), (2, 0) for correct shape for $y = 3 + 2x $, touching the x -axis for (-1.5, 0), (0, 3)
(ii)	$2 - x = 3 + 2x$ leading to $x = -\frac{1}{3}$ $2 - x = -3 - 2x$ leading to $x = -5$ Alternative: $(2 - x)^2 = (3 + 4x)^2$ leading to $15x^2 + 28x + 5 = 0$ $x = -\frac{1}{3}, x = -5$	B1 M1 A1 M1 A1,A1	for $x = -\frac{1}{3}$ for correct attempt to deal with 'negative' branch. for $x = -5$ for equating and squaring to obtain a 3 term quadratic equation A1 for each.
5 (a) (i)	${}^9P_6 = 60480$	B1	Must be evaluated
(ii)	${}^4P_2 \times {}^3P_2 \times 2 = 144$	M1,A1	M1 for attempt a product of 3 perms
(iii)	840×2 1680	B1,B1	B1 for either 840, or realising that there are 2 possible positions for the symbols
(b) (i)	${}^{10}C_6 \times {}^5C_3$ 2100	M1 A1	for unsimplified form
(ii)	${}^8C_4 \times {}^4C_2$ 420	M1 A1	for unsimplified form
6 (i)	$f(x) > 6$	B1	Allow B1 for $y > 6$
(ii)	$f^{-1}(x) = \frac{1}{4} \ln(x - 6)$ Domain: $x > 6$ Range: $f^{-1}(x) \in \mathbb{R}$	M1 A1 B1 B1	for a complete method must be $f^{-1}(x) =$ or $y = \dots$ must be using the correct variable in both
(iii)	$f'(x) = 4e^{4x}$	B1	
(iv)	$6 + e^{4x} = 4e^{4x}$ leading to $x = \frac{1}{4} \ln 2$	M1 A1	for a complete, correct method

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Question	Answer	Marks	Guidance
9 (i)	$\frac{7}{2}r^2\theta = \frac{1}{2}r^2(2\pi - \theta)$	M1	for a valid method
	$\theta = \frac{\pi}{4}$ oe	A1	allow in degrees
	(ii) $r + r + \frac{\pi}{4}r = 20$, leading to	M1	for valid method
	$r = 7.180(3..)$	A1	Must show enough accuracy to get A1
(iii)	Perimeter $= \frac{\pi}{4}r + 2r \tan \frac{\pi}{8}$	B1,B1	B1 for arc length, B1 for twice AC
	$= 5.6394 + 5.9484$ $= 11.6$	B1	for 11.6
(iv)	Area $= (r \times AC) - \frac{1}{2}r^2 \frac{\pi}{4}$	B1,B1	B1 for area of quadrilateral, allow unsimplified, B1 for sector area
	$= 21.356 - 20.246$ or equivalent method using triangles	B1	for area in given range
	$1.08 \leq \text{Area} \leq 1.11$		
10 (i)	$x \times \frac{3}{2} \times 2(2x-1)^{\frac{1}{2}} + (2x-1)^{\frac{3}{2}}$	B1	for $\frac{3}{2} \times 2(2x-1)^{\frac{1}{2}}$
		M1	for attempt at differentiation of a product
		A1	for all else correct
	(ii) $3 \int x(2x-1)^{\frac{1}{2}} dx = x(2x-1)^{\frac{3}{2}} - \int (2x-1)^{\frac{3}{2}} dx$	M1	for attempt to use part (i)
	$= x(2x-1)^{\frac{3}{2}} - \frac{1}{2} \times \frac{2}{5} (2x-1)^{\frac{5}{2}}$	B1,B1	B1 for $x(2x-1)^{\frac{3}{2}}$, allow if divided by 3 B1 for $\frac{1}{2} \times \frac{2}{5} (2x-1)^{\frac{5}{2}}$, allow if divided by 3
	$\int x(2x-1)^{\frac{1}{2}} dx = \frac{1}{3} (2x-1)^{\frac{3}{2}} \left(x - \frac{1}{5} (2x-1) \right)$	M1	for taking out a common factor of $(2x-1)^{\frac{3}{2}}$
	$= \frac{(2x-1)^{\frac{3}{2}}}{15} (3x+1)$	DM1 A1	for attempt to obtain a linear factor
	(iii) $\left(\frac{1}{15} \times 4 \right) - 0$	M1 A1FT	for attempt to use limits correctly FT on their $\frac{px+q}{15}$

Page 6	Mark Scheme	Syllabus	Paper
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Question	Answer	Marks	Guidance
11 (i)	$\frac{1}{\operatorname{cosec} \theta - 1} - \frac{1}{\operatorname{cosec} \theta + 1} = \frac{\operatorname{cosec} \theta + 1 - \operatorname{cosec} \theta + 1}{\operatorname{cosec}^2 \theta - 1}$	M1	for attempt to obtain a single fraction
	$= \frac{2}{\cot^2 \theta}$	A1	all correct as shown
	$= 2 \tan^2 \theta$	M1	for use of correct identity
		A1	for 'finishing off'
	Alternative scheme: $\frac{1}{\operatorname{cosec} \theta - 1} - \frac{1}{\operatorname{cosec} \theta + 1} = \frac{\sin \theta}{1 - \sin \theta} - \frac{\sin \theta}{1 + \sin \theta}$	M1	for attempt to obtain a single fraction in terms of $\sin \theta$ only
	$= \frac{(\sin \theta + \sin^2 \theta) - (\sin \theta - \sin^2 \theta)}{1 - \sin^2 \theta}$	A1	all correct as shown
	$= \frac{2 \sin^2 \theta}{\cos^2 \theta}$	M1	for use of correct identity
	$= 2 \tan^2 \theta$	A1	for 'finishing off'
	(ii) $2 \tan^2 \theta = 6 + \tan \theta$ $(2 \tan \theta + 3)(\tan \theta - 2) = 0$ $\tan \theta = -\frac{3}{2}, \tan \theta = 2$	M1	for attempt to use (i), to obtain a quadratic equation and valid attempt to solve
	$\theta = 63.4^\circ, 123.7^\circ, 243.4^\circ, 303.7^\circ$	DM1	for attempt to solve trig equation
		A1,A1	for each 'pair'

CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International General Certificate of Secondary Education

MARK SCHEME for the October/November 2015 series

0606 ADDITIONAL MATHEMATICS

0606/11

Paper 1, maximum raw mark 80

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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

1	$kx^2 + (2k - 8)x + k = 0$ $b^2 - 4ac > 0$ so $(2k - 8)^2 - 4k^2 (> 0)$ $4k^2 - 32k + 64 - 4k^2 (> 0)$ leading to $k < 2$ only	M1 DM1 DM1 A1	for attempt to obtain a 3 term quadratic in the form $ax^2 + bx + c = 0$, where b contains a term in k and a constant for use of $b^2 - 4ac$ for attempt to simplify and solve for k A1 must have correct sign
2	$\left(\frac{dy}{dx}\right) = -5x(+c)$ When $x = -1$, $\frac{dy}{dx} = 2$ leading to $\frac{dy}{dx} = -5x - 3$ $y = -\frac{5x^2}{2} - 3x + d$ When $x = -1$, $y = 3$ leading to $y = \frac{5}{2} - \frac{5x^2}{2} - 3x$ Alternative scheme: $y = ax^2 + bx + c$ so $\frac{dy}{dx} = 2ax + b$ When $x = -1$, $\frac{dy}{dx} = 2$ so $-2a + b = 2$ $\frac{d^2y}{dx^2} = 2a$ so $a = -\frac{5}{2}$, $b = -3$, $c = \frac{5}{2}$	M1 A1 DM1 A1 M1 A1 DM1 A1	for attempt to integrate, do not penalise omission of arbitrary constant. Must have $\frac{dy}{dx} = \dots$ for attempt to integrate <i>their</i> $\frac{dy}{dx}$, but penalise omission of arbitrary constant. for use of $y = ax^2 + bx + c$, differentiation and use of conditions to give an equation in a and b for a correct equation for a second differentiation to obtain a for a , b and c all correct

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3	$\sqrt{(\sec^2 \theta - 1)} + \sqrt{(\operatorname{cosec}^2 \theta - 1)} = \sec \theta \operatorname{cosec} \theta$ <p>LHS = $\tan \theta + \cot \theta$ $= \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}$ $= \frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta \cos \theta}$ $= \frac{1}{\sin \theta \cos \theta}$ $= \sec \theta \operatorname{cosec} \theta$</p> <p>Alternate scheme:</p> <p>LHS = $\tan \theta + \cot \theta$ $= \tan \theta + \frac{1}{\tan \theta}$ $= \frac{\tan^2 \theta + 1}{\tan \theta}$ $= \frac{\sec^2 \theta}{\tan \theta}$ $= \frac{\sec \theta}{\tan \theta} \times \sec \theta$ $= \operatorname{cosec} \theta \sec \theta$</p>	<p>B1 B1 M1 M1 A1</p> <p>B1 M1 B1 M1 A1</p>	<p>may be implied by the next line</p> <p>for dealing with $\tan \theta$ and $\cot \theta$ in terms of $\sin \theta$ and $\cos \theta$</p> <p>for attempt to obtain as a single fraction</p> <p>for the use of $\sin^2 \theta + \cos^2 \theta = 1$ in correct context</p> <p>Must be convinced as AG</p> <p>may be implied by subsequent work</p> <p>for attempt to obtain as a single fraction</p> <p>for use of the correct identity</p> <p>for ‘splitting’ $\sec^2 \theta$</p> <p>Must be convinced as AG</p>
4	<p>(a) (i) 28</p> <p>(ii) 20160</p> <p>(iii) $6 \times (5 \times 4 \times 3)$ oe to give 360 $6 \times (5 \times 4 \times 3) \times 2$ $= 720$</p> <p>(b) Either ${}^{10}C_6 - {}^7C_6 = 210 - 7$ $= 203$</p> <p>Or $1W \ 5M = 63$ $2W \ 4M = 105$ $3W \ 3M = 35$ Total = 203</p>	<p>B1 B1 B1 B1 B1, B1 B1 B1 B1 B1</p>	<p>for realising that the music books can be arranged amongst themselves and consideration of the other 5 books</p> <p>for the realisation that the above arrangement can be either side of the clock.</p> <p>B1 for ${}^{10}C_6$, B1 for 7C_6</p> <p>for 1 case correct, must be considering more than 1 different case, allow C notation</p> <p>for the other 2 cases, allow C notation</p> <p>for final result</p>

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5	(i)	$\frac{dy}{dx} = (x-3) \frac{4x}{2x^2+1} + \ln(2x^2+1)$ <p>when $x=2$, $\frac{dy}{dx} = -\frac{8}{9} + \ln 9$ oe or 1.31 or better</p>	B1 M1 A1 A1	for correct differentiation of \ln function for attempt to differentiate a product for correct product, terms must be bracketed where appropriate for correct final answer
	(ii)	$\partial y \approx (\text{answer to (i)}) \times 0.03$ $= 0.0393$, allow awrt 0.039	M1 A1FT	for attempt to use small changes follow through on <i>their</i> numerical answer to (i) allow to 2 sf or better
6	(i)	$A \cap B = \{3\}$	B1	
	(ii)	$A \cup C = \{1, 3, 5, 6, 7, 9, 11, 12\}$	B1	
	(iii)	$A' \cap C = \{1, 5, 7, 11\}$	B1	
	(iv)	$(D \cup B)' = \{1, 9\}$	B1	
	(v)	Any set containing up to 5 positive even numbers ≤ 12	B1	
7	(i)	Gradient $= \frac{0.2}{0.8} = 0.25$ $b = 0.25$ Either $6 = 0.25(2.2) + c$ Or $5.8 = 0.25(1.4) + c$ leading to $A = 233$ or $e^{5.45}$ Alternative schemes: Either $6 = b(2.2) + c$ $5.8 = b(1.4) + c$ Or $e^6 = A(e^{2.2})^b$ $e^{5.8} = A(e^{1.4})^b$ Leading to $A = 233$ or $e^{5.45}$ and $b = 0.25$	M1 A1 M1 A1 M1 DM1 A1, A1	for attempt to find the gradient for a correct substitution of values from either point and attempt to obtain c or solution by simultaneous equations dealing with $c = \ln A$ for 2 simultaneous equations as shown for attempt to solve to get at least one solution for one unknown A1 for each
	(ii)	Either $y = 233 \times 5^{0.25}$ Or $\ln y = 0.25 \ln 5 + \ln 233$ leading to $y = 348$	M1 A1	for correct use of either equation in attempt to obtain y using <i>their</i> value of A and of b found in (i)

Page 5	Mark Scheme	Syllabus	Paper
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8	$\frac{dy}{dx} = \frac{2(x^2 + 5)^{\frac{1}{2}} - \frac{1}{2}(2x)(x^2 + 5)^{-\frac{1}{2}}(2x - 1)}{x^2 + 5}$ <p>or</p> $\frac{dy}{dx} = 2(x^2 + 5)^{-\frac{1}{2}} - \frac{1}{2}(2x)(x^2 + 5)^{-\frac{3}{2}}(2x - 1)$ <p>When $x = 2, y = 1$ and $\frac{dy}{dx} = \frac{4}{9}$ (allow 0.444 or 0.44)</p> <p>Equation of tangent: $y - 1 = \frac{4}{9}(x - 2)$ ($9y = 4x + 1$)</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>B1, B1</p> <p>M1</p> <p>A1</p>	<p>for $\frac{1}{2}(2x)(x^2 + 5)^{-\frac{1}{2}}$ for a quotient or $-\frac{1}{2}(2x)(x^2 + 5)^{-\frac{3}{2}}$ for a product allow if either seen in separate working for attempt to differentiate a quotient or a correct product for all correct, allow unsimplified</p> <p>B1 for each</p> <p>for attempt at straight line, must be tangent using <i>their</i> gradient and y allow unsimplified.</p>
9 (i)	$\frac{2}{3}(4 + x)^{\frac{3}{2}} (+c)$	<p>B1, B1</p>	<p>B1 for $k(4 + x)^{\frac{3}{2}}$ only, B1 for $\frac{2}{3}(4 + x)^{\frac{3}{2}}$ only Condone omission of c</p>
(ii)	<p>Area of trapezium $= \left(\frac{1}{2} \times 5 \times 5\right)$ $= 12.5$</p> <p>Area $= \left[\frac{2}{3}(4 + x)^{\frac{3}{2}}\right]_0^5 - \left(\frac{1}{2} \times 5 \times 5\right)$ $= \left(\frac{2}{3} \times 27\right) - \frac{16}{3} - \frac{25}{2}$ $= \frac{1}{6}$ or awrt 0.17</p> <p>Alternative scheme: Equation of AB $y = \frac{1}{5}x + 2$ Area $= \int_0^5 \sqrt{4 + x} - \left(\frac{1}{5}x + 2\right) dx$ $= \left[\frac{2}{3}(4 + x)^{\frac{3}{2}} - \frac{x^2}{10} - 2x\right]_0^5$ $= \left(\frac{2}{3} \times 27\right) - \frac{16}{3} - \frac{25}{2}$ $= \frac{1}{6}$ or awrt 0.17</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>A1</p>	<p>for attempt to find the area of the trapezium</p> <p>for correct use of limits using $k(4 + x)^{\frac{3}{2}}$ only (must be using 5 and 0) for $18 - \frac{16}{3}$ or equivalent</p> <p>for a correct attempt to find the equation of AB</p> <p>for correct use of limits using $k(4 + x)^{\frac{3}{2}}$ only (must be using 5 and 0) for $18 - \frac{16}{3}$ or equivalent for 12.5 or equivalent</p>

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10	(i)	All sides are equal to the radii of the circles which are also equal	B1	for a convincing argument
	(ii)	Angle $CBE = \frac{2\pi}{3}$	B1	must be in terms of π , allow 0.667π , or better
	(iii)	$DE = 10\sqrt{3}$	M1	for correct attempt to find DE using <i>their</i> angle CBE
			A1	for correct DE , allow 17.3 or better
		Arc $CE = 10 \times \frac{2\pi}{3}$	M1	for attempt to find arc length with <i>their</i> angle CBE (20.94)
		Perimeter $= 20 + 10\sqrt{3} + \frac{20\pi}{3}$	M1	for $10 + 10 + DE +$ an arc length
		$= 58.3$ or 58.2	A1	allow unsimplified
	(iv)	Area of sector: $\frac{1}{2} \times 10^2 \times \frac{2\pi}{3} = \frac{100\pi}{3}$	M1	for sector area using <i>their</i> angle CBE allow unsimplified, may be implied
		Area of triangle: $\frac{1}{2} \times 10^2 \times \sin \frac{2\pi}{3} = 25\sqrt{3}$	M1	for triangle area using <i>their</i> angle DBE which must be the same as <i>their</i> angle CBE , allow unsimplified, may be implied
		Area $= \frac{100\pi}{3} + 25\sqrt{3}$ or awrt 148	A1	allow in either form

Page 7	Mark Scheme	Syllabus	Paper
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11	(a) (i)	$(x+3)^2 - 5$	B1, B1	B1 for 3, B1 for -5
	(ii)	$y \geq 4$ or $f \geq 4$	B1	Correct notation or statement must be used
	(iii)	$y = \sqrt{x+5} - 3$	M1	for a correct attempt to find the inverse function
			A1	must be in the correct form and positive root only
		Domain $x \geq 4$	B1FT	Follow through on <i>their</i> answer to (ii), must be using x
	(b)	$h^2 g(x) = h^2(e^x)$	M1	for correct order
		$= h(5e^x + 2)$	M1	for dealing with h^2
		$= 25e^x + 12$		
		$25e^x + 12 = 37,$	DM1	for solution of equation (dependent on both previous M marks)
		leading to $x = 0$	A1	
		Alternative scheme 1:		
		$hg(x) = h^{-1}(37)$	M1	for correct order
		$h^{-1}(37) = 7$	M1	for dealing with $h^{-1}(37)$
		$5e^x + 2 = 7,$	DM1	for solution of equation (dependent on both previous M marks)
		leading to $x = 0$	A1	
		Alternative scheme 2:		
		$g(x) = h^{-2}(37)$	M1	for correct order
		$h^{-2}(37) = 1$	M1	for dealing with $h^{-2}(37)$
		$e^x = 1,$	DM1	for solution of equation (dependent on both previous M marks)
		leading to $x = 0$	A1	

Page 8	Mark Scheme	Syllabus	Paper
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12	$x^2 + 6x - 16 = 0$ or $y^2 + 10y - 75 = 0$ leading to $(x + 8)(x - 2) = 0$ or $(y - 5)(y + 15) = 0$	M1	for attempt to obtain a 3 term quadratic in terms of one variable only
	so $x = 2, y = 5$ and $x = -8, y = -15$	DM1	for attempt to solve quadratic equation
	Midpoint $(-3, -5)$	A1, A1	A1 for each 'pair' of values.
	Gradient = 2, so perpendicular gradient = $-\frac{1}{2}$	B1	
	Perpendicular bisector: $y + 5 = -\frac{1}{2}(x + 3)$ $(2y + x + 13 = 0)$	M1	for attempt at straight line equation, must be using midpoint and perpendicular gradient
	Point C $(-13, 0)$	M1	for use of $y = 0$ in <i>their</i> line equation (but not $2x - y + 1 = 0$)
	Area = $\frac{1}{2} \begin{vmatrix} -13 & 2 & -8 & -13 \\ 0 & 5 & -15 & 0 \end{vmatrix}$ = 125	M1	for correct attempt to find area, may be using <i>their</i> values for A, B and C (C must lie on the x-axis)
	Alternative method for area: $CM^2 = 125, AB^2 = 500$ Area = $\frac{1}{2} \times \sqrt{125} \times \sqrt{500}$ = 125	A1	
		M1	for correct attempt to find area may be using <i>their</i> values for A, B and C
		A1	

CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International General Certificate of Secondary Education

MARK SCHEME for the October/November 2015 series

0606 ADDITIONAL MATHEMATICS

0606/12

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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Page 2	Mark Scheme	Syllabus	Paper
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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

1	$kx^2 + (2k - 8)x + k = 0$ $b^2 - 4ac > 0$ so $(2k - 8)^2 - 4k^2 (> 0)$ $4k^2 - 32k + 64 - 4k^2 (> 0)$ leading to $k < 2$ only	M1 DM1 DM1 A1	for attempt to obtain a 3 term quadratic in the form $ax^2 + bx + c = 0$, where b contains a term in k and a constant for use of $b^2 - 4ac$ for attempt to simplify and solve for k A1 must have correct sign
2	$\left(\frac{dy}{dx}\right) = -5x(+c)$ When $x = -1$, $\frac{dy}{dx} = 2$ leading to $\frac{dy}{dx} = -5x - 3$ $y = -\frac{5x^2}{2} - 3x + d$ When $x = -1$, $y = 3$ leading to $y = \frac{5}{2} - \frac{5x^2}{2} - 3x$ Alternative scheme: $y = ax^2 + bx + c$ so $\frac{dy}{dx} = 2ax + b$ When $x = -1$, $\frac{dy}{dx} = 2$ so $-2a + b = 2$ $\frac{d^2y}{dx^2} = 2a$ so $a = -\frac{5}{2}$, $b = -3$, $c = \frac{5}{2}$	M1 A1 DM1 A1 M1 A1 DM1 A1	for attempt to integrate, do not penalise omission of arbitrary constant. Must have $\frac{dy}{dx} = \dots$ for attempt to integrate <i>their</i> $\frac{dy}{dx}$, but penalise omission of arbitrary constant. for use of $y = ax^2 + bx + c$, differentiation and use of conditions to give an equation in a and b for a correct equation for a second differentiation to obtain a for a , b and c all correct

Page 3	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2015	0606	12

3	$\sqrt{(\sec^2 \theta - 1)} + \sqrt{(\operatorname{cosec}^2 \theta - 1)} = \sec \theta \operatorname{cosec} \theta$ <p>LHS = $\tan \theta + \cot \theta$ $= \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}$ $= \frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta \cos \theta}$ $= \frac{1}{\sin \theta \cos \theta}$ $= \sec \theta \operatorname{cosec} \theta$</p> <p>Alternate scheme:</p> <p>LHS = $\tan \theta + \cot \theta$ $= \tan \theta + \frac{1}{\tan \theta}$ $= \frac{\tan^2 \theta + 1}{\tan \theta}$ $= \frac{\sec^2 \theta}{\tan \theta}$ $= \frac{\sec \theta}{\tan \theta} \times \sec \theta$ $= \operatorname{cosec} \theta \sec \theta$</p>	<p>B1 B1 M1 M1 A1</p> <p>B1 M1 B1 M1 A1</p>	<p>may be implied by the next line</p> <p>for dealing with $\tan \theta$ and $\cot \theta$ in terms of $\sin \theta$ and $\cos \theta$</p> <p>for attempt to obtain as a single fraction</p> <p>for the use of $\sin^2 \theta + \cos^2 \theta = 1$ in correct context</p> <p>Must be convinced as AG</p> <p>may be implied by subsequent work</p> <p>for attempt to obtain as a single fraction</p> <p>for use of the correct identity</p> <p>for ‘splitting’ $\sec^2 \theta$</p> <p>Must be convinced as AG</p>
4	<p>(a) (i) 28</p> <p>(ii) 20160</p> <p>(iii) $6 \times (5 \times 4 \times 3)$ oe to give 360 $6 \times (5 \times 4 \times 3) \times 2$ $= 720$</p> <p>(b) Either ${}^{10}C_6 - {}^7C_6 = 210 - 7$ $= 203$</p> <p>Or 1W 5M = 63 2W 4M = 105 3W 3M = 35 Total = 203</p>	<p>B1 B1 B1 B1 B1, B1 B1 B1 B1 B1</p>	<p>for realising that the music books can be arranged amongst themselves and consideration of the other 5 books</p> <p>for the realisation that the above arrangement can be either side of the clock.</p> <p>B1 for ${}^{10}C_6$, B1 for 7C_6</p> <p>for 1 case correct, must be considering more than 1 different case, allow C notation</p> <p>for the other 2 cases, allow C notation</p> <p>for final result</p>

Page 4	Mark Scheme	Syllabus	Paper
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5	(i)	$\frac{dy}{dx} = (x-3)\frac{4x}{2x^2+1} + \ln(2x^2+1)$ <p>when $x=2$, $\frac{dy}{dx} = -\frac{8}{9} + \ln 9$ oe or 1.31 or better</p>	B1 M1 A1 A1	for correct differentiation of \ln function for attempt to differentiate a product for correct product, terms must be bracketed where appropriate for correct final answer
	(ii)	$\partial y \approx (\text{answer to (i)}) \times 0.03$ $= 0.0393$, allow awrt 0.039	M1 A1FT	for attempt to use small changes follow through on <i>their</i> numerical answer to (i) allow to 2 sf or better
6	(i)	$A \cap B = \{3\}$	B1	
	(ii)	$A \cup C = \{1, 3, 5, 6, 7, 9, 11, 12\}$	B1	
	(iii)	$A' \cap C = \{1, 5, 7, 11\}$	B1	
	(iv)	$(D \cup B)' = \{1, 9\}$	B1	
	(v)	Any set containing up to 5 positive even numbers ≤ 12	B1	
7	(i)	Gradient $= \frac{0.2}{0.8} = 0.25$ $b = 0.25$ Either $6 = 0.25(2.2) + c$ Or $5.8 = 0.25(1.4) + c$ leading to $A = 233$ or $e^{5.45}$ Alternative schemes: Either $6 = b(2.2) + c$ $5.8 = b(1.4) + c$ Or $e^6 = A(e^{2.2})^b$ $e^{5.8} = A(e^{1.4})^b$ Leading to $A = 233$ or $e^{5.45}$ and $b = 0.25$	M1 A1 M1 A1 M1 DM1 A1, A1	for attempt to find the gradient for a correct substitution of values from either point and attempt to obtain c or solution by simultaneous equations dealing with $c = \ln A$ for 2 simultaneous equations as shown for attempt to solve to get at least one solution for one unknown A1 for each
	(ii)	Either $y = 233 \times 5^{0.25}$ Or $\ln y = 0.25 \ln 5 + \ln 233$ leading to $y = 348$	M1 A1	for correct use of either equation in attempt to obtain y using <i>their</i> value of A and of b found in (i)

Page 5	Mark Scheme	Syllabus	Paper
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8	$\frac{dy}{dx} = \frac{2(x^2 + 5)^{\frac{1}{2}} - \frac{1}{2}(2x)(x^2 + 5)^{-\frac{1}{2}}(2x - 1)}{x^2 + 5}$ <p>or</p> $\frac{dy}{dx} = 2(x^2 + 5)^{-\frac{1}{2}} - \frac{1}{2}(2x)(x^2 + 5)^{-\frac{3}{2}}(2x - 1)$ <p>When $x = 2, y = 1$ and $\frac{dy}{dx} = \frac{4}{9}$ (allow 0.444 or 0.44)</p> <p>Equation of tangent: $y - 1 = \frac{4}{9}(x - 2)$ ($9y = 4x + 1$)</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>B1, B1</p> <p>M1</p> <p>A1</p>	<p>for $\frac{1}{2}(2x)(x^2 + 5)^{-\frac{1}{2}}$ for a quotient or $-\frac{1}{2}(2x)(x^2 + 5)^{-\frac{3}{2}}$ for a product allow if either seen in separate working for attempt to differentiate a quotient or a correct product for all correct, allow unsimplified</p> <p>B1 for each</p> <p>for attempt at straight line, must be tangent using <i>their</i> gradient and y allow unsimplified.</p>
9 (i)	$\frac{2}{3}(4 + x)^{\frac{3}{2}} (+c)$	B1, B1	B1 for $k(4 + x)^{\frac{3}{2}}$ only, B1 for $\frac{2}{3}(4 + x)^{\frac{3}{2}}$ only Condone omission of c
(ii)	<p>Area of trapezium $= \left(\frac{1}{2} \times 5 \times 5\right)$ $= 12.5$</p> <p>Area $= \left[\frac{2}{3}(4 + x)^{\frac{3}{2}}\right]_0^5 - \left(\frac{1}{2} \times 5 \times 5\right)$ $= \left(\frac{2}{3} \times 27\right) - \frac{16}{3} - \frac{25}{2}$ $= \frac{1}{6}$ or awrt 0.17</p> <p>Alternative scheme: Equation of AB $y = \frac{1}{5}x + 2$ Area $= \int_0^5 \sqrt{4 + x} - \left(\frac{1}{5}x + 2\right) dx$ $= \left[\frac{2}{3}(4 + x)^{\frac{3}{2}} - \frac{x^2}{10} - 2x\right]_0^5$ $= \left(\frac{2}{3} \times 27\right) - \frac{16}{3} - \frac{25}{2}$ $= \frac{1}{6}$ or awrt 0.17</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>A1</p>	<p>for attempt to find the area of the trapezium</p> <p>for correct use of limits using $k(4 + x)^{\frac{3}{2}}$ only (must be using 5 and 0) for $18 - \frac{16}{3}$ or equivalent</p> <p>for a correct attempt to find the equation of AB</p> <p>for correct use of limits using $k(4 + x)^{\frac{3}{2}}$ only (must be using 5 and 0) for $18 - \frac{16}{3}$ or equivalent for 12.5 or equivalent</p>

Page 6	Mark Scheme	Syllabus	Paper
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10	(i)	All sides are equal to the radii of the circles which are also equal	B1	for a convincing argument
	(ii)	Angle $CBE = \frac{2\pi}{3}$	B1	must be in terms of π , allow 0.667π , or better
	(iii)	$DE = 10\sqrt{3}$	M1	for correct attempt to find DE using <i>their</i> angle CBE
			A1	for correct DE , allow 17.3 or better
		Arc $CE = 10 \times \frac{2\pi}{3}$	M1	for attempt to find arc length with <i>their</i> angle CBE (20.94)
		Perimeter $= 20 + 10\sqrt{3} + \frac{20\pi}{3}$ $= 58.3$ or 58.2	M1	for $10 + 10 + DE$ + an arc length
			A1	allow unsimplified
	(iv)	Area of sector: $\frac{1}{2} \times 10^2 \times \frac{2\pi}{3} = \frac{100\pi}{3}$	M1	for sector area using <i>their</i> angle CBE allow unsimplified, may be implied
		Area of triangle: $\frac{1}{2} \times 10^2 \times \sin \frac{2\pi}{3} = 25\sqrt{3}$	M1	for triangle area using <i>their</i> angle DBE which must be the same as <i>their</i> angle CBE , allow unsimplified, may be implied
		Area $= \frac{100\pi}{3} + 25\sqrt{3}$ or awrt 148	A1	allow in either form

