

Extended Mathematics
Topic : Vector-Function-Transformation

Year :May 2013 -May 2024

Paper - 4

Answers

Question 1

(i)	Translation, $\begin{pmatrix} -5 \\ 8 \end{pmatrix}$ oe	1,1	Brackets needed for vector Not $(-5, 8)$, $(-5 \ 8)$
(ii)	correct trapezium at $(2, 2)$ $(4, 3)$ $(4, 5)$ $(2, 5)$	2	SC1 for reflection in $x = -1$ or vertices only

Question 2

(a)	$\frac{-1 \pm \sqrt{1^2 - 4 \times 1 \times (-3)}}{2}$	2	B1 for $\sqrt{1^2 - 4 \times 1 \times (-3)}$ or better and if in the form $\frac{p + \sqrt{q}}{r}$ or $\frac{p - \sqrt{q}}{r}$
	-2.30, 1.30 final answer	2	then B1 for $p = -1$ and $r = 2(1)$ or better
			B1 B1 SC1 for -2.30 and 1.30 seen or -2.3 or -2.303 to -2.302 and 1.3 or 1.302 to 1.303 or final answer -1.30 and 2.30
(b)	4, 30, 53	3	M1 for $(2x + 7)^2 + (2x + 7) - 3$ and B1 for $(2x + 7)^2 = 4x^2 + 14x + 14x + 49$ oe
(c)	$\frac{x - 7}{2}$	2	M1 for $y - 7 = 2x$ or $x = 2y + 7$ or -7 then $\div 2$ clearly seen in correct order with arrow or better or $\frac{y - 7}{2}$
(d)	-2	1	
(e)	1.158×10^{77}	4	B3 for 1.16×10^{77} or $1.1579... \times 10^{77}$ or 1.157×10^{77} or B2 for 2^{256} seen or B1 for 2^8 seen or 256

Question 3

(a)	Enlargement [centre] $(-3, 4)$ [scale factor] 3	1 1 1	Do not allow column vector for coordinates
(b) (i)	Image at $(1, 5), (4, 5), (4, 6), (1, 7)$	2	SC1 for translation by $\begin{pmatrix} 5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 4 \end{pmatrix}$
(ii)	Image at $(5, 1), (8, 1), (8, 3), (5, 2)$	2	SC1 for reflection in $y = 2$
(iii)	Image at $(-4, 3), (-1, 3), (-1, 6), (-4, 9)$	2	SC1 for three correct vertices or shape with vertices at $(-4, 1)$ and $(-1, 1), (-1, 4)$ and $(-4, 7)$

Question 4

(a) (i)	$\frac{3}{2}$ or 1.5	2	M1 for $\frac{14 - (-4)}{8 - (-4)}$ oe
(ii)	$y = \frac{3}{2}x + 2$ oe	2	B1 for $y = \text{their } \frac{3}{2}x + c$ o.e. or $y = mx + 2, m \neq 0$ SC1 for $\frac{3}{2}x + 2$
(iii)	$\begin{pmatrix} 12 \\ 18 \end{pmatrix}$	1	
(iv)	21.6 or 21.63[...]	2	M1 FT for $\text{their } 12^2 + \text{their } 18^2$ oe

(b) (i)	(a) $3b - 4a$	1	
	(b) $\frac{1}{5}(6b - 8a)$ oe simplified	2	M1 for $\frac{1}{5}(12a + 6b) - 4a$ or $AR = AO + OR$
	(c) $6a + 3b$ oe simplified	1	

Question 5

(a) (i) Reflection $x = -2$ oe	2	B1 for either
(ii) Translation $\begin{pmatrix} -7 \\ 2 \end{pmatrix}$ oe	2	B1 for either
(iii) Stretch x -axis oe invariant [factor] 3	3	B1 for each
(b) (i) Triangle with coords at (8, 2) (7, 3) and (7, 5)	2	B1 for rotation about (6, 0) but 90° anticlockwise Or for rotation 90° clockwise around any point
(ii) Triangle with coords at (-2, -5) (-6, -5) and (-8, -7)	2	B1 for 2 correct points or for enlargement of SF -2 any centre

Question 6

(a) (i) -6	1	
(ii) 2.75 oe	2	M1 for $[g(x) =] 0.5$ or $7/14$ Or $\left(\frac{7}{x+1}\right)^2 + 5\left(\frac{7}{x+1}\right)$ oe
(b) $\frac{x-3}{4}$ or $\frac{x}{4} - \frac{3}{4}$ Final answer	2	M1 for $y - 3 = 4x$ or better or $x = 4y + 3$ or better or $\frac{y}{4} = \frac{3}{4} + x$ or flowchart with - 3 then $\div 4$

(c) (i) 5

2

M1 for $4x = 23 - 3$ or $x + \frac{3}{4} = \frac{23}{4}$ or better

(ii) $x^2 + 5x - 7 = 0$

B1

May be implied by correct values in formula

$$\frac{-5 \pm \sqrt{5^2 - 4(1)(-7)}}{2(1)} \text{ oe}$$

B1

B1 for $\sqrt{5^2 - 4(1)(-7)}$ or better [53]

B1

If in form $\frac{p + \sqrt{q}}{r}$ or $\frac{p - \sqrt{q}}{r}$, **B1** for -5 and $2(1)$ or better

No recovery of full line unless seen

1.14 and -6.14 final answers

B1

Or SC1 for 1.1 or 1.140... and -6.1 or $-6.140 \dots$

B1

Or answers -1.14 and 6.14

Question 7

(i) -15

2

B1 for $[h(3) =] 8$ seen
or **M1** for $1 - 2(x^2 - 1)$ or better

(ii) $\frac{1-x}{2}$ or $\frac{1}{2} - \frac{x}{2}$ oe final answer

2

M1 for $2x = 1 - y$ or $x = 1 - 2y$ or better

(iii) $-2, 2$

3

M1 for $x^2 - 1 = 3$ or better
B1 for one answer

(iv) $\frac{1}{8}$ oe nfw

3

M2 for $8x = 1$ or $8x - 1 = 0$
or **M1** for $1 - 2(3x) [= 2x]$

Question 8

(a) (i) Correct reflection to $(4, 8)$
 $(2, 9)$ $(4, 9)$

2

SC1 for reflection in line $x = 5$
or reflection in $y = k$
Ignore additional triangles

(ii) Correct rotation to $(4, 2)$, $(4, 3)$
 $(6, 3)$

2

SC1 for rotation 180° with incorrect centre
Ignore additional triangles

(b) (i) $\mathbf{p} + 2\mathbf{s}$ final answer	2	M1 for recognising \overrightarrow{OQ} as position vector soi
(ii) $\mathbf{s} + \frac{1}{2}\mathbf{p}$ final answer	2	B1 for $\mathbf{s} + k\mathbf{p}$ or $k\mathbf{s} + \frac{1}{2}\mathbf{p}$ or correct route ($k \neq 0$)
(c) parallel and $OQ = 2SR$ oe	1	

Question 9

(a) $4 - 6x$ final answer	1	
(b) $9x - 8$ final answer	2	M1 for $4 - 3(4 - 3x)$ seen
(c) $\frac{1}{27}$ final answer	3	M2 for 3^{-3} soi by final answer 0.037037... to 3sf or better or M1 for $[g(-1) =] 3$ soi
(d) $\frac{4-x}{3}$ oe final answer	2	M1 for a correct first step $3x = 4 - y$ oe or $x = 4 - 3y$ or $\frac{y}{3} = \frac{4}{3} - x$
(e) $\frac{4}{3}$ or $1\frac{1}{3}$ or 1.33 or better	3	M2 for $3x - 4 = 0$ or better or M1 for $3^{-(4-3x)}$

