For each of the following problems, decide which is the BEST of the choices given. If the exact numerical value is not one of the choices, select the choice that best approximates this value. Then fill in the corresponding oval on the answer sheet.

<u>Notes</u>: (1) A scientific or graphing calculator will be necessary for answering some (but not all) of the questions on this test. For each question, you will have to decide whether or not you should use a calculator.

(2) For some questions in this test you may have to decide whether your calculator should be in the radian mode or the degree mode.

(3) Figures that accompany problems on this test are intended to provide information useful in solving the problems. They are drawn as accurately as possible EXCEPT when it is stated in a specific problem that its figure is not drawn to scale. All figures lie in a plane unless otherwise indicated.

(4) Unless otherwise specified, the domain of any function f is assumed to be the set of all real numbers x for which f(x) is a real number. The range of f is assumed to be the set of all real numbers f(x), where x is in the domain of f.

(5) Reference information that may be useful in answering the questions on this test can be found below.

THE FOLLOWING INFORMATION IS FOR YOUR REFERENCE IN ANSWERING SOME OF THE QUES-TIONS ON THIS TEST.

Volume of a right circular cone with radius *r* and height *h*:

$$V = \frac{1}{3}\pi r^2 h$$

MATHEMATICS LEVEL 2

Lateral area of a right circular cone with circumference of

the base *c* and slant height $\ell: S = \frac{1}{2}c\ell$

Volume of a sphere with radius r: $V = \frac{4}{3}\pi r^3$

Surface area of a sphere with radius $r: S = 4\pi r^2$

Volume of a pyramid with base area *B* and height *h*:

 $V = \frac{1}{3}Bh$

- 1. If r s > r + s, then which of the following must be true?
 - (A) r > s
 - (B) s < 0
 - (C) r < 0
 - (D) r < s
 - (E) s > 0
- 2. If f(x) = |x| + 10, for which of the following values of x does f(x) = f(-x)?
 - (A) -10 only
 - (B) -10 and 10 only
 - (C) All real x
 - (D) All real x except 10
 - (E) All real x except -10 and 10



2 2 2 2 2 2 2 2 MATHEMATICS LEVEL 2—Continued

USE THIS SPACE FOR SCRATCHWORK.

3. $\frac{15!}{13!2!} =$ (A) 0 (B) 0.58 (C) 1 (D) 105 (E) 210



5. Which of the following is the complete solu set of the system:

 $A = \{(x, y): x^2 + y^2 = 25\} \text{ and } B = \{(x, y): y = x + 1\}?$

- (A) $\{(5,5)\}$
- (B) $\{(16, 9)\}\$ (C) $\{(-4, -3)\}$
- (D) $\{(-4, -3), (3, 4)\}$
- (E) $\{(-3, -4), (4, 3)\}$





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MATHEMATICS LEVEL 2—Continued



- (C) jk 1
- (D) $j^2 1$
- (E) $k^2 1$
- 7. All of the following can be formed by the intersection of a right cylinder and a plane EXCEPT:
 - (A) A line
 - (B) A circle
 - (C) An ellipse
 - (D) A parabola
 - (E) A triangle

8. If $f(x) = \sqrt[3]{x}$ and $g(x) = \frac{1}{2}\sqrt{x} + 1$, then f(g(2.3)) =h.satprep.co.

- (A) 0.1
- (B) 1.2
- (C) 1.3
- (D) 1.8
- (E) 2.3
- 9. If *x* mod *y* is the remainder when *x* is divided by y, then $(61 \mod 7) - (5 \mod 5) =$
 - (A) 2
 - (B) 3
 - (C) 4
 - (D) 5
 - (E) 6



MATHEMATICS LEVEL 2—Continued

10. Which of the following must be true?

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- I. $\sin(-\theta) = -\sin \theta$
- II. $\cos(-\theta) = -\cos\theta$
- III. $\tan(-\theta) = -\tan \theta$, where $\tan \theta$ is defined
- (A) I only
- (B) II only
- (C) III only
- (D) I and III only
- (E) I, II, and III

11. If for all real numbers x, a function f(x) is defined $(2, x \neq 13)$ b

_

y
$$f(x) = \begin{cases} 1, x + 10, \\ 4, x = 13 \end{cases}$$
, then $f(15) - f(14)$

(A) -2 (B) 0 (C) 1 (D) 2 (E) 4

12. If $\frac{x^5}{25} = 25$, then x =(A) 1.00 (B) 1.90 (C) 2.19 (D) 3.62

- (E) 5.00
- 222.5 13. If the ratio of sec x to csc x is 1:4, then the ratio of tan x to cot x is
 - (A) 1:16
 - (B) 1:4
 - (C) 1:1
 - (D) 4:1
 - (E) 16:1