Page 7	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2015	0606	12

11	(a) (i)	$(x+3)^2 - 5$	B1, B1	B1 for 3, B1 for -5
	(ii)	$y \geq 4$ or $f \geq 4$	B1	Correct notation or statement must be used
	(iii)	$y = \sqrt{x+5} - 3$	M1	for a correct attempt to find the inverse function
			A1	must be in the correct form and positive root only
		Domain $x \geq 4$	B1FT	Follow through on <i>their</i> answer to (ii), must be using x
	(b)	$h^2 g(x) = h^2(e^x)$	M1	for correct order
		$= h(5e^x + 2)$	M1	for dealing with h^2
		$= 25e^x + 12$		
		$25e^x + 12 = 37,$	DM1	for solution of equation (dependent on both previous M marks)
		leading to $x = 0$	A1	
		Alternative scheme 1:		
		$hg(x) = h^{-1}(37)$	M1	for correct order
		$h^{-1}(37) = 7$	M1	for dealing with $h^{-1}(37)$
		$5e^x + 2 = 7,$	DM1	for solution of equation (dependent on both previous M marks)
		leading to $x = 0$	A1	
		Alternative scheme 2:		
		$g(x) = h^{-2}(37)$	M1	for correct order
		$h^{-2}(37) = 1$	M1	for dealing with $h^{-2}(37)$
		$e^x = 1,$	DM1	for solution of equation (dependent on both previous M marks)
		leading to $x = 0$	A1	

Page 8	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2015	0606	12

12	$x^2 + 6x - 16 = 0$ or $y^2 + 10y - 75 = 0$ leading to $(x + 8)(x - 2) = 0$ or $(y - 5)(y + 15) = 0$	M1	for attempt to obtain a 3 term quadratic in terms of one variable only
	so $x = 2, y = 5$ and $x = -8, y = -15$	DM1	for attempt to solve quadratic equation
	Midpoint $(-3, -5)$	A1, A1	A1 for each 'pair' of values.
	Gradient = 2, so perpendicular gradient = $-\frac{1}{2}$	B1	
	Perpendicular bisector: $y + 5 = -\frac{1}{2}(x + 3)$ $(2y + x + 13 = 0)$	M1	for attempt at straight line equation, must be using midpoint and perpendicular gradient
	Point C $(-13, 0)$	M1	for use of $y = 0$ in <i>their</i> line equation (but not $2x - y + 1 = 0$)
	Area = $\frac{1}{2} \begin{vmatrix} -13 & 2 & -8 & -13 \\ 0 & 5 & -15 & 0 \end{vmatrix}$ = 125	M1	for correct attempt to find area, may be using <i>their</i> values for A, B and C (C must lie on the x-axis)
	Alternative method for area: $CM^2 = 125, AB^2 = 500$ Area = $\frac{1}{2} \times \sqrt{125} \times \sqrt{500}$ = 125	A1	
		M1	for correct attempt to find area may be using <i>their</i> values for A, B and C
		A1	

CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International General Certificate of Secondary Education

MARK SCHEME for the October/November 2015 series

0606 ADDITIONAL MATHEMATICS

0606/13

Paper 1, maximum raw mark 80

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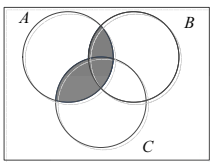
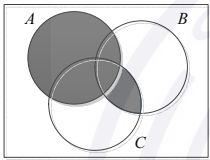
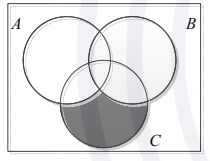
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Page 2	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2015	0606	13

Abbreviations


Awrt	answers which round to
Cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

1	(i)		B1	
	(ii)		B1	
	(iii)		B1	
2	$\cos\left(3x - \frac{\pi}{4}\right) = (\pm)\frac{1}{\sqrt{2}} \text{ oe}$ $3x - \frac{\pi}{4} = -\frac{\pi}{4}, \frac{\pi}{4}, \frac{3\pi}{4}$ $x = \left(-\frac{\pi}{4} + \frac{\pi}{4}\right) \div 3, \left(\frac{\pi}{4} + \frac{\pi}{4}\right) \div 3, \left(\frac{3\pi}{4} + \frac{\pi}{4}\right) \div 3 \text{ oe}$ $x = 0 \text{ and } \frac{\pi}{6} \text{ (or 0 and 0.524)}$ $x = \frac{\pi}{3} \text{ (or 1.05)}$			
			M1	division by 2 and square root
			DM1	correct order of operations in order to obtain a solution
			A2/1/0	A2 for 3 solutions and no extras in the range A1 for 2 solutions A0 for one solution or no solutions

Page 3	Mark Scheme	Syllabus	Paper
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3	(a)	$\begin{pmatrix} 12 & 16 & 4 \\ 30 & 32 & 10 \end{pmatrix}$	B2,1,0	B2 for 6 elements correct, B1 for 5 elements correct
	(b)	$\begin{pmatrix} 28 & -24 \\ -8 & 76 \end{pmatrix} = m \begin{pmatrix} 4 & 6 \\ 2 & -8 \end{pmatrix} + n \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ $-24 = 6m \text{ or } -8 = 2m \text{ giving } m = -4$ $28 = 4m + n \text{ or } 76 = -8m + n$ $n = 44$	B2,1,0 B1 M1 A1	B2 for 4 correct elements in \mathbf{X}^2 B1 for 3 correct elements in \mathbf{X}^2 For $m = -4$ using correct I complete method to obtain n
	(c)	$a^2 - 6 = 0$ $\text{so } a = \pm\sqrt{6}$	B2,1,0	B2 for $a = \pm\sqrt{6}$ or $a = \pm 2.45$, with no incorrect statements seen or B1 for $a = \pm\sqrt{6}$ or $a = \pm 2.45$ seen or B1 for $a = \sqrt{6}$ and no incorrect working
4	(i)	$\frac{1}{2}(4\sqrt{3}+1) \times BC = \frac{47}{2}$ $BC = \frac{47}{(4\sqrt{3}+1)} \times \frac{(4\sqrt{3}-1)}{(4\sqrt{3}-1)}$ $BC = 4\sqrt{3}-1$	B1 M1 A1	correct use of the area correct rationalisation Dependent on all method being seen
		Alternative method $\frac{1}{2}(4\sqrt{3}+1) \times BC = \frac{47}{2}$ $(4\sqrt{3}+1)(a\sqrt{3}+b) = 47$	B1	
		Leading to $12a + b = 47$ and $a + 4b = 0$ Solution of simultaneous equations $BC = 4\sqrt{3}-1$	M1 A1	Dependent on all method seen including solution of simultaneous equations
	(ii)	$(4\sqrt{3}+1)^2 + (4\sqrt{3}-1)^2$ $= (48 + 8\sqrt{3} + 1) + (48 - 8\sqrt{3} + 1)$ $AC^2 = 98$ $AC = 7\sqrt{2} \text{ or } p = 7$	B1FT B1cao	6 correct FT terms seen 98 and $7\sqrt{2}$ or 98 and $p = 7$

Page 4	Mark Scheme	Syllabus	Paper
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5	When $x = \frac{\pi}{4}, y = 2$	B1	$y = 2$
	$\frac{dy}{dx} = 5\sec^2 x$	B1	$5\sec^2 x$
	When $x = \frac{\pi}{4}, \frac{dy}{dx} = 10$	B1	10 from differentiation
	Equation of normal $y - 2 = -\frac{1}{10}\left(x - \frac{\pi}{4}\right)$	M1	$y - \text{their } 2 = -\frac{1}{\text{their } 10}\left(x - \frac{\pi}{4}\right)$
	$10y + x - 20 - \frac{\pi}{4} = 0$ or $10y + x - 20.8 = 0$ oe	A1	allow unsimplified
6	(i)		
		B1 B1 B1	shape intercepts on x-axis intercept on y-axis for a curve with a maximum and two arms
	(ii)	M1	$(2, \pm 16)$ seen or $(2, k)$ where $k > 0$
	$(2, 16)$	A1	$(2, 16)$ or $x = 2$ and $y = 16$ only
	(iii)		
	$k = 0$	B1	
	$k > 16$	B1	

Page 6	Mark Scheme	Syllabus	Paper
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9	(a) (i)	Number of arrangements with Maths books as one item = $4!$ or $4 \times 3!$	M1	$4!(\times 2)$ or $4 \times 3!(\times 2)$ oe
		or Maths books can be arranged $2!$ ways and History $3!$ ways = $2! \times 3!$		$2! \times 3!(\times 4)$ or $2 \times 3!(\times 4)$ oe
		$2 \times 4!$ or $2 \times 4 \times 3!$ or $4 \times 2 \times 3! = 48$	A1	A1 for 48
	(ii)	$5! - 48$ or $6 \times 2 \times 3!$	M1	$5! - \text{their answer to (i)}$
		72	A1	or for $6 \times 2 \times 3$
	(b) (i)	3003	B1	
	(ii)	$3003 - 6 - 135$	M1	<i>their</i> answer to (i) – $6 - {}^6C_4 \times 9$
		2862	B1	135 subtracted
		or $2M\ 3W = 720$ $3M\ 2W = 1260$ $4M\ 1W = 756$ $5M = 126$ 2862	M1 B1 A1	complete correct method using 4 cases, may be implied by working. Must have at least one correct any 3 correct

Page 7	Mark Scheme	Syllabus	Paper
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10	(i)	$10^2 = 6^2 + 6^2 - 2 \times 6 \times 6 \times \cos ABC$ or $\sin\left(\frac{ABC}{2}\right) = \frac{5}{6}$ or $ABC = \pi - \sin^{-1} \frac{10\sqrt{11}}{36}$ $ABC = 1.9702$	M1	correct cosine rule statement or correct statement for $\sin \frac{ABC}{2}$ or equating areas oe
			A1	1.9702 or better
	(ii)	$XY = 2$ Arc length $6\left(\frac{\pi - 1.970}{2}\right)$ oe	B1	for XY (may be implied by later work, allow on diagram)
			B1	correct arc length (unsimplified)
		Perimeter = $2 + 2\left(6\left(\frac{\pi - 1.970}{2}\right)\right)$ = 9.03	M1	their $2 + 2 \times 6 \times$ their angle C
			A1	
	(iii)	$\left(\frac{1}{2} \times 6^2 \left(\frac{\pi - 1.970}{2}\right) - \frac{1}{2} \times 5 \times \sqrt{11}\right) \times 2$ = 4.50 or 4.51 or better	M1	sector area using their C
			M1	area of $\triangle ABM$ where M is the midpoint of AC , or ($\triangle s$ ABY and BXY) or $\triangle ABC$
			A1	Answers to 3sf or better

Page 8	Mark Scheme	Syllabus	Paper
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11	$x^2 - 2x - 3 = 0$ or $y^2 - 6y + 5 = 0$	M1	substitution and simplification to obtain a three term quadratic equation in one variable
	leading to (3, 5) and (-1, 1)	A1,A1	A1 for each 'pair' from a correct quadratic equation, correctly obtained.
	Midpoint (1, 3)	B1cao	midpoint
	(Gradient - 1)	M1	perpendicular bisector, must be using <i>their</i> perpendicular gradient and <i>their</i> midpoint
	Perpendicular bisector $y = 4 - x$	M1	substitution and simplification to obtain a three term quadratic equation in one variable.
	Meets the curve again if $x^2 + 10x - 15 = 0$ or $y^2 - 18y + 41 = 0$	M1	
	leading to $x = -5 \pm 2\sqrt{10}$, $y = 9 \mp 2\sqrt{10}$	A1,A1	A1 for each 'pair'
	$CD^2 = (4\sqrt{10})^2 + (4\sqrt{10})^2$	M1	Pythagoras using <i>their</i> coordinates from solution of second quadratic. $(x_1 - x_2)^2 + (y_1 - y_2)^2$ must be seen if not using correct coordinates.
	$CD = 8\sqrt{5}$	A1	A1 for $8\sqrt{5}$ from $\sqrt{320}$ and all correct so far.

Page 9	Mark Scheme	Syllabus	Paper
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12 (a)	$2^{2x-1} \times 2^{2(x+y)} = 2^7$ and $\frac{3^{2(2y-x)}}{3^{3(y-4)}} = 1$	M1	expressing 4^{x+y} , 128 as powers of 2 and 9^{2y-x} , 27^{y-4} as powers of 3
	$2x - 1 + 2(x + y) = 7$ oe	A1	Correct equation from correct working
	$2(2y - x) = 3(y - 4)$ oe	A1	Correct equation from correct working
	leading to $x = 4$, $y = -4$	A1	for both
	<u>Example of Alternative method</u>		
	Method mark as above	M1	As before
	$2x - 1 + 2(x + y) = 7$	A1	One of the correct equations in x and y
	leading to $y = \frac{(8 - 4x)}{2}$		
	Correctly substituted in $\frac{3^{2(2y-x)}}{3^{3(y-4)}} = 1$		
	Leading to $2\left(\frac{2(8 - 4x)}{2} - x\right) = 3\left(\frac{(8 - 4x)}{2} - 4\right)$	A1	Correct, unsimplified, equation in x or y only
(b)	Leading to $x = 4$ and $y = -4$	A1	Both answers
	$(2(5^z) - 1)(5^z + 1) = 0$	M1	solution of quadratic
	leading to $2.5^z = 1$ ($5^z = -1$)	A1	correct solution
	$5^z = 0.5$	DM1	correct attempt to solve $2.5^z = k$, where k is positive
	$z = \frac{\log 0.5}{\log 5}$ or $z = -0.431$ or better	A1	must have one solution only

CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International General Certificate of Secondary Education

MARK SCHEME for the May/June 2015 series

0606 ADDITIONAL MATHEMATICS

0606/11

Paper 1, maximum raw mark 80

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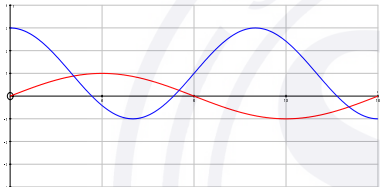
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Page 2	Mark Scheme	Syllabus	Paper
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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

1	(i)	180° or π radians or 3.14 radians (or better)	B1	
	(ii)	2	B1	
	(iii) (a)		B1	$y = \sin 2x$ all correct
	(b)		B1	for either $\uparrow \downarrow \uparrow$ starting at their highest value and ending at their lowest value Or a curve with highest value at $y = 3$ and lowest value at $y = -1$ completely correct graph
(iv)		3	B1	
2	(i)	$\tan \theta = \frac{(8 + 5\sqrt{2})(4 - 3\sqrt{2})}{(4 + 3\sqrt{2})(4 - 3\sqrt{2})}$ $= \frac{32 - 24\sqrt{2} + 20\sqrt{2} - 30}{16 - 18}$ $= 1 + 2\sqrt{2} \text{ cao}$	M1	attempt to obtain $\tan \theta$ and rationalise. Must be convinced that no calculators are being used
			A1	

Page 4	Mark Scheme	Syllabus	Paper
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4	(a)	$\mathbf{X}^2 = \begin{pmatrix} 4-4k & -8 \\ 2k & -4k \end{pmatrix}$	B2,1,0	-1 each incorrect element
	(b)	Use of $\mathbf{AA}^{-1} = \mathbf{I}$ $\begin{pmatrix} a & 1 \\ b & 5 \end{pmatrix} \begin{pmatrix} \frac{5}{6} & -\frac{1}{6} \\ -\frac{2}{3} & \frac{1}{3} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ Any 2 equations will give $a = 2, b = 4$	M1 A1,A1	use of $\mathbf{AA}^{-1} = \mathbf{I}$ and an attempt to obtain at least one equation.
		Alternative method 1: $\frac{1}{5a-b} \begin{pmatrix} 5 & -1 \\ b & a \end{pmatrix} = \begin{pmatrix} \frac{5}{6} & -\frac{1}{6} \\ -\frac{2}{3} & \frac{1}{3} \end{pmatrix}$ Compare any 2 terms to give $a = 2, b = 4$	M1 A1,A1	correct attempt to obtain \mathbf{A}^{-1} and comparison of at least one term.
		Alternative method 2: Inverse of $\frac{1}{6} \begin{pmatrix} 5 & -1 \\ -4 & 2 \end{pmatrix} = \begin{pmatrix} 2 & 1 \\ 4 & 5 \end{pmatrix}$	M1 A1,A1	reasoning and attempt at inverse
5		$3x-1 = x(3x-1) + x^2 - 4$ or $y = \left(\frac{y+1}{3}\right)y + \left(\frac{y+1}{3}\right)^2 - 4$ $4x^2 - 4x - 3 = 0$ or $4y^2 - 4y - 35 = 0$ $(2x-3)(2x+1) = 0$ or $(2y-7)(2y+5) = 0$ leading to $x = \frac{3}{2}, x = -\frac{1}{2}$ and $y = \frac{7}{2}, y = -\frac{5}{2}$ Midpoint $\left(\frac{1}{2}, \frac{1}{2}\right)$ Perpendicular gradient $= -\frac{1}{3}$ Perp bisector: $y - \frac{1}{2} = -\frac{1}{3}\left(x - \frac{1}{2}\right)$ $(3y + x - 2 = 0)$	M1 DM1 A1 A1 B1 M1 M1 A1	equate and attempt to obtain an equation in 1 variable forming a 3 term quadratic equation and attempt to solve x values y values for midpoint, allow anywhere correct attempt to obtain the gradient of the perpendicular, using AB straight line equation through the midpoint; must be convinced it is a perpendicular gradient. allow unsimplified

Page 5	Mark Scheme	Syllabus	Paper
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6	(i)	$f\left(\frac{1}{2}\right) = \frac{a}{8} - \frac{15}{4} + \frac{b}{2} - 2 = 0$ <p>leading to $a + 4b = 46$ $f(1) = a - 15 + b - 2 = 5$ leading to $a + b = 22$</p> <p>giving $b = 8$ (AG), $a = 14$</p>	M1 correct use of either $f\left(\frac{1}{2}\right)$ or $f(1)$ paired correctly A1 both equations correct (allow unsimplified) M1,A1 M1 for solution of equations A1 for both a and b . AG for b .
	(ii)	$(2x-1)(7x^2-4x+2)$	M1,A1 M1 for valid attempt to obtain $g(x)$, by either observation or by algebraic long division.
	(iii)	$7x^2 - 4x + 2 = 0$ has no real solutions as $b^2 < 4ac$ $16 < 56$	M1 use of $b^2 - 4ac$ A1 correct conclusion; must be from a correct $g(x)$ or $2g(x)$ www
7	(i)	$\frac{dy}{dx} = \frac{(x-1)\left(\frac{8x}{4x^2+2}\right) - \ln(4x^2+3)}{(x-1)^2}$ <p>When $x = 0$, $y = -\ln 3$ oe</p> <p>$\frac{dy}{dx} = -\ln 3$ so gradient of normal is $\frac{1}{\ln 3}$ (allow numerical equivalent)</p> <p>normal equation $y + \ln 3 = \frac{1}{\ln 3}x$ or $y = 0.910x - 1.10$, or $y = \frac{10}{11}x - \frac{11}{10}$ cao (Allow $y = 0.91x - 1.1$)</p>	M1 differentiation of a quotient (or product) B1 correct differentiation of $\ln(4x^2+3)$ A1 all else correct B1 for y value M1 valid attempt to obtain gradient of the normal M1 attempt at normal equation must be using a perpendicular A1
	(ii)	<p>when $x = 0$, $y = -\ln 3$ when $y = 0$, $x = (\ln 3)^2$ Area = ± 0.66 or ± 0.67 or awrt these or $\frac{1}{2}(\ln 3)^3$</p>	M1 valid attempt at area A1

Page 6	Mark Scheme	Syllabus	Paper
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8	(i)	Range for f: $y \geq 3$ Range for g: $y \geq 9$	B1 B1	
	(ii)	$x = -2 + \sqrt{y-5}$ $g^{-1}(x) = -2 + \sqrt{x-5}$ Domain of g^{-1} : $x \geq 9$ Alternative method: $y^2 + 4y + 9 - x = 0$ $y = \frac{-4 + \sqrt{16 - 4(9-x)}}{2}$	M1 A1 B1	attempt to obtain the inverse function Must be correct form for domain
	(iii)	Need $g(3e^{2x})$ $(3e^{2x} + 2)^2 + 5 = 41$ or $9e^{4x} + 12e^{2x} - 32 = 0$ $(3e^{2x} - 4)(3e^{2x} + 8) = 0$ leading to $3e^{2x} + 2 = \pm 6$ so $x = \frac{1}{2} \ln \frac{4}{3}$ or $e^{2x} = \frac{4}{3}$ so $x = \frac{1}{2} \ln \frac{4}{3}$ Alternative method: Using $f(x) = g^{-1}(41)$, $g^{-1}(41) = 4$ leading to $3e^{2x} = 4$, so $x = \frac{1}{2} \ln \frac{4}{3}$	M1 DM1 M1 A1 M1 DM1 M1 A1	correct order correct attempt to solve the equation dealing with the exponential correctly in order to reach a solution for x Allow equivalent logarithmic forms
	(iv)	$g'(x) = 6e^{2x}$ $g'(\ln 4) = 96$	B1 B1	B1 for each

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9	(i)	$\frac{dy}{dx} = 3x^2 - 10x + 3$ When $x = 0$, for curve $\frac{dy}{dx} = 3$, gradient of line also 3 so line is a tangent. Alternate method: $3x + 10 = x^3 - 5x^2 + 3x + 10$ leading to $x^2 = 0$, so tangent at $x = 0$	M1 for differentiation A1 comparing both gradients
	(ii)	When $\frac{dy}{dx} = 0$, $(3x - 1)(x - 3) = 0$ $x = \frac{1}{3}$, $x = 3$	M1 equating gradient to zero and valid attempt to solve A1,A1 A1 for each
	(iii)	Area = $\frac{1}{2}(10 + 19)3 - \int_0^3 x^3 - 5x^2 + 3x + 10 dx$ $= \frac{87}{2} - \left[\frac{x^4}{4} - \frac{5x^3}{3} + \frac{3x^2}{2} + 10x \right]_0^3$ $= \frac{87}{2} - \left(\frac{81}{4} - 45 + \frac{27}{2} + 30 \right)$ $= 24.7$ or 24.8 Alternative method: Area = $\int_0^3 (3x + 10) - (x^3 - 5x^2 + 3x + 10) dx$ $= \int_0^3 -x^3 + 5x^2 dx$ $= \left[-\frac{x^4}{4} + \frac{5x^3}{3} \right]_0^3 = \frac{99}{4}$	B1 area of the trapezium M1 attempt to obtain the area enclosed by the curve and the coordinate axes, by integration A1 integration all correct DM1 correct application of limits (must be using <i>their</i> 3 from (ii) and 0) A1 B1 correct use of 'Y-y' M1 attempt to integrate A1 integration all correct DM1 correct application of limits A1
10	(a)	$\sin^2 x = \frac{1}{4}$ $\sin x = (\pm) \frac{1}{2}$ $x = 30^\circ, 150^\circ, 210^\circ, 330^\circ$	M1 using $\operatorname{cosec} x = \frac{1}{\sin x}$ and obtaining $\sin x = \dots$ A1,A1 A1 for one correct pair, A1 for another correct pair with no extra solutions

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(b)	$(\sec^2 3y - 1) - 2 \sec 3y - 2 = 0$ $\sec^2 3y - 2 \sec 3y - 3 = 0$ $(\sec 3y + 1)(\sec 3y - 3) = 0$ leading to $\cos 3y = -1$, $\cos 3y = \frac{1}{3}$ $3y = 180^\circ, 540^\circ$ $3y = 70.5^\circ, 289.5^\circ, 430.5^\circ$ $y = 60^\circ, 180^\circ, 23.5^\circ, 96.5^\circ, 143.5^\circ$ Alternative 1: $\sec^2 3y - 2 \sec 3y - 3 = 0$ leading to $3 \cos^2 3y + 2 \cos 3y - 1$ $(3 \cos y - 1)(\cos y + 1) = 0$ Alternative 2: $\frac{\sin^2 y}{\cos^2 y} - \frac{2}{\cos y} - 2 = 0$ $(1 - \cos^2 x) - 2 \cos x - 2 \cos^2 x = 0$	M1 use of the correct identity M1 attempt to obtain a 3 term quadratic equation in $\sec 3y$ and attempt to solve dealing with \sec and $3y$ correctly M1 A1,A1 A1 for a correct pair, A1 for a second correct pair, A1 for correct 5 th solution and no other within the range A1 M1 use of the correct identity M1 attempt to obtain a quadratic equation in $\cos 3y$ and attempt to solve dealing with $3y$ correctly M1 A marks as above M1 use of the correct identity, $\tan y = \frac{\sin y}{\cos y}$ and $\sec y = \frac{1}{\cos y}$, then as before
	(c) $z - \frac{\pi}{3} = \frac{\pi}{3}, \frac{4\pi}{3}$ $z = \frac{2\pi}{3}, \frac{5\pi}{3}$ or 2.09 or 2.1, 5.24	M1 correct order of operations A1,A1 A1 for a correct solution A1 for a second correct solution and no other within the range

CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International General Certificate of Secondary Education

MARK SCHEME for the May/June 2015 series

0606 ADDITIONAL MATHEMATICS

0606/12

Paper 1, maximum raw mark 80

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Page 2	Mark Scheme	Syllabus	Paper
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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

1	$k^2 - 4(2k + 5) < 0$	M1	use of $b^2 - 4ac$, (not as part of quadratic formula unless isolated at a later stage) with correct values for a , b and c
	$k^2 - 8k - 20 < 0$		
	$(k - 10)(k + 2) < 0$	M1	Do not need to see $<$ at this point
	critical values of 10 and -2	A1	attempt to obtain critical values
	$-2 < k < 10$	A1	correct critical values
	Alternative 1:		
	$\frac{dy}{dx} = 2(2k + 5)x + k$	M1	correct range
	When $\frac{dy}{dx} = 0$, $x = \frac{-k}{2(2k + 5)}$, $y = \frac{8k + 20 - k^2}{4(2k + 5)}$	M1	attempt to differentiate, equate to zero and substitute x value back in to obtain a y value
	When $y = 0$, obtain critical values of 10 and -2	M1	consider $y = 0$ in order to obtain critical values
	$-2 < k < 10$	A1	correct critical values
	Alternative 2:		
	$y = (2k + 5) \left(\left(x + \frac{k}{2(2k + 5)} \right)^2 - \frac{k^2}{4(2k + 5)} \right) + 1$	M1	correct range
	Looking at $1 - \frac{k^2}{4(2k + 5)} = 0$ leads to	M1	attempt to complete the square and consider $1 - \frac{k^2}{4(2k + 5)}$
	critical values of 10 and -2	M1	attempt to solve above = to 0, to obtain critical values
	$-2 < k < 10$	A1	correct critical values
		A1	correct range

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2	$\frac{\tan \theta + \cot \theta}{\operatorname{cosec} \theta} = \frac{\frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{\sin \theta}}{\frac{1}{\sin \theta}}$ $= \frac{\frac{\sin^2 \theta + \cos^2 \theta}{\sin \theta \cos \theta}}{\frac{1}{\sin \theta}}$ $= \frac{1}{\cos \theta}$ $= \sec \theta$ <p>Alternative:</p> $\frac{\tan \theta + \cot \theta}{\operatorname{cosec} \theta} = \frac{\frac{\tan^2 \theta + 1}{\tan \theta}}{\operatorname{cosec} \theta}$ $= \frac{\sec^2 \theta}{\tan \theta \frac{1}{\sin \theta}}$ $= \frac{\sec^2 \theta}{\sec \theta}$ $= \sec \theta$	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>for $\tan \theta = \frac{\sin \theta}{\cos \theta}$, $\cot \theta = \frac{\cos \theta}{\sin \theta}$ and $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$; allow when used</p> <p>dealing correctly with fractions in the numerator; allow when seen</p> <p>use of the appropriate identity; allow when seen</p> <p>must be convinced it is from completely correct work (beware missing brackets)</p> <p>for either $\tan \theta = \frac{1}{\cot \theta}$ or $\cot \theta = \frac{1}{\tan \theta}$ and $\operatorname{cosec} \theta = \frac{1}{\sin \theta}$; allow when used</p> <p>dealing correctly with fractions in numerator; allow when seen</p> <p>use of the appropriate identity; allow when seen</p> <p>must be convinced it is from completely correct work</p>
3	$\mathbf{A}^{-1} = \frac{1}{2} \begin{pmatrix} 3 & -2 \\ -5 & 4 \end{pmatrix}$ $\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 3 & -2 \\ -5 & 4 \end{pmatrix} \begin{pmatrix} 8 \\ 9 \end{pmatrix}$ $\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{2} \begin{pmatrix} 6 \\ -4 \end{pmatrix}$ $x = 3, y = -2$	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1, A1</p>	<p>$\frac{1}{2}$ multiplied by a matrix</p> <p>for matrix</p> <p>attempt to use the inverse matrix, must be pre-multiplication</p>

Page 4	Mark Scheme	Syllabus	Paper
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4	(i)	<p>Area =</p> $\left(\frac{1}{2} \times 12^2 \times 1.7\right) + \left(\frac{1}{2} \times 12^2 \sin(2\pi - 1.7 - 2.4)\right)$ <p>= awrt 181</p>	<p>B1,B1</p> <p>M1</p> <p>A1</p>	<p>B1 for sector area, allow unsimplified</p> <p>B1 for correct angle BOC, allow unsimplified</p> <p>correct attempt at area of triangle, allow unsimplified using <i>their</i> angle BOC</p> <p>(Their angle BOC must not be 1.7 or 2.4)</p>
	(ii)	$BC^2 = 12^2 + 12^2 - (2 \times 12 \times 12 \cos 2.1832)$ <p>or $BC = 2 \times 12 \times \sin\left(\frac{2\pi - 4.1}{2}\right)$</p> $BC = 21.296$ <p>Perimeter = $(12 \times 1.7) + 12 + 12 + 21.296$</p> $= 65.7$	<p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>correct attempt at BC, may be seen in (i), allow if used in (ii). Allow use of <i>their</i> angle BOC.</p> <p>for arc length, allow unsimplified for a correct 'plan' (an arc + 2 radii and BC)</p>
5	(a) (i)	20160	B1	
	(ii)	$3 \times {}^6P_4 \times 2$ $= 2160$	B1,B1	<p>B1 for 6P_4 (must be seen in a product)</p> <p>B1 for all correct, with no further working</p>
	(iii)	$5 \times 2 \times {}^6P_4$ $= 3600$ <p>Alternative 1:</p> ${}^6C_4 \times 5! \times 2$ $= 3600$ <p>Alternative 2:</p> $({}^7P_5 - {}^6P_5) \times 2$ $= 3600$ <p>Alternative 3:</p> $2!({}^6P_4 + ({}^6P_1 \times {}^5P_3) + ({}^6P_2 \times {}^4P_2) + ({}^6P_3 \times {}^3P_1) + {}^6P_4)$ $= 3600$	<p>B1,B1</p> <p>B1</p> <p>B2</p> <p>B1</p> <p>B2</p> <p>B1</p> <p>B2</p> <p>B1</p>	<p>B1 for 6P_4 (must be seen in a product)</p> <p>B1 for 5 (must be in a product)</p> <p>B1 for all correct, with no further working</p> <p>for ${}^6C_4 \times 5!$</p> <p>for ${}^6C_4 \times 5! \times 2$</p> <p>for $({}^7P_5 - {}^6P_5)$</p> <p>for $({}^7P_5 - {}^6P_5) \times 2$</p> <p>4 terms correct or omission of 2! in each term</p> <p>all correct</p>