Question 10

(a) $4 - 6x$ final answer	1	
(b) $9x - 8$ final answer	2	M1 for $4 - 3(4 - 3x)$ seen
(c) $\frac{1}{27}$ final answer	3	M2 for 3^{-3} soi by final answer 0.037037... to 3sf or better or M1 for $[g(-1) =] 3$ soi
(d) $\frac{4-x}{3}$ oe final answer	2	M1 for a correct first step $3x = 4 - y$ oe or $x = 4 - 3y$ or $\frac{y}{3} = \frac{4}{3} - x$
(e) $\frac{4}{3}$ or $1\frac{1}{3}$ or 1.33 or better	3	M2 for $3x - 4 = 0$ or better or M1 for $3^{-(4-3x)}$

Question 11

(a) (i)	$\begin{pmatrix} 2 \\ 4 \end{pmatrix}$	1	
(ii)	5.83 to 5.831	2	M1 for $3^2 + 5^2$ seen
(b) (i)	$-2\mathbf{p} + \mathbf{q}$ oe	1	accept unsimplified
(ii)	$\overrightarrow{PS} = -\mathbf{p} + 2\mathbf{q}$ or $\overrightarrow{SP} = \mathbf{p} - 2\mathbf{q}$	B1	
	$\overrightarrow{MS} = -\frac{2}{3}\mathbf{p} + \frac{4}{3}\mathbf{q}$ seen	B1	
	or $\overrightarrow{SM} = \frac{2}{3}\mathbf{p} - \frac{4}{3}\mathbf{q}$ seen		
	or $\overrightarrow{RM} = \frac{2}{3}(-2\mathbf{p} + \mathbf{q})$ soi		
	or $\overrightarrow{MR} = \frac{2}{3}(2\mathbf{p} - \mathbf{q})$ soi		
	or $\overrightarrow{MQ} = \frac{1}{3}(-2\mathbf{p} + \mathbf{q})$ soi		
	or $\overrightarrow{QM} = \frac{1}{3}(2\mathbf{p} - \mathbf{q})$ soi		
	$\overrightarrow{PM} = \mathbf{p} + \overrightarrow{RM}$	M1	Any correct route for \overrightarrow{PM} eg $\overrightarrow{PR} + \overrightarrow{RM}$
	or $\mathbf{p} - \overrightarrow{MR}$		
	or $-\mathbf{p} + \mathbf{q} + \overrightarrow{QM}$		
	or $-\mathbf{p} + \mathbf{q} - \overrightarrow{MQ}$		
	[$= -\frac{1}{3}\mathbf{p} + \frac{2}{3}\mathbf{q}$]		
	1 : 3 nfw	A1	After 0 scored, SC1 for 1 : 3

Question 12

(a)	2	2	B1 for $g\left(\frac{1}{2}\right) = \frac{1}{2}$ soi or $[fg=]\frac{1}{1-x}$
(b)	$1-x$	1	Accept equivalents e.g. $-(x-1)$
(c)	$x^2 - 2x + 2$	3	M1 for $(1-x)^2 + 1$ B1 for $[(1-x)^2 =]1-x-x+x^2$ or better
(d)	-6	1	
(e)	$\sqrt{(-3)^2 - 4(1)(1)}$ or better $p = -(-3)$ and $r = 2 \times 1$ oe	B1	or for $\left(x - \frac{3}{2}\right)^2$ Must see $\frac{p+\sqrt{q}}{r}$ or $\frac{p-\sqrt{q}}{r}$ or both
	0.38, 2.62		or for $\frac{3}{2} + or - \sqrt{\left(\frac{3}{2}\right)^2 - 1}$
(f)	$f(x)$ and $g(x)$	B1B1 1	SC1 for answers 0.4 and 2.6 or 0.3819 to 0.3820 and 2.618... or 0.38 and 2.62 seen in working or for -0.38 and -2.62 as final ans Accept f and g or $1/x$ and $1-x$

Question 13

(a)	Image at $(-3, 2), (-5, 2), (-5, 4), (-3, 3)$	2	SC1 reflection in $y = -1$ or $x = k$ or 4 correct points not joined
(b)	Image at $(-2, -4), (-6, -4), (-6, -8), (-2, -6)$	2	SC1 other enlargement of scale factor -2, correct size and correct orientation or 4 correct points not joined

Question 14

(a) (i)	$(-5, 7)$	1	
(ii)	5	2	M1 for $\sqrt{(-3)^2 + 4^2}$ or better
(b) (i)	(a) $\frac{3}{5}\mathbf{a} + \frac{2}{5}\mathbf{b}$ or $\frac{1}{5}(3\mathbf{a} + 2\mathbf{b})$ final answer	2	M1 for any correct vector path for \overrightarrow{ON}
	(b) $\frac{2}{5}\mathbf{a}$	2	M1 for any correct vector path for \overrightarrow{NY}
(ii)	$NY = \frac{2}{5}BC$ oe [NY] parallel to [BC]	1dep	dep on (b)(i)(b) correct
		1dep	dep on $\overrightarrow{NY} = k\mathbf{a}$, $k \neq 1$

Question 15

(i)	5	1	
(ii)	$-2\frac{1}{3}$ oe	2	B1 for $[h(-1) =] \frac{1}{3}$ soi or M1 for $2(3^x) - 3$
(iii)	$\frac{x+3}{2}$ or $\frac{x}{2} + 1.5$ as final ans	2	M1 for $y + 3 = 2x$ or $x = 2y - 3$ or $\frac{y}{2} = x - 1.5$ or better or correct reverse flowchart
(iv)	$4x - 9$ as final answer nfw	2	M1 for $2(2x - 3) - 3$
(v)	$(2x - 3)(x + 1) = 1 + 2(x + 1)$ $2x^2 - 3x + 2x - 3$ or better seen $2x^2 - 3x - 6 = 0$	M1 B1 A1	$(2x - 5)(x + 1) = 1$ (eliminate fractions) $2x^2 - 5x + 2x - 5$ or better seen No errors or omissions seen

Question 16

(i)	Image: $(-4, -3), (-4, -1), (-3, -1)$	2	SC1 for translation $\begin{pmatrix} -5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -4 \end{pmatrix}$
(ii)	Image: $(1, -1), (3, -1), (3, -2)$	2	SC1 for rotation about the origin but 90° anticlockwise

Question 17

(a) (i)	8	1	
(ii)	4	2	M1 for $[g(17) =] \frac{7}{14}$ or $2\left(\frac{7}{x-3}\right)^2 + 7\left(\frac{7}{x-3}\right)$
(b)	4 or -4	3	M2 for $x^2 = 16$ or $x^2 - 16 = 0$ or M1 for $7 = (x-3)(x+3)$ or better
(c)	$2x^2 + 7x - 11 [= 0]$ soi	B1	
	$\frac{-7 \pm \sqrt{(7)^2 - 4(2)(-11)}}{2(2)}$	B1FT	FT $2x^2 + 7x \pm$ their k [$k \neq 0$] oe
		B1FT	B1FT for $\sqrt{7^2 - 4(2)(-11)}$ or better or $\left(x + \frac{7}{4}\right)^2$ oe If in form $\frac{p + \sqrt{q}}{r}$ or $\frac{p - \sqrt{q}}{r}$, B1FT for -7 and 2(2) or better or $-\frac{7}{4} +$ or $-\sqrt{\frac{137}{16}}$ oe
	-4.68, 1.18 final answers	B1B1	If B0 , SC1 for answers -4.7 and 1.2 or -4.676... and 1.176.. seen or for -4.68 and 1.18 seen or for answer 4.68 and -1.18
(d)	$\frac{x+2}{5}$ or $\frac{x}{5} + \frac{2}{5}$	2	M1 for correct first step or better, e.g. $5y = x + 2$ or $x = \frac{y+2}{5}$ or $x = 5y - 2$ or $y + 2 = 5x$ or $\frac{y}{5} = x - \frac{2}{5}$
(e)	-2	1	