MATHEMATICS LEVEL 2—Continued

2

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- 14. In Figure 2, rectangle J contains all points (x, y). What is the area of a rectangle that contains all points (2x, y - 1)?
 - (A) 12
 - (B) 18
 - (C) 24
 - (D) 36
 - (E) 48
- 15. In right triangle ABC, $\angle B$ measures 90°, $\angle C$ measures 27°, and AB = 9. What is the length of the hypotenuse of $\triangle ABC$?
 - (A) 4.1
 - (B) 10.1
 - (C) 17.7
 - (D) 19.8
 - (E) 21.2
- 16. Which of the following is a zero of $f(x) = x^2 + 6x - 12$?
 - (A)-15.16
 - (B) -7.58
 - (C) 0.67
 - (D) 3.16



(E) 7.58

2 2 2 2 2 2 2 2 2

MATHEMATICS LEVEL 2—Continued

17. If $\sin x = m$ and 0 < x < 90, then $\tan x =$ USE THIS SPACE FOR SCRATCHWORK. (A) $\frac{1}{m^2}$ (B) $\frac{m}{\sqrt{1-m^2}}$ (C) $\frac{1-m^2}{m}$ (D) $\frac{m}{1-m^2}$ (E) $\frac{m^2}{\sqrt{1-m^2}}$ 18. If $\log_y 2 = 8$, then y =(A) 0.25 (B) 1.04 (C) 1.09 (D) 2.83 (E) 3.00 19. If $\sin \theta = \frac{1}{3}$ and $-\frac{\pi}{4} \le \theta \le \frac{\pi}{4}$, then $\cos (2\theta) =$ (A) $-\frac{7}{9}$ (B) $-\frac{2}{3}$ (C) $\frac{2}{3}$ (D) $\frac{7}{9}$ 1 (E)

GO ON TO THE NEXT PAGE

2 2 2 2 2 2 2

MATHEMATICS LEVEL 2—Continued

20. If $f(x) = \sqrt{x} - 1$, for all x > 0, then $f^{-1}(x) =$

USE THIS SPACE FOR SCRATCHWORK.

(A) $(x + 1)^2$

2

- (B) $x^2 + 2$
- (C) $x^2 + 1$
- (D) $(x-1)^2$
- (E) $(x+2)^2$
- 21. When $4x^2 + 6x + L$ is divided by x + 1, the remainder is 2. Which of the following is the value of *L* ?
 - (A) 4
 - (B) 6
 - (C) 10 (D) 12
 - (E) 12 (E) 15
- 22. What is the length of the major axis of the ellipse given by the equation $\frac{x^2}{10} + \frac{y^2}{20} = 1$? (A) 3.2 (B) 4.5 (C) 8.9 (D) 10.0 (E) 20.0
 - (E) 20.0



2 2 2 2 2 2 2

MATHEMATICS LEVEL 2—Continued

23. If f(x) = [x], where [x] is the greatest integer less

USE THIS SPACE FOR SCRATCHWORK.

than or equal to *x*, which of the following is a

graph of $f\left(\frac{x}{2}\right) - 1$?



MATHEMATICS LEVEL 2—Continued

24. Which of the following is equal to the positive value of sec $(\cos^{-1}(0.3527))$?

- (A) 0.01
- (B) 0.94
- (C) 1.69
- (D) 2.84
- (E) 69.35
- 25. If $f(x) = x^2 + 5x + 6$, for what value of x will f(x)have its minimum value?
 - (A) -3
 - (B) $-\frac{5}{2}$
 - (C) –2
 - 0
 - (D) $\frac{5}{2}$
 - (E)
- 26. If the 20th term of an arithmetic sequence is 20 and the 50th term is 100, what is the first term of the sequence?
 - (A) -33.33
 - (B) -30.67
 - (C) 1.00
 - 2.00 (D)
 - (E) 2.67
- 27. The polar equation $r \sin \theta = 1$ defines the graph of
 - (A) a line
 - (B) a circle
 - (C) an ellipse
 - (D) a parabola
 - (E) a hyperbola



MATHEMATICS LEVEL 2—Continued

28. For which of the following functions f is f^{-1} a function?

USE THIS SPACE FOR SCRATCHWORK.

- I. $f(x) = x^2$
- II. $f(x) = x^3$
- III. f(x) = |x|
- (A) I only
- (B) II only
- (C) I and III only
- (D) II and III only
- (E) I, II, and III
- $\frac{x}{2}$? 29. What is lim
 - (A) –2
 - (B) -1
 - (C) 1
 - (D) 2
 - (E) The limit does not exist.