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(b) (i)	${}^{14}C_4 \times {}^{10}C_4$ or ${}^{14}C_8 \times {}^8C_4$ (or numerical or factorial equivalent) $= 210210$	B1,B1	B1 for either ${}^{14}C_4$ or ${}^{14}C_8$ as part of a product B1 for correct answer, with no further working
	(ii) ${}^8C_4 \times {}^6C_4$ $= 1050$	B1,B1	B1 for either 8C_4 or 6C_4 as part of a product B1 for correct answer with no further working
6 (i)	$10\ln 4$ or 13.9 or better	B1	
(ii)	$\left(\frac{dx}{dt}\right) \frac{20t}{t^2 + 4} - 4$ <p>When $\frac{dx}{dt} = 0, \frac{20t}{t^2 + 4} = 4$</p> <p>leading to $t^2 - 5t + 4 = 0$ $t = 1, t = 4$</p>	M1	attempt to differentiate and equate to zero
		B1	$\frac{20t}{t^2 + 4}$ or equivalent seen
		DM1	attempt to solve <i>their</i> $\frac{dx}{dt} = 0$, must be a 2 or 3 term quadratic equation with real roots
		A1	for both

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(iii)	<p>If $(v =) \frac{20t}{t^2 + 4} - 4$</p> <p>$(a =) \frac{20(t^2 + 4) - 20t(2t)}{(t^2 + 4)^2}$</p> <p>$20(4 - t^2)$ or $80 - 20t^2$ or $4 - t^2$ or equivalent expression involving $-t^2$</p> <p>When acceleration is 0, $t = 2$ only</p> <p>Alternative 1 for first 3 marks:</p> <p>If $(v =) \frac{20t - 4t^2 - 16}{t^2 + 4}$</p> <p>$(a =) \frac{(t^2 + 4)(20 - 8t) - (20t - 4t^2 - 16)(2t)}{(t^2 + 4)^2}$</p> <p>Alternative 2 for M1 mark:</p> <p>If $(v =) 20t(t^2 + 4)^{-1} - 4$</p> <p>$(a =) 20t(-2t(t^2 + 4)^{-2}) + 20(t^2 + 4)^{-1}$</p> <p>Alternative 3 for the first 3 marks</p> <p>If $(v =) (20t - 4t^2 - 16)(t^2 + 4)^{-1}$</p> <p>$(a =) (20t - 4t^2 - 16)(-2t(t^2 + 4)^{-2}) + (20 - 8t)(t^2 + 4)^{-1}$</p> <p>Numerator $= -2t(20t - 4t^2 - 16) + (20 - 8t)(t^2 + 4)$</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>attempt to differentiate <i>their</i> $\frac{dx}{dt}$</p> <p>$20(t^2 + 4)$</p> <p>$20t(2t)$</p> <p>$20(4 - t^2)$ or $80 - 20t^2$ or $4 - t^2$</p> <p>$t = 2$, dependent on obtaining first and second A marks</p> <p>attempt to differentiate <i>their</i> $\frac{dx}{dt}$</p> <p>for $(t^2 + 4)(20 - 8t)$</p> <p>for $(20t - 4t^2 - 16)(2t)$</p> <p>attempt to differentiate <i>their</i> $\frac{dx}{dt}$</p> <p>attempt to differentiate <i>their</i> $\frac{dx}{dt}$</p> <p>for $2t(20t - 4t^2 - 16)$</p> <p>for $(20 - 8t)(t^2 + 4)$</p>
	<p>7 (i) $\overrightarrow{DA} = 3\mathbf{a} - \mathbf{b}$</p> <p>(ii) $\overrightarrow{DB} = 7\mathbf{a} - \mathbf{b}$</p> <p>(iii) $\overrightarrow{AX} = \lambda(4\mathbf{a} + \mathbf{b})$</p> <p>(iv) $\overrightarrow{DX} = 3\mathbf{a} - \mathbf{b} + \lambda(4\mathbf{a} + \mathbf{b})$</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p>mark final answer, allow unsimplified</p> <p>mark final answer, allow unsimplified</p> <p>mark final answer, allow unsimplified</p> <p><i>their</i> (i) + <i>their</i> (iii) or equivalent valid method or $3\mathbf{a} - \mathbf{b} + \text{their (iii)}$</p> <p>Allow unsimplified</p>

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(v)	$3\mathbf{a} - \mathbf{b} + \lambda(4\mathbf{a} + \mathbf{b}) = \mu(7\mathbf{a} - \mathbf{b})$ Equate like vectors: $3 + 4\lambda = 7\mu$ $-1 + \lambda = -\mu$ leads to $\lambda = \frac{4}{11}, \mu = \frac{7}{11}$	M1 DM1 A1,A1	equating <i>their (iv)</i> and $\mu \times$ <i>their (ii)</i> for an attempt to equate like vectors and attempt to solve 2 linear equations for λ and μ A1 for each
8 (i)	$5e^{2x} - \frac{1}{2}e^{-2k} \quad (+c)$	B1, B1	B1 for each term, allow unsimplified
(ii)	$\left(5e^{2k} - \frac{1}{2}e^{-2k}\right) - \left(5e^{-2k} - \frac{1}{2}e^{2k}\right)$	M1 A1	use of limits provided integration has taken place. Signs must be correct if brackets are not included. allow any correct form
(iii)	$\left(5e^{2k} - \frac{1}{2}e^{-2k}\right) \left(5e^{-2k} - \frac{1}{2}e^{2k}\right) = -60$ or $\frac{11}{2}e^{2k} - \frac{11}{2}e^{-2k} = -60$ or equivalent leading to $11e^{2k} - 11e^{-2k} + 120 = 0$	 B1 DB1	correct expression from (ii) either simplified or unsimplified equated to -60 , must be first line seen. must be convinced as AG
(iv)	$11y^2 + 120y - 11 = 0$ $(11y - 1)(y + 11) = 0$ leading to $k = \frac{1}{2}\ln\frac{1}{11}, \ln\frac{1}{\sqrt{11}}, -\ln\sqrt{11}, -\frac{1}{2}\ln 11$	 M1 DM1 A1	attempt to obtain a quadratic equation in y or e^{2k} and solve to get y or e^{2k} (only need positive solution) attempt to deal with e to get $k =$. any of given answers only.

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9	$\frac{dy}{dx} = 4 - 6\sin 2x$ When $x = \frac{\pi}{4}$, $y = \pi$ $\frac{dy}{dx} = -2$ so gradient of normal $= \frac{1}{2}$ Normal equation $y - \pi = \frac{1}{2}\left(x - \frac{\pi}{4}\right)$ When $x = 0$, $y = \frac{7\pi}{8}$ When $y = 0$, $x = -\frac{7\pi}{4}$ Area $= \frac{1}{2} \times \frac{7\pi}{4} \times \frac{7\pi}{8} = \frac{49\pi^2}{64}$	M1,A1 B1 DM1 DM1 A1 A1 B1ft	M1 for attempt to differentiate A1 for all correct for y for substitution of $x = \frac{\pi}{4}$ into <i>their</i> $\frac{dy}{dx}$ and use of ' $m_1 m_2 = -1$ ', dependent on first M1 correct attempt to obtain the equation of the normal, dependent on previous DM mark must be terms of π must be terms of π Follow through on <i>their</i> x and y intercepts; must be exact values
10 (a)	$\cos^2 3x = \frac{1}{2}$, $\cos 3x = (\pm)\frac{1}{\sqrt{2}}$ $3x = 45^\circ, 135^\circ, 225^\circ, 315^\circ$ $x = 15^\circ, 45^\circ, 75^\circ, 105^\circ$	M1 A1,A1	complete correct method, dealing with sec and 3, correctly A1 for each correct pair
(b)	$3(\cot^2 y + 1) + 5\cot y - 5 = 0$ Leading to $3\cot^2 y + 5\cot y - 2 = 0$ or $2\tan^2 y - 5\tan y - 3 = 0$ $(3\cot y - 1)(\cot y + 2) = 0$ or $(\tan y - 3)(2\tan y + 1) = 0$ $\tan y = 3$, $\tan y = \frac{1}{2}$ $y = 71.6^\circ, 251.6^\circ$ $153.4^\circ, 333.4^\circ$	M1 M1 M1 M1 A1,A1	use of a correct identity to get an equation in terms of one trig ratio only for $\cot y = \frac{1}{\tan y}$ to obtain either a quadratic equation in $\tan y$ or solutions in terms of $\tan y$; allow where appropriate for solution of a quadratic equation in terms of either $\tan y$ or $\cot y$ A1 for each correct 'pair'
(c)	$\sin\left(z + \frac{\pi}{3}\right) = \frac{1}{2}$ $z + \frac{\pi}{3} = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{13\pi}{6}$ $z = \frac{\pi}{2}, \frac{11\pi}{6}$ (allow 1.57, 5.76)	M1 A1 M1 A1	completely correct method of solution one correct solution in range correct attempt to obtain a second solution within the range second correct solution (and no other)

CAMBRIDGE INTERNATIONAL EXAMINATIONS

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MARK SCHEME for the May/June 2015 series

0606 ADDITIONAL MATHEMATICS

0606/13

Paper 1, maximum raw mark 80

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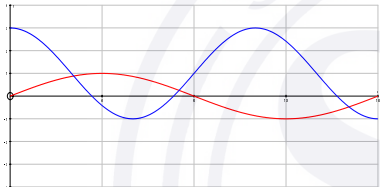
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Abbreviations

awrt	answers which round to
cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
rot	rounded or truncated
SC	Special Case
soi	seen or implied
www	without wrong working

1	(i)	180° or π radians or 3.14 radians (or better)	B1	
	(ii)	2	B1	
	(iii) (a)		B1	$y = \sin 2x$ all correct
	(b)		B1	for either $\uparrow \downarrow \uparrow$ starting at their highest value and ending at their lowest value Or a curve with highest value at $y = 3$ and lowest value at $y = -1$ B1 completely correct graph
(iv)		3	B1	
2	(i)	$\tan \theta = \frac{(8 + 5\sqrt{2})(4 - 3\sqrt{2})}{(4 + 3\sqrt{2})(4 - 3\sqrt{2})}$ $= \frac{32 - 24\sqrt{2} + 20\sqrt{2} - 30}{16 - 18}$ $= 1 + 2\sqrt{2} \text{ cao}$	M1 A1	attempt to obtain $\tan \theta$ and rationalise. Must be convinced that no calculators are being used

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4	(a)	$\mathbf{X}^2 = \begin{pmatrix} 4-4k & -8 \\ 2k & -4k \end{pmatrix}$	B2,1,0	-1 each incorrect element
	(b)	<p>Use of $\mathbf{AA}^{-1} = \mathbf{I}$</p> $\begin{pmatrix} a & 1 \\ b & 5 \end{pmatrix} \begin{pmatrix} \frac{5}{6} & -\frac{1}{6} \\ -\frac{2}{3} & \frac{1}{3} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ <p>Any 2 equations will give $a = 2, b = 4$</p> <p>Alternative method 1:</p> $\frac{1}{5a-b} \begin{pmatrix} 5 & -1 \\ b & a \end{pmatrix} = \begin{pmatrix} \frac{5}{6} & -\frac{1}{6} \\ -\frac{2}{3} & \frac{1}{3} \end{pmatrix}$ <p>Compare any 2 terms to give $a = 2, b = 4$</p> <p>Alternative method 2:</p> <p>Inverse of $\frac{1}{6} \begin{pmatrix} 5 & -1 \\ -4 & 2 \end{pmatrix} = \begin{pmatrix} 2 & 1 \\ 4 & 5 \end{pmatrix}$</p>	<p>M1</p> <p>A1,A1</p> <p>M1</p> <p>A1,A1</p> <p>M1</p> <p>A1,A1</p>	<p>use of $\mathbf{AA}^{-1} = \mathbf{I}$ and an attempt to obtain at least one equation.</p> <p>correct attempt to obtain \mathbf{A}^{-1} and comparison of at least one term.</p> <p>reasoning and attempt at inverse</p>
5		<p>$3x-1 = x(3x-1) + x^2 - 4$ or</p> <p>$y = \left(\frac{y+1}{3}\right)y + \left(\frac{y+1}{3}\right)^2 - 4$</p> <p>$4x^2 - 4x - 3 = 0$ or $4y^2 - 4y - 35 = 0$</p> <p>$(2x-3)(2x+1) = 0$ or $(2y-7)(2y+5) = 0$</p> <p>leading to $x = \frac{3}{2}, x = -\frac{1}{2}$ and</p> <p>$y = \frac{7}{2}, y = -\frac{5}{2}$</p> <p>Midpoint $\left(\frac{1}{2}, \frac{1}{2}\right)$</p> <p>Perpendicular gradient $= -\frac{1}{3}$</p> <p>Perp bisector: $y - \frac{1}{2} = -\frac{1}{3}\left(x - \frac{1}{2}\right)$</p> <p>$(3y + x - 2 = 0)$</p>	<p>M1</p> <p>DM1</p> <p>A1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>equate and attempt to obtain an equation in 1 variable</p> <p>forming a 3 term quadratic equation and attempt to solve</p> <p>x values</p> <p>y values</p> <p>for midpoint, allow anywhere</p> <p>correct attempt to obtain the gradient of the perpendicular, using AB</p> <p>straight line equation through the midpoint; must be convinced it is a perpendicular gradient.</p> <p>allow unsimplified</p>

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6	(i)	$f\left(\frac{1}{2}\right) = \frac{a}{8} - \frac{15}{4} + \frac{b}{2} - 2 = 0$ <p>leading to $a + 4b = 46$ $f(1) = a - 15 + b - 2 = 5$ leading to $a + b = 22$</p> <p>giving $b = 8$ (AG), $a = 14$</p>	M1 correct use of either $f\left(\frac{1}{2}\right)$ or $f(1)$ paired correctly A1 both equations correct (allow unsimplified) M1,A1 M1 for solution of equations A1 for both a and b . AG for b .
	(ii)	$(2x-1)(7x^2-4x+2)$	M1,A1 M1 for valid attempt to obtain $g(x)$, by either observation or by algebraic long division.
	(iii)	$7x^2 - 4x + 2 = 0$ has no real solutions as $b^2 < 4ac$ $16 < 56$	M1 use of $b^2 - 4ac$ A1 correct conclusion; must be from a correct $g(x)$ or $2g(x)$ www
7	(i)	$\frac{dy}{dx} = \frac{(x-1)\left(\frac{8x}{4x^2+2}\right) - \ln(4x^2+3)}{(x-1)^2}$ <p>When $x = 0$, $y = -\ln 3$ oe</p> <p>$\frac{dy}{dx} = -\ln 3$ so gradient of normal is $\frac{1}{\ln 3}$ (allow numerical equivalent)</p> <p>normal equation $y + \ln 3 = \frac{1}{\ln 3}x$ or $y = 0.910x - 1.10$, or $y = \frac{10}{11}x - \frac{11}{10}$ cao (Allow $y = 0.91x - 1.1$)</p>	M1 differentiation of a quotient (or product) B1 correct differentiation of $\ln(4x^2+3)$ A1 all else correct B1 for y value M1 valid attempt to obtain gradient of the normal M1 attempt at normal equation must be using a perpendicular A1
	(ii)	<p>when $x = 0$, $y = -\ln 3$ when $y = 0$, $x = (\ln 3)^2$ Area = ± 0.66 or ± 0.67 or awrt these or $\frac{1}{2}(\ln 3)^3$</p>	M1 valid attempt at area A1

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8	(i)	Range for f: $y \geq 3$ Range for g: $y \geq 9$	B1 B1	
	(ii)	$x = -2 + \sqrt{y-5}$ $g^{-1}(x) = -2 + \sqrt{x-5}$ Domain of g^{-1} : $x \geq 9$ Alternative method: $y^2 + 4y + 9 - x = 0$ $y = \frac{-4 + \sqrt{16 - 4(9-x)}}{2}$	M1 A1 B1	attempt to obtain the inverse function Must be correct form for domain
	(iii)	Need $g(3e^{2x})$ $(3e^{2x} + 2)^2 + 5 = 41$ or $9e^{4x} + 12e^{2x} - 32 = 0$ $(3e^{2x} - 4)(3e^{2x} + 8) = 0$ leading to $3e^{2x} + 2 = \pm 6$ so $x = \frac{1}{2} \ln \frac{4}{3}$ or $e^{2x} = \frac{4}{3}$ so $x = \frac{1}{2} \ln \frac{4}{3}$ Alternative method: Using $f(x) = g^{-1}(41)$, $g^{-1}(41) = 4$ leading to $3e^{2x} = 4$, so $x = \frac{1}{2} \ln \frac{4}{3}$	M1 DM1 M1 A1 M1 DM1 M1 A1	correct order correct attempt to solve the equation dealing with the exponential correctly in order to reach a solution for x Allow equivalent logarithmic forms
	(iv)	$g'(x) = 6e^{2x}$ $g'(\ln 4) = 96$	B1 B1	B1 for each

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9	(i)	$\frac{dy}{dx} = 3x^2 - 10x + 3$ When $x = 0$, for curve $\frac{dy}{dx} = 3$, gradient of line also 3 so line is a tangent. Alternate method: $3x + 10 = x^3 - 5x^2 + 3x + 10$ leading to $x^2 = 0$, so tangent at $x = 0$	M1 for differentiation A1 comparing both gradients
	(ii)	When $\frac{dy}{dx} = 0$, $(3x - 1)(x - 3) = 0$ $x = \frac{1}{3}$, $x = 3$	M1 equating gradient to zero and valid attempt to solve A1,A1 A1 for each
	(iii)	Area = $\frac{1}{2}(10 + 19)3 - \int_0^3 x^3 - 5x^2 + 3x + 10 dx$ $= \frac{87}{2} - \left[\frac{x^4}{4} - \frac{5x^3}{3} + \frac{3x^2}{2} + 10x \right]_0^3$ $= \frac{87}{2} - \left(\frac{81}{4} - 45 + \frac{27}{2} + 30 \right)$ $= 24.7$ or 24.8 Alternative method: Area = $\int_0^3 (3x + 10) - (x^3 - 5x^2 + 3x + 10) dx$ $= \int_0^3 -x^3 + 5x^2 dx$ $= \left[-\frac{x^4}{4} + \frac{5x^3}{3} \right]_0^3 = \frac{99}{4}$	B1 area of the trapezium M1 attempt to obtain the area enclosed by the curve and the coordinate axes, by integration A1 integration all correct DM1 correct application of limits (must be using <i>their</i> 3 from (ii) and 0) A1 B1 correct use of 'Y-y' M1 attempt to integrate A1 integration all correct DM1 correct application of limits A1
10	(a)	$\sin^2 x = \frac{1}{4}$ $\sin x = (\pm) \frac{1}{2}$ $x = 30^\circ, 150^\circ, 210^\circ, 330^\circ$	M1 using $\operatorname{cosec} x = \frac{1}{\sin x}$ and obtaining $\sin x = \dots$ A1,A1 A1 for one correct pair, A1 for another correct pair with no extra solutions

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(b)	$(\sec^2 3y - 1) - 2\sec 3y - 2 = 0$ $\sec^2 3y - 2\sec 3y - 3 = 0$ $(\sec 3y + 1)(\sec 3y - 3) = 0$ leading to $\cos 3y = -1$, $\cos 3y = \frac{1}{3}$ $3y = 180^\circ, 540^\circ$ $3y = 70.5^\circ, 289.5^\circ, 430.5^\circ$ $y = 60^\circ, 180^\circ, 23.5^\circ, 96.5^\circ, 143.5^\circ$ Alternative 1: $\sec^2 3y - 2\sec 3y - 3 = 0$ leading to $3\cos^2 3y + 2\cos 3y - 1$ $(3\cos y - 1)(\cos y + 1) = 0$ Alternative 2: $\frac{\sin^2 y}{\cos^2 y} - \frac{2}{\cos y} - 2 = 0$ $(1 - \cos^2 x) - 2\cos x - 2\cos^2 x = 0$	M1 use of the correct identity M1 attempt to obtain a 3 term quadratic equation in $\sec 3y$ and attempt to solve dealing with \sec and $3y$ correctly M1 A1,A1 A1 for a correct pair, A1 for a second correct pair, A1 for correct 5 th solution and no other within the range A1 M1 use of the correct identity M1 attempt to obtain a quadratic equation in $\cos 3y$ and attempt to solve dealing with $3y$ correctly M1 A marks as above M1 use of the correct identity, $\tan y = \frac{\sin y}{\cos y}$ and $\sec y = \frac{1}{\cos y}$, then as before
	(c) $z - \frac{\pi}{3} = \frac{\pi}{3}, \frac{4\pi}{3}$ $z = \frac{2\pi}{3}, \frac{5\pi}{3}$ or 2.09 or 2.1, 5.24	M1 correct order of operations A1,A1 A1 for a correct solution A1 for a second correct solution and no other within the range

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MARK SCHEME for the March 2015 series

0606 ADDITIONAL MATHEMATICS

0606/12

Paper 12, maximum raw mark 80

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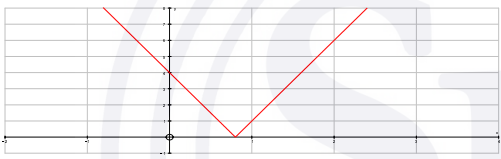
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1	(i)	Members who play football or cricket , or both	B1	
	(ii)	Members who do not play tennis	B1	
	(iii)	There are no members who play both football and tennis	B1	
	(iv)	There are 10 members who play both cricket and tennis.	B1	
2		$kx - 3 = 2x^2 - 3x + k$ $2x^2 - x(k + 3) + (k + 3) = 0$ Using $b^2 - 4ac$, $(k + 3)^2 - (4 \times 2 \times (k + 3)) (< 0)$ $(k + 3)(k - 5) (< 0)$ Critical values $k = -3, 5$ so $-3 < k < 5$	M1 DM1 DM1 A1 A1	for attempt to obtain a 3 term quadratic equation in terms of x for use of $b^2 - 4ac$ for attempt to solve quadratic equation, dependent on both previous M marks for both critical values for correct range
	(i)		B1 B1 B1	for shape, must touch the x -axis in the correct quadrant for y intercept for x intercept
	(ii)	$4 - 5x = \pm 9$ or $(4 - 5x)^2 = 81$ leading to $x = -1, x = \frac{13}{5}$	M1 A1, A1	for attempt to obtain 2 solutions, must be a complete method A1 for each
4	(i)	$729 + 2916x + 4860x^2$	B1, B1 B1	B1 for each correct term
	(ii)	$2 \times \text{their } 4860 - \text{their } 2916 = 6804$	M1 A1	for attempt at 2 terms, must be as shown

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5	(i)	<p>gradient = 4 Using either (2, 1) or (3, 5), $c = -7$ $e^y = 4x + c$ so $y = \ln(4x - 7)$</p> <p>Alternative method: $\frac{y-1}{5-1} = \frac{x-2}{3-2}$ or equivalent</p> <p>$e^y = 4x - 7$ so $y = \ln(4x - 7)$</p>	<p>B1 M1</p> <p>M1,A1</p>	<p>for gradient, seen or implied for attempt at straight line equation to obtain a value for c</p> <p>for correct method to deal with e^y</p>
	(ii)	$x > \frac{7}{4}$	B1ft	ft on <i>their</i> $4x - 7$
	(iii)	<p>$\ln 6 = \ln(4x - 7)$ so $x = \frac{13}{4}$</p>	B1ft	ft on <i>their</i> $4x - 7$
6	(i)	<p>$\frac{dy}{dx} = \frac{x(2\sec^2 2x) - \tan 2x}{x^2}$</p> <p>Or $\frac{dy}{dx} = x^{-1}(2\sec^2 2x) + (-x^{-2})\tan 2x$</p>	<p>M1 A2,1,0</p>	<p>for attempt to differentiate a quotient (or product) –1 each error</p>
	(ii)	<p>When $x = \frac{\pi}{8}$, $y = \frac{8}{\pi}$ (2.546)</p> <p>When $x = \frac{\pi}{8}$, $\frac{dy}{dx} = \frac{\frac{\pi}{2} - 1}{\frac{\pi^2}{64}}$ $= \frac{32}{\pi} - \frac{64}{\pi^2}$ (3.701)</p> <p>Equation of the normal: $y - \frac{8}{\pi} = -\frac{\pi^2}{32(\pi - 2)}\left(x - \frac{\pi}{8}\right)$ $y = -0.27x + 2.65$ (allow 2.66)</p>	<p>B1</p> <p>M1 A1</p>	<p>for y-coordinate (allow 2.55)</p> <p>for an attempt at the normal, must be working with a perpendicular gradient allow in unsimplified form in terms of π or simplified decimal form</p>

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7	(i)	$p\left(\frac{1}{2}\right): \frac{a}{8} + \frac{b}{4} - \frac{3}{2} - 4 = 0$ Simplifies to $a + 2b = 44$ $p(-2): -8a + 4b + 6 - 4 = -10$ Simplifies to $2a - b = 3$ oe Leads to $a = 10, b = 17$	M1 M1 DM1 A1	for correct use of $x = \frac{1}{2}$ for correct use of $x = -2$ for solution of equations for both, be careful as AG for a , allow verification
	(ii)	$p(x) = 10x^3 + 17x^2 - 3x - 4$ $= (2x - 1)(5x^2 + 11x + 4)$	B2,1,0	-1 each error
	(iii)	$x = \frac{1}{2}$ $x = \frac{-11 \pm \sqrt{41}}{10}$	B1 B1, B1	
8	(a) (i)	Range $0 \leq y \leq 1$	B1	
	(ii)	Any suitable domain to give a one-one function	B1	e.g. $0 \leq x \leq \frac{\pi}{4}$
	(b) (i)	$y = 2 + 4 \ln x$ oe $\ln x = \frac{y-2}{4}$ oe $g^{-1}(x) = e^{\frac{x-2}{4}}$ Domain $x \in$ Range $y > 0$	M1 A1 B1 B1	for a complete method to find the inverse must be in the correct form
	(ii)	$g(x^2 + 4) = 10$ $2 + 4 \ln(x^2 + 4) = 10$ leading to $x = 1.84$ only Alternative method: $h(x) = x^2 + 4 = g^{-1}(10)$ $g^{-1}(10) = e^2$, so $x^2 + 4 = e^2$ leading to $x = 1.84$ only	M1 DM1 A1 M1 DM1 A1	for correct order for attempt to solve for one solution only for correct order for attempt to solve for one solution only
	(iii)	$\frac{4}{x} = 2x$ $x^2 = 2$ $x = \sqrt{2}$	B1 M1 A1	for given equation, allow in this form for attempt to solve, must be using derivatives for one solution only, allow 1.41 or better.