Question 18

(a)	Enlargement [SF] $-\frac{1}{2}$ oe [centre] (2, 5)	3	B1 for each
(b) (i)	Image at (-2, 6), (-8, 3), (-4, 3)	2	SC1 for reflection in any vertical line or for 3 correct points not joined
(ii)	Image at (3, -2), (3, 2), (6, 4)	2	SC1 for rotation 90° [anti clockwise] around origin at (-3, 2) (-3, -2) (-6, -4) or for 3 correct points not joined
(iii)	Image at (-5, 1), (-3, -2), (1, -2)	2	SC1 for translation by $\begin{pmatrix} -1 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -5 \end{pmatrix}$ or for 3 correct points not joined

Question 19

(a) (i)	Rotation [centre] (0, 0) or origin 90° [anticlockwise] oe	1 1 1	
(ii)	Enlargement [centre] (-2, 1) [s.f.] - 2	1 1 1	
(b)	vertices at (-3, 4) (-3, 5) (-3, 6) (-2, 6)	2	SC1 for translation by $\begin{pmatrix} 2 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 1 \end{pmatrix}$
(c)	vertices at (7, 3) (7, 4) (7, 5) (6, 5)	2	SC1 for reflection in $y = 1$ or reflection in any vertical line

Question 20

(a)	9	2	B1 for $[f(3) =] 5$ or $2(2x - 1) - 1$
(b)	$4x^2 - 2x$ or $2x(2x - 1)$ final answer	3	M1 for $(2x - 1)^2 + (2x - 1)$ B1 for $[(2x - 1)^2 =] 4x^2 - 2x - 2x + 1$ or $(2x - 1)(2x - 1 + 1)$
(c)	$\frac{x+1}{2}$ oe final answer	2	M1 for $x = 2y - 1$ or $y + 1 = 2x$ or $\frac{y}{2} = x - \frac{1}{2}$
(d)	$\frac{4x+4}{x(x+2)}$ or $\frac{4x+4}{x^2+2x}$ or $\frac{4(x+1)}{x(x+2)}$ or $\frac{4(x+1)}{x^2+2x}$ final answer	4	B1 for $x(x+2)$ oe isw as common denominator B2 for $4x + 4$ as numerator or B1 for $2(x+2) + 2x$ or better as numerator

Question 21

(a) (i)	Triangle at $(-3, 1), (-3, 3), (-4, 3)$	2	SC1 for reflection in line $y = -1$ at $(1, -3), (1, -5), (2, -5)$ or reflection in any vertical line or three correct points not joined
(ii)	Triangle at $(-1, -1), (-2, -3), (-1, -3)$	2	SC1 for rotation 180° but other centre or three correct points not joined
(b) (i)	Translation	1	
	$\begin{pmatrix} -2 \\ 2 \end{pmatrix}$ oe	1	
(ii)	Enlargement	1	
	$(0, 3)$	1	
	[factor] 3	1	

Question 22

(a) (i)	9.43[...]	2	M1 for $5^2 + ([-]8)^2$ or better
(ii)	(-3, 5)	1	
(b) (i)	(a) $\frac{1}{2}(\mathbf{a} + \mathbf{b})$ or $\frac{1}{2}\mathbf{a} + \frac{1}{2}\mathbf{b}$	2	M1 for $\mathbf{a} + \frac{1}{2}\mathbf{AB}$ oe, e.g $\mathbf{a} + \mathbf{AM}$, $\mathbf{OA} + \frac{1}{2}\mathbf{AB}$
	(b) $\frac{1}{4}(\mathbf{a} + \mathbf{b})$ or $\frac{1}{4}\mathbf{a} + \frac{1}{4}\mathbf{b}$	1FT	FT $\frac{1}{2}$ their (b)(i)(a) <u>in terms of a and/or b</u> in simplest form
	(c) $\frac{1}{4}(\mathbf{b} - 3\mathbf{a})$ or $\frac{1}{4}\mathbf{b} - \frac{3}{4}\mathbf{a}$	2	M1 for $-\mathbf{a} +$ their (b)(i)(b) or any correct route
(ii)	3 : 4 final answer	3	M1 for $[\mathbf{AN} =] -\mathbf{a} + \frac{1}{3}\mathbf{b}$

Question 23

(a) (i)	image at (1, 4) (1, 5) (2, 5) (4, 4)	2	SC1 for translation by $\begin{pmatrix} -1 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 3 \end{pmatrix}$ or 4 correct vertices plotted but not joined
(ii)	image at (-2, -1) (-5, -1) (-2, -2) (-3, -2)	2	SC1 for correct size and orientation, wrong position or 4 correct vertices plotted but not joined
(b)	enlargement	B1	
	[centre] (1, 0)	B1	not as column vector
	[scale factor] -3	B1	

Question 24

(a)	8	1	
(b)	3	2	B1 for $[g(0.5) =] 2$ soi or M1 for $2\left(\frac{1}{x}\right) - 1$ or better
(c)	$\frac{x+1}{2}$ final answer	2	M1 for $x = 2y - 1$ or $y + 1 = 2x$ or better or $\frac{y}{2} = x - \frac{1}{2}$
(d)	$4x - 3$	2	M1 for $2(2x - 1) - 1$
(e)	$4x^2 - 4x + 7$	2	B1 for $[(2x - 1)^2] = 4x^2 - 2x - 2x + 1$

(f)	x	1
(g)	$g^{-1}(x) = g(x)$	1
(h)	$fh(x)$	1

Question 25

(a) (i)	Image at $(-2, 5), (1, 5), (1, 7)$	2	SC1 for translation $\begin{pmatrix} -4 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 4 \end{pmatrix}$ or 3 correct vertices plotted but not joined
(ii)	Image at $(2, -3), (5, -3), (5, -5)$	2	SC1 for a reflection in a horizontal line or in the line $x = -1$ or 3 correct vertices plotted but not joined
(b)	Rotation 180 oe $(-1, 0)$	1 1 1	Alt Enlargement SF -1 $(-1, 0)$ Not as column vector
(c) (i)	Reflection $y = -x$ oe	1 1	

Question 26

(a) (i)	11	1	
(ii)	256	2	M1 for $[g(3) =] 8$ or 2^3 or 2^{2^x}
(b)	$\frac{x-5}{2}$ oe final answer	2	M1 for $x = 2y + 5$ or $2x = y - 5$ or better or $\frac{y}{2} = x + \frac{5}{2}$
(c)	$19 - 6x$ final answer	2	M1 for $2(7 - 3x) + 5$
(d)	$-1, 0, 1, 2$	3	Additional values count as errors B2 for one error /omission or B1 for two errors/omissions or M2 for $-2 < x \leq 2$ oe seen or M1 for $-2 < x$ or $x \leq 2$ or $x = -2$ and $x = 2$ or $-4 < 2x \leq 4$

Question 27

(a) (i)	Rotation	1	
	[+] 90 or 90 anticlockwise oe	1	
	$(0, 2)$	1	Not as column vector
(ii)	Reflection	1	
	$y = 1$ oe	1	
(iii)	Enlargement	1	
	[s f] $-\frac{1}{2}$ oe	1	
	Origin oe	1	
	Image at $(4, 1)$ $(6, 1)$ $(6, 5)$ $(4, 3)$	2	ruled or good freehand SC1 for translation $\begin{pmatrix} 2 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -3 \end{pmatrix}$ or for 4 correct vertices not joined

Question 28

(a)	$\mathbf{b} - \mathbf{a}$ or $-\mathbf{a} + \mathbf{b}$	1	
(b)	$\frac{4}{5}\mathbf{b} - \frac{3}{10}\mathbf{a}$ or $\frac{1}{10}(8\mathbf{b} - 3\mathbf{a})$	4	B3 for correct unsimplified expression in \mathbf{a} and \mathbf{b}