30. If
$$f(x) = \frac{e^{7x} + \sqrt{3}}{2}$$
, and $g(f(x)) = x$, then $g(x) = (A) \frac{\ln(2x - \sqrt{3})}{7}$

(B)
$$\frac{2x - \sqrt{3}}{e^7}$$

(C) $\frac{2x - \sqrt{3}}{7}$

(D)
$$7 \ln (2x - \sqrt{3})$$

(E) $\frac{(2x - \sqrt{3}) \ln e}{7}$

7



2 2 2 2 2 2 2 2

MATHEMATICS LEVEL 2—Continued

31. A cube is inscribed in a sphere of radius 6. What is the volume of the cube?

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- (A) $36\sqrt{3}$ (B) 36π (C) 216 (D) $192\sqrt{3}$ (E) $216\sqrt{3}$
- 32. A right circular cone has height *h* and radius *r*. If the cone is cut into two pieces by a plane that passes through the midpoint of the height and is parallel to the base, then the volume of the larger of the two resulting solids is



34. If the graph of the equation $y = 2x^2 - 6x + c$ is tangent to the *x*-axis, then the value of *c* is

(A) 3 (B) 3.5 (C) 4 (D) 4.5 (E) 5



2 2 2 2 2 2 2 2 2

MATHEMATICS LEVEL 2—Continued



37. If two coins are removed at random from a purse containing three nickels and eight dimes, what is the probability that both coins will be dimes?

(A)
$$\frac{14}{55}$$
 (B) $\frac{49}{110}$ (C) $\frac{28}{55}$ (D) $\frac{64}{121}$ (E) $\frac{32}{55}$



2 2 2 2 2 2 2

MATHEMATICS LEVEL 2—Continued

38. A function g(x) is odd if g(-x) = -g(x) for all x and even if g(x) = g(-x) for all x. Which of the following is the graph of a function that is both odd and even?



- 39. Points *A* and *B* lie on the edge of a circle with center *O*. If the circle has a radius of 5, and if the measure of $\angle AOB$ is 70°, what is the length of chord *AB* ?
 - (A) 2.9
 - (B) 4.7
 - (C) 5.0
 - (D) 5.7
 - (E) 9.4





- 41. Vectors v and w have components (-3, 4) and (12, 5), respectively. If z = -(v + w), then z has components
 - (A) (-9, -9)
 - (B) (5, 13)
 - $(C) \ (-5, 13)$
 - (D) (9,9)
 - (E) $\left(\frac{9}{2}, \frac{9}{2}\right)$



MATHEMATICS LEVEL 2—Continued

2

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42. If
$$f(x) = \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}}$$
, then for which of the follow-

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ing values of x does f(x) = 0.33 ?

(A) 0.62

2

2

- (B) 0.71
- (C) 1.36
- (D) 3.93
- (E) 4.95

43. The system of equations given by

2x + 3y = 7

10x + cy = 3has solutions for all values of *c* EXCEPT

- (A)-15
- (B) -3
- (C) 3
- (D) 10
- (E) 15
- 44. If $f(x, y) = \frac{xy}{3}$ for all *x*, *y*, f(a, b) = 15, f(b, c) = 20, and f(a, c) = 10, which of the following could

be the product of *a*, *b*, and *c*?

- (A) 18.26
- (B) 54.77
- (C) 284.60
- (D) 1,800.00
- (E) 3,000.00



45. If x > 0 and y > 1, then $\log_{y^2} y = 0$

- I. $\log_x y^2$
- II. $\log_{x} \sqrt{y}$

III.
$$\log_x \left(\frac{y}{2}\right)$$

- (A) I only
- (B) II only
- (C) III only
- (D) I and II only
- (E) II and III only
- 46. Carlos is filling a spherical balloon with water. If he increases the volume of the balloon from 4,188.79 cubic centimeters to 14,137.167 cubic centimeters in 12 seconds, then what is the average rate at which he has increased the balloon's surface area?
 - (A) 130.9 square centimeters per second
 - (B) 314.159 square centimeters per second
 - (C) 829.031 square centimeters per second
 - (D) 1,570.796 square centimeters per second
 - (E) 9,948.377 square centimeters per second
- 47. What is the value of |6 3i|?
 - (A) –3
 - (B) $3\sqrt{2}$
 - (C) $3\sqrt{5}$
 - (D) 9
 - (E) 15



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MATHEMATICS LEVEL 2—Continued

- 48. The menu of a certain restaurant lists 10 items in column A and 20 items in column B. A family plans to share 5 items from column A and 5 items from column B. If none of the items are found in both columns, then how many different combinations of items could the family choose?
 - 25 (A)
 - (B) 200
 - 3,425 (C)
 - (D) 3,907,008
 - (E) 5.63×10^{10}
- 49. *y* varies directly as the square of *x*. When y = 2.5, x = 0.5. If y = 80, then x could equal
 - (A) $-2\sqrt{2}$
 - (B) –8
 - (C) -10
 - (D) -16
 - (E) -64
- 50. Seven blue marbles and six red marbles are held in a single container. Marbles are randomly selected one at a time and not returned to the container. If the first two marbles selected are blue, what is the tprep.co? probability that at least two red marbles will be chosen in the next three selections?

(A)
$$\frac{5}{33}$$
 (B) $\frac{5}{11}$ (C) $\frac{6}{11}$ (D) $\frac{19}{33}$ (E) $\frac{2}{3}$

STOP

IF YOU FINISH BEFORE TIME IS CALLED, YOU MAY CHECK YOUR WORK ON THIS TEST ONLY. DO NOT WORK ON ANY OTHER TEST IN THIS BOOK.