Page 5	Mark Scheme	Syllabus	Paper
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9	(i)	$\text{Area of triangular face} = \frac{1}{2}x^2 \frac{\sqrt{3}}{2} = \frac{\sqrt{3}x^2}{4}$ $\text{Volume of prism} = \frac{\sqrt{3}x^2}{4} \times y$ $\frac{\sqrt{3}x^2}{4} \times y = 200\sqrt{3}$ $\text{so } x^2 y = 800$ $A = 2 \times \frac{\sqrt{3}x^2}{4} + 2xy$ $\text{leading to } A = \frac{\sqrt{3}x^2}{2} + \frac{1600}{x}$	B1 for area of triangular face M1 for attempt at volume <i>their</i> area \times y
	(ii)	$\frac{dA}{dx} = \sqrt{3}x - \frac{1600}{x^2}$ $\text{When } \frac{dA}{dx} = 0, x^3 = \frac{1600}{\sqrt{3}}$ $x = 9.74$ $\text{so } A = 246$ $\frac{d^2A}{dx^2} = \sqrt{3} + \frac{3200}{x^3} \text{ which is positive for } x = 9.74$ $\text{so the value is a minimum}$	A1 for correct relationship between x and y M1 for a correct attempt to obtain surface area using <i>their</i> area of triangular face A1 for eliminating y correctly to obtain given answer M1 for attempt to differentiate M1 for equating $\frac{dA}{dx}$ to 0 and attempt to solve A1 for correct x A1 for correct A M1 for attempt at second derivative and conclusion, or alternate methods A1ft for a correct conclusion from completely correct work, follow through on <i>their</i> positive x value.
10	(i)	$\tan \theta = \frac{1+2\sqrt{5}}{6+3\sqrt{5}} \times \frac{6-3\sqrt{5}}{6-3\sqrt{5}}$ $= \frac{6-3\sqrt{5}+12\sqrt{5}-30}{36-45}$ $= \frac{8}{3} - \sqrt{5}$	M1 for attempt at $\cot \theta$ together with rationalisation Must be convinced that a calculator is not being used. A1, A1 A1 for each term
	(ii)	$\tan^2 \theta + 1 = \sec^2 \theta$ $\frac{64}{9} - \frac{16\sqrt{5}}{3} + 5 + 1 = \operatorname{cosec}^2 \theta$ $\text{so } \operatorname{cosec}^2 \theta = \frac{118}{9} - \frac{16\sqrt{5}}{3}$ $\text{Alternate solutions are acceptable}$	M1 for attempt to use the correct identity or correct use of Pythagoras' theorem together with <i>their</i> answer to (i) Must be convinced that a calculator is not being used. A1, A1 A1 for each term

Page 6	Mark Scheme	Syllabus	Paper
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11 (a) (i)	$\text{LHS} = \frac{\frac{1}{\sin y}}{\frac{\cos y}{\sin y} + \frac{\sin y}{\cos y}}$ $= \frac{\frac{1}{\sin y}}{\frac{\cos^2 y + \sin^2 y}{\sin y \cos y}}$ $= \frac{1}{\sin y} \times \sin y \cos y$ $= \cos y$	M1	for dealing with cosec, cot and tan in terms of sin and cos
		M1	for use of $\sin^2 y + \cos^2 y = 1$
		A1	for correct simplification to get the required result.
	(ii)	M1	for use of (i) and correct attempt to deal with multiple angle
		A1, A1	A1 for each 'pair' of solutions
(b)	$2 \sin x + 8(1 - \sin^2 x) = 5$ $8 \sin^2 x - 2 \sin x - 3 = 0$ $(4 \sin x - 3)(2 \sin x + 1) = 0$ $\sin x = \frac{3}{4}, \quad \sin x = -\frac{1}{2}$ $x = 48.6^\circ, 131.4^\circ \quad 210^\circ, 330^\circ$	M1	for use of correct identity
		M1	for attempt to solve quadratic equation
		A1, A1	A1 for each pair of solutions

CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International General Certificate of Secondary Education

MARK SCHEME for the October/November 2014 series

0606 ADDITIONAL MATHEMATICS

0606/11

Paper 1, maximum raw mark 80

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Page 2	Mark Scheme	Syllabus	Paper
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1	$\frac{dy}{dx} = 2x - \frac{16}{x^2}$ <p>When $\frac{dy}{dx} = 0$,</p> $x = 2, y = 12$	<p>M1 A1</p> <p>for attempt to differentiate all correct</p> <p>DM1</p> <p>for equating $\frac{dy}{dx}$ to zero and an attempt to solve for x.</p> <p>A1</p> <p>A1 for both, but no extra solutions</p>
2 (a)		<p>B1</p> <p>for correct shape</p> <p>B1</p> <p>for max value of 2, starting at (0, 2) and finishing at (180°, 2)</p> <p>B1</p> <p>for min value of -4</p>
(b) (i)	4	<p>B1</p> <p>must be positive</p>
(ii)	60° or $\frac{\pi}{3}$ or 1.05 rad	<p>B1</p>
3 (i)	$y = 4(x+3)^{\frac{1}{2}} + c$ $10 = 4\left(9^{\frac{1}{2}}\right) + c$ $c = -2$ $y = 4(x+3)^{\frac{1}{2}} - 2$	<p>M1, A1</p> <p>M1</p> <p>A1</p> <p>M1 for $(x+3)^{\frac{1}{2}}$, A1 for $4(x+3)^{\frac{1}{2}}$</p> <p>for a correct attempt to find c, but must be from an attempt to integrate</p> <p>Allow A1 for $c = -2$</p>
(ii)	$6 = 4(x+3)^{\frac{1}{2}} - 2$ $x = 1$	<p>A1 ft</p> <p>ft for substitution into <i>their</i> equation to obtain x; must have the first M1</p>

Page 3	Mark Scheme	Syllabus	Paper
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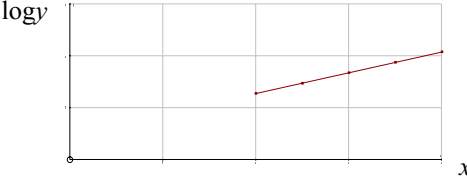
4	(i)	$5y^2 - 7y + 2 = 0$	B1, B1	B1 for 5, B1 for -7
	(ii)	$(5y - 2)(y - 1) = 0$ $y = \frac{2}{5}, x = \frac{\ln 0.4}{\ln 5}$ $x = -0.569$ $y = 1, x = 0$	M1 M1 A1 B1	for solution of quadratic equation from (i) for use of logarithms to solve equation of the type $5^x = k$ must be evaluated to 3sf or better
5	(i)	$\frac{dy}{dx} = 3x^2 - \frac{1}{x}$ When $x = 1, y = 1$ and $\frac{dy}{dx} = 2$ Tangent: $y - 1 = 2(x - 1)$ $(y = 2x - 1)$	M1 B1 DM1 A1	for attempt to differentiate for $y = 1$ for attempt to find equation of tangent allow equation unsimplified
	(ii)	Mid-point (5, 9) $9 = 2(5) - 1$ Alternative Method: Tangent equation $y = 2x - 1$ Equation of line joining (-2, 16) and (12, 2) $y = -x + 14$ Solve simultaneously $x = 5, y = 9$ Mid-point (5, 9)	B1 B1 B1 B1	for midpoint from given coordinates for checking the mid-point lies on tangent for a complete method to find the coordinates of the point of intersection for midpoint from given coordinates
6	(i)	$(2 + px)^6 = 64 + 192px + 240p^2x^2 \dots$ $240p^2 = 60$ $p = \frac{1}{2}$	B1 M1 A1	for $240p^2$ or $240p^2x^2$ or ${}^6C_2 \times 2^4 \times (px)^2$ or ${}^6C_2 \times 2^4 \times p^2$ or ${}^6C_2 \times 2^4 \times p^2x^2$ for equating <i>their</i> term in x^2 to 60 and attempt to solve
	(ii)	$(3 - x)(64 + 192px + 240p^2x^2 \dots)$ Coefficient of x^2 is $180 - 192p = 84$	B1 ft M1 A1	ft for $192p, 96$ or $192 \times \text{their } p$ for $180 - 192p$

Page 4	Mark Scheme	Syllabus	Paper
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7	(i)	$\mathbf{A}^{-1} = \frac{1}{5ab} \begin{pmatrix} b & -2b \\ a & 3a \end{pmatrix}$	B1, B1	B1 for $\frac{1}{5ab}$, B1 for $\begin{pmatrix} b & -2b \\ a & 3a \end{pmatrix}$
	(ii)	$\mathbf{X} = \mathbf{BA}^{-1}$ $= \begin{pmatrix} -a & b \\ 2a & 2b \end{pmatrix} \begin{pmatrix} \frac{1}{5a} & -\frac{2}{5a} \\ \frac{1}{5b} & \frac{3}{5b} \end{pmatrix}$ $= \begin{pmatrix} 0 & 1 \\ \frac{4}{5} & \frac{2}{5} \end{pmatrix}$	M1 DM1 A1 A1	for post-multiplication by inverse matrix for correct attempt at matrix multiplication, needs at least one term correct for their \mathbf{BA}^{-1} (allow unsimplified) for each correct pair of elements, must be simplified
	(iii)	Area $AQB = 12.5$	A1	

8	(i)	$\overline{AB} = \begin{pmatrix} 12 \\ 16 \end{pmatrix}$, at P , $x = -2 + \frac{1}{4}(12)$ so at P , $x = 1$ $y = 3 + \frac{1}{4}(16)$, $y = 7$	B1 B1	for convincing argument for $x = 1$ for $y = 7$
	(ii)	Gradient of $AB = \frac{16}{12}$, so perp gradient = $-\frac{3}{4}$ Perp line: $y - 7 = -\frac{3}{4}(x - 1)$ $(3x + 4y = 31)$	M1 M1 A1	for finding gradient of perpendicular for equation of perpendicular through their P Allow unsimplified
	(iii)	$Q\left(0, \frac{31}{4}\right)$	B1 ft M1	ft on their perpendicular line, may be implied for any valid method of finding the area of the correct triangle, allow use of <i>their</i> Q ; must be in the form $(0, q)$.
			A1	

Page 5	Mark Scheme	Syllabus	Paper
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9	(i)	$\log y = \log a + x \log b$ <table border="1"><tr><td>x</td><td>2</td><td>2.5</td><td>3</td><td>3.5</td><td>4</td></tr><tr><td>$\lg y$</td><td>1.27</td><td>1.47</td><td>1.67</td><td>1.87</td><td>2.07</td></tr></table> <table border="1"><tr><td></td><td>2</td><td>2.5</td><td>3</td><td>3.5</td><td>4</td></tr><tr><td>$\ln y$</td><td>2.93</td><td>3.39</td><td>3.84</td><td>4.31</td><td>4.76</td></tr></table> 	x	2	2.5	3	3.5	4	$\lg y$	1.27	1.47	1.67	1.87	2.07		2	2.5	3	3.5	4	$\ln y$	2.93	3.39	3.84	4.31	4.76	B1 for the statement, may be seen or implied in later work,
	x	2	2.5	3	3.5	4																					
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	2	2.5	3	3.5	4																						
$\ln y$	2.93	3.39	3.84	4.31	4.76																						
(ii)	<p>Gradient = $\log b$ $\lg b = 0.4$ or $\ln b = 0.92$</p> <p>$b = 2.5$ (allow 2.4 to 2.6)</p> <p>Intercept = $\log a$ $\lg a = 0.47$ or $\ln a = 1.10$</p> <p>$a = 3$ (allow 2.8 to 3.2)</p> <p>Alternative method: Simultaneous equations may be used provided points that are on the plotted straight line are used.</p> <p>$a = 3$ (allow 2.8 to 3.2) $b = 2.5$ (allow 2.4 to 2.6)</p>	<p>M1 for attempt to draw graph of x against $\log y$</p> <p>A2,1,0 –1 each error in points plotted</p> <p>DM1 for attempt to find gradient and equate it to $\log b$, dependent on M1 in (i)</p> <p>A1</p> <p>DM1 for attempt to equate y-intercept to $\log a$ or use <i>their</i> equation with <i>their</i> gradient and a point on the line, dependent on M1 in (i)</p> <p>A1</p> <p>DM1 for a pair of equations using points on the line, dependent on M1 in (i)</p> <p>DM1 for solution of these equations, dependent on M1 in (i)</p> <p>A1 for each</p> <p>A1</p>																									

Page 6	Mark Scheme	Syllabus	Paper
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10	(a) (i)	360	B1	
	(ii)	60	B1	
	(iii)	36	B1	
	(b) (i)	${}^8C_5 \times {}^{12}C_5$ $56 \times 792 = 44352$	B1, B1 B1	B1 for each, allow unevaluated with no extra terms Final answer must be evaluated and from multiplication
	(ii)	4 places are accounted for Gender no longer 'important' Need ${}^{16}C_6 = 8008$ Alternative Method $({}^6C_6 \times {}^{10}C_0) + ({}^6C_5 \times {}^{10}C_1) \dots ({}^6C_0 \times {}^{10}C_6)$ $1 + 60 + 675 + 2400 + 3150 + 1512 + 210 = 8008$	M1 A1 M1 A1	for realising that 4 places are accounted or that gender is no longer important for 8008 for at least 5 of the 7 cases, allow unsimplified
11	(a)	$2 \cos 3x - \frac{\cos 3x}{\sin 3x} = 0$ $\cos 3x \left(2 - \frac{1}{\sin 3x} \right) = 0$ Leading to $\cos 3x = 0$, $3x = 90^\circ, 270^\circ$ $x = 30^\circ, 90^\circ$ and $\sin 3x = \frac{1}{2}$, $3x = 30^\circ, 150^\circ$ $x = 10^\circ, 50^\circ$	M1 DM1 A1 DM1 A1	for use of $\cot 3x = \frac{\cos 3x}{\sin 3x}$, may be implied for attempt to solve $\cos 3x = 0$ correctly from correct factorisation to obtain x A1 for both, no excess solutions in the range for attempt to solve $\sin 3x = \frac{1}{2}$ correctly to obtain x A1 for both, condone excess solutions
	(b)	$\cos \left(y + \frac{\pi}{2} \right) = -\frac{1}{2}$ $y + \frac{\pi}{2} = \frac{2\pi}{3}, \frac{4\pi}{3}$ so $y = \frac{\pi}{6}, \frac{5\pi}{6}$ (0.524, 2.62)	M1 DM1 A1, A1	for dealing with $\sec \left(y + \frac{\pi}{2} \right)$ correctly for correct order of operations, must not mix degrees and radians

Page 7	Mark Scheme	Syllabus	Paper
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12 (i)	$\overrightarrow{AQ} = \lambda \mathbf{b} - \mathbf{a}$	B1	
(ii)	$\overrightarrow{BP} = \mu \mathbf{a} - \mathbf{b}$	B1	
(iii)	$\overrightarrow{OR} = \mathbf{a} + \frac{1}{3}(\lambda \mathbf{b} - \mathbf{a})$ or $\lambda \mathbf{b} - \frac{2}{3}(\lambda \mathbf{b} - \mathbf{a})$ $= \frac{2}{3}\mathbf{a} + \frac{1}{3}\lambda \mathbf{b}$	M1 A1	for $\mathbf{a} + \frac{1}{3}$ their (i) Allow unsimplified
(iv)	$\overrightarrow{OR} = \mathbf{b} + \frac{7}{8}(\mu \mathbf{a} - \mathbf{b})$ or $\mu \mathbf{a} - \frac{1}{8}(\mu \mathbf{a} - \mathbf{b})$ $= \frac{1}{8}\mathbf{b} + \frac{7}{8}\mu \mathbf{a}$	M1 A1	for $\mathbf{b} + \frac{7}{8}$ their (ii) Allow unsimplified
(v)	$\frac{2}{3}\mathbf{a} + \frac{1}{3}\lambda \mathbf{b} = \frac{1}{8}\mathbf{b} + \frac{7}{8}\mu \mathbf{a}$ $\frac{2}{3} = \frac{7}{8}\mu, \mu = \frac{16}{21}$ Allow 0.762 $\frac{1}{3}\lambda = \frac{1}{8}, \lambda = \frac{3}{8}$ Allow 0.375	M1 A1 A1	for equating (iii) and (iv) and then equating like vectors

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0606/12

Paper 1, maximum raw mark 80

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1	$\frac{dy}{dx} = 2x - \frac{16}{x^2}$ <p>When $\frac{dy}{dx} = 0$,</p> $x = 2, y = 12$	M1 A1 DM1 A1	for attempt to differentiate all correct for equating $\frac{dy}{dx}$ to zero and an attempt to solve for x . A1 for both, but no extra solutions
2 (a)		B1 B1 B1	for correct shape for max value of 2, starting at (0, 2) and finishing at (180°, 2) for min value of -4
(b) (i)	4	B1	must be positive
(ii)	60° or $\frac{\pi}{3}$ or 1.05 rad	B1	
3 (i)	$y = 4(x+3)^{\frac{1}{2}} + c$ $10 = 4\left(9^{\frac{1}{2}}\right) + c$ $c = -2$ $y = 4(x+3)^{\frac{1}{2}} - 2$	M1, A1 M1 A1	M1 for $(x+3)^{\frac{1}{2}}$, A1 for $4(x+3)^{\frac{1}{2}}$ for a correct attempt to find c , but must be from an attempt to integrate Allow A1 for $c = -2$
(ii)	$6 = 4(x+3)^{\frac{1}{2}} - 2$ $x = 1$	A1 ft	ft for substitution into <i>their</i> equation to obtain x ; must have the first M1

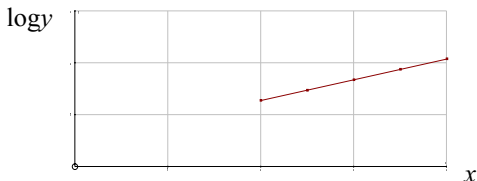
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4	(i)	$5y^2 - 7y + 2 = 0$	B1, B1	B1 for 5, B1 for -7
	(ii)	$(5y - 2)(y - 1) = 0$ $y = \frac{2}{5}, x = \frac{\ln 0.4}{\ln 5}$ $x = -0.569$ $y = 1, x = 0$	M1 M1 A1 B1	for solution of quadratic equation from (i) for use of logarithms to solve equation of the type $5^x = k$ must be evaluated to 3sf or better
5	(i)	$\frac{dy}{dx} = 3x^2 - \frac{1}{x}$ When $x = 1, y = 1$ and $\frac{dy}{dx} = 2$ Tangent: $y - 1 = 2(x - 1)$ $(y = 2x - 1)$	M1 B1 DM1 A1	for attempt to differentiate for $y = 1$ for attempt to find equation of tangent allow equation unsimplified
	(ii)	Mid-point (5, 9) $9 = 2(5) - 1$ Alternative Method: Tangent equation $y = 2x - 1$ Equation of line joining (-2, 16) and (12, 2) $y = -x + 14$ Solve simultaneously $x = 5, y = 9$ Mid-point (5, 9)	B1 B1 B1 B1	for midpoint from given coordinates for checking the mid-point lies on tangent for a complete method to find the coordinates of the point of intersection for midpoint from given coordinates
6	(i)	$(2 + px)^6 = 64 + 192px + 240p^2x^2 \dots$ $240p^2 = 60$ $p = \frac{1}{2}$	B1 M1 A1	for $240p^2$ or $240p^2x^2$ or ${}^6C_2 \times 2^4 \times (px)^2$ or ${}^6C_2 \times 2^4 \times p^2$ or ${}^6C_2 \times 2^4 \times p^2x^2$ for equating <i>their</i> term in x^2 to 60 and attempt to solve
	(ii)	$(3 - x)(64 + 192px + 240p^2x^2 \dots)$ Coefficient of x^2 is $180 - 192p$ $= 84$	B1 ft M1 A1	ft for $192p, 96$ or $192 \times \text{their } p$ for $180 - 192p$

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7	(i)	$\mathbf{A}^{-1} = \frac{1}{5ab} \begin{pmatrix} b & -2b \\ a & 3a \end{pmatrix}$	B1, B1	B1 for $\frac{1}{5ab}$, B1 for $\begin{pmatrix} b & -2b \\ a & 3a \end{pmatrix}$
	(ii)	$\mathbf{X} = \mathbf{BA}^{-1}$ $= \begin{pmatrix} -a & b \\ 2a & 2b \end{pmatrix} \begin{pmatrix} \frac{1}{5a} & -\frac{2}{5a} \\ \frac{1}{5b} & \frac{3}{5b} \end{pmatrix}$ $= \begin{pmatrix} 0 & 1 \\ \frac{4}{5} & \frac{2}{5} \end{pmatrix}$	M1 DM1 A1 A1	for post-multiplication by inverse matrix for correct attempt at matrix multiplication, needs at least one term correct for their \mathbf{BA}^{-1} (allow unsimplified) for each correct pair of elements, must be simplified
	(iii)	Area $AQB = 12.5$		
8	(i)	$\overline{AB} = \begin{pmatrix} 12 \\ 16 \end{pmatrix}$, at P , $x = -2 + \frac{1}{4}(12)$ so at P , $x = 1$ $y = 3 + \frac{1}{4}(16)$, $y = 7$	B1 B1	for convincing argument for $x = 1$ for $y = 7$
	(ii)	Gradient of $AB = \frac{16}{12}$, so perp gradient = $-\frac{3}{4}$ Perp line: $y - 7 = -\frac{3}{4}(x - 1)$ $(3x + 4y = 31)$	M1 M1 A1	for finding gradient of perpendicular for equation of perpendicular through their P Allow unsimplified
	(iii)	$Q\left(0, \frac{31}{4}\right)$ Area $AQB = 12.5$	B1 ft M1 A1	ft on their perpendicular line, may be implied for any valid method of finding the area of the correct triangle, allow use of <i>their</i> Q ; must be in the form $(0, q)$.

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	2	2.5	3	3.5	4																						
$\ln y$	2.93	3.39	3.84	4.31	4.76																						
(ii)	<p>Gradient = $\log b$ $\lg b = 0.4$ or $\ln b = 0.92$</p> <p>$b = 2.5$ (allow 2.4 to 2.6)</p> <p>Intercept = $\log a$ $\lg a = 0.47$ or $\ln a = 1.10$</p> <p>$a = 3$ (allow 2.8 to 3.2)</p> <p>Alternative method: Simultaneous equations may be used provided points that are on the plotted straight line are used.</p> <p>$a = 3$ (allow 2.8 to 3.2) $b = 2.5$ (allow 2.4 to 2.6)</p>	<p>M1 for attempt to draw graph of x against $\log y$</p> <p>A2,1,0 –1 each error in points plotted</p> <p>DM1 for attempt to find gradient and equate it to $\log b$, dependent on M1 in (i)</p> <p>A1</p> <p>DM1 for attempt to equate y-intercept to $\log a$ or use <i>their</i> equation with <i>their</i> gradient and a point on the line, dependent on M1 in (i)</p> <p>A1</p> <p>DM1 for a pair of equations using points on the line, dependent on M1 in (i)</p> <p>DM1 for solution of these equations, dependent on M1 in (i)</p> <p>A1 for each</p> <p>A1</p>																									

Page 6	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2014	0606	12

10	(a) (i)	360	B1	
	(ii)	60	B1	
	(iii)	36	B1	
	(b) (i)	${}^8C_5 \times {}^{12}C_5$ $56 \times 792 = 44352$	B1, B1 B1	B1 for each, allow unevaluated with no extra terms Final answer must be evaluated and from multiplication
	(ii)	4 places are accounted for Gender no longer 'important' Need ${}^{16}C_6 = 8008$ Alternative Method $({}^6C_6 \times {}^{10}C_0) + ({}^6C_5 \times {}^{10}C_1) \dots ({}^6C_0 \times {}^{10}C_6)$ $1 + 60 + 675 + 2400 + 3150 + 1512 + 210 = 8008$	M1 A1 M1 A1	for realising that 4 places are accounted or that gender is no longer important for 8008 for at least 5 of the 7 cases, allow unsimplified
11	(a)	$2 \cos 3x - \frac{\cos 3x}{\sin 3x} = 0$ $\cos 3x \left(2 - \frac{1}{\sin 3x} \right) = 0$ Leading to $\cos 3x = 0$, $3x = 90^\circ, 270^\circ$ $x = 30^\circ, 90^\circ$	M1 DM1 A1	for use of $\cot 3x = \frac{\cos 3x}{\sin 3x}$, may be implied for attempt to solve $\cos 3x = 0$ correctly from correct factorisation to obtain x A1 for both, no excess solutions in the range
	(b)	and $\sin 3x = \frac{1}{2}$, $3x = 30^\circ, 150^\circ$ $x = 10^\circ, 50^\circ$ $\cos \left(y + \frac{\pi}{2} \right) = -\frac{1}{2}$ $y + \frac{\pi}{2} = \frac{2\pi}{3}, \frac{4\pi}{3}$ so $y = \frac{\pi}{6}, \frac{5\pi}{6}$ (0.524, 2.62)	DM1 A1 M1 DM1 A1, A1	for attempt to solve $\sin 3x = \frac{1}{2}$ correctly to obtain x A1 for both, condone excess solutions for dealing with $\sec \left(y + \frac{\pi}{2} \right)$ correctly for correct order of operations, must not mix degrees and radians

Page 7	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2014	0606	12

12 (i)	$\overrightarrow{AQ} = \lambda \mathbf{b} - \mathbf{a}$	B1	
(ii)	$\overrightarrow{BP} = \mu \mathbf{a} - \mathbf{b}$	B1	
(iii)	$\overrightarrow{OR} = \mathbf{a} + \frac{1}{3}(\lambda \mathbf{b} - \mathbf{a})$ or $\lambda \mathbf{b} - \frac{2}{3}(\lambda \mathbf{b} - \mathbf{a})$ $= \frac{2}{3}\mathbf{a} + \frac{1}{3}\lambda \mathbf{b}$	M1 A1	for $\mathbf{a} + \frac{1}{3}$ their (i) Allow unsimplified
(iv)	$\overrightarrow{OR} = \mathbf{b} + \frac{7}{8}(\mu \mathbf{a} - \mathbf{b})$ or $\mu \mathbf{a} - \frac{1}{8}(\mu \mathbf{a} - \mathbf{b})$ $= \frac{1}{8}\mathbf{b} + \frac{7}{8}\mu \mathbf{a}$	M1 A1	for $\mathbf{b} + \frac{7}{8}$ their (ii) Allow unsimplified
(v)	$\frac{2}{3}\mathbf{a} + \frac{1}{3}\lambda \mathbf{b} = \frac{1}{8}\mathbf{b} + \frac{7}{8}\mu \mathbf{a}$ $\frac{2}{3} = \frac{7}{8}\mu, \mu = \frac{16}{21}$ Allow 0.762 $\frac{1}{3}\lambda = \frac{1}{8}, \lambda = \frac{3}{8}$ Allow 0.375	M1 A1 A1	for equating (iii) and (iv) and then equating like vectors

CAMBRIDGE INTERNATIONAL EXAMINATIONS

Cambridge International General Certificate of Secondary Education

MARK SCHEME for the October/November 2014 series

0606 ADDITIONAL MATHEMATICS

0606/13

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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Page 2	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2014	0606	13

1	$a = 3$ $b = 2$ $c = 4$	B1 B1 B1	
2	$x^2 = 16$ or $y^2 - 4y + 3 = 0$ $x = \pm 4$ $y = 1, 3$ Points $(-4, 1)$ and $(4, 3)$ Line $AB = \sqrt{8^2 + 2^2}$ $= \sqrt{68}$ or $2\sqrt{17}$	M1 A1 A1 M1 A1	for correct elimination of one variable and attempt to form a quadratic equation in x or y . for use of Pythagoras theorem allow either form
3	(i) $n(A) = 2$ $n(B) = 3$ $n(C) = 0$ (ii) $A \cup B = \{-1, -2, -3, 3\}$ (iii) $A \cap B = \{-2\}$ (iv) ξ , 'the universal set', R , 'real numbers', $\{x : x \in \quad\}$	B1 B1 B1 B1 B1 B1	B0 for $n(2)$, $\{2\}$, $\{0\}$, \emptyset , $\{\}$ etc.
4	(a) $\tan x = -\frac{5}{3}$ $x = 121.0^\circ, 301.0^\circ$ (b) $\sin\left(3y + \frac{\pi}{4}\right) = \frac{1}{2}$ $3y + \frac{\pi}{4} = \frac{\pi}{6}, \frac{5\pi}{6}, \frac{13\pi}{6}, \frac{17\pi}{6}$ $3y = -\frac{\pi}{12}, \frac{7\pi}{12}, \frac{23\pi}{12}, \frac{31\pi}{12}$ $y = \frac{7\pi}{36}, \frac{23\pi}{36}, \frac{31\pi}{36}$ (0.611, 2.01 and 2.71)	M1 A1 A1ft M1 A1 DM1 A1, A1	Correct statement or $\tan x = -1.67$ A1 for either correct solution ft from <i>their</i> first solution for dealing correctly with cosec and attempt to solve subsequent equation for $\frac{\pi}{6}, \frac{5\pi}{6}$, or $\frac{13\pi}{6}$, or $\frac{17\pi}{6}$ for correct order of operations A1 for one correct solution A1 for both the other correct solutions and no others in range.