Question 29

(a) (i)	11	1	
(ii)	$14x + 3$ final answer	1	
(b)	$17 - 21x$ final answer	2	M1 for $7(2 - 3x) + 3$ oe
(c)	$-\frac{1}{9}$	3	M1 for $3(2 - 3x) = 7$ oe M1 for correct first step
(d)	-1.3	3	M1 for $2 - 3(x + 4) - (7x + 3) = 0$ M1 for $-10x - 13 = 0$ oe If 0 scored, SC1 for answer -0.7 oe after $2 - 3(x + 4) - 7x + 3 = 0$ shown previously

Question 30

(a) (i)	y	1	
(ii)	$x + y$	1	
(iii)	$x + 2y$	2	M1 for a correct unsimplified route or identifying \overline{OS}
(b)	$-(\frac{1}{2}x + y)$ oe	2	M1 for a correct unsimplified route or $\overline{GR} = -\frac{1}{2}x$ or $\overline{RG} = \frac{1}{2}x$
(c) (i)	$\overline{MG} = 2x + 2y$	2	M1 for a correct unsimplified route e.g. $2\overline{PQ}$
(ii)	$\overline{MH} = x + y$ or $\overline{HG} = x + y$	M1	Accept $\overline{HM} = -x - y$ or $\overline{GH} = -x - y$
	$\overline{MG} = 2\overline{MH}$ oe	A1	Dep on (c)(i) correct, arrows essential

Question 31

(a) (i)	Rotation	1	
	90° [anticlockwise] oe	1	
	(4, 4)	1	
(ii)	Enlargement	1	
	[centre] (5, 1)	1	
	[scale factor] 2	1	
(b) (i)	Image at (-2, 5) (-2, 7) (-1, 7)	2	B1 for translation by $\begin{pmatrix} -5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 3 \end{pmatrix}$
(ii)	Image at (-2, 1) (-2, -1) (-1, -1)	2FT	FT <i>their</i> triangle P reflected in line $y = 3$ B1 for reflection of triangle P in the line $x = 3$ or $y = k$

Question 32

(i)	Correct image (2, -5) (4, -5) (4, -1)	2	SC1 for reflection in $y = 0$ or 3 correct points not joined
(ii)	Correct image (-2, 1) (-6, 1) (-6, -1)	2	SC1 for rotation 90 clockwise any centre or 3 correct points not joined
(iii)	Translation by $\begin{pmatrix} 1 \\ 9 \end{pmatrix}$	2	B1 for each
(iv)	Enlargement	1	
	[SF] $-\frac{1}{2}$ oe	1	
	[Centre] (2, 1)	1	

Question 33

<p>(a) (i) -3</p>		2	<p>M1 for $[g(1)=] -2$ provided not used in a product or for $5\left(\frac{4}{x-3}\right)+7$ or better</p>
<p>(ii) $\frac{4}{5x+4}$ final answer</p>		2	<p>M1 for $\frac{4}{5x+7-3}$</p>
<p>(iii) $\frac{4+3x}{x}$ or $\frac{4}{x}+3$ final answer</p>		3	<p>M2 for $xy = 4 + 3x$ or $y - 3 = \frac{4}{x}$ or $x = \frac{4}{y} + 3$ or $x = \frac{4+3y}{y}$ or M1 for $x = \frac{4}{y-3}$ or $y(x-3) = 4$ or $x-3 = \frac{4}{y}$ or $x(y-3) = 4$</p>
<p>(iv) 2</p>		1	
<p>(b) (i) $(5x+7)(x-3) = 4$ $5x^2 - 15x + 7x - 21 = 4$ oe $5x^2 - 8x - 25 = 0$</p>		<p>M1 B1 A1</p>	<p>Condone omission of '=' for the B mark Dep on M1B1 and no errors or omissions at any stage seen</p>
<p>(ii) $\sqrt{(-8)^2 - 4(5)(-25)}$ or better</p>		B1	<p>or for $\left(x - \frac{4}{5}\right)^2$ oe</p>
<p>$p = -(-8)$ and $r = 5 \times 2$ oe</p> <p>-1.57 and 3.17</p>		<p>B1 B1B1</p>	<p>must see $\frac{p+\sqrt{q}}{r}$ or $\frac{p-\sqrt{q}}{r}$ or both or for $\frac{4}{5} + \sqrt{\left(\frac{4}{5}\right)^2 + 5}$ or $\frac{4}{5} - \sqrt{\left(\frac{4}{5}\right)^2 + 5}$ SC1 for final answers -1.6 or -1.574 to -1.575 and 3.2 or 3.174 to 3.175 or -1.57 and 3.17 seen in working or for -3.17 and 1.57 as final ans</p>

Question 34

(i)	Image at (3, 1), (5, 1), (5, 4), (4, 4), (4, 2), (3, 2)	2	SC1 reflection in $y = 1$ or $x = k$ or 6 correct points not joined
(ii)	Image at (2, 1), (6, 1), (6, -5), (4, -5), (4, -1), (2, -1)	2	SC1 for other enlargement of scale factor -2 , correct size and correct orientation or 6 correct points but not joined

Question 35

(a)	2	2	M1 for $2x + 1 = 1 + 4$
(b)	17	2	B1 for $[h(3) =] 8$ soi or $2 \times 2^x + 1$ oe
(c)	$\frac{x-1}{2}$ oe final answer	2	M1 for $y - 1 = 2x$ or $\frac{y}{2} = x + \frac{1}{2}$ or $x = 2y + 1$
(d)	$4x^2 + 4x + 5$ final answer	3	M1 for $(2x+1)^2 + 4$ and B1 for $[(2x+1)^2 =] 4x^2 + 2x + 2x + 1$ or better
(e)	$\sqrt{2}$ or 1.41 or 1.414....	1	
(f)	-1	1	

Question 36

(a) (i)	$\frac{1}{2}\mathbf{p}$	1	
(ii)	$\frac{1}{2}\mathbf{p} - \frac{1}{3}\mathbf{r}$	1	
(iii)	$\mathbf{p} + \frac{2}{3}\mathbf{r}$	1	
(b)	$\mathbf{r} + \frac{3}{2}\mathbf{p}$	2	M1 for correct unsimplified answer or for correct route or for recognising \overline{OU} as position vector
(c)	6 nfw	3	B2 for $(2k)^2 + ([-]k)^2 = 180$ oe or M1 for $(2k)^2 + ([-]k)^2$ oe

Question 37

(i)	Triangle drawn, vertices $(2, -4), (2, -5), (4, -4)$	2	SC1 for translation $\begin{pmatrix} 5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -2 \end{pmatrix}$ or correct points not joined
(ii)	Triangle drawn, vertices $(-3, 4), (-3, 5), (-1, 4)$	2	SC1 for reflection in line $y = k$ or line $x = 1$ or correct points not joined
(iii)	Enlargement	1	
	[factor] 3	1	
	[centre] $(-6, -5)$	1	

Question 38

(a) (i)	$\begin{pmatrix} 12 \\ -5 \end{pmatrix}$	2	M1 for $\begin{pmatrix} 12 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -5 \end{pmatrix}$
(ii)	13 nfw	2FT	M1FT for $\sqrt{\text{their } 12^2 + \text{their } (-5)^2}$ FT dep on <i>their</i> (a) being $\begin{pmatrix} a \\ b \end{pmatrix}$ where a, b are both non-zero
(b)(i)(a)	$\mathbf{b} - \mathbf{a}$	1	
(i)(b)	$\frac{3}{5}(\mathbf{b} - \mathbf{a})$ or $\frac{3}{5}\mathbf{b} - \frac{3}{5}\mathbf{a}$ final answer	1FT	FT $\frac{3}{5}$ <i>their</i> vector, in terms of \mathbf{a} and \mathbf{b} , in (b)(i)(a)
(i)(c)	$\frac{1}{5}(2\mathbf{a} + 3\mathbf{b})$ or $\frac{2}{5}\mathbf{a} + \frac{3}{5}\mathbf{b}$ final answer	2	M1 for $\mathbf{a} + \text{their}$ vector in (b)(i)(b) or any correct route
(ii)	$\frac{3}{2}\text{oe}$	1	