Page 3	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2014	0606	13

5	(a) (i)	$\begin{pmatrix} 12 & 2 & 1 \\ 9 & 3 & 0 \\ 8 & 5 & 1 \\ 11 & 2 & 0 \end{pmatrix} \begin{pmatrix} 0.5 \\ 0.4 \\ 0.45 \end{pmatrix} = \begin{pmatrix} 7.25 \\ 5.70 \\ 6.45 \\ 6.30 \end{pmatrix}$ or $(0.5 \ 0.4 \ 0.45) \begin{pmatrix} 12 & 9 & 8 & 11 \\ 2 & 3 & 5 & 2 \\ 1 & 0 & 1 & 0 \end{pmatrix}$ $= (7.25 \ 5.70 \ 6.45 \ 6.30)$	M1	for correct compatible matrices in the correct order. Allow 1 error in each matrix. Allow if done in cents
	(ii)	25.70	DM1	for a correct method for multiplying their matrices to obtain an appropriate 4 by 1 or 1 by 4 matrix.
	(b)	$Y = X^{-1}$ or $Y = X^{-1}I$	A2,1,0	A2 all correct or A1 3 correct elements.
		$Y = \frac{1}{22} \begin{pmatrix} 1 & -4 \\ 5 & 2 \end{pmatrix} \text{ or } \begin{pmatrix} \frac{1}{22} & -\frac{4}{22} \\ \frac{5}{22} & \frac{2}{22} \end{pmatrix}$ Alternative method: $\begin{pmatrix} 2 & 4 \\ -5 & 1 \end{pmatrix} \begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ $2a + 4c = 1, \ 2b + 4d = 0$ $-5a + c = 0, \ -5b + d = 1$ leading to $= \frac{1}{22} \begin{pmatrix} 1 & -4 \\ 5 & 2 \end{pmatrix}$ oe	B1	Allow 25.7

M1

for matrix algebra

A1for $\frac{1}{22} \begin{pmatrix} & \\ & \end{pmatrix}$ **A1**for $k \begin{pmatrix} 1 & -4 \\ 5 & 2 \end{pmatrix}$ **M1**

for a complete method using simultaneous equations

A1
 $a = \frac{1}{22} \text{ and } c = \frac{5}{22}$
or $b = -\frac{4}{22} \text{ and } d = \frac{2}{22}$
A1

for correct matrix

Page 4	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2014	0606	13

6	(i)	$\cos 0.9 = \frac{6}{OC} \quad \text{or} \quad \frac{OC}{\sin 0.9} = \frac{12}{\sin(\pi - 1.8)}$ $OC = \frac{6}{\cos 0.9} = 9.652\dots$ $\text{or } OC = \frac{12 \sin 0.9}{\sin(\pi - 1.8)} = 9.652\dots$	M1	for correct use of cosine, sine rule, cosine rule or any other valid method
	(ii)	$\text{Perimeter} = (0.9 \times 12) + 9.652 + (12 - 9.652)$ $= 22.8$	B1 M1 A1	for arc length for attempt to add the correct lengths
	(iii)	$\text{Area} = \left(\frac{1}{2} \times 12^2 \times 0.9 \right) - \left(\frac{1}{2} \times 9.652^2 \sin(\pi - 1.8) \right)$ $64.8 - 45.36$ $= 19.4 \text{ to } 19.5$ Alternative Method: $\frac{1}{2}(12 - 9.652) \times 9.652 \times \sin 1.8$ $\frac{1}{2}12^2(0.9 - \sin 0.9)$ $11.04 + 8.40$ $\text{Area} = 19.4 \text{ to } 19.5$	B1 B1 B1 B1 B1 B1 B1	for area of sector, allow unsimplified for area of isosceles triangle $\frac{1}{2}(9.65(2\dots))^2 \sin(\pi - 1.8)$ or $\frac{1}{2}(12 \times 6 \tan 0.9)$ or $\frac{1}{2}(12 \times 9.65(2\dots) \times \sin 0.9)$, allow unsimplified. for answer in range 19.4 to 19.5 for area of triangle ACB , unsimplified for area of segment, unsimplified answer in range 19.4 to 19.5
	7	$1 + 2\log_5 x = \log_5(18x - 9)$ $\log_5 5 + \log_5 x^2 = \log_5(18x - 9)$ $5x^2 = 18x - 9$ $(5x - 3)(x - 3) = 0$ $x = \frac{3}{5}, 3$	B1, B1 M1 DM1 A1	B1 for dealing with '1', B1 for dealing with '2' for a correct use of addition or subtraction of logarithms for elimination of logarithms to form a 3 term quadratic and for solution of quadratic for both x values

Page 5	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2014	0606	13

8	(i)	$f'(x) = \left(x \times \frac{3x^2}{x^3} \right) + (\ln x^3)$ $= 3 + 3 \ln x, = 3(1 + \ln x)$ <p>or $f(x) = 3x \ln x$</p> $f'(x) = \left(3x \times \frac{1}{x} \right) + 3 \ln x,$ $= 3(1 + \ln x)$	M1 B1 A1 B1 M1 A1	for differentiation of a product for differentiation of $\ln x^3$ for simplification to gain <u>given answer</u> for use of $\ln x^3 = 3 \ln x$ for differentiation of a product for simplification to gain <u>given answer</u>
	(ii)	$\int 3(1 + \ln x) dx = x \ln x^3 \text{ or } 3x \ln x$ $\int 1 + \ln x dx = \frac{1}{3} x \ln x^3 \text{ or } x \ln x$	M1 A1	for realising that differentiation is the reverse of integration and using (i)
	(iii)	$x \ln x - \int 1 dx \text{ or } \left[\frac{1}{3} x \ln x^3 \right] - \int 1 dx$ $\left[x \ln x - x \right]_1^2 \text{ or } \left[\frac{1}{3} x \ln x^3 - x \right]_1^2$ $= 2 \ln 2 - 2 + 1$ $= -1 + \ln 4$	DM1 DM1 A1	for using answer to (ii) and subtracting $\int 1 dx$ dependent on M mark in (ii) for correct application of limits from correct working
9	(a)	$5^p = 625, \text{ so } p = 4$ ${}^4C_1 5^{p-1}(-q) = -1500$ $4 \times 125(-q) = -1500$ $q = 3$ ${}^4C_2 5^{p-2} q^2 = r$ $r = 1350$	B1 M1 A1 M1 A1	<i>their</i> p substituted in ${}^pC_1 5^{p-1}(-q)$ or in ${}^pC_1 5^{p-1}(-qx)$ unsimplified <i>their</i> p and q substituted in ${}^pC_2 5^{p-2}(-q)^2$ or ${}^pC_2 5^{p-2}(-qx)^2$ unsimplified
	(b)	${}^{12}C_3 (2x)^9 \left(\frac{1}{4x^3} \right)^3$ <p>Term is 1760</p>	M1 DM1 A1	for identifying correct term for attempt to evaluate correct expression must be evaluated

Page 6	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2014	0606	13

10	(a)	$\frac{5^x}{5^{2(3y-2)}} = 1 \text{ or } \frac{3^x}{3^{3(y-1)}} = 3^4 \text{ oe}$ $x = 6y - 4$ $x = 3y + 1$ Leads to $x = 6, y = \frac{5}{3}$	M1 for obtaining one correct equation in powers of 5, 3, 25, 27 or 81 A1 for $x = 6y - 4$ oe linear equation A1 for $x = 3y + 1$ oe linear equation M1 for attempt to solve linear simultaneous equations which have been obtained correctly A1 for both.
	(b)	Using the cosine rule: $(1 + 2\sqrt{3})^2 = (2 + \sqrt{3})^2 + 2^2 - 4(2 + \sqrt{3})\cos A$ $\cos A = \frac{(13 + 4\sqrt{3}) - (7 + 4\sqrt{3}) - 4}{-4(2 + \sqrt{3})} \text{ oe}$ $\cos A = \frac{-1}{2(2 + \sqrt{3})} \times \frac{2 - \sqrt{3}}{2 - \sqrt{3}}$ $\cos A = -1 + \frac{\sqrt{3}}{2}$	M1 for correct substitution in cosine rule, may use in form of $\cos A = \dots$ DM1 for attempt to make $\cos A$ subject and simplify DM1 for rationalisation. A1

Page 7	Mark Scheme	Syllabus	Paper
	Cambridge IGCSE – October/November 2014	0606	13

11	(i)	$\frac{dy}{dx} = (x+5)2(x-1) + (x-1)^2$ $\frac{dy}{dx} = (x-1)(3x+9)$ When $\frac{dy}{dx} = 0$ $x = 1$ $x = -3$ Alternative method: $y = x^3 + 3x^2 - 9x + 5$ $\frac{dy}{dx} = 3x^2 + 6x - 9$ When $\frac{dy}{dx} = 0$ $x = 1$ $x = -3$	M1 A1 DM1 A1 A1 M1 A1	for differentiation of a product, allow unsimplified correct for equating to zero and solution of quadratic for expansion of brackets and differentiation of each term of a 4 term cubic for equating to zero and solution of 3 term quadratic
	(ii)	$\int x^3 + 3x^2 - 9x + 5 dx$ $= \frac{x^4}{4} + x^3 - \frac{9x^2}{2} + 5x (+c)$	M1 A2,1,0	for correct attempt to obtain and integrate a 4 term cubic A2 for 4 correct terms or A1 for 3 correct terms
	(iii)	$\left[\frac{x^4}{4} + x^3 - \frac{9x^2}{2} + 5x \right]_{-5}^1$ $= \left(\frac{1}{4} + 1 - \frac{9}{2} + 5 \right) - \left(\frac{625}{4} - 125 - \frac{225}{2} - 25 \right)$ $= 108$	M1 A1	for correct substitution of limits 1 and -5 for <i>their</i> (ii)
	(iv)	When $x = -3, y = 32$ $k > 32$	M1 A1	for realising that the y-coordinate of the maximum point is needed.

MARK SCHEME for the May/June 2014 series

0606 ADDITIONAL MATHEMATICS

0606/11

Paper 1, maximum raw mark 80

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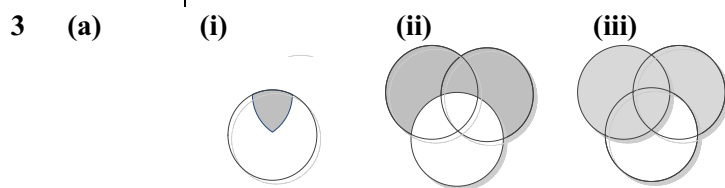
Cambridge is publishing the mark schemes for the May/June 2014 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.

Page 2	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	11

1	$\text{LHS} = \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta}{1 + \sin \theta}$ $= \frac{\sin \theta(1 + \sin \theta) + \cos^2 \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1 + \sin \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1}{\cos \theta} \text{ leading to } \sec \theta$	B1	B1 for use of $\tan \theta = \frac{\sin \theta}{\cos \theta}$
		M1	M1 for attempt to obtain a single fraction
		DM1	DM1 for use of $\sin^2 \theta + \cos^2 \theta = 1$
		A1	A1 for ‘finishing off’
	<p>Alternative solution:</p> $\text{LHS} = \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta(1 - \sin \theta)}{(1 + \sin \theta)(1 - \sin \theta)}$ $= \frac{\sin \theta}{\cos \theta} + \frac{\cos \theta(1 - \sin \theta)}{\cos^2 \theta}$ $= \frac{\sin \theta}{\cos \theta} + \frac{(1 - \sin \theta)}{\cos \theta}$ $= \frac{1}{\cos \theta} \text{ leading to } \sec \theta$	B1	B1 for use of $\tan \theta = \frac{\sin \theta}{\cos \theta}$
		M1	M1 for multiplication by $(1 - \sin \theta)$
		DM1	DM1 for use of $\sin^2 \theta + \cos^2 \theta = 1$
		A1	A1 for ‘finishing off’
	<p>Alternative solution:</p> $\text{LHS} = \frac{\tan \theta(1 + \sin \theta) + \cos \theta}{1 + \sin \theta}$ $= \frac{\frac{\sin \theta}{\cos \theta} + \frac{\sin^2}{\cos \theta} + \cos \theta}{1 + \sin \theta}$ $= \frac{\sin \theta + \sin^2 \theta + \cos^2 \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1 + \sin \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1}{\cos \theta} \text{ leading to } \sec \theta$	M1	M1 for attempt to obtain a single fraction
		B1	B1 for use of $\tan \theta = \frac{\sin \theta}{\cos \theta}$
		DM1	DM1 for use of $\sin^2 \theta + \cos^2 \theta = 1$
		A1	A1 for ‘finishing off’

Page 3	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	11

2	(i)	$ a = \sqrt{4^2 + 3^2} = 5$ $ b + c = \sqrt{(-3)^2 + 4^2} = 5$	M1	M1 for finding the modulus of either a or b + c
	(ii)	$\lambda \begin{pmatrix} 4 \\ 3 \end{pmatrix} + \mu \begin{pmatrix} 2 \\ 2 \end{pmatrix} = 7 \begin{pmatrix} -5 \\ 2 \end{pmatrix}$ $4\lambda + 2\mu = -35$ and $3\lambda + 2\mu = 14$ leading to $\lambda = -49$, $\mu = 80.5$	A1 M1 DM1 A1	A1 for completion M1 for equating like vectors and obtaining 2 linear equations DM1 for solution of simultaneous equations A1 for both


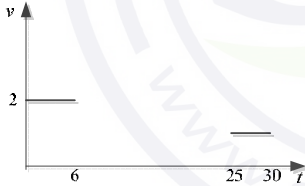


- (b) (i)
(ii)

Page 4	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	11

6	(i)	$\mathbf{AB} = \begin{pmatrix} 10 & 19 \\ 32 & 37 \\ 14 & 14 \end{pmatrix}$	M1 A1	M1 for at least 3 correct elements of a 3×2 matrix A1 for all correct
	(ii)	$\mathbf{B}^{-1} = \frac{1}{7} \begin{pmatrix} 5 & -1 \\ -3 & 2 \end{pmatrix}$	B1 B1	B1 for $\frac{1}{7}$, B1 for $\begin{pmatrix} 5 & -1 \\ -3 & 2 \end{pmatrix}$
	(iii)	$2 \begin{pmatrix} 2 & 1 \\ 3 & 5 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} -3 \\ -22 \end{pmatrix}$	M1	M1 for obtaining in matrix form
		$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{7} \begin{pmatrix} 5 & -1 \\ -3 & 2 \end{pmatrix} \begin{pmatrix} -1.5 \\ -11 \end{pmatrix} = \frac{1}{7} \begin{pmatrix} 3.5 \\ -17.5 \end{pmatrix}$ $x = 0.5, y = -2.5$	M1 A1	M1 for pre-multiplying by \mathbf{B}^{-1} A1 for both
7	(i)	$y = 2x^2 - \frac{1}{x+1} (+c)$ when $x = \frac{1}{2}, y = \frac{5}{6}$ so $\frac{5}{6} = \frac{1}{2} - \frac{2}{3} + c$ leading to $c = 1$ $\left(y = 2x^2 - \frac{1}{x+1} + 1 \right)$	B1 B1 M1 A1	B1 for each correct term M1 for attempt to find $+c$, must have at least 1 of the previous B marks Allow A1 for $c = 1$
	(ii)	When $x = 1, y = \frac{5}{2}$ $\frac{dy}{dx} = \frac{17}{4}$ so gradient of normal $= -\frac{4}{17}$ Equation of normal $y - \frac{5}{2} = -\frac{4}{17}(x - 1)$ $(8x + 34y - 93 = 0)$	M1 B1 DM1 A1	M1 for using $x = 1$ in their (i) to find y B1 for gradient of normal DM1 for attempt at normal equation A1 – allow unsimplified (fractions must not contain decimals)

Page 5	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	11

8	(i)	$\log p = n \log V + \log k$ <table border="1"><tr><td>$\ln V$</td><td>2.30</td><td>3.91</td><td>4.61</td><td>5.30</td></tr><tr><td>$\ln p$</td><td>4.55</td><td>2.14</td><td>1.10</td><td>0.10</td></tr></table> <table border="1"><tr><td>$\lg V$</td><td>1</td><td>1.70</td><td>2</td><td>2.30</td></tr><tr><td>$\lg p$</td><td>1.98</td><td>0.93</td><td>0.48</td><td>0.04</td></tr></table> 	$\ln V$	2.30	3.91	4.61	5.30	$\ln p$	4.55	2.14	1.10	0.10	$\lg V$	1	1.70	2	2.30	$\lg p$	1.98	0.93	0.48	0.04	B1	B1 for statement, but may be implied by later work.
	$\ln V$	2.30	3.91	4.61	5.30																			
	$\ln p$	4.55	2.14	1.10	0.10																			
	$\lg V$	1	1.70	2	2.30																			
$\lg p$	1.98	0.93	0.48	0.04																				
(ii)	Use of gradient = n $n = -1.5$ (allow -1.4 to -1.6)	M1 A2,1,0	M1 for plotting a suitable graph –1 for each error in points plotted																					
(iii)	Allow 13 to 16	DM1 A1	DM1 for equating numerical gradient to n																					
		DM1 A1	DM1 for use of <i>their</i> graph or substitution into <i>their</i> equation.																					
9	(a)	Distance travelled = area under graph $= \frac{1}{2}(60 + 20) \times 12 = 480$	M1 A1	M1 for realising that area represents distance travelled and attempt to find area																				
	(b)		B1 B1 B1	B1 for velocity of 2 ms^{-1} for $0 \leq t \leq 6$ B1 for velocity of zero for <i>their</i> '6' to <i>their</i> '25' B1 for velocity of 1 ms^{-1} for $25 \leq t \leq 30$																				
	(c) (i)	$v = 4 - \frac{16}{t+1}$ When $v = 0$, $t = 3$	M1 DM1 A1	M1 for attempt at differentiation DM1 for equating velocity to zero and attempt to solve																				
	(ii)	$a = \frac{16}{(t+1)^2}$ $0.25(t+1)^2 = 16$ $t = 7$	M1 A1	M1 for attempt at differentiation and equating to 0.25 with attempt to solve																				

Page 6	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	11

10	(a)	1 digit even numbers 2	B1	
		2 digit even numbers $4 \times 2 = 8$	B1	
		3 digit even numbers $3 \times 3 \times 2 = 18$	B1	
		Total = 28	B1	
	(b) (i)	3M 5W = 35	B1	
		4M 4W = 175	B1	
		5M 3W = 210	B1	
		Total = 420	B1	B1 for addition to obtain final answer, must be evaluated.
		or ${}^{12}C_8 - 6M\ 2W - 7M\ 1W$ $495 - 70 - 5 = 420$		or: as above, final B1 for subtraction to get final answer
	(ii)	Oldest man in, oldest woman out and vice-versa		
		${}^{10}C_7 \times 2 = 240$	B1, B1	B1 for ${}^{10}C_7$, B1 for realising there are 2 identical cases
		Alternative: 1 man out 1 woman in 6 men 4 women		
		6M 1W : ${}^6C_6 \times {}^4C_1 = 4$		
		5M 2W : ${}^6C_5 \times {}^4C_2 = 36$		
		4M 3W : ${}^6C_4 \times {}^4C_3 = 60$		
		3M 4W : ${}^6C_3 \times {}^4C_4 = 20$		
		Total = 120	B1	All separate cases correct for B1
		There are 2 identical cases to consider, so 240 ways in all.	B1	B1 for realising there are 2 identical cases, which have integer values

Page 7	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	11

11	(a)	$5\sin 2x + 3\cos 2x = 0$ $\tan 2x = -0.6$ $2x = 149^\circ, 329^\circ$ $x = 74.5^\circ, 164.5^\circ$ Alternatives: $\sin(2x + 31^\circ) = 0$ or $\cos(2x - 59^\circ) = 0$	M1 DM1 A1,A1 M1	In each case the last A mark is for a second correct solution and no extra solutions within the range M1 for use of tan DM1 for dealing with $2x$ correctly A1 for each M1 for either, then mark as above
	(b)	$2\cot^2 y + 3\operatorname{cosec} y = 0$ $2(\operatorname{cosec}^2 y - 1) + 3\operatorname{cosec} y = 0$ $2\operatorname{cosec}^2 y + 3\operatorname{cosec} y - 2 = 0$ $(2\operatorname{cosec} y - 1)(\operatorname{cosec} y + 2) = 0$ One valid solution $\operatorname{cosec} y = -2, \sin y = -\frac{1}{2}$ $y = 210^\circ, 330^\circ$ Alternative: $2\frac{\cos^2 y}{\sin^2 y} + \frac{3}{\sin y} = 0$ leads to $2\sin^2 y - 3\sin y - 2 = 0$ and $\sin y = -\frac{1}{2}$ only $y = 210^\circ, 330^\circ$	M1 M1 M1 A1,A1 M1 M1 A1A1	M1 for use of correct identity M1 for attempt to factorise a 3 term quadratic equation A1 for each M1 for use of $\cot y = \frac{\cos y}{\sin y}$ and $\operatorname{cosec} y = \frac{1}{\sin y}$ M1 for attempt to factorise a 3 term quadratic equation
	(c)	$3\cos(z + 1.2) = 2$ $\cos(z + 1.2) = \frac{2}{3}$ $(z + 1.2) = 0.8411, 5.442, 7.124$ $z = 4.24, 5.92$	M1 A1 A1A1	M1 for correct order of operations to end up with 0.8411 radians or better A1 for one of 5.441 or 7.124 (or better) A1 for each valid solution

MARK SCHEME for the May/June 2014 series

0606 ADDITIONAL MATHEMATICS

0606/12

Paper 1, maximum raw mark 80


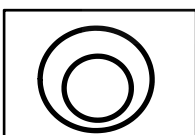
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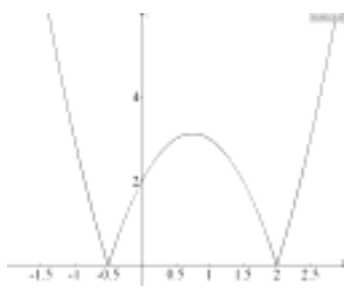
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Page 2	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	12

1	$\frac{\cos^2 A + (1 + \sin A)^2}{(1 + \sin A)\cos A}$ $\frac{\cos^2 A + 1 + 2 \sin A + \sin^2 A}{(1 + \sin A)\cos A}$ $= \frac{2(1 + \sin A)}{(1 + \sin A)\cos A}$ $= \frac{2}{\cos A} = 2 \sec A$ <p>Alternative:</p> $\frac{\cos A(1 - \sin A)}{(1 + \sin A)(1 - \sin A)} + \frac{1 + \sin A}{\cos A}$ $= \frac{\cos A(1 - \sin A)}{1 - \sin^2 A} + \frac{1 + \sin A}{\cos A}$ $= \frac{\cos A(1 - \sin A)}{\cos^2 A} + \frac{1 + \sin A}{\cos A}$ $= \frac{1 - \sin A}{\cos A} + \frac{1 + \sin A}{\cos A}$ $= \frac{2}{\cos A} = 2 \sec A$	<p>M1</p> <p>M1</p> <p>DM1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>M1 for obtaining a single fraction, correctly</p> <p>M1 for expansion of $(1 + \sin A)^2$ and use of identity</p> <p>DM1 for factorisation and cancelling of $(1 + \sin A)$ factor</p> <p>A1 for use of $\frac{1}{\cos A} = \sec A$ and final answer</p> <p>M1 for multiplying first term by $\frac{1 - \sin A}{1 - \sin A}$</p> <p>M1 for expansion of $(1 - \sin A)(1 + \sin A)$ and use of identity</p> <p>M1 for simplification of the 2 terms</p> <p>A1 for use of $\frac{1}{\cos A} = \sec A$ and final answer</p>
2 (a) (i)	 <p>(i)</p>  <p>(b) (i) 6</p> <p>(ii) 5</p> <p>(iii) 9</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p>	

Page 3	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	12

3	(i)		B1 B1 B1	B1 for shape B1 for $y = 2$ (must have a graph) B1 for $x = -0.5$ and 2 (must have a graph)
	(ii)	<p>Maximum point occurs when $y = \frac{25}{8}$</p> <p>so $k > \frac{25}{8}$</p>	M1 A1	M1 for obtaining the value of y at the maximum point, by either completing the square, differentiation, use of discriminant or symmetry. Must have the correct sign for A1 Ignore any upper limits
4		$\int_0^a \sin 3x \, dx = \frac{1}{3} \quad dx = \frac{1}{3}$ $\left[-\frac{2}{3} \cos 3x \right]_0^a = \frac{1}{3}$ $\left(-\frac{2}{3} \cos 3a \right) - \left(-\frac{2}{3} \right) = \frac{1}{3}$ $\cos 3a = 0.5$ $3a = \frac{\pi}{3}, \quad a = \frac{\pi}{9}$	B1, B1 M1 A1 M1 A1	B1 for $k \cos 3x$ only, B1 for $-\frac{2}{3} \cos 3x$ only M1 for correct substitution of the correct limits into their result A1 for correct equation M1 for correct method of solution of equation of the form $\cos ma = k$ A1 allow 0.349, must be a radian answer
5	(i)	$2^{5x} \times 2^{2y} = 2^{-3}$ leads to $5x + 2y = -3$	B1, B1 DB1	B1 for 2^{2y} , B1 for 2^{-3} , B1 for dealing with indices correctly to obtain given answer
	(ii)	$7^x \times 49^{2y} = 1$ can be written as $x + 4y = 0$ <p>Solving $5x + 2y = -3$ and $x + 4y = 0$ leads to</p> $x = -\frac{2}{3}, \quad y = \frac{1}{6}$	B1 B1 M1 A1	B1 for either 7^{4y} or 7^0 seen B1 for $x + 4y = 0$ M1 for solution of their simultaneous equations, must both be linear A1 for both, allow equivalent fractions only

Page 4	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	12

6	(a)	YX and ZY	B1,B1	B1 for each, must be in correct order,
	(b)	$\mathbf{B} = \mathbf{A}^{-1} \begin{pmatrix} 3 & 9 \\ -6 & -3 \end{pmatrix},$ $= -\frac{1}{3} \begin{pmatrix} 1 & 2 \\ 4 & 5 \end{pmatrix} \begin{pmatrix} 3 & 9 \\ -6 & -3 \end{pmatrix}$ $= -\frac{1}{3} \begin{pmatrix} -9 & 3 \\ -18 & 21 \end{pmatrix} \text{ or } \begin{pmatrix} 3 & -1 \\ 6 & -7 \end{pmatrix}$ <p>Alternative method:</p> $\begin{pmatrix} 5 & -2 \\ -4 & 1 \end{pmatrix} \begin{pmatrix} a & b \\ c & d \end{pmatrix} = \begin{pmatrix} 3 & 9 \\ -6 & -3 \end{pmatrix}$ <p>Leads to $5a - 2c = 3$, $5b - 2d = 9$ $-4a + c = -6$, $-4b + d = -3$</p> <p>Solutions give matrix</p> $-\frac{1}{3} \begin{pmatrix} -9 & 3 \\ -18 & 21 \end{pmatrix} \text{ or } \begin{pmatrix} 3 & -1 \\ 6 & -7 \end{pmatrix}$	M1 B1,B1 DM1 A1 M1 A2,1,0 M1 A1	M1 for pre-multiplication by \mathbf{A}^{-1} B1 for $-\frac{1}{3}$, B1 for $\begin{pmatrix} 1 & 2 \\ 4 & 5 \end{pmatrix}$ DM1 for attempt at matrix multiplication A1 allow in either form M1 for a complete method to obtain 4 equations -1 for each incorrect equation M1 for solution to find 4 unknowns A1 for a correct, final matrix

Page 5	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	12

7	(i)	$\sin \frac{\theta}{2} = \frac{6}{8}, \frac{\theta}{2} = 0.8481$ or better or $12^2 = 8^2 + 8^2 - 128 \cos \theta$ $\theta = 1.6961$ or better or using areas $\frac{1}{2} \times 12 \times 2\sqrt{7} = \frac{1}{2} 8^2 \sin \theta$ oe $\sin \theta = 0.9922, \theta = 1.4455$ or 1.6961	M1 M1 for a complete method to find either θ or $\frac{\theta}{2}$ A1 Answer given.
	(ii)	Arc length = $(2\pi - 1.696) \times 8$ $(36.697$ or $36.7)$ Perimeter = $12 + (2\pi - 1.696) \times 8$ $= 48.7$	M1 M1 for correct attempt at a minor or major arc length A1 A1 for correct major arc length, allow unsimplified A1 A1 for 48.7 or better
	(iii)	Area = $\frac{8^2}{2} (2\pi - 1.696) + \frac{8^2}{2} \sin 1.696$ $= 178.5, 178.6, \text{awrt } 179$ Alternative: Area = $\pi 8^2 - \left(\frac{1}{2} 8^2 (1.696) - \frac{8^2}{2} \sin 1.696 \right)$	M1,M1 M1 for correct attempt to find area of major sector A1 M1 for correct attempt to find area of triangle, using any method M1 for attempt at area of circle – area of minor sector M1 for area of triangle

Page 6	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	12

8	(a) (i)	720	B1	
	(ii)	240	B1	
	(iii)	Starts with either a 2 or a 4: 48 ways	B1	allow unevaluated
		Does not start with either a 2 or a 4: 96 ways (i.e. starts with 1 or 5)	B1	allow unevaluated
		Total = 144	B1	must be evaluated
		Alternative 1:		
		Ends with a 2, starts with a 1,4 or 5 : 72 ways	B1	
		Ends with a 4, starts with a 1,2 or 5 : 72 ways	B1	
		Total =144	B1	
		Alternative 2:		
	(b)	$240 - (2 \times 2 \times {}^4P_3) \text{ or } (4 \times {}^4P_3 \times 2) - (2 \times {}^4P_3)$ =144	B2 B1	B2 for correct expression seen, allow P notation
		Alternative 3:		
		${}^3P_1 \times {}^4P_3 \times {}^2P_1 \text{ or } 3 \times 4 \times 2$ =144	B2 B1	Allow P notation here, for B2
		With twins : ${}^{16}C_4 (=1820)$	B1	
		Without twins: ${}^{16}C_6 (=8008)$	B1	
		Total: 9828	B1	
		Alternative:		
		${}^{18}C_6 - (2 \times {}^{16}C_5)$ = 9828	B1,B1 B1	B1 for ${}^{18}C_6 - \dots, ,$ B1 for $2 \times {}^{16}C_5$

Page 7	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	12

9	(i)	$h = \frac{4000}{\pi r^2} \text{ or } \pi r^2 h = 4000$ $A = 2\pi r h + 2\pi r^2$ $A = 2\pi r \frac{4000}{\pi r^2} + 2\pi r^2$	B1 M1 A1	M1 for substitution of h or $\pi r h$ into <i>their</i> equation for A A1 Answer given
	(ii)	$\frac{dA}{dr} = -\frac{8000}{r^2} + 4\pi r$ <p>When $\frac{dA}{dr} = 0$, $r^3 = \frac{8000}{4\pi}$</p> <p>leading to $A = 1395, 1390$</p> $\frac{d^2 A}{dr^2} = \frac{16000}{r^3} + 4\pi,$ <p>which, is positive so a minimum.</p>	B1, B1 M1 M1 A1 √B1	B1 for each term correct M1 for equating to zero and attempt to find r^3 M1 for substitution of their r to obtain A . A1 for 1390 or awrt 1395 √B1 for a complete correct method and conclusion.