Question 39

(a)	Triangle drawn at (-4, 3), (-1, 3), (-1, 4)	2	SC1 for correct reflection in $x = k$ or $y = 1$
(b)	Triangle drawn at (1, 7), (1, 6), (4, 6)	2	SC1 for translation by $\begin{pmatrix} -2 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 3 \end{pmatrix}$
(c)	Triangle drawn at (2, 3), (2, 1), (8, 1)	2	M1 for two correct vertices or SC1 for correct enlargement about the wrong centre
(d)	Rotation 90° clockwise oe (7, 4)	1 1 1	Accept -90°

Question 40

(a) (i)	1.5 oe	1	
(ii)	$\frac{3}{y-2}$ oe final answer	3	M1 for correct removal of fraction M1 for collection of terms in x and factorises OR M1 subtracts 2 from both sides M1 multiplies by x to remove fraction and M1 for correct division by expression of the form $ay + b$, a and $b \neq 0$
(b) (i)	-3	1	
(ii)	65 536 final answer	2	B1 for h(16) oe e.g. h(2 ⁴)
(iii)	-6	2	M1 for $2 - x = 2^3$ oe
(iv)	3	1	

Question 41

(a)	236	3	B2 for 243 and 7 or M2 for $3^{2(2)+1} - (2(3^{[1]} + 1))$ oe B1 for h(5) or f(3) soi or M1 for $3^{2x+1} - (2(3^x) + 1)$ or better
(b)	$6x + 1$ final answer	2	M1 for $3(2x + 1) - 2$
(c)	$x < 3$ oe final answer	2	M1 for $1 + 2 > 3x - 2x$ or $2x - 3x > -2 - 1$ oe
(d)	-2	1	
(e)	$\frac{x+2}{3}$ oe final answer	2	M1 for $x = 3y - 2$ or $y + 2 = 3x$ or $\frac{y}{3} = x - \frac{2}{3}$
(f)	$\frac{6x^2 - x + 3}{2x + 1}$ final answer	3	M1 for $5 + (2x + 1)(3x - 2)$ or better isw B1 for common denominator $2x + 1$ isw
(g)	9	1	

Question 42

(a) (i)	Image at $(-2, -4), (4, -4), (4, 0)$	2	SC1 for translation $\begin{pmatrix} -4 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -8 \end{pmatrix}$
(ii)	8.94 or 8.944...	2	M1 for $\sqrt{(-4)^2 + (-8)^2}$ or $\sqrt{4^2 + 8^2}$
(b) (i)	Enlargement [factor] 0.5 oe [centre] (0, 0) oe	1 1 1	

Question 43

(a)(i)	Translation	1
	$\begin{pmatrix} 3 \\ -13 \end{pmatrix}$ oe	1
(a)(ii)	Enlargement	1
	[sf] $-\frac{1}{2}$ oe	1
	(0, -4)	1

(b)	Image at (0, 0) (0, 6) (-4, 6) (-4, 2)	2	B1 for rotation of 90° anticlockwise about the wrong centre or 90° clockwise about (3, -1) or 4 points correct but not joined.
(c)	Image at (4, 0) (10, 0) (10, -4) (6, -4)	2	B1 for reflection in $y = k$ or in $x = 1$ or 4 points correct but not joined

Question 44

(a)	-11	1	
(b)	7	2	M1 for $3x - 2 = 19$ or better
(c)	25	2	M1 for $3 \times 3^x - 2$ oe
(d)	$9x^2 - 8x + 2$ final answer	3	M1 for $(3x - 2)^2 + 3x - 2 + x$ oe B1 for $[(3x - 2)^2 =] 9x^2 - 6x - 6x + 4$ oe
(e)	$\frac{x+2}{3}$ oe final answer	2	M1 for $x = 3y - 2$ or $y + 2 = 3x$ or $\frac{y}{3} = x - \frac{2}{3}$ or better

Question 46

(i)	Image at (8, 1), (10, 5), (8, 5)	2	B1 for translation $\begin{pmatrix} 6 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -5 \end{pmatrix}$ or 3 correct points not joined
(ii)	Image at (4, 10), (4, 8), (8, 8)	2	B1 for rotation 90° anticlockwise but different centre or for rotation 90° clockwise about (4, 10) or 3 correct points not joined
(iii)	Image at (6, 3), (6, 5), (7, 5)	2	B1 for enlargement factor $\frac{1}{2}$ but incorrect centre or 3 correct points not joined

Question 47

(a)(i)	Image at (5, 1), (7, 1), (7, 4)	2	B1 reflection in $y = 4$ or $x = k$
(a)(ii)	Image at (-1, 1), (-4, 1), (-1, 3)	2	B1 correct size and correct orientation wrong position or for rotation 90° clockwise around (0, 0)
(a)(iii)	Image at (2, -4), (4, -4), (2, -1)	2	B1 for translation by $\begin{pmatrix} 1 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -5 \end{pmatrix}$
(b)	Enlargement	1	
	[sf] - 0.5 oe	1	
	(5, 5)	1	

Question 48

(i)	Image at (0, 1), (0, 2), (-3, 1)	2	B1 for reflection in $y = 0$ or $x = k$
(ii)	Image at (0, 0), (0, -2), (6, -2)	2	B1 for correct size and correct orientation wrong position or for 2 correct vertices plotted
(iii)	Image at (-5, 4), (-5, 5), (-2, 4)	2	B1 for translation by $\begin{pmatrix} -5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 3 \end{pmatrix}$
(b)	Rotation 90° clockwise oe (4, -1)	3	B1 for each

Question 49

(a)	3	1	
(b)	$-\frac{2}{5}$ oe	2	M1 for $2(1-2x) = x+4$
(c)	$-2x-7$ final answer	2	M1 for $1-2(x+4)$
(d)	26	2	B1 for $h(5)$ soi or M1 for $(x^2+1)^2+1$
(e)	$\frac{1-x}{2}$ oe final answer	2	M1 for $x = 1-2y$ or $2x = 1-y$ or $\frac{y}{2} = \frac{1}{2} - x$ or $y-1 = -2x$

(f)	$[p =] - 20$ $[q =] 26$	4	B3 for $[hgf(x)] = 4x^2 - 20x + 26$ seen and not spoiled by further working or M1 for $(1 - 2x) + 4$ M1 dep for $(their (5 - 2x))^2 + 1$ B1FT dep for $25 - 10x - 10x + 4x^2$
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Question 50

(a)(i)	Correct translation	2	B1 for translation $\begin{pmatrix} 6 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -2 \end{pmatrix}$
(a)(ii)	Correct rotation	2	B1 for rotation 180° but other centre
(a)(iii)	Correct reflection	2	B1 for reflection in $y = -x$
(b)(i)	Enlargement [factor] $\frac{1}{2}$ or 0.5 [centre] (0, 0) oe	3	B1 for each
(c)	± 2.5	3	B2 for $25u^2 = 156.25$ or $5u = [\pm]12.5$ or M1 for $(4u)^2 + (3u)^2$

Question 51

(a)(i)	26	2	M1 for $g(5)$ or for $(x^2 + 1)^2 + 1$
(a)(ii)	$x^2 + 4x + 5$	2	M1 for $(x + 2)^2 + 1$
(a)(iii)	5	2	M1 for $2x - 3 = 7$
(a)(iv)	$\frac{x+3}{2}$ oe	2	M1 for $x = 2y - 3$ or $y + 3 = 2x$ or $\frac{y}{2} = x - \frac{3}{2}$ oe
(b)(i)	[0].70 cao	2	B1 for [0].696 to [0].697
(b)(ii)	4 cao	1	

Question 52

(a)(i)	1	2	M1 for $h(0)$ or for 2^{8-3x}
(a)(ii)	8	2	M1 for $g(\frac{1}{4})$ or for $\frac{10}{2^x + 1}$
(a)(iii)	$\frac{10-x}{x}$ or $\frac{10}{x} - 1$ final answer	3	M2 for $x = \frac{10-y}{y}$ or better or $xy = 10 - x$ or better or $y + 1 = \frac{10}{x}$ or M1 for $x(y + 1) = 10$ or $y(x + 1) = 10$ or $x = \frac{10}{y+1}$ or $x + 1 = \frac{10}{y}$
(a)(iv)	5	1	
(b)	$\frac{-3x^2 + 5x + 18}{x + 1}$ final answer	3	M1 for $\frac{(8-3x)(x+1) + 10}{x+1}$ B1 for $-3x^2 - 3x + 8x + 8$ [+10]

Question 53

(a)(i)	Image at (3, -3), (7, -3), (7, -5)	2	B1 for reflection in any $x = k$ or if 3 correct points not joined
(a)(ii)	Image at (-5, 1), (-1, 1), (-5, -1)	2	B1 for translation by $\begin{pmatrix} -2 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 4 \end{pmatrix}$ or if 3 correct points not joined
(a)(iii)	Image at (6, 3), (6, 4), (4, 3)	3	B2 for correct size and orientation but wrong position or if 3 correct points not joined B1 for enlargement SF $\frac{1}{2}$ with centre (3, 1)
(b)	Rotation 90° [anticlockwise]oe (-6, -2)	3	B1 for each

Question 54

(a)(i)	12.6 or 12.64 to 12.65	3	M2 for $12^2 + (-4)^2$ OR B1 for $\begin{pmatrix} 12 \\ -4 \end{pmatrix}$ M1 for $(their\ 12)^2 + (their\ -4)^2$
(a)(ii)	$\begin{pmatrix} -11 \\ 13 \end{pmatrix}$	2	B1 for $\begin{pmatrix} -11 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 13 \end{pmatrix}$ or for $[\overline{BA} =] \begin{pmatrix} -8 \\ 7 \end{pmatrix}$
(b)	$\frac{1}{2}(\mathbf{b} - \mathbf{a})$ oe	2	M1 for correct route or correct unsimplified answer or B1 for $\overline{QS} = \mathbf{b} - \mathbf{a}$ oe

Question 55

(a)(i)	Translation $\begin{pmatrix} -8 \\ 2 \end{pmatrix}$ oe	2	B1 for each
(a)(ii)	Enlargement [sf =] $\frac{1}{2}$ oe $(-4, 0)$	3	B1 for each
(a)(iii)	Rotation 90° clockwise oe $(1, -1)$	3	B1 for each
(b)	Triangle with $(1, -1), (5, -1), (1, 7)$	2	B1 for correct size and orientation in wrong position or for 3 correct points not joined

Question 56

(a)(i)	$\begin{pmatrix} -19 \\ -2 \end{pmatrix}$	2	B1 for answer $\begin{pmatrix} -19 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -2 \end{pmatrix}$ or for $\begin{pmatrix} -9 \\ 6 \end{pmatrix}$ or $\pm \begin{pmatrix} 10 \\ 8 \end{pmatrix}$ seen
(a)(ii)	3.61 or 3.605 to 3.606	2	M1 for $\sqrt{([-]3)^2 + 2^2}$ oe
(a)(iii)	$-3m + 5n = 14$ and $2m + 4n = 9$	B1	Accept equivalents
	$[m =] -\frac{1}{2}$ or -0.5 and $[n =] 2\frac{1}{2}$ or 2.5 or $\frac{5}{2}$ with evidence of a correct algebraic method	4	M1 for correctly equating one set of coefficients of <i>their</i> equations or rearranges one of <i>their</i> equations to make <i>m</i> or <i>n</i> the subject e.g. $[m =] \frac{1}{2}(9 - 4n)$ oe M1 for correct method to eliminate one variable for <i>their</i> equations or correctly substitutes <i>their m</i> or <i>their n</i> into the other equation e.g. $-\frac{3(9 - 4n)}{2} + 5n = 14$ oe B1 for one correct answer
(b)(i)(a)	$-\mathbf{a} + 2\mathbf{c}$	1	
(b)(i)(b)	$\frac{3}{8}(-\mathbf{a} + 2\mathbf{c})$ or $-\frac{3}{8}\mathbf{a} + \frac{3}{4}\mathbf{c}$ oe	1	FT $\frac{3}{8}$ (<i>their (b)(i)(a)</i>) in simplest form
(b)(i)(c)	$\frac{1}{2}(5\mathbf{a} - 2\mathbf{c})$ or $\frac{5}{2}\mathbf{a} - \mathbf{c}$ oe	1	
(b)(i)(d)	$\frac{1}{8}(5\mathbf{a} - 2\mathbf{c})$ or $\frac{5}{8}\mathbf{a} - \frac{1}{4}\mathbf{c}$ oe	2	M1 for a correct unsimplified route
1(b)(ii)	4	1	

Question 57

(a)	Rotation 90 ^[o] clockwise oe Origin oe	3	B1 for each
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(b)(i)	Image at $(-4, -1)$ $(-4, -4)$ $(-2, -4)$	1	
(b)(ii)	Image at $(3, -1)$ $(5, -1)$ $(3, -4)$	2	B1 for translation by $\begin{pmatrix} 7 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -5 \end{pmatrix}$ or for 3 correct points not joined

Question 58

(a)(i)	Translation $\begin{pmatrix} 5 \\ 8 \end{pmatrix}$	2	B1 for each Accept 5 right and 8 up
(a)(ii)	Enlargement [sf] 0.5 oe [centre] $(0, -7)$	3	B1 for each
(a)(iii)	Rotation 90 [anticlockwise] oe Origin oe	3	B1 for each
(b)	Image at $(-8, 1)$ $(-8, 5)$ $(-8, 7)$ $(-4, 1)$	2	B1 for reflection of flag A in the line $x = -1$ or $y = k$ or for vertices of triangle in correct place but not joined

Question 59

(a)	-3	1	
(b)	$\frac{12}{11}$ oe	2	M1 for $\frac{3}{x+2} + 2$ soi
(c)	$64x - 45$ final answer	2	M1 for $8(8x - 5) - 5$ isw
(d)	$\frac{x+5}{8}$ oe final answer	2	M1 for a correct first step $y + 5 = 8x$, $\frac{y}{8} = x - \frac{5}{8}$ or $x = 8y - 5$
(e)	$\frac{8x^2 + 11x - 13}{x+2}$ final answer	3	M1 for $(8x - 5)(x + 2) - 3$ oe isw B1 for common denominator $(x + 2)$

(f)(i)	$(8x - 5)^2 + 6 = 19$	M1	
	$64x^2 - 40x - 40x + 25$	B1	
	$64x^2 - 40x - 40x + 25 + 6 = 19$ oe leading to $16x^2 - 20x + 3 = 0$	A1	with no errors and must show $(8x - 5)^2 + 6 = 19$ with no omissions after this
(f)(ii)	$\frac{[- -]20 \pm \sqrt{([- -]20)^2 - 4(16)(3)}}{2 \times 16}$ oe	2	B1 for $\sqrt{([- -]20)^2 - 4(16)(3)}$ or better or B1 for $\frac{[- -]20 + \sqrt{q}}{2(16)}$ oe or $\frac{[- -]20 - \sqrt{q}}{2(16)}$
	0.17 and 1.08 final ans	2	B1 for each If 0 scored, SC1 for answer 0.2 and 1.1 or answer - 0.17 and -1.08 or 0.174... and 1.075 to 1.076 seen or 0.17 and 1.08 seen in working