Page 8	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	12

10 (i)	Velocity = $26 \times \frac{1}{13}(5\mathbf{i} + 12\mathbf{j})$ = $10\mathbf{i} + 24\mathbf{j}$	M1	M1 for $\frac{1}{13}(5\mathbf{i} + 12\mathbf{j})$
		A1	
	Alternative 1: $ 10\mathbf{i} + 24\mathbf{j} = \sqrt{10^2 + 24^2}$ = 26	M1	M1 for working from given answer to obtain the given speed
	Showing that one vector is a multiple of the other, hence same direction	A1	A1 for a completely correct method
	Alternative 2: $\sqrt{5^2 + 12^2} = 13$, $13k = 26$, so $k = 2$ Velocity = $2(5\mathbf{i} + 12\mathbf{j})$,	M1	M1 for attempt to obtain the 'multiple' and apply to the direction vector
	Velocity = $10\mathbf{i} + 24\mathbf{j}$	A1	A1 for a completely correct method
	Alternative 3: Use of trig: $\tan \alpha = \frac{12}{5}$, $\alpha = 67.4^\circ$ Velocity $26 \cos 67.4^\circ \mathbf{i} + 26 \sin 67.4^\circ \mathbf{j}$	M1	M1 for reaching this stage
	Velocity = $10\mathbf{i} + 24\mathbf{j}$	A1	A1 for a completely correct method
	(ii) Position vector = $4(10\mathbf{i} + 24\mathbf{j})$ or $40\mathbf{i} + 96\mathbf{j}$	B1	Allow either form for B1
	(iii) $(40\mathbf{i} + 96\mathbf{j}) + (10\mathbf{i} + 24\mathbf{j})t$ oe	M1	M1 for <i>their</i> (ii) + $(10\mathbf{i} + 24\mathbf{j})t$ or $(10\mathbf{i} + 24\mathbf{j}) \times (t + 4)$
		A1	A1 correct answer only
(iv)	$(120\mathbf{i} + 81\mathbf{j}) + (-22\mathbf{i} + 30\mathbf{j})t$ oe	B1	
(v)	$40 + 10t = 120 - 22t$ or $96 + 24t = 81 + 30t$ $t = 2.5$ or 18:30 Position vector = $65\mathbf{i} + 156\mathbf{j}$	M1	M1 for equating like vectors
		A1	A1 Allow for $t = 2.5$
		DM1	DM1 for use of t to obtain position vector
		A1	A1 cao

Page 9	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	12

11	(a)	$\tan x(\tan x + 5) = 0$ $\tan x = 0, \quad x = 0^\circ, 180^\circ$ $\tan x = -5, \quad x = 101.3^\circ$	B1,B1 B1	B1 for each, must be from correct work
	(b)	$2(1 - \sin^2 y) - \sin y - 1 = 0$ $2 \sin^2 y + \sin y - 1 = 0$ $(2 \sin y - 1)(\sin y + 1) = 0$ $\sin y = \frac{1}{2}, y = 30^\circ, 150^\circ$ $\sin y = -1, y = 270^\circ$	M1 A1,A1 A1	M1 for use of correct identity and attempt to solve resulting 3 term quadratic equation.
	(c)	$\cos\left(2z - \frac{\pi}{6}\right) = \frac{1}{2}$ $\left(2z - \frac{\pi}{6}\right) = \frac{\pi}{3}$ $z = \frac{\pi}{4} \text{ or } 0.785 \text{ or better}$ $\left(2z - \frac{\pi}{6}\right) = \frac{5\pi}{3}$ $z = \frac{11\pi}{12} \text{ or } 2.88 \text{ or better}$	M1 A1 M1 A1	M1 for dealing with sec correctly and obtaining $\frac{\pi}{3}$ or 1.05 M1 for obtaining a second equation $\left(2z - \frac{\pi}{6}\right) = 2\pi - \text{their } \frac{\pi}{3}$ or

MARK SCHEME for the May/June 2014 series

0606 ADDITIONAL MATHEMATICS

0606/13

Paper 1, maximum raw mark 80

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Page 2	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	13

1	(i)	$y = 3(x-1)^2 + 2$ $a = 3, b = 1, c = 2$	B1, B1, B1	B1 for each, may be given in the form $y = 3(x-1)^2 + 2$
	(ii)	(1, 2)	√B1	Follow through on their answers to (i) If using differentiation, follow through on their x only.
2		$2^{4x} \times 4^y \times 8^{x-y} = 1$ Considering powers of either 2, 4 or 8 $7x - y = 0$ $3^{x+y} = \frac{1}{3}$	M1	M1 for considering powers of either 2, 4 or 8 and forming an equation using these powers
		Considering powers of 3 $x + y = -1$	B1	B1 for equation considering powers of 3
		Solving both simultaneously gives $x = -\frac{1}{8}, y = -\frac{7}{8}$	M1 A1	M1 for attempt to solve their equations A1 for both
3	(i)	$f(-3) = -27 + 9p - 3p^2 + 21$ $= 9p - 3p^2 - 6$	M1 A1	M1 for substitution of $x = -3$ A1 answer must be simplified
	(ii)	$9p - 3p^2 - 6 < 0$ $(p-1)(p-2) > 0$ Critical values 1 and 2 $p < 1, p > 2$	M1 A1 A1	M1 for attempt to factorise A1 for critical values A1 for correct range
4	(i)	$V = x(24 - 2x)^2$ $= x(576 - 96x + 4x^2)$ $= 4x^3 - 96x^2 + 576x$	M1 A1	M1 for attempt at a product of 3 lengths, 2 of which must be the same A1 for expansion to reach given answer
	(ii)	$\frac{dV}{dx} = 12x^2 - 192x + 576$ When $\frac{dV}{dx} = 0, 12x^2 - 192x + 576 = 0$	M1 DM1	M1 for attempt to differentiate DM1 for equating $\frac{dV}{dx}$ to zero and attempt to solve
		leading to $(x-4)(x-12) = 0$ with $x = 4$ the only possible solution $V = 1024$	A1 A1	A1 for $x = 4$ A1 for $V = 1024$

Page 3	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	13

5	(i)	$64 - 960x + 6000x^2$	B1, B1, B1	B1 for each correct term
	(ii)	$(64 - 960x + 6000x^2)(a^3 + 3a^2bx),$ $64a^3 = 512, a = 2$ $-960a^3 + 3a^2b(64) = 0$ leading to $b = 10$	B1 B1 M1 A1	B1 for first two terms of $(a + bx)^3$ B1 for equating constant term to 512 and obtaining $a = 2$ M1 for attempt to equate coefficient of x to zero, must have two terms involved A1 for $b = 10$
6		When $x = 2, y = -4$ $\frac{dy}{dx} = x\left(\frac{2x}{3}\right)(x^2 - 12)^{-\frac{2}{3}} + (x^2 - 12)^{\frac{1}{3}}$ When $x = 2, \frac{dy}{dx} = -\frac{4}{3}$ Normal: $y + 4 = \frac{3}{4}(x - 2)$ $(4y = 3x - 22)$	B1 M1, B1 A1 M1 A1	B1 for $y = -4$ M1 for differentiation of a product B1 for $\frac{2x}{3}(x^2 - 12)^{-\frac{2}{3}}$ M1 for attempt at normal equation A1 allow unsimplified
	7	(a) (i) 15120 (ii) $(5 \times 4) \times (4 \times 3 \times 2)$ 480 (b) (i) 5456 (ii) ${}^{18}C_2 \times 15$ 2295 (iii) 5456 – Number of ways only girls get tickets 5456 – 455 = 5001 Or 1B 2G 1890 2B 1G 2295 3B 816 Total 5001	B1 M1 A1 B1 M1 A1 M1 A1 M1 A1	 M1 for attempt to multiply number of ways of getting 4 letters by the number of ways of getting 2 digits. M1 for attempt at an appropriate product, at least one term must be correct. M1 for a complete correct method <i>their (i)</i> – number of ways only girls get tickets M1 must be considering at least 2 of the cases shown

Page 4	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	13

8	(i)	1	B1	
	(ii)	$a = 8e^{-2t}$ $8e^{-2t} = 6, -2t = \ln \frac{3}{4}$ $t = 0.144$	M1 DM1	M1 for attempt to differentiate DM1 for correct attempt to solve equation in the form $e^{-2t} = \text{constant}$
	(iii)	$s = 5t + 2e^{-2t} \quad (+c)$ When $t = 0, s = 0$, so $c = -2$ When $t = 1.5, s = 5.60$ Alternative: $s = \left[5t + 2e^{-2t} \right]_0^{1.5}$ Leading to $s = 5.60$	A1 M1 DM1, A1 M1, A1 M1 DM1 A1 M1 A1	A1 must be at least 3 sf M1 for attempt to integrate DM1 for attempt to find c , A1 c correct M1 for substitution of $t = 1.5$ M1 for attempt to integrate DM1 for attempt to use limits A1 all correct M1 for evaluation of square bracket notation
	(iv)	Velocity is always +ve, so no change in direction	A1 B1	Allow any valid argument.
9	(i)	$\cos x (3 \sin x - 2) = 0$ $\cos x = 0, x = 90^\circ$ $\sin x = \frac{2}{3},$ $x = 41.8^\circ, 138.2^\circ$	B1 M1 A1, √A1	B1 for 90° M1 for attempt to solve $\sin x = \frac{2}{3}$ Follow through on their first answer
	(ii)	$10 \sin^2 y + \cos y = 8$ $10(1 - \cos^2 y) + \cos y = 8$ $10 \cos^2 y - \cos y - 2 = 0$ $(2 \cos y - 1)(5 \cos y + 2) = 0$ $\cos y = \frac{1}{2}, \cos y = -\frac{2}{5}$ $y = 60^\circ, 300^\circ \text{ and } y = 113.6^\circ, 246.4^\circ$	M1 M1 M1 A1, A1	M1 for use of correct identity M1 for attempt to reduce to a 3 term quadratic and attempt to solve quadratic M1 for attempt to solve using factors in terms of cos A1 for any 'pair'

Page 5	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	13

10 (i)	<table border="1"><tr><td>x^2</td><td>2.25</td><td>3.06</td><td>4</td><td>5.06</td></tr><tr><td>$\lg y$</td><td>0.59</td><td>0.92</td><td>1.29</td><td>1.71</td></tr></table>	x^2	2.25	3.06	4	5.06	$\lg y$	0.59	0.92	1.29	1.71	B1	
x^2	2.25	3.06	4	5.06									
$\lg y$	0.59	0.92	1.29	1.71									
(ii)		M1 A1, 0	M1 for plotting $\log y$ against x^2 –1 each error, poor point plotting, poor line drawing										
(iii)	Gradient: $\lg b = 0.4$, $b = 2.5$ (allow 2.45 to 2.55) Intercept : $\lg A = -0.3$, $A = 0.5$ (allow 0.4 to 0.6)	M1 A1 M1 A1	M1 for correct use of gradient M1 for correct use intercept										
(iv)	2.1 (allow 2 to 2.2)	M1, A1											

Page 6	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2014	0606	13

11	(i)	<p>at A $\sqrt{3} \sin 3x + \cos 3x = 0$</p> <p>$\tan 3x = -\frac{1}{\sqrt{3}}, 3x = \frac{5\pi}{6} \quad 150^\circ$</p> <p>$x = \frac{5\pi}{18} (0.873) \text{ (allow } 50^\circ)$</p>	<p>M1</p> <p>DM1</p> <p>A1</p>	<p>M1 for equating to zero and attempt to solve using tan</p> <p>DM1 for dealing with $3x$</p>
	(ii)	<p>$\frac{dy}{dx} = 3\sqrt{3} \cos 3x - 3 \sin 3x$</p> <p>When $\frac{dy}{dx} = 0, \tan 3x = \sqrt{3}, 3x = \frac{\pi}{3} \text{ or } 3x = 60^\circ,$</p> <p>$x = \frac{\pi}{9} (0.349) \text{ (allow } 20^\circ)$</p>	<p>B1, B1</p> <p>M1</p> <p>A1</p>	<p>B1 for $\frac{dy}{dx}$</p> <p>M1 for attempt to solve $\frac{dy}{dx} = 0$</p>
	(iii)	<p>Area = $\left[-\frac{\sqrt{3}}{3} \cos 3x + \frac{1}{3}x + \frac{1}{3} \sin 3x \right]_{\frac{\pi}{9}}^{\frac{5\pi}{18}}$</p> <p>$= \left(-\frac{\sqrt{3}}{3} \cos \frac{5\pi}{6} + \frac{1}{3} \sin \frac{5\pi}{6} \right) - \left(-\frac{\sqrt{3}}{3} \cos \frac{\pi}{3} + \frac{1}{3} \sin \frac{\pi}{3} \right)$</p> <p>$= \frac{2}{3} \text{ or } 0.667 \text{ or better}$</p>	<p>M1</p> <p>A1, A1</p> <p>DM1</p> <p>A1</p>	<p>M1 for attempt to integrate</p> <p>A1 for each term</p> <p>DM1 for correct application of their limits</p>

MARK SCHEME for the October/November 2013 series

0606 ADDITIONAL MATHEMATICS

0606/11

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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Page 2	Mark Scheme	Syllabus	Paper
	IGCSE – October/November 2013	0606	11

Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
 - A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
 - B Accuracy mark for a correct result or statement independent of method marks.
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 - The symbol \square implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously ‘correct’ answers or results obtained from incorrect working.
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Page 3	Mark Scheme	Syllabus	Paper
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1	$a = 3, b = 2, c = 1$	B1, B1, B1 [3]	B1 for each
2	<p>Using $b^2 - 4ac, 9 = 4(k + 1)^2$ $4k^2 + 8k - 5 = 0$</p> $k = -\frac{5}{2}, \left(\frac{1}{2}\right)$ <p>To be below the x-axis $k < -\frac{5}{2}$</p> <p>Or: $\frac{dy}{dx} = 2(k + 1)x - 3$ when $\frac{dy}{dx} = 0, x = \frac{3}{2(k + 1)}$ $\therefore y = (k + 1)\frac{9}{4(k + 1)^2} - \frac{9}{2(k + 1)} + (k + 1)$ To lie under the x-axis, $y < 0$ $\therefore (k + 1)\frac{9}{4(k + 1)^2} - \frac{9}{2(k + 1)} + (k + 1) < 0$ leading to $9 = 4(k + 1)^2$ or equivalent then as for previous method</p>	<p>M1 DM1</p> <p>A1</p> <p>A1 [4]</p> <p>M1</p>	<p>M1 for any use of $b^2 - 4ac$ DM1 for solution of their quadratic in k</p> <p>A1 for critical value(s), $\frac{1}{2}$ not necessary</p> <p>A1 for $k < -\frac{5}{2}$ only</p> <p>M1 for a complete method to this point.</p>

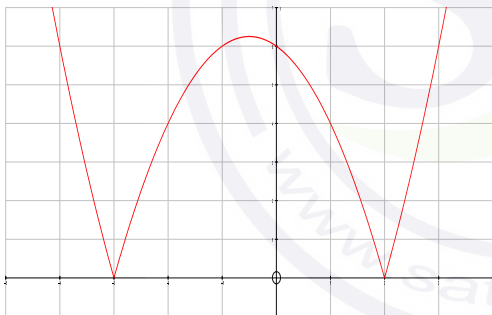
Page 4	Mark Scheme	Syllabus	Paper
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<p>3</p> $\frac{1 + \sin \theta}{\cos \theta} + \frac{\cos \theta}{1 + \sin \theta} + \frac{(1 + \sin \theta)^2 + \cos^2 \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1 + 2 \sin \theta + \sin^2 \theta + \cos^2 \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{2 + 2 \sin \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{2(1 + \sin \theta)}{\cos \theta(1 + \sin \theta)}$ $= 2 \sec \theta$ <p>Alternative solution:</p> $\sec \theta + \tan \theta + \frac{1}{\sec \theta + \tan \theta}$ $= \frac{(\sec \theta + \tan \theta)^2 + 1}{\sec \theta + \tan \theta}$ $= \frac{\sec^2 \theta + 2 \sec \theta \tan \theta + \tan^2 \theta + 1}{\sec \theta + \tan \theta}$ $= \frac{2 \sec^2 \theta + 2 \sec \theta \tan \theta}{\sec \theta + \tan \theta}$ $= \frac{2 \sec \theta (\sec \theta + \tan \theta)}{\sec \theta + \tan \theta}$ $= 2 \sec \theta$	<p>M1</p> <p>DM1</p> <p>DM1</p> <p>A1</p> <p>[4]</p> <p>M1</p> <p>DM1</p> <p>DM1</p> <p>A1</p>	<p>M1 for dealing with the fractions, denominator must be correct, be generous with numerator</p> <p>M1 for expansion and use of $\cos^2 \theta + \sin^2 \theta = 1$</p> <p>M1 for attempt to factorise</p> <p>A1 for obtaining final answer correctly</p> <p>M1 for dealing with the fractions</p> <p>M1 for expansion and use of $\tan^2 \theta + 1 = \sec^2 \theta$</p> <p>DM1 for attempt to factorise</p> <p>A1 for obtaining final answer correctly</p>
<p>4 (i) $n(A) = 3$</p> <p>(ii) $n(B) = 4$</p> <p>(iii) $A \cup B = \{60^\circ, 240^\circ, 300^\circ, 420^\circ, 600^\circ\}$</p> <p>(iv) $A \cap B = \{60^\circ, 420^\circ\}$</p>	<p>B1</p> <p>[1]</p> <p>B1</p> <p>[1]</p> <p>√B1</p> <p>[1]</p> <p>√B1</p> <p>[1]</p>	<p>If elements listed for (i), then they must be correct elements to get B1 leading to $n(A) = 3$. If they are not listed and correct answer given then B1.</p> <p>If elements listed for (ii), then they must be correct elements leading to $n(B) = 4$ to get B1. If they are not listed and correct answer given then B1.</p> <p>Follow through on any sets listed in (i) and (ii). Do not allow any repetitions.</p> <p>Follow through on any sets listed in (i) and (ii).</p>

Page 5	Mark Scheme	Syllabus	Paper
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<p>5 (i) $9x - \frac{1}{3}\cos 3x (+c)$</p> <p>(ii) $\left[9x - \frac{1}{3}\cos 3x\right]_{\frac{\pi}{9}}^{\pi}$ $= \left(9\pi - \frac{1}{3}\cos 3\pi\right) - \left(\pi - \frac{1}{3}\cos \frac{\pi}{3}\right)$ $= 8\pi + \frac{1}{2}$</p>	<p>B1, B1, B1 [3]</p> <p>M1</p> <p>A1, A1 [3]</p>	<p>B1 for $9x$, B1 for $\frac{1}{3}$ or $\cos 3x$</p> <p>B1 for $-\frac{1}{3}\cos 3x$</p> <p>Condone omission of $+c$</p> <p>M1 for correct use of limits in their answer to (i)</p> <p>A1 for each term</p>
<p>6 $f\left(\frac{1}{2}\right) = \frac{a}{8} + 1 + \frac{b}{2} - 2$</p> <p>leading to $a + 4b - 8 = 0$</p> <p>$f(2) = 2f(-1)$</p> <p>$8a + 16 + 2b - 2 = 2(-a + 4 - b - 2)$</p> <p>leading to $10a + 4b + 10 = 0$ or equivalent</p> <p>$\therefore a = -2, b = \frac{5}{2}$</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>DM1 A1 [6]</p>	<p>M1 for substitution of $x = \frac{1}{2}$ into $f(x)$</p> <p>A1 for correct equation in any form</p> <p>M1 for attempt to substitute $x = 2$ or $x = -1$ into $f(x)$ and use $f(2) = \pm 2f(-1)$ or $2f(2) = \pm f(-1)$</p> <p>A1 for a correct equation in any form</p> <p>DM1 (on both previous M marks) for attempt to solve simultaneous equations to obtain either a or b</p> <p>A1 for both correct</p>

Page 6	Mark Scheme	Syllabus	Paper
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<p>7 (a) (i) 360</p> <p>(ii) 120</p> <p>(b) (i) 924</p> <p>(ii) 28</p> <p>(iii) $924 - ({}^8C_3 \times {}^4C_3) - ({}^8C_2 \times {}^4C_4)$ (i.e. $924 - 3M\ 3W - 2M\ 4W$)</p> <p>$924 - 224 - 28$ $= 672$</p> <p>Or: $4M\ 2W\ {}^8C_4 \times {}^4C_2 = 420$ $5M\ 1W\ {}^8C_3 \times {}^4C_1 = 224$ $6M\ {}^8C_6 = 28$</p> <p>Total $= 672$</p>	<p>B1</p> <p>[1]</p> <p>B1</p> <p>[1]</p> <p>B1</p> <p>[1]</p> <p>B1</p> <p>[1]</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>[3]</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>M1 for 3 terms, at least 2 of which must be correct in terms of C notation or evaluated.</p> <p>A1 for any pair (must be evaluated) A1 for final answer</p> <p>M1 for 3 terms, at least 2 of which must be correct in terms of C notation or evaluated. A1 for any pair (must be evaluated)</p> <p>A1 for final answer</p>
<p>8 (i)</p>  <p>(ii) $\left(-\frac{1}{2}, \frac{25}{4}\right)$</p> <p>(iii) $k > \frac{25}{4}$ or $\frac{25}{4} < k \leq 14$</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p> <p>[4]</p> <p>B1, B1</p> <p>[2]</p> <p>B1</p> <p>[1]</p>	<p>B1 for correct shape</p> <p>B1 for $(-3, 0)$ or -3 seen on graph</p> <p>B1 for $(2, 0)$ or 2 seen on graph</p> <p>B1 for $(0, 6)$ or 6 seen on graph or in a table</p> <p>B1 for each</p>

Page 7	Mark Scheme	Syllabus	Paper
	IGCSE – October/November 2013	0606	11

<p>9 (a) $12x^2 \ln(2x+1) + 4x^3 \left(\frac{2}{2x+1} \right)$</p>	<p>M1 A2, 1, 0 [3]</p>	<p>M1 for differentiation of a correct product –1 for each error</p>
<p>(b) (i) $\frac{dy}{dx} = \frac{(x+2)^{\frac{1}{2}} 2 - 2x(x+2)^{-\frac{1}{2}} \frac{1}{2}}{x+2}$</p> <p>$= \frac{(x+2)^{\frac{1}{2}}}{(x+2)} (2(x+2) - x)$</p> <p>$= \frac{x+4}{(x+2)^{\frac{3}{2}}}$</p> <p>Or:</p> <p>$\frac{dy}{dx} = 2x \left(-\frac{1}{2} \right) (x+2)^{-\frac{3}{2}} + (x+2)^{-\frac{1}{2}} (2)$</p> <p>$= (x+2)^{-\frac{3}{2}} (2(x+2) - x)$</p> <p>$= \frac{x+4}{(x+2)^{\frac{3}{2}}}$</p>	<p>M1, A1</p> <p>DM1</p> <p>A1 [4]</p>	<p>M1 for differentiation of a quotient involving $(x+2)^{\frac{1}{2}}$</p> <p>A1 all correct unsimplified DM1 for attempt to simplify</p> <p>A1 for correct simplification to obtain the given answer</p>
<p>(ii) $\frac{10x}{\sqrt{x+2}} (+c)$</p>	<p>M1, A1 [2]</p>	<p>M1 for $\frac{1}{5} \times \frac{2x}{\sqrt{x+2}}$ or $5 \times \frac{2x}{\sqrt{x+2}}$ A1 correct only, allow unsimplified. Condone omission of + c</p>
<p>(iii) $\left[\frac{10x}{\sqrt{x+2}} \right]_2^7 = \frac{70}{3} - \frac{20}{2}$</p> <p>$= \frac{40}{3}$</p>	<p>M1</p> <p>A1 [2]</p>	<p>M1 for correct application of limits in their answer to (b)(ii)</p>

Page 8	Mark Scheme	Syllabus	Paper
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<p>10 (i) $\sqrt{20}$ or 4.47</p> <p>(ii) Grad $AB = \frac{1}{2}$, \perp grad $= -2$ \perp line $y - 4 = -2(x - 1)$ $(y = -2x + 6)$</p> <p>(iii) Coords of $C(x, y)$ and $BC^2 = 20$ $(x - 1)^2 + (y - 4)^2 = 20$ or Coords of $C(x, y)$ and $AC^2 = 40$ $(x + 3)^2 + (y - 2)^2 = 40$</p> <p>Need intersection with $y = -2x + 6$,</p> <p>leads to $5x^2 - 10x - 15 = 0$ or $5y^2 - 40y - 15 = 0$</p> <p>giving $x = 3, -1$ and $y = 0, 8$</p> <p>Or, using vector approach: $\overrightarrow{AB} = \begin{pmatrix} 4 \\ 2 \end{pmatrix}$ $\overrightarrow{OC} = \begin{pmatrix} 1 \\ 4 \end{pmatrix} + \begin{pmatrix} -2 \\ 4 \end{pmatrix} = \begin{pmatrix} -1 \\ 8 \end{pmatrix}$ $\overrightarrow{OC} = \begin{pmatrix} 1 \\ 4 \end{pmatrix} + \begin{pmatrix} 2 \\ -4 \end{pmatrix} = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$</p>	<p>B1 [1]</p> <p>M1</p> <p>M1, A1</p> <p>[3]</p> <p>M1</p> <p>A1</p> <p>DM1</p> <p>DM1 A1, A1 [6]</p> <p>B1</p> <p>M1 A1, A1</p> <p>A1, A1</p>	<p>M1 for attempt at a perp gradient</p> <p>M1 for attempt at straight line equation, must be perpendicular and passing through B. A1 allow unsimplified</p> <p>M1 for attempt to obtain relationship using an appropriate length and the point (1, 4) or (-3, 2) A1 for a correct equation</p> <p>DM1 for attempt to solve with $y = -2x + 6$ and obtain a quadratic equation in terms of one variable only</p> <p>M1 for attempt to solve quadratic A1 for each 'pair'</p> <p>May be implied</p> <p>M1 for correct approach A1 for each element correct</p> <p>A1 for each element correct</p>
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Page 9	Mark Scheme	Syllabus	Paper
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<p>11 (a) (i) $\begin{pmatrix} 4 & 3 \\ 4 & 3 \end{pmatrix}$</p> <p>(ii) $\mathbf{A}^2 = \begin{pmatrix} 16 & 9 \\ 12 & 13 \end{pmatrix}$</p> <p>(iii) \mathbf{B} is the inverse matrix of \mathbf{A}^2 $= \frac{1}{100} \begin{pmatrix} 13 & -9 \\ -12 & 16 \end{pmatrix}$</p> <p>(b) $\det \mathbf{C} = x(x-1) - (-1)(x^2 - x + 1)$ $= 2x^2 - 2x + 1$</p> <p>$b^2 - 4ac < 0, 4 - 8 < 0$</p> <p>No real solutions (so $\det \mathbf{C} \neq 0$)</p>	<p>B1 [1]</p> <p>B1, B1 [2]</p> <p>B1, B1 [2]</p> <p>M1 A1</p> <p>DM1</p> <p>A1 [4]</p>	<p>B1 for any 2 correct elements B1 for all correct</p> <p>Follow through on their \mathbf{A}^2</p> <p>M1 for attempt to obtain $\det \mathbf{C}$ A1 for this correct quadratic expression from a correct $\det \mathbf{C}$</p> <p>DM1 for use of discriminant or attempt to solve using the formula, or attempt to complete the square in order to show there are no real roots.</p> <p>A1 for correct reasoning or statement that there are no real roots.</p>
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Page 10	Mark Scheme	Syllabus	Paper
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12	(a) (i)	$f(-10) = 299, f(8) = 191$ Min point at $(0, -1)$ or when $y = -1$	M1 B1	M1 for substitution of either $x = -10$ or $x = 8$, may be seen on diagram B1 May be implied from final answer, may be seen on diagram Must have \leq for A1, do not allow x
		\therefore range $-1 \leq y \leq 299$	A1	
			[3]	
	(ii)	$x \geq 0$ or equivalent	B1	Allow any domain which will make f a one-one function Assume upper and lower bound when necessary.
			[1]	
	(b) (i)	$g^{-1}(x) = \ln\left(\frac{x+2}{4}\right)$	M1	M1 for complete method to find the form inverse function, must involve \ln or \lg if appropriate. May still be in terms of y .
		or $\frac{\lg\left(\frac{x+2}{4}\right)}{\lg e}$	A1	
			[2]	
	(ii)	$gh(x) = g(\ln 5x)$ $= 4e^{\ln 5x} - 2$	M1 A1	M1 for correct order A1 for correct expression $4e^{\ln 5x} - 2$
		$20x - 2 = 18, x = 1$	A1	
			[3]	
	Or	$h(x) = g^{-1}(18)$ $\ln 5x = \ln 5$	M1 A1	M1 for correct order A1 for correct equation
		leading to $x = 1$	A1	

MARK SCHEME for the October/November 2013 series

0606 ADDITIONAL MATHEMATICS

0606/12

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Page 3	Mark Scheme	Syllabus	Paper
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1	$a = 3, b = 2, c = 1$	B1, B1, B1 [3]	B1 for each
2	<p>Using $b^2 - 4ac, 9 = 4(k + 1)^2$ $4k^2 + 8k - 5 = 0$</p> $k = -\frac{5}{2}, \left(\frac{1}{2}\right)$ <p>To be below the x-axis $k < -\frac{5}{2}$</p> <p>Or: $\frac{dy}{dx} = 2(k + 1)x - 3$ when $\frac{dy}{dx} = 0, x = \frac{3}{2(k + 1)}$ $\therefore y = (k + 1)\frac{9}{4(k + 1)^2} - \frac{9}{2(k + 1)} + (k + 1)$ To lie under the x-axis, $y < 0$ $\therefore (k + 1)\frac{9}{4(k + 1)^2} - \frac{9}{2(k + 1)} + (k + 1) < 0$ leading to $9 = 4(k + 1)^2$ or equivalent then as for previous method</p>	<p>M1 DM1</p> <p>A1</p> <p>A1 [4]</p> <p>M1</p>	<p>M1 for any use of $b^2 - 4ac$ DM1 for solution of their quadratic in k</p> <p>A1 for critical value(s), $\frac{1}{2}$ not necessary</p> <p>A1 for $k < -\frac{5}{2}$ only</p> <p>M1 for a complete method to this point.</p>

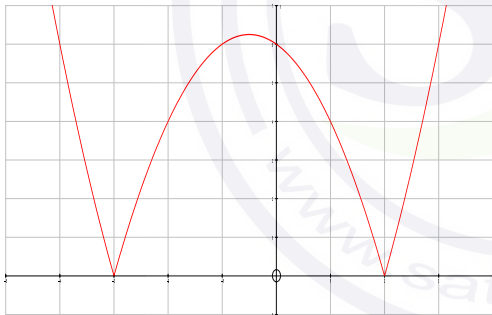
Page 4	Mark Scheme	Syllabus	Paper
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<p>3</p> $\frac{1 + \sin \theta}{\cos \theta} + \frac{\cos \theta}{1 + \sin \theta} + \frac{(1 + \sin \theta)^2 + \cos^2 \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{1 + 2 \sin \theta + \sin^2 \theta + \cos^2 \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{2 + 2 \sin \theta}{\cos \theta(1 + \sin \theta)}$ $= \frac{2(1 + \sin \theta)}{\cos \theta(1 + \sin \theta)}$ $= 2 \sec \theta$ <p>Alternative solution:</p> $\sec \theta + \tan \theta + \frac{1}{\sec \theta + \tan \theta}$ $= \frac{(\sec \theta + \tan \theta)^2 + 1}{\sec \theta + \tan \theta}$ $= \frac{\sec^2 \theta + 2 \sec \theta \tan \theta + \tan^2 \theta + 1}{\sec \theta + \tan \theta}$ $= \frac{2 \sec^2 \theta + 2 \sec \theta \tan \theta}{\sec \theta + \tan \theta}$ $= \frac{2 \sec \theta (\sec \theta + \tan \theta)}{\sec \theta + \tan \theta}$ $= 2 \sec \theta$	<p>M1</p> <p>DM1</p> <p>DM1</p> <p>A1</p> <p>[4]</p> <p>M1</p> <p>DM1</p> <p>DM1</p> <p>A1</p>	<p>M1 for dealing with the fractions, denominator must be correct, be generous with numerator</p> <p>M1 for expansion and use of $\cos^2 \theta + \sin^2 \theta = 1$</p> <p>M1 for attempt to factorise</p> <p>A1 for obtaining final answer correctly</p> <p>M1 for dealing with the fractions</p> <p>M1 for expansion and use of $\tan^2 \theta + 1 = \sec^2 \theta$</p> <p>DM1 for attempt to factorise</p> <p>A1 for obtaining final answer correctly</p>
<p>4 (i) $n(A) = 3$</p> <p>(ii) $n(B) = 4$</p> <p>(iii) $A \cup B = \{60^\circ, 240^\circ, 300^\circ, 420^\circ, 600^\circ\}$</p> <p>(iv) $A \cap B = \{60^\circ, 420^\circ\}$</p>	<p>B1</p> <p>[1]</p> <p>B1</p> <p>[1]</p> <p>√B1</p> <p>[1]</p> <p>√B1</p> <p>[1]</p>	<p>If elements listed for (i), then they must be correct elements to get B1 leading to $n(A) = 3$. If they are not listed and correct answer given then B1.</p> <p>If elements listed for (ii), then they must be correct elements leading to $n(B) = 4$ to get B1. If they are not listed and correct answer given then B1.</p> <p>Follow through on any sets listed in (i) and (ii). Do not allow any repetitions.</p> <p>Follow through on any sets listed in (i) and (ii).</p>