Question 60

(a)(i)	Reflection $x = 1.5$	2	B1 for each
(a)(ii)	Rotation $(0, -1)$ 90° [anticlockwise] oe	3	B1 for each
(b)(i)	Image at $(5, -1)$ $(6, -1)$ $(6, -3)$	2	B1 for correct size and orientation but wrong position If 0 scored, SC1 for enlargement SF $\frac{1}{2}$ with centre $(3, 0)$
(b)(ii)	Image at $(-6, 3)$ $(-4, 3)$ $(-6, 7)$	2	B1 for translation $\begin{pmatrix} -3 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 1 \end{pmatrix}$

Question 61

(a)(i)	Reflection $x = 1.5$	2	B1 for each
(a)(ii)	Rotation $(0, -1)$ 90° [anticlockwise] oe	3	B1 for each
(b)(i)	Image at $(5, -1)$ $(6, -1)$ $(6, -3)$	2	B1 for correct size and orientation but wrong position If 0 scored, SC1 for enlargement SF $\frac{1}{2}$ with centre $(3, 0)$
(b)(ii)	Image at $(-6, 3)$ $(-4, 3)$ $(-6, 7)$	2	B1 for translation $\begin{pmatrix} -3 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 1 \end{pmatrix}$

Question 62

(a)	82	2	M1 for $(3^x)^2+1$ soi by $(3^2)^2+1$ or $g(9)$ isw
(b)	$\frac{x+2}{7}$ final answer	2	M1 for $y+2=7x$ or $\frac{y}{7}=x-\frac{2}{7}$ or $x=7y-2$
(c)	$[a=] 1, [b=] 2, [c=] 2$	3	B2 for $x^4+x^2+x^2+1+1$ or M1 for $(x^2+1)^2+1$
(d)	$\frac{6}{7}$ oe	3	M2 for $7x-2=4$ or M1 for $3^x=81$ soi $f(x)=4$ or for $3^{7x-2}=81$ or better

Question 63

(a)(i)	Image at (1, 7), (4, 7), (4, 9), (3, 9)	2	B1 for translation by $\begin{pmatrix} -1 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 6 \end{pmatrix}$
(a)(ii)	Image at (5, 3), (6, 3), (8, 5), (5, 5)	2	B1 for 180° rotation with wrong centre
(a)(iii)	Rotation 180° (4.5, 6) OR Enlargement, [factor] – 1 (4.5, 6)	3	B1 for rotation B1 for 180° B1FT for centre from <i>their</i> (a)(i) B1 for enlargement B1 for – 1 B1FT for centre from <i>their</i> (a)(i)
(b)(i)	Image at (1, 2), (1, 5), (3, 5), (3, 4)	2	B1 for $y = x$ drawn or for 3 correct points

Question 64

(a)(i)	5	1	
(a)(ii)	1	2	M1 for $h(0)$ or 3^{9-x^2} or better
(a)(iii)	$9 - 4x^2$ final answer	1	
(a)(iv)	$15 - 2x^2$ final answer	2	M1 for $2(9 - x^2) - 3$ or better
(b)	$\frac{x+3}{2}$ final answer	2	M1 for $x = 2y - 3$ or $y + 3 = 2x$ or better or $\frac{y}{2} = x - \frac{3}{2}$
(c)	1.8 or $1\frac{4}{5}$ or $\frac{9}{5}$	2	M1 for $10x - 15 = 3$ or $2x - 3 = \frac{3}{5}$
(d)	-1 and 4 nfww	4	M1 for $9 - (2x - 3)^2 = -16$ A1 for $4x^2 - 12x - 16 = 0$ oe M1 (dep on first M1) for correct factors or use of formula or completing the square for their 3-term quadratic

		OR
		M1 for $9 - y^2 = -16$
		A1 for $y^2 = 25$
		M1 (dep on first M1) for $2x - 3 = \pm 5$
(e)	$\frac{1}{9}$	1

Question 65

(a)	Reflection $y = -1$	2	B1 for each
(b)(i)	Image at (-6, 5) (-6, 7) (-5, 7) (-4, 5)	2	B1 for translation by $\begin{pmatrix} -3 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 4 \end{pmatrix}$
(b)(ii)	Image at (1, -1) (3, -1) (3, -3) (2, -3)	2	B1 for shape correct size and orientation but wrong position
(b)(iii)	Image at (1, 2) (1, 6) (3, 6) (5, 2)	2	B1 for shape correct size and orientation, wrong position

Question 66

(i)	$\begin{pmatrix} 0 \\ 5 \end{pmatrix}$	1
(ii)	$\begin{pmatrix} -3 \\ -1 \end{pmatrix}$	1

(iii)	3.22 or 3.216... to 3.220...	6	B3 for [angle $AOB =$] 36.8 or 36.9 or 36.84 to 36.87 or M2 for $\tan[AOB] = \frac{3}{4}$ oe or for $[AOB =]2 \times \sin^{-1}$ $\left(\frac{\sqrt{(5-4)^2 + (0-(-3))^2}}{10}\right)$ oe or for $\cos [AOB =]$ $\frac{5^2 + 5^2 - \left(\sqrt{(5-4)^2 + (0-(-3))^2}\right)^2}{2 \times 5 \times 5}$ oe or M1 for recognition of right-angle with perpendicular from B to OA or x -axis or for $[AB^2 =](5-4)^2 + (0-(-3))^2$ or better oe or $(their\ AB)^2 = 5^2 + 5^2 - 2 \times 5 \times 5 \times \cos OAB$ oe M2 for $\frac{their\ angle\ AOB}{360} \times 2 \times \pi \times 5$ oe or M1 for radius = 5 soi
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Question 67

(a)(i)	13	1	
(a)(ii)	3	2	M1 for $h\left(\frac{10}{30}\right)$ oe soi or $27^{\frac{10}{x}}$
(a)(iii)	$\frac{7-x}{2}$ oe final answer	2	M1 for $x = 7 - 2y$ or $y - 7 = -2x$ or $7 - y = 2x$ or $-\frac{y}{2} = -\frac{7}{2} + x$ oe
(b)	0.75 oe final answer	3	M1 for $\frac{10}{2x+1} = 4$ M1 for $10 = 8x + 4$ or better
(c)	$\frac{70-19x}{x(7-2x)}$ or $\frac{70-19x}{7x-2x^2}$ final answer	3	M1 for $x + 10(7-2x)$ or better isw B1 for common denominator $x(7-2x)$ oe isw
(d)	3 final answer	1	

Question 68

(a)(i)	(3, 5.5)	2	B1 for either value correct
(a)(ii)	$\frac{5}{4}x + \frac{7}{4}$ final answer	3	B2 for answer $\frac{5}{4}x + c$ oe or for correct equation in different form or M1 for $\frac{8-3}{5-1}$ oe and M1 for correct substitution shown of (1, 3) or (5, 8) or <i>their</i> (a)(i) into $y = (\text{their } m)x + c$ oe
(b)(i)	(6, 1) (10, 6)	2	B1 for 2 or 3 values correct
(b)(ii)	(-3, 1) (-8, 5)	2	B1 for 2 or 3 values correct If 0 scored, SC1 for (3, -1) and (8, -5)
(b)(iii)	(3, 3) (-1, 8)	2	B1 for 2 or 3 values correct but not for (1, 3) and (5, 8)

Question 69

(a)(i)	$4x - 13$ final answer	1	
(a)(ii)	$25x^2$ final answer	1	
(b)	$\frac{x+1}{4}$ or $\frac{x}{4} + \frac{1}{4}$	2	M1 for correct first step $x = 4y - 1$ or $y + 1 = 4x$ or $\frac{y}{4} = x - \frac{1}{4}$
(c)	0.6934 final answer	3	B2 for 0.69336... or $3^{-\frac{1}{3}}$ oe or 0.693 or M1 for $3^{-3^{-x}}$ oe
(d)(i)	$(3x - 2)^2 - 3^{-(-3)}$	M1	
	$9x^2 - 6x - 6x + 4 - 27$ or $9x^2 - 12x + 4 - 27$ leading to $9x^2 - 12x - 23$	A1	with no errors seen