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<p>5 (i) $9x - \frac{1}{3}\cos 3x (+c)$</p> <p>(ii) $\left[9x - \frac{1}{3}\cos 3x\right]_{\frac{\pi}{9}}^{\pi}$ $= \left(9\pi - \frac{1}{3}\cos 3\pi\right) - \left(\pi - \frac{1}{3}\cos \frac{\pi}{3}\right)$ $= 8\pi + \frac{1}{2}$</p>	<p>B1, B1, B1 [3]</p> <p>M1</p> <p>A1, A1 [3]</p>	<p>B1 for $9x$, B1 for $\frac{1}{3}$ or $\cos 3x$</p> <p>B1 for $-\frac{1}{3}\cos 3x$</p> <p>Condone omission of $+c$</p> <p>M1 for correct use of limits in their answer to (i)</p> <p>A1 for each term</p>
<p>6 $f\left(\frac{1}{2}\right) = \frac{a}{8} + 1 + \frac{b}{2} - 2$</p> <p>leading to $a + 4b - 8 = 0$</p> <p>$f(2) = 2f(-1)$</p> <p>$8a + 16 + 2b - 2 = 2(-a + 4 - b - 2)$</p> <p>leading to $10a + 4b + 10 = 0$ or equivalent</p> <p>$\therefore a = -2, b = \frac{5}{2}$</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>DM1 A1 [6]</p>	<p>M1 for substitution of $x = \frac{1}{2}$ into $f(x)$</p> <p>A1 for correct equation in any form</p> <p>M1 for attempt to substitute $x = 2$ or $x = -1$ into $f(x)$ and use $f(2) = \pm 2f(-1)$ or $2f(2) = \pm f(-1)$</p> <p>A1 for a correct equation in any form</p> <p>DM1 (on both previous M marks) for attempt to solve simultaneous equations to obtain either a or b</p> <p>A1 for both correct</p>

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<p>7 (a) (i) 360</p> <p>(ii) 120</p> <p>(b) (i) 924</p> <p>(ii) 28</p> <p>(iii) $924 - ({}^8C_3 \times {}^4C_3) - ({}^8C_2 \times {}^4C_4)$ (i.e. $924 - 3M\ 3W - 2M\ 4W$)</p> <p>$924 - 224 - 28$ $= 672$</p> <p>Or: $4M\ 2W\ {}^8C_4 \times {}^4C_2 = 420$ $5M\ 1W\ {}^8C_5 \times {}^4C_1 = 224$ $6M\ {}^8C_6 = 28$</p> <p>Total $= 672$</p>	<p>B1 [1]</p> <p>B1 [1]</p> <p>B1 [1]</p> <p>B1 [1]</p> <p>M1</p> <p>A1 A1 [3]</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>M1 for 3 terms, at least 2 of which must be correct in terms of C notation or evaluated.</p> <p>A1 for any pair (must be evaluated) A1 for final answer</p> <p>M1 for 3 terms, at least 2 of which must be correct in terms of C notation or evaluated. A1 for any pair (must be evaluated)</p> <p>A1 for final answer</p>
<p>8 (i)</p>  <p>(ii) $\left(-\frac{1}{2}, \frac{25}{4}\right)$</p> <p>(iii) $k > \frac{25}{4}$ or $\frac{25}{4} < k \leq 14$</p>	<p>B1 B1 B1 B1 [4]</p> <p>B1, B1 [2]</p> <p>B1 [1]</p>	<p>B1 for correct shape</p> <p>B1 for $(-3, 0)$ or -3 seen on graph</p> <p>B1 for $(2, 0)$ or 2 seen on graph</p> <p>B1 for $(0, 6)$ or 6 seen on graph or in a table</p> <p>B1 for each</p>

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<p>9 (a) $12x^2 \ln(2x+1) + 4x^3 \left(\frac{2}{2x+1} \right)$</p>	<p>M1 A2, 1, 0 [3]</p>	<p>M1 for differentiation of a correct product –1 for each error</p>
<p>(b) (i) $\frac{dy}{dx} = \frac{(x+2)^{\frac{1}{2}} 2 - 2x(x+2)^{-\frac{1}{2}} \frac{1}{2}}{x+2}$</p> <p>$= \frac{(x+2)^{\frac{1}{2}}}{(x+2)} (2(x+2) - x)$</p> <p>$= \frac{x+4}{(x+2)^{\frac{3}{2}}}$</p> <p>Or:</p> <p>$\frac{dy}{dx} = 2x \left(-\frac{1}{2} \right) (x+2)^{-\frac{3}{2}} + (x+2)^{-\frac{1}{2}} (2)$</p> <p>$= (x+2)^{-\frac{3}{2}} (2(x+2) - x)$</p> <p>$= \frac{x+4}{(x+2)^{\frac{3}{2}}}$</p>	<p>M1, A1</p> <p>DM1</p> <p>A1 [4]</p>	<p>M1 for differentiation of a quotient involving $(x+2)^{\frac{1}{2}}$</p> <p>A1 all correct unsimplified DM1 for attempt to simplify</p> <p>A1 for correct simplification to obtain the given answer</p>
<p>(ii) $\frac{10x}{\sqrt{x+2}} (+c)$</p>	<p>M1, A1 [2]</p>	<p>M1 for $\frac{1}{5} \times \frac{2x}{\sqrt{x+2}}$ or $5 \times \frac{2x}{\sqrt{x+2}}$ A1 correct only, allow unsimplified. Condone omission of + c</p>
<p>(iii) $\left[\frac{10x}{\sqrt{x+2}} \right]_2^7 = \frac{70}{3} - \frac{20}{2}$</p> <p>$= \frac{40}{3}$</p>	<p>M1</p> <p>A1 [2]</p>	<p>M1 for correct application of limits in their answer to (b)(ii)</p>

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<p>10 (i) $\sqrt{20}$ or 4.47</p> <p>(ii) Grad $AB = \frac{1}{2}$, \perp grad $= -2$ \perp line $y - 4 = -2(x - 1)$ $(y = -2x + 6)$</p> <p>(iii) Coords of $C(x, y)$ and $BC^2 = 20$ $(x - 1)^2 + (y - 4)^2 = 20$ or Coords of $C(x, y)$ and $AC^2 = 40$ $(x + 3)^2 + (y - 2)^2 = 40$</p> <p>Need intersection with $y = -2x + 6$,</p> <p>leads to $5x^2 - 10x - 15 = 0$ or $5y^2 - 40y - 15 = 0$</p> <p>giving $x = 3, -1$ and $y = 0, 8$</p> <p>Or, using vector approach: $\overrightarrow{AB} = \begin{pmatrix} 4 \\ 2 \end{pmatrix}$ $\overrightarrow{OC} = \begin{pmatrix} 1 \\ 4 \end{pmatrix} + \begin{pmatrix} -2 \\ 4 \end{pmatrix} = \begin{pmatrix} -1 \\ 8 \end{pmatrix}$ $\overrightarrow{OC} = \begin{pmatrix} 1 \\ 4 \end{pmatrix} + \begin{pmatrix} 2 \\ -4 \end{pmatrix} = \begin{pmatrix} 3 \\ 0 \end{pmatrix}$</p>	<p>B1 [1]</p> <p>M1</p> <p>M1, A1</p> <p>[3]</p> <p>M1</p> <p>A1</p> <p>DM1</p> <p>DM1 A1, A1 [6]</p> <p>B1</p> <p>M1 A1, A1</p> <p>A1, A1</p>	<p>M1 for attempt at a perp gradient</p> <p>M1 for attempt at straight line equation, must be perpendicular and passing through B. A1 allow unsimplified</p> <p>M1 for attempt to obtain relationship using an appropriate length and the point (1, 4) or (-3, 2) A1 for a correct equation</p> <p>DM1 for attempt to solve with $y = -2x + 6$ and obtain a quadratic equation in terms of one variable only</p> <p>M1 for attempt to solve quadratic A1 for each 'pair'</p> <p>May be implied</p> <p>M1 for correct approach A1 for each element correct</p> <p>A1 for each element correct</p>
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<p>11 (a) (i) $\begin{pmatrix} 4 & 3 \\ 4 & 3 \end{pmatrix}$</p> <p>(ii) $\mathbf{A}^2 = \begin{pmatrix} 16 & 9 \\ 12 & 13 \end{pmatrix}$</p> <p>(iii) \mathbf{B} is the inverse matrix of \mathbf{A}^2 $= \frac{1}{100} \begin{pmatrix} 13 & -9 \\ -12 & 16 \end{pmatrix}$</p> <p>(b) $\det \mathbf{C} = x(x-1) - (-1)(x^2 - x + 1)$ $= 2x^2 - 2x + 1$</p> <p>$b^2 - 4ac < 0, 4 - 8 < 0$</p> <p>No real solutions (so $\det \mathbf{C} \neq 0$)</p>	<p>B1 [1]</p> <p>B1, B1 [2]</p> <p>B1, B1 [2]</p> <p>M1 A1</p> <p>DM1</p> <p>A1 [4]</p>	<p>B1 for any 2 correct elements B1 for all correct</p> <p>Follow through on their \mathbf{A}^2</p> <p>M1 for attempt to obtain $\det \mathbf{C}$ A1 for this correct quadratic expression from a correct $\det \mathbf{C}$</p> <p>DM1 for use of discriminant or attempt to solve using the formula, or attempt to complete the square in order to show there are no real roots.</p> <p>A1 for correct reasoning or statement that there are no real roots.</p>
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12	(a) (i)	$f(-10) = 299, f(8) = 191$ Min point at $(0, -1)$ or when $y = -1$	M1 B1	M1 for substitution of either $x = -10$ or $x = 8$, may be seen on diagram B1 May be implied from final answer, may be seen on diagram Must have \leq for A1, do not allow x
		\therefore range $-1 \leq y \leq 299$	A1	
			[3]	
	(ii)	$x \geq 0$ or equivalent	B1	Allow any domain which will make f a one-one function Assume upper and lower bound when necessary.
			[1]	
	(b) (i)	$g^{-1}(x) = \ln\left(\frac{x+2}{4}\right)$	M1	M1 for complete method to find the form inverse function, must involve \ln or \lg if appropriate. May still be in terms of y .
		or $\frac{\lg\left(\frac{x+2}{4}\right)}{\lg e}$	A1	
			[2]	
	(ii)	$gh(x) = g(\ln 5x)$ $= 4e^{\ln 5x} - 2$	M1 A1	M1 for correct order A1 for correct expression $4e^{\ln 5x} - 2$
		$20x - 2 = 18, x = 1$	A1	
			[3]	
	Or	$h(x) = g^{-1}(18)$ $\ln 5x = \ln 5$	M1 A1	M1 for correct order A1 for correct equation
		leading to $x = 1$	A1	

MARK SCHEME for the October/November 2013 series

0606 ADDITIONAL MATHEMATICS

0606/13

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.

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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Accuracy mark for a correct result or statement independent of method marks.

When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.

The symbol \checkmark implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously “correct” answers or results obtained from incorrect working.

Note: B2 or A2 means that the candidate can earn 2 or 0.
B2, 1, 0 means that the candidate can earn anything from 0 to 2.

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<p>1 (i) ${}^6C_2 (2^4) (px)^2$ or $\binom{6}{2} 2^4 (px)^2$</p> $240p^2 = 60$ $p = \frac{1}{2}$ <p>(ii) coefficients of the terms needed</p> $(-1) {}^6C_1 (2)^5 p + (3 \times 60)$ $= 84$	<p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p> <p>M1</p> <p>B1</p> <p>A1</p> <p>[3]</p>	<p>Seen or implied, unsimplified</p> <p>M1 for their coefficient of $x^2 = 60$ and attempt to solve</p> <p>M1 for realising that 2 terms are involved</p> <p>B1 for $(-1) {}^6C_1 (2)^5 p$ or $-192p$, using their p.</p>
<p>2 $\lg \frac{y^2}{5y+60} = \lg 10$</p> <p>Or $\lg y^2 = \lg 10 (5y+60)$</p> $y^2 - 50y - 600 = 0$ <p>leading to $y = -10, 60$</p> <p>y must be positive so $y = 60$</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>DM1</p> <p>A1</p> <p>[5]</p>	<p>B1 for $2 \lg y = \lg y^2$</p> <p>B1 for $1 = \lg 10$ or equivalent, allow when seen</p> <p>M1 for use of $\log A - \log B = \log A/B$ or $\log A + \log B = \log AB$</p> <p>DM1 for forming a 3 term quadratic equation and an attempt to solve</p> <p>A1 for $y = 60$ only</p>

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<p>4 (i) $\frac{dy}{dx} = \frac{(x+3)^2 2e^{2x} - e^{2x} 2(x+3)}{(x+3)^4}$</p> $= \frac{2e^{2x}(x+2)}{(x+3)^3}, A = 2$ <p>Alt solution</p> $\frac{dy}{dx} = e^{2x} (-2(x+3)^{-3}) + 2e^{2x}(x+3)^{-2}$ $= \frac{2e^{2x}(x+2)}{(x+3)^3}, A = 2$ <p>(ii) $x = -2, y = e^{-4}$</p>	<p>M1</p> <p>A2, 1, 0</p> <p>A1</p> <p>[4]</p> <p>M1</p> <p>A2,1,0</p> <p>A1</p> <p>B1, B1</p> <p>[2]</p>	<p>M1 for attempt at quotient rule</p> <p>–1 for each error</p> <p>Must be convinced of correct simplification e.g. sight of $(x+3-1)$ or $(x+2)(x+3)$</p> <p>M1 for attempt at product rule</p> <p>–1 for each error</p> <p>Must be convinced of correct simplification e.g. sight of $(x+3-1)$ or $(x+2)(x+3)$</p> <p>Accept $1/e^4$</p>
<p>5 (i) $f^2(x) = f(2x^3)$</p> $= 2(2x^3)^3 \text{ or } 2\left(2\left(\frac{1}{2}\right)^3\right)^3$ $= 2^{-5}$ <p>Alt method</p> $f\left(\frac{1}{2}\right) = \frac{1}{4} \quad f\left(\frac{1}{4}\right) = 2^{-5}$ <p>(ii) $f'(x) = g'(x)$</p> $6x^2 = 4 - 10x$ <p>Leading to $(3x-1)(x+2) = 0$</p> $x = \frac{1}{3}, -2$	<p>M1</p> <p>A1</p> <p>[2]</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>[4]</p>	<p>M1 for $= 2(2x^3)^3$ or $2\left(2\left(\frac{1}{2}\right)^3\right)^3$</p> <p>For 2^{-5} only</p> <p>M1 for f of their $f\left(\frac{1}{2}\right)$</p> <p>For 2^{-5} only</p> <p>B1 for $6x^2$</p> <p>B1 for $4 - 10x$</p> <p>M1 for solution of quadratic equation obtained from differentiation of both</p> <p>A1 for both</p>

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<p>6 Area under the curve:</p> $\int_0^{\sqrt{2}} 4 - x^2 \, dx = \left[4x - \frac{x^3}{3} \right]_0^{\sqrt{2}}$ $= \left(4\sqrt{2} - \frac{2\sqrt{2}}{3} \right) - (0)$ $= \frac{10\sqrt{2}}{3}$ <p>Area of trapezium =</p> $\frac{1}{2}(4 + 2)(\sqrt{2}) = 3\sqrt{2}$ <p>Shaded area = $\frac{10\sqrt{2}}{3} - 3\sqrt{2}$</p> <p>Shaded area = $\frac{\sqrt{2}}{3}$</p> <p>Or: Equation of chord:</p> $y = 4 - \sqrt{2}x$ <p>Shaded area = $\int_0^{\sqrt{2}} 4 - x^2 - 4 + \sqrt{2}x \, dx$</p> $\left[\frac{\sqrt{2}}{2}x^2 - \frac{x^3}{3} \right]_0^{\sqrt{2}} = \frac{\sqrt{2}}{3}$	<p>M1 A1</p> <p>DM1</p> <p>B1 M1 A1 [6]</p> <p>B1</p> <p>M1 M1</p> <p>√A1 DM1 A1 [6]</p>	<p>M1 for attempt to integrate</p> <p>DM1 for application of limits</p> <p>B1 for area of trapezium, allow unsimplified</p> <p>M1 for subtraction of the two areas</p> <p>Must be in this form</p> <p>B1 for the equation of the chord unsimplified</p> <p>M1 for subtraction M1 for attempt to integrate</p> <p>√A1 for $\left[-m \frac{x^2}{2} - \frac{x^3}{3} \right]$ or equivalent, where m is the gradient of their chord DM1 for application of limits</p>
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<p>7 (i) $2t^2 - 2(t^2 - t + 1)$</p> <p>Leading to, $t = \frac{3}{2}$</p> <p>(ii) $A = \begin{pmatrix} 6 & 2 \\ 7 & 3 \end{pmatrix}, A^{-1} = \frac{1}{4} \begin{pmatrix} 3 & -2 \\ -7 & 6 \end{pmatrix}$</p> <p>$\begin{pmatrix} 6 & 2 \\ 7 & 3 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 10 \\ 11 \end{pmatrix}$</p> <p>$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{4} \begin{pmatrix} 3 & -2 \\ -7 & 6 \end{pmatrix} \begin{pmatrix} 10 \\ 11 \end{pmatrix}$</p> <p>$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$, leading to $x = 2, y = -1$</p>	<p>B1</p> <p>M1 A1 [3]</p> <p>B1, B1</p> <p>B1</p> <p>M1</p> <p>A1 [5]</p>	<p>Correct determinant seen unsimplified</p> <p>M1 for simplification and solution A1 for solution of $\det A=1$ only, not $1/\det A=1$</p> <p>B1 for $\frac{1}{4}$, B1 for matrix</p> <p>B1 for dealing correctly with the factor of 2</p> <p>M1 for pre-multiplying their $\begin{pmatrix} 10 \\ 11 \end{pmatrix}$ by their A^{-1} to obtain a column matrix</p> <p>Allow $\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 2 \\ -1 \end{pmatrix}$ for A1</p>
<p>8 (i) $\frac{1}{2}(4^2)\sin\theta = 7.5$</p> <p>$\sin\theta = \frac{15}{16}, \theta = 1.215\dots$</p> <p>(ii) $\sin\frac{\theta}{2} = \frac{\frac{1}{2}CD}{4}, (CD = 4.567)$</p> <p>Arc length = $6(1.215)$</p> <p>Perimeter = $2 + 2 + 6(1.215) + \text{their } CD$</p> <p>= awrt 15.9</p> <p>(iii) Area = $\frac{1}{2}6^2(1.215) - 7.5$</p> <p>= 14.4 (awrt)</p>	<p>M1</p> <p>A1 [2]</p> <p>M1</p> <p>B1</p> <p>M1</p> <p>A1 [4]</p> <p>B1 M1</p> <p>A1 [3]</p>	<p>M1 for attempt to find the area of the triangle and equate to 7.5</p> <p>A1 for solution to obtain the given answer Solution must include 1.2153.... or 1.2154</p> <p>M1 for attempt to find CD</p> <p>B1 for arc length</p> <p>M1 for sum of 4 appropriate lengths</p> <p>B1 for sector area M1 for subtraction of the 2 areas</p>

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<p>9 (a) (i) $6(1 - \cos^2 x) = 5 + \cos x$ $6 \cos^2 x + \cos x - 1 = 0$ $(3 \cos x - 1)(2 \cos x + 1) = 0$</p> <p>$x = 70.5^\circ \quad x = 120^\circ$</p> <p>(ii) $\cos x = \sin y$</p> <p>$\sin y = \frac{1}{3}$ only so $y = 19.5^\circ, 160.5^\circ$</p> <p>(b) $\cot z (4 \cot z - 3) = 0$</p> <p>$\cot z = 0, \quad z = \frac{\pi}{2}$</p> <p>$\cot z = \frac{3}{4}, \tan z = \frac{4}{3}$ so $z = 0.927$</p>	<p>M1 M1</p> <p>A1, A1 [4]</p> <p>DM1 $\sqrt{A1}, \sqrt{A1}$ [3]</p> <p>M1</p> <p>B1</p> <p>M1 A1 [4]</p>	<p>M1 for use of $\sin^2 x = (1 - \cos^2 x)$ correctly M1 for solution of a 3 term quadratic in \cos and attempt at solution of a trig equation</p> <p>A1 for each correct solution</p> <p>DM1 for relating $\cos x$ and $\sin y$ or other correct method of solution</p> <p>M1 for attempt to use a factor</p> <p>B1 for $\frac{\pi}{2}$ (1.57)</p> <p>M1 dealing with \cot and attempt at solution</p>										
<p>10 (i) $\lg s$</p> <p>(ii)</p> <table border="1"><tr><td>$\lg s$</td><td>0.3</td><td>0.6</td><td>0.78</td><td>0.9</td></tr><tr><td>$\lg t$</td><td>1.4</td><td>0.8</td><td>0.44</td><td>0.19</td></tr></table> <p>(iii) <u>No marks in this part unless $\lg t$ v $\lg s$ graph is used</u> Gradient : $n = -2$ (allow $-2.1 \rightarrow -1.9$)</p> <p>Intercept : $\log k$, or other method $k = 100$ (allow $90 \rightarrow 120$)</p> <p>Alt method Using simultaneous equations, points used must lie on the plotted line.</p> <p>(iv) When $t = 4$, $\lg t = 0.6$ so $\lg s = 0.69$ $s = 4.9$ (allow $4.8 \rightarrow 5.2$)</p>	$\lg s$	0.3	0.6	0.78	0.9	$\lg t$	1.4	0.8	0.44	0.19	<p>B1 [1]</p> <p>M1 DM1 A1 [3]</p> <p>M1A1</p> <p>M1, A1 [4]</p> <p>M2 A1, A1</p> <p>M1 A1 [2]</p>	<p>Allow in table or on graph if no contradiction</p> <p><u>No marks for graph unless $\lg t$ against $\lg s$ (or $\ln t$ against $\ln s$)</u></p> <p>M1 for 3 or more points correct DM1 for a line through 3 or 4 correct points A1 all points correct with a straight line extending at least from first point to last point</p> <p>M1 calculates gradient A1 for $n = -2$</p> <p>M1 for use of intercept and dealing with logarithm correctly (can use another point)</p> <p>Must attempt to solve 2 valid equations. $k = 100$ and $n = -2$</p> <p>M1 for valid method using either the correct graph or using $\lg t = n \lg s + \lg k$ or $t = ks^n$ using their n and their k</p>
$\lg s$	0.3	0.6	0.78	0.9								
$\lg t$	1.4	0.8	0.44	0.19								

Page 9	Mark Scheme	Syllabus	Paper
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<p>11 (i) $\left[e^{2x} + \frac{5}{4}e^{-2x} \right]_0^k$</p> <p>$\left(e^{2k} + \frac{5}{4}e^{-2k} \right) - \left(1 + \frac{5}{4} \right) = 3$</p> <p>$e^{2k} + \frac{5}{4}e^{-2k} - \frac{12}{4} = 0$</p> <p>$4e^{4k} - 12e^{2k} + 5 = 0$</p> <p>(ii) $4y^2 - 12y + 5 = 0$</p> <p>leading to $e^{2k} = \frac{5}{2}, e^{-2k} = \frac{1}{2}$</p> <p>$k = 0.458, -0.347$</p>	<p>B1, B1</p> <p>M1</p> <p>M1</p> <p>A1 [5]</p> <p>M1</p> <p>M1</p> <p>A1, A1 [4]</p>	<p>B1 for each term integrated correctly, allow unsimplified</p> <p>M1 for application of limits to an integral of the form $Ae^{2x} \pm Be^{-2x}$</p> <p>M1 for equating to $\frac{3}{4}$ and attempt to rearrange to obtain a 3 term equation. Must be using an integral of the form $Ae^{2x} \pm Be^{-2x}$</p> <p>Answer given, so must be convinced</p> <p>M1 for solution of quadratic equation</p> <p>M1 for solving equations involving exponentials</p> <p>A1 for each</p>
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MARK SCHEME for the May/June 2013 series

0606 ADDITIONAL MATHEMATICS

0606/11

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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Page 2	Mark Scheme	Syllabus	Paper
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Mark Scheme Notes

Marks are of the following three types:

M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.

A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

B Accuracy mark for a correct result or statement independent of method marks.

- When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol \checkmark implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously “correct” answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
B2, 1, 0 means that the candidate can earn anything from 0 to 2.

Page 3	Mark Scheme	Syllabus	Paper
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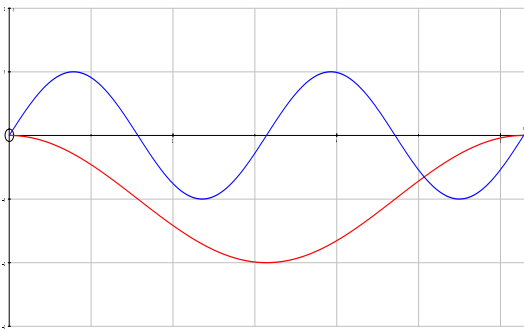
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ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)

Penalties

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S –1	Occasionally used for persistent slackness – usually discussed at a meeting.
EX –1	Applied to A or B marks when extra solutions are offered to a particular equation. Again, this is usually discussed at the meeting.

Page 4	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2013	0606	11

1	(i)		B1	correct shape for $y = \cos x - 1$
	(ii)		B1	all correct
	(iii)	3	B1	correct shape for $y = \sin 2x$ all correct
2	Either gradient = 1 intercept = 2 $\ln b = \text{gradient}$ or $\ln A = \text{intercept}$ $b = e$ or 2.72 $A = e^2, A = 7.39$		B1	
	Or $e^4 = Ab^2$ and $e^{10} = Ab^8$		B1	
	leading to $b^6 = e^6$ or $e^4 = e^2 A$ or $e^{10} = e^8 A$		M1	M1, need to equate either gradient to $\ln b$ or intercept to $\ln A$
	$b = e$ or 2.72		A1	
	$A = e^2, A = 7.39$		A1	
	Or $10 = 8 \ln b + \ln A$		[B1 B1	B1 for each equation
	$4 = 2 \ln b + \ln A$		M1	M1 for attempt to solve for either A or b
	leading to $\ln b = 1$ or $6 = 3 \ln A$		A1	
	$b = e$ or 2.72		A1]	
	$A = e^2, A = 7.39$		[B1	
			B1	
			M1	M1 for attempt to solve for either A or b
			A1	
		A1]		

Page 5	Mark Scheme	Syllabus	Paper
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3	(i)	${}^{14}C_6 = 3003$	B1	
	(ii)	${}^5C_3 \times {}^9C_3 = 840$	M1 A1	M1 for product of 2 combinations
	(iii)	<p>Either $3003 - {}^9C_6 = 2919$</p> <p>Or</p> <p>1M + 5W: $5 \times {}^9C_5 = 630$ 2M + 4W: ${}^5C_2 \times {}^9C_4 = 1260$ 3M + 3W: 840 (part (ii)) 4M + 2W: ${}^5C_4 \times {}^9C_2 = 180$ 5M + 1W: $1 \times {}^9C_1 = 9$ Total: 2919</p>	<p>M1 B1 A1</p> <p>[B2 1 0</p> <p>B1]</p>	<p>M1 for 3003 – number of committees containing no men B1 for 9C_6</p> <p>–1 each error</p> <p>B1 for correct final answer</p>
4	(i)	2	B1	
	(ii)	$\log_4 y^2 - \log_4 (5y - 12) (= \log_4 2)$ $\log_4 \left(\frac{y^2}{5y - 12} \right) (= \log_4 2)$ $y^2 - 10y + 24 = 0$ $y = 4, 6$	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>B1 for power</p> <p>correct division</p> <p>attempt at solution of a 3 term quadratic</p> <p>A1 for both</p>
5	(i)	$x + \frac{6}{x} (+c)$	B1 B1	B1 for each term
	(ii)	$\left(3k + \frac{6}{3k} \right) - \left(k + \frac{6}{k} \right) (= 2)$ $2k^2 - 2k - 4 = 0$	<p>M1</p> <p>M1</p> <p>DM1</p>	<p>correct use of limits</p> <p>attempt to obtain a 3 term quadratic from 2 brackets equated to 2</p> <p>DM1 or solution of quadratic dependent on 2nd M1</p>
		leading to $k = 2$	A1	

Page 6	Mark Scheme	Syllabus	Paper
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6	<p>(i) $A^{-1} = \frac{1}{13} \begin{pmatrix} 5 & 1 \\ -3 & 2 \end{pmatrix}$</p> <p>(ii) Either</p> $\begin{pmatrix} a & b \\ c & -1 \end{pmatrix} = \frac{1}{13} \begin{pmatrix} 5 & 1 \\ -3 & 2 \end{pmatrix} \begin{pmatrix} 7 & 5 \\ 17 & d \end{pmatrix}$ $= \frac{1}{13} \begin{pmatrix} 52 & 25+d \\ 13 & -15+2d \end{pmatrix}$ <p>leading to $a = 4, c = 1$</p> <p>and $b = 2, d = 1$</p> <p>Or</p> $\begin{pmatrix} 2 & -1 \\ 3 & 5 \end{pmatrix} \begin{pmatrix} a & b \\ c & -1 \end{pmatrix} = \begin{pmatrix} 7 & 5 \\ 17 & d \end{pmatrix}$ $2a - c = 7, 3a + 5c = 17, a = 4, c = 1$ $2b + 1 = 5, 3b - 5 = d, b = 2, d = 1$	<p>B1 B1</p> <p>M1</p> <p>DM1</p> <p>A3,2,1,0</p> <p>[M1</p> <p>DM1</p> <p>A3,2,1,0]</p>	<p>B1 for matrix, B1 for multiplying by a correct determinant</p> <p>evidence of multiplication of both sides by A^{-1}</p> <p>DM1 for attempt to equate like elements</p> <p>–1 each error</p> <p>M1 for evidence of matrix multiplication</p> <p>DM1 for attempt to equate like elements –1 each error</p>
7	<p>(i) $\tan B = \frac{\sqrt{5+1}}{\sqrt{5-2}}$</p> $= \frac{\sqrt{5+1}}{\sqrt{5-2}} \times \frac{\sqrt{5+2}}{\sqrt{5+2}}$ $= 7 + 3\sqrt{5}$ <p>(ii) $(7 + 3\sqrt{5})^2 + 1 = \sec^2 B$</p> $\sec^2 B = 95 + 42\sqrt{5}$ <p>Or</p> $\sec^2 B = \frac{1}{\cos^2 B} = \frac{(\sqrt{5+1})^2 + (\sqrt{5-2})^2}{(\sqrt{5-2})^2}$ $\sec^2 B = \frac{15 - 2\sqrt{5}}{9 - 4\sqrt{5}} \times \frac{9 + 4\sqrt{5}}{9 + 4\sqrt{5}}$ $\sec^2 B = 95 + 42\sqrt{5}$	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1 M1</p> <p>$\sqrt{A1}$ $\sqrt{A1}$</p> <p>[M1</p> <p>M1</p> <p>A1 A1]</p>	<p>attempt at rationalisation (Allow if inverse is used)</p> <p>M1 for attempt to use the correct identity M1 for simplification to give 3 or 4 terms</p> <p>cao A1 for 95, A1 for $42\sqrt{5}$</p> <p>M1 for attempt to use to find BC^2</p> <p>M1 for use of $\sec B = \frac{1}{\cos B}$</p> <p>A1 for 95, A1 for $52\sqrt{5}$</p>

Page 7	Mark Scheme	Syllabus	Paper
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8	(i)	Either $\tan \frac{\theta}{2} = \frac{8}{6}$	M1	M1 for use of trig to obtain half angle
		$\frac{\theta}{2} = 0.927\dots$		Can use $\sin \frac{\theta}{2} = \frac{8}{10}$ or $\cos \frac{\theta}{2} = \frac{6}{10}$
		$\theta = 1.855$	A1	A1 Allow if done in degrees and converted
		Or Area of triangle $MEF = 48$	[M1]	M1 for a complete method to find the obtuse angle
		$\frac{1}{2} \times 10^2 \times \sin \theta = 48$		
	(ii)	$\theta = 1.287, \pi - 1.287$		
		$\theta = 1.855$	A1]	
		Or $16^2 = 10^2 + 10^2 - (2 \times 10 \times \cos \theta)$	[M1]	M1 for use of the cosine rule, need to see working as answer given
		$\theta = 1.855$	A1]	
		radius = 10	B1	B1 for the radius, allow anywhere
(iii)		$P = (10 \times 1.855) + 10 + 10 + 16$	M1 M1	M1 for use of arc length M1 for method, must be arc +3 sides
		$= 54.6 \text{ or } 54.5 \text{ or } 54.55$	A1	
		$A = 256 - 2 \left(\frac{1}{2} \times 8 \times 6 \right) - \frac{1}{2} 10^2 (1.855)$	M1 M1	M1 for area of sector M1 for a correct plan to obtain the required area
		$= 115.25 \text{ or } 115.3 \text{ or } 115$	A1	
		awrt 115		

Page 8	Mark Scheme	Syllabus	Paper
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9	(i)	$\overrightarrow{AP} = \frac{3}{4}(\mathbf{b} - \mathbf{a})$	B1	
		$\overrightarrow{OP} = \mathbf{a} + \frac{3}{4}(\mathbf{b} - \mathbf{a}), \text{ or}$	M1	M1 for attempt at vector addition
		$\overrightarrow{OP} = \mathbf{a} - \frac{1}{4}(\mathbf{b} - \mathbf{a}),$		
		$= \frac{1}{4}(\mathbf{a} + 3\mathbf{b})$	A1	Answer given
	(ii)	$\overrightarrow{OQ} = \frac{2}{5}\mathbf{c}, \text{ or } \overrightarrow{QC} = \frac{3}{5}\mathbf{c} \text{ or } \overrightarrow{CQ} = -\frac{3}{5}\mathbf{c}$	B1	B1 for \overrightarrow{OQ} , \overrightarrow{QC} or \overrightarrow{CQ}
		$\overrightarrow{PQ} = \overrightarrow{OQ} - \overrightarrow{OP}$	M1	M1 for correct vector addition/subtraction
		$= \frac{2}{5}\mathbf{c} - \frac{\mathbf{a}}{4} - \frac{3\mathbf{b}}{4}$	A1	
	(iii)	$2\mathbf{c} - \frac{5\mathbf{a}}{4} - \frac{15\mathbf{b}}{4} = 6(\mathbf{c} - \mathbf{b})$	M1	M1 for use of <i>their</i> vectors and attempt to get $k\mathbf{c}$
		$\mathbf{c} = \frac{9\mathbf{b} - 5\mathbf{a}}{16}$	A1	
10	(i)	When $x = 2, y = -5$	B1	B1 for $y = -5$
		$\frac{dy}{dx} = 3x^2 - 8x + 1$	M1	M1 for attempt to differentiate
		when $x = 2, \frac{dy}{dx} = -3$	DM1	DM1 for attempt at tangent equation – must be tangent with use of $x = 2$
		Tangent: $y + 5 = -3(x - 2)$ ($y = 1 - 3x$)	A1	allow unsimplified
	(ii)	$1 - 3x = x^3 - 4x^2 + x + 1$	M1	M1 for equating tangent and curve equations
		$x(x - 2)^2 = 0$	DM1	DM1 for attempt to solve resulting cubic equation
		Meets at (0, 1)	A1 A1	A1 for each coordinate

Page 9	Mark Scheme	Syllabus	Paper
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(iii)	<p>Grad of perp = $\frac{1}{3}$</p> <p>Midpoint (1, -2)</p> <p>Perp bisector $y + 2 = \frac{1}{3}(x - 1)$</p>	<p>√B1</p> <p>M1</p> <p>M1 A1</p>	<p>√B1 on <i>their</i> gradient in (i) only</p> <p>M1 for attempt to find the midpoint</p> <p>M1 for attempt at line equation – must be perp bisector A1 allow unsimplified</p>
11 (a)	<p>$\sin\left(x + \frac{\pi}{3}\right) = -\frac{1}{2}$</p> <p>$x + \frac{\pi}{3} = \frac{7\pi}{6}, \frac{11\pi}{6}$</p> <p>$x = \frac{5\pi}{6}, \frac{3\pi}{2}$</p>	<p>B1</p> <p>B1</p> <p>B1 B1</p>	<p>B1 for $\frac{7\pi}{6}$ and $\frac{11\pi}{6}$</p> <p>B1 for first correct solution B1 for a second correct solution with all solutions in radians and with no excess solutions within the range</p>
(b)	<p>$\tan y - 2 = \frac{1}{\tan y}$</p> <p>$\tan^2 y - 2 \tan y - 1 = 0$</p> <p>$\tan y = 1 \pm \sqrt{2}$</p> <p>$y = 67.5^\circ, 157.5^\circ$</p>	<p>B1</p> <p>M1 A1</p> <p>DM1</p> <p>A1 A1</p>	<p>B1 for a correct equation</p> <p>M1 for attempt to obtain a 3 term quadratic equation A1 for a correct equation equated to zero</p> <p>DM1 for solution of quadratic</p> <p>A1 for first correct solution A1 for a second correct solution with all solutions in degrees and with no excess solutions within the range.</p>

MARK SCHEME for the May/June 2013 series

0606 ADDITIONAL MATHEMATICS

0606/12

Paper 1, maximum raw mark 80

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Page 2	Mark Scheme	Syllabus	Paper
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Page 4	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2013	0606	12

1	(i) (ii) (iii)	$n(A \cap B) = 5$ $n(A) = 16$ $n(B' \cap A)$	B1 B1 B1	
2	(i) (ii) <			

Page 5	Mark Scheme	Syllabus	Paper
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4	<p>EITHER $2x^2 + kx + 2k - 6 = 0$ has no real roots $k^2 - 16k + 48 < 0$ $(k - 4)(k - 12) < 0$</p> <p>Critical values 4 and 12 $4 < k < 12$ or $k > 4$ and $k < 12$</p> <p>OR $\left(x + \frac{k}{4}\right)^2 - \frac{k^2}{16} + k - 3 = 0$</p> <p>$-\frac{k^2}{16} + k - 3 > 0$ so $k^2 - 16k + 48 < 0$</p> <p>OR $\frac{dy}{dx} = 4x + k$</p> <p>When $\frac{dy}{dx} = 0$, $k = -4x$ By substitution $x^2 + 4x + 3 < 0$ leading to $x = -1$, $k = 4$</p> <p>and $x = -3$, $k = 12$ $4 < k < 12$ or $k > 4$ and $k < 12$</p> <p>OR $\frac{dy}{dx} = 4x + k$</p> <p>When $\frac{dy}{dx} = 0$, $x = -\frac{k}{4}$ leading to $k^2 - 16k + 48 < 0$</p>	<p>M1 DM1</p> <p>A1 A1</p> <p>[M1]</p> <p>[M1]</p> <p>DM1</p> <p>A1 A1]</p> <p>[M1]</p>	<p>M1 for attempted use of $b^2 - 4ac$ DM1 for attempt to obtain critical values from a 3 term quadratic</p> <p>A1 for both critical values A1 for correct final answer</p> <p>M1 for attempting to complete the square and obtain a 3 term quadratic</p> <p>Then as EITHER</p> <p>M1 for differentiation, equating to zero and obtaining a quadratic equation in x</p> <p>DM1 for attempt to obtain critical values of k from a 3 term quadratic in x followed by substitution to obtain a value for k</p> <p>A1 for both critical values A1 for correct final answer</p> <p>M1 for differentiation, equating to zero and obtaining a quadratic equation in k</p> <p>Then as EITHER</p>
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Page 6	Mark Scheme	Syllabus	Paper
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5	$2\left(\frac{15-4y}{3}\right)y=9 \text{ or } 2x\left(\frac{15-3x}{4}\right)=9$ $8y^2-30y+27=0 \text{ or } 3x^2-15x+18=0$ $(4y-9)(2y-3)=0 \text{ or } (x-3)(x-2)=0$ $x=2, y=\frac{9}{4} \text{ and } x=3, y=\frac{3}{2}$ $AB^2=1^2+(0.75)^2, AB=1.25$	<p>M1</p> <p>DM1</p> <p>A1, A1</p> <p>M1, A1</p>	<p>M1 for attempt to obtain equation in one variable</p> <p>DM1 for attempt to solve a 3 term quadratic in that variable</p> <p>A1 for each 'pair', x values must be simplified to single integer form</p> <p>M1 for a correct attempt to find AB, must have non zero differences and be using points calculated previously.</p>
6	$\frac{dy}{dx}=3\sec^2x$ <p>When $x=\frac{3\pi}{4}$, $\frac{dy}{dx}=6$</p> $y=5$ <p>Perpendicular gradient $= -\frac{1}{6}$</p> <p>Equation of normal $y+5=-\frac{1}{6}\left(x-\frac{3\pi}{4}\right)$</p> <p>When $x=0$, $y=\frac{\pi}{8}-5$ o.e.</p> <p>or -4.61 or -4.6 but not -4.60</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>B1 for $3\sec^2x$</p> <p>B1 for $\frac{dy}{dx}=6$, may be implied by later work</p> <p>B1 for y</p> <p>M1 for perpendicular gradient from $\frac{dy}{dx}$</p> <p>M1 for attempt at the normal using <i>their</i> y value correctly and $x=\frac{3\pi}{4}$ and substitution of $x=0$</p> <p>A1 for obtaining y value</p>

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7	(i)	$f(-2)$ leads to $68 = b - 2a$	M1	attempt at $f(-2) = 0$ allow unsimplified
		$f(1)$ leads to $26 = a + b$	M1	attempt at $f(1) = 27$ allow unsimplified
		$a = -14, b = 40$	A1, B1	A1 for $b = 40$, B1 for $a = -14$
	(ii)	$f(x) = (x + 2)(6x^2 - 17x + 20)$	B2, 1, 0	-1 each error
	(iii)	$6x^2 - 17x + 20 = 0$ has no real roots	B1	B1 for dealing with quadratic factor either by use of formula, completing the square or use of $b^2 - 4ac$ to show that there are no real solutions
		$x = -2$	B1	
8	(a) (i)	$\begin{pmatrix} 22 & -2 \\ -3 & 31 \end{pmatrix}$	B2, 1, 0	-1 each element error
	(ii)	$\begin{pmatrix} 16 & 6 \\ 9 & -11 \end{pmatrix}$	B2, 1, 0	-1 each element error
	(b) (i)	$\frac{1}{18+9} \begin{pmatrix} 3 & -1 \\ 9 & 6 \end{pmatrix}$	B1, B1	B1 for $\frac{1}{\text{determinant}}$ (allow unsimplified), B1 for matrix
	(ii)	$\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{27} \begin{pmatrix} 3 & -1 \\ 9 & 6 \end{pmatrix} \begin{pmatrix} 5 \\ 1.5 \end{pmatrix},$ $= \frac{1}{27} \begin{pmatrix} 13.5 \\ 54 \end{pmatrix}$	M1	M1 for correct use of inverse matrix, including correct multiplication to solve equation
		$x = 0.5, y = 2$	A1, A1	A1 for each

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9	(i)	$\left(1 + \frac{1}{2}x\right)^n = 1 + n\left(\frac{x}{2}\right) + \frac{n(n-1)}{2}\left(\frac{x}{2}\right)^2$	B1, B1	B1 for 1 + second term, B1 for 3rd term Allow unsimplified
	(ii)	$(1-x)\left(1 + n\left(\frac{x}{2}\right) + \frac{n(n-1)}{2}\left(\frac{x}{2}\right)^2\right)$	M1	dealing with 2 terms involving x^2
		Multiply x and $\frac{n}{2}x$ to get $\frac{n}{2}(x^2)$	DM1	attempt to obtain one term
		Multiply 1 and $\frac{n(n-1)x^2}{8}$ or $\frac{n(n-1)x^2}{4}$	DM1	attempt to obtain a second term
		$\frac{n^2 - n}{8} - \frac{n}{2} = \frac{25}{4}$ $n^2 - 5n - 50 = 0$ $n = 10$	A1 A1	correct quadratic equation A1 for $n = 10$ only
10	(a) (i)	$\frac{1}{3}(2x-5)^{\frac{3}{2}}$	B1, B1	B1 for $k(2x-5)^{\frac{3}{2}}$, B1 for $\frac{1}{3}(2x-5)^{\frac{3}{2}}$
	(ii)	$\frac{125}{3} - \frac{1}{3} = \frac{124}{3}$ Allow awrt 41.3	M1, A1	M1 for correct use of limits
	(b) (i)	$x^3 \frac{1}{x} + 3x^2 \ln x$	B1, B1	B1 for each term, allow unsimplified
	(ii)	$\int 3x^2 \ln x dx = x^3 \ln x - \int x^2 dx$ o.e. $\int x^2 dx = \frac{x^3}{3}$ or	M1 A1	for a use of answer to (i) A1 for integrating x^2 or dividing by 3
		$\int x^2 \ln x dx = \frac{1}{3}(x^3 \ln x - \int x^2 dx)$ o.e. $\int x^2 \ln x dx = \frac{1}{3}\left(x^3 \ln x - \frac{x^3}{3}\right) (+c)$	A1	

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11	(a)	$\cos 2x + \frac{2}{\cos 2x} + 3 = 0$ <p>leading to $\cos^2 2x + 3 \cos 2x + 2 = 0$ $2 \sec^2 2x + 3 \sec 2x + 1 = 0$</p> <p>$(\cos 2x + 2)(\cos 2x + 1) = 0$ or $(2 \sec 2x + 1)(\sec 2x + 1) = 0$</p> <p>leading to $\cos 2x = -1$ or $\sec 2x = -1$ only $2x = 180^\circ, 540^\circ$ $x = 90^\circ, 270^\circ$</p>	M1	dealing with sec or cos
	(b)	$\sin^2\left(y - \frac{\pi}{6}\right) = \frac{1}{2} \text{ so}$ $\sin\left(y - \frac{\pi}{6}\right) = \frac{1}{\sqrt{2}}$ $\left(y - \frac{\pi}{6}\right) = \frac{\pi}{4}, \frac{3\pi}{4}$ $y = \frac{5\pi}{12}, \frac{11\pi}{12}$ <p>Allow awrt 1.31, 2.88</p>	M1 DM1 A1, A1	<div>simplification to correct 3 term quadratic in $\sec 2x$ or $\cos 2x$ (does not have to be equated to zero)</div> <div>attempt to solve a 3 term quadratic, must obtain solutions in terms of $\cos 2x$</div> <div>division by 2 and square root</div> <div>correct order of operation and attempt to solve</div>
12	(i)	$\frac{dy}{dt} = 36 - 6t$ <p>When $\frac{dy}{dt} = 0, t = 6$</p>	M1 A1	attempt to differentiate and equate to zero
	(ii)	When $v = 0, t = 12$	M1, A1	M1 for equating v to zero and attempt to solve
	(iii)	$s = 18t^2 - t^3 (+c)$ <p>When $t = 12, s = 864$</p>	M1, A1	M1 for a correct attempt to integrate at least one term, allow unsimplified A1 for all correct A1 for $s = 864$
	(iv)	<p>When $s = 0, t = 18$</p> <p>$v = -324$</p> <p>So speed is 324</p>	M1 √A1 DM1	M1 for substitution of $s = 0$ into <i>their</i> s equation √A1 on <i>their</i> s DM1 for substitution of <i>their</i> t back into v equation A1 for 324 only

MARK SCHEME for the May/June 2013 series

0606 ADDITIONAL MATHEMATICS

0606/13

Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2013 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.

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Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
 - A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
 - B Accuracy mark for a correct result or statement independent of method marks.
- When a part of a question has two or more “method” steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
 - The symbol \checkmark implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously “correct” answers or results obtained from incorrect working.
 - Note: B2 or A2 means that the candidate can earn 2 or 0.
B2, 1, 0 means that the candidate can earn anything from 0 to 2.

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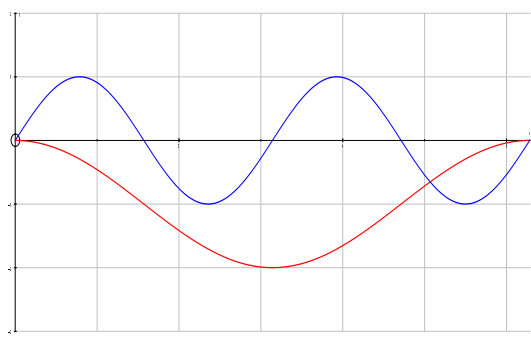
The following abbreviations may be used in a mark scheme or used on the scripts:

AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no “follow through” from a previous error is allowed)
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
SOS	See Other Solution (the candidate makes a better attempt at the same question)

Penalties

MR –1	A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become “follow through $\sqrt{}$ ” marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy.
OW –1,2	This is deducted from A or B marks when essential working is omitted.
PA –1	This is deducted from A or B marks in the case of premature approximation.
S –1	Occasionally used for persistent slackness – usually discussed at a meeting.
EX –1	Applied to A or B marks when extra solutions are offered to a particular equation. Again, this is usually discussed at the meeting.

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1	(i)		B1	correct shape for $y = \cos x - 1$
	(ii)		B1	all correct
	(iii)		B1	all correct
2	3		B1	
	<p>Either gradient = 1</p> <p>intercept = 2</p> <p>$\ln b = \text{gradient}$ or $\ln A = \text{intercept}$</p> <p>$b = e$ or 2.72</p> <p>$A = e^2, A = 7.39$</p> <p>Or $e^4 = Ab^2$ and $e^{10} = Ab^8$</p> <p>leading to $b^6 = e^6$ or $e^4 = e^2 A$ or $e^{10} = e^8 A$</p> <p>$b = e$ or 2.72</p> <p>$A = e^2, A = 7.39$</p> <p>Or $10 = 8 \ln b + \ln A$</p> <p>$4 = 2 \ln b + \ln A$</p> <p>leading to $\ln b = 1$ or $6 = 3 \ln A$</p> <p>$b = e$ or 2.72</p> <p>$A = e^2, A = 7.39$</p>		<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p> <p>[B1 B1</p> <p>M1</p> <p>A1</p> <p>A1]</p> <p>[B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1]</p>	<p>M1, need to equate either gradient to $\ln b$ or intercept to $\ln A$</p> <p>B1 for each equation</p> <p>M1 for attempt to solve for either A or b</p> <p>M1 for attempt to solve for either A or b</p>

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3	(i)	${}^{14}C_6 = 3003$	B1	
	(ii)	${}^5C_3 \times {}^9C_3 = 840$	M1 A1	M1 for product of 2 combinations
	(iii)	<p>Either $3003 - {}^9C_6 = 2919$</p> <p>Or</p> <p>1M + 5W: $5 \times {}^9C_5 = 630$ 2M + 4W: ${}^5C_2 \times {}^9C_4 = 1260$ 3M + 3W: 840 (part (ii)) 4M + 2W: ${}^5C_4 \times {}^9C_2 = 180$ 5M + 1W: $1 \times {}^9C_1 = 9$ Total: 2919</p>	<p>M1 B1 A1</p> <p>[B2 1 0</p> <p>B1]</p>	<p>M1 for 3003 – number of committees containing no men B1 for 9C_6</p> <p>–1 each error</p> <p>B1 for correct final answer</p>
4	(i)	2	B1	
	(ii)	$\log_4 y^2 - \log_4 (5y - 12) (= \log_4 2)$ $\log_4 \left(\frac{y^2}{5y - 12} \right) (= \log_4 2)$ $y^2 - 10y + 24 = 0$ $y = 4, 6$	<p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>B1 for power</p> <p>correct division</p> <p>attempt at solution of a 3 term quadratic</p> <p>A1 for both</p>
5	(i)	$x + \frac{6}{x} (+c)$	B1 B1	B1 for each term
	(ii)	$\left(3k + \frac{6}{3k} \right) - \left(k + \frac{6}{k} \right) (= 2)$ $2k^2 - 2k - 4 = 0$	<p>M1</p> <p>M1</p> <p>DM1</p> <p>A1</p>	<p>correct use of limits</p> <p>attempt to obtain a 3 term quadratic from 2 brackets equated to 2</p> <p>DM1 or solution of quadratic dependent on 2nd M1</p>
		leading to $k = 2$		

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6	<p>(i) $A^{-1} = \frac{1}{13} \begin{pmatrix} 5 & 1 \\ -3 & 2 \end{pmatrix}$</p> <p>(ii) Either</p> $\begin{pmatrix} a & b \\ c & -1 \end{pmatrix} = \frac{1}{13} \begin{pmatrix} 5 & 1 \\ -3 & 2 \end{pmatrix} \begin{pmatrix} 7 & 5 \\ 17 & d \end{pmatrix}$ $= \frac{1}{13} \begin{pmatrix} 52 & 25+d \\ 13 & -15+2d \end{pmatrix}$ <p>leading to $a = 4, c = 1$</p> <p>and $b = 2, d = 1$</p> <p>Or</p> $\begin{pmatrix} 2 & -1 \\ 3 & 5 \end{pmatrix} \begin{pmatrix} a & b \\ c & -1 \end{pmatrix} = \begin{pmatrix} 7 & 5 \\ 17 & d \end{pmatrix}$ $2a - c = 7, 3a + 5c = 17, a = 4, c = 1$ $2b + 1 = 5, 3b - 5 = d, b = 2, d = 1$	<p>B1 B1</p> <p>M1</p> <p>DM1</p> <p>A3,2,1,0</p> <p>[M1]</p> <p>DM1</p> <p>A3,2,1,0]</p>	<p>B1 for matrix, B1 for multiplying by a correct determinant</p> <p>evidence of multiplication of both sides by A^{-1}</p> <p>DM1 for attempt to equate like elements</p> <p>–1 each error</p> <p>M1 for evidence of matrix multiplication</p> <p>DM1 for attempt to equate like elements –1 each error</p>
7	<p>(i) $\tan B = \frac{\sqrt{5+1}}{\sqrt{5-2}}$</p> $= \frac{\sqrt{5+1}}{\sqrt{5-2}} \times \frac{\sqrt{5+2}}{\sqrt{5+2}}$ $= 7 + 3\sqrt{5}$ <p>(ii) $(7 + 3\sqrt{5})^2 + 1 = \sec^2 B$</p> $\sec^2 B = 95 + 42\sqrt{5}$ <p>Or</p> $\sec^2 B = \frac{1}{\cos^2 B} = \frac{(\sqrt{5+1})^2 + (\sqrt{5-2})^2}{(\sqrt{5-2})^2}$ $\sec^2 B = \frac{15 - 2\sqrt{5}}{9 - 4\sqrt{5}} \times \frac{9 + 4\sqrt{5}}{9 + 4\sqrt{5}}$ $\sec^2 B = 95 + 42\sqrt{5}$	<p>B1</p> <p>M1</p> <p>A1</p> <p>M1 M1</p> <p>$\sqrt{A1}$ $\sqrt{A1}$</p> <p>[M1]</p> <p>M1</p> <p>A1 A1]</p>	<p>attempt at rationalisation (Allow if inverse is used)</p> <p>M1 for attempt to use the correct identity M1 for simplification to give 3 or 4 terms</p> <p>cao A1 for 95, A1 for $42\sqrt{5}$</p> <p>M1 for attempt to use to find BC^2</p> <p>M1 for use of $\sec B = \frac{1}{\cos B}$</p> <p>A1 for 95, A1 for $52\sqrt{5}$</p>

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8	(i)	Either $\tan \frac{\theta}{2} = \frac{8}{6}$	M1	M1 for use of trig to obtain half angle
		$\frac{\theta}{2} = 0.927\dots$		Can use $\sin \frac{\theta}{2} = \frac{8}{10}$ or $\cos \frac{\theta}{2} = \frac{6}{10}$
		$\theta = 1.855$	A1	A1 Allow if done in degrees and converted
		Or Area of triangle $MEF = 48$	[M1]	M1 for a complete method to find the obtuse angle
		$\frac{1}{2} \times 10^2 \times \sin \theta = 48$		
	(ii)	$\theta = 1.287, \pi - 1.287$		
		$\theta = 1.855$	A1]	
		Or $16^2 = 10^2 + 10^2 - (2 \times 10 \times \cos \theta)$	[M1]	M1 for use of the cosine rule, need to see working as answer given
		$\theta = 1.855$	A1]	
		radius = 10	B1	B1 for the radius, allow anywhere
(iii)		$P = (10 \times 1.855) + 10 + 10 + 16$	M1 M1	M1 for use of arc length M1 for method, must be arc +3 sides
		$= 54.6 \text{ or } 54.5 \text{ or } 54.55$	A1	
		$A = 256 - 2 \left(\frac{1}{2} \times 8 \times 6 \right) - \frac{1}{2} 10^2 (1.855)$	M1 M1	M1 for area of sector M1 for a correct plan to obtain the required area
		$= 115.25 \text{ or } 115.3 \text{ or } 115$	A1	
		awrt 115		

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9	(i)	$\overrightarrow{AP} = \frac{3}{4}(\mathbf{b} - \mathbf{a})$	B1	
		$\overrightarrow{OP} = \mathbf{a} + \frac{3}{4}(\mathbf{b} - \mathbf{a}), \text{ or}$	M1	M1 for attempt at vector addition
		$\overrightarrow{OP} = \mathbf{a} - \frac{1}{4}(\mathbf{b} - \mathbf{a}),$		
		$= \frac{1}{4}(\mathbf{a} + 3\mathbf{b})$	A1	Answer given
	(ii)	$\overrightarrow{OQ} = \frac{2}{5}\mathbf{c}, \text{ or } \overrightarrow{QC} = \frac{3}{5}\mathbf{c} \text{ or } \overrightarrow{CQ} = -\frac{3}{5}\mathbf{c}$	B1	B1 for \overrightarrow{OQ} , \overrightarrow{QC} or \overrightarrow{CQ}
		$\overrightarrow{PQ} = \overrightarrow{OQ} - \overrightarrow{OP}$	M1	M1 for correct vector addition/subtraction
		$= \frac{2}{5}\mathbf{c} - \frac{\mathbf{a}}{4} - \frac{3\mathbf{b}}{4}$	A1	
	(iii)	$2\mathbf{c} - \frac{5\mathbf{a}}{4} - \frac{15\mathbf{b}}{4} = 6(\mathbf{c} - \mathbf{b})$	M1	M1 for use of <i>their</i> vectors and attempt to get $k\mathbf{c}$
		$\mathbf{c} = \frac{9\mathbf{b} - 5\mathbf{a}}{16}$	A1	
10	(i)	When $x = 2, y = -5$	B1	B1 for $y = -5$
		$\frac{dy}{dx} = 3x^2 - 8x + 1$	M1	M1 for attempt to differentiate
		when $x = 2, \frac{dy}{dx} = -3$	DM1	DM1 for attempt at tangent equation – must be tangent with use of $x = 2$
		Tangent: $y + 5 = -3(x - 2)$ ($y = 1 - 3x$)	A1	allow unsimplified
	(ii)	$1 - 3x = x^3 - 4x^2 + x + 1$	M1	M1 for equating tangent and curve equations
		$x(x - 2)^2 = 0$	DM1	DM1 for attempt to solve resulting cubic equation
		Meets at (0, 1)	A1 A1	A1 for each coordinate

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(iii)	<p>Grad of perp = $\frac{1}{3}$</p> <p>Midpoint (1, -2)</p> <p>Perp bisector $y + 2 = \frac{1}{3}(x - 1)$</p>	<p>√B1</p> <p>M1</p> <p>M1 A1</p>	<p>√B1 on <i>their</i> gradient in (i) only</p> <p>M1 for attempt to find the midpoint</p> <p>M1 for attempt at line equation – must be perp bisector A1 allow unsimplified</p>
11 (a)	<p>$\sin\left(x + \frac{\pi}{3}\right) = -\frac{1}{2}$</p> <p>$x + \frac{\pi}{3} = \frac{7\pi}{6}, \frac{11\pi}{6}$</p> <p>$x = \frac{5\pi}{6}, \frac{3\pi}{2}$</p>	<p>B1</p> <p>B1</p> <p>B1 B1</p>	<p>B1 for $\frac{7\pi}{6}$ and $\frac{11\pi}{6}$</p> <p>B1 for first correct solution B1 for a second correct solution with all solutions in radians and with no excess solutions within the range</p>
(b)	<p>$\tan y - 2 = \frac{1}{\tan y}$</p> <p>$\tan^2 y - 2 \tan y - 1 = 0$</p> <p>$\tan y = 1 \pm \sqrt{2}$</p> <p>$y = 67.5^\circ, 157.5^\circ$</p>	<p>B1</p> <p>M1 A1</p> <p>DM1</p> <p>A1 A1</p>	<p>B1 for a correct equation</p> <p>M1 for attempt to obtain a 3 term quadratic equation A1 for a correct equation equated to zero</p> <p>DM1 for solution of quadratic</p> <p>A1 for first correct solution A1 for a second correct solution with all solutions in degrees and with no excess solutions within the range.</p>