(d)(ii)	$\frac{-(-12) \pm \sqrt{(-12)^2 - 4(9)(-23)}}{2 \times 9}$ or better	B2	B1 for $\sqrt{(-12)^2 - 4(9)(-23)}$ oe or $\frac{-(-12) + \sqrt{q}}{2 \times 9}$ oe or $\frac{-(-12) - \sqrt{q}}{2 \times 9}$ oe or both
	- 1.07, 2.40 final answers	B2	B1 for each If B0 , SC1 for answers - 1.1 or -1.06 or -1.065... to - 1.065 and 2.4 or 2.39 or 2.398 to 2.398... or - 1.07 and 2.40 seen in working or for -2.40 and 1.07 as final answer
(e)	-5 final answer	2	M1 for $243 = 3^{-x}$

Question 70

(a)	4	1	
(b)	52	2	M1 for $f(8)$ seen or $7 \times \frac{2x}{x-3} - 4$
(c)	$7x^2 - 4$	1	
(d)	$\frac{7x^2 - 21x + 12}{2(x-3)}$ or $\frac{7x^2 - 21x + 12}{2x-6}$ final answer	3	M1 for $(7x-4)(x-3) + 2 \times 2x$ B1 for denominator $2(x-3)$ or $2x-6$
(e)	-3	2	M1 for $7x+14-4=-11$
(f)	$[p =] 0$ and $[p =] 1$	2	B1 for each

Question 71

(a)(i)	triangle with vertices at (-2, -1) (-8, -1) (-2, -5)	2	B1 for correct reflection in $y = x$
(a)(ii)	triangle with vertices at (-1, -1) (-1, -7) (3, -7)	2	B1 for translation by $\begin{pmatrix} k \\ -9 \end{pmatrix}$ or $\begin{pmatrix} -2 \\ k \end{pmatrix}$
(b)(i)	Enlargement [centre] (-7, 8) [sf] $\frac{1}{2}$	3	B1 for each
(b)(ii)	Rotation [centre] (0, 0) 90° clockwise oe	3	B1 for each

Question 72

i(a)	256	1	
i(b)	8	2	M1 for $3(x^2 + 1) + 2$ or for $3(2) + 2$
i(c)	$9x^2 + 12x + 5$	3	M1 for $(3x + 2)^2 + 1$ B1 for $[(3x + 2)^2 =] 9x^2 + 6x + 6x + 4$ oe
i(d)	16	2	M1 for $3x + 2 = 7^2 + 1$ or better
i(e)	$\frac{x-2}{3}$ oe final answer	2	M1 for $x = 3y + 2$ or for $y - 2 = 3x$ or for $\frac{y}{3} = x + \frac{2}{3}$
i(f)	$\frac{4x^2 + 2x + 1}{3x + 2}$ final answer	3	B1 for $x^2 + 1 + x(3x + 2)$ or better seen M1 for common denominator $3x + 2$
i(g)	16	1	

Question 73

(a)(i)	$\begin{pmatrix} 6 \\ 17 \end{pmatrix}$	2	B1 for each
(a)(ii)	6.4[0] or 6.403...	2	M1 for $4^2 + 5^2$
(b)	(1, 2)	1	
(c)	(0, -2)	1	
(d)	$\frac{1}{2}\mathbf{c} + \frac{1}{3}\mathbf{d}$	3	B2 for correct unsimplified answer or M1 for $\overrightarrow{CT} = -\mathbf{c} + \frac{2}{3}\mathbf{d}$ oe or $\overrightarrow{TC} = \mathbf{c} - \frac{2}{3}\mathbf{d}$ oe or for correct route

Question 74

(a)	Triangle at $(-4, -4)$ $(-1, -3)$ $(-4, -3)$	2	B1 for correct points not joined or for reflection in any $y = k$ or for reflection in $x = -1$
(b)	Triangle at $(1, 1)$ $(1, 4)$ $(2, 4)$	2	B1 for correct points not joined or rotation 90 clockwise around any point or rotation 90 anticlockwise around $(0, 0)$
(c)	Translation $\begin{pmatrix} 5 \\ -6 \end{pmatrix}$	2	B1 for translation or correct vector oe

Question 75

(a)	-23	2	M1 for $4 - 3(3^x)$ oe soi
(b)	$\frac{4-x}{3}$ oe final answer	2	M1 for $x = 4 - 3y$ or $y + 3x = 4$ or $x + 3y = 4$ or $\frac{y}{-3} = \frac{4}{-3} + x$ oe or $\frac{x}{-3} = \frac{4}{-3} + y$ oe
(c)(i)	$1 + 6x$ final answer	2	M1 for $4 - 3(1 - 2x)$
(c)(ii)	$20 - 36x$ or $4(5 - 9x)$ final answer	4	B3 for $20 - 36x$ seen in working then spoiled OR M1 for $(4 - 3x)^2 + 4 - 3x - 9(x^2 + x)$ or better B1 for $[(4 - 3x)^2 =] 16 - 12x - 12x + 9x^2$ or better B1 for answer $20 - kx$ or $k - 36x$ oe or answer $20 - 36x + kx^2$ $k \neq 0$
(d)	$-\frac{1}{2}$ oe	2	M1 for $(3^2)^{kx}$ or $9^{kx} = 9^{\frac{1}{2}x}$ oe

Question 76

(a)(i)	Triangle at $(-3, 2)$ $(-3, 3)$ $(-5, 2)$	2	B1 for correct rotation about incorrect point or for rotation 90 clockwise around $(0, 0)$
(a)(ii)	Triangle at $(5, -2)$ $(6, -2)$ $(5, 0)$	2	B1 for translation by $\begin{pmatrix} 3 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -5 \end{pmatrix}$
(b)	Enlargement [SF] 3 [Centre] $(1, 4)$	3	B1 for each

Question 77

(a)(i)	10	1	
(a)(ii)	-19	1	FT 1 - 2 <i>their (a)(i)</i>
(b)	$\frac{1-x}{2}$ oe final answer	2	M1 for $x = 1 - 2y$ or $y + 2x = 1$ or $\frac{y}{2} = \frac{1}{2} - x$ or $y - 1 = -2x$ or better
(c)	$\frac{1}{2}$ oe	1	
(d)	$4x^2 - 8x + 2$ final answer	4	M1 for $(1 - 2x)(1 - 2x) - (1 - 2(1 - 2x))$ or better B1 for $1 - 2x - 2x + 4x^2$ B1 for $-(1 - 2 + 4x)$ or better or $[+]$ $1 - 4x$ or for correct answer seen then spoiled
(e)	x final answer	1	
(f)	3125	1	
(g)	25	1	
(h)	-2	2	B1 for $\frac{1}{25}$ or 0.04

Question 78

(a)	Translation $\begin{pmatrix} 1 \\ -6 \end{pmatrix}$	2	B1 for each
(b)(i)	Image at (0, 1), (-3, 1), (-3, 2)	2	B1 for reflection in $x = k$ or $y = 1$
(b)(ii)	Image at (5, -4), (5, -1), (4, -1)	2	B1 for rotation 90° anticlockwise with other centre or for rotation 90° clockwise about (6, 0)
(b)(iii)	Image at (-1, -2), (-7, -2), (-7, -4)	2	B1 for enlargement, factor -2 with other centre

Question 79

(a)	Image at (4, -1) (4, -4) (5, -4)	2	B1 for translation by $\begin{pmatrix} 8 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -6 \end{pmatrix}$ or for correct vertices not joined
(b)	Image at (-4, -4) (-4, -7) (-3, -4)	2	B1 for reflection in $x = -1$ or $y = k$ or for correct vertices not joined
(c)	Enlargement 3 (-5, 5)	3	B1 for each
(d)	Rotation 90° clockwise (1, 1)	3	B1 for each

Question 80

(a)(i)	rotation 90 anticlockwise (-3, 2)	3	B1 for each
(a)(ii)	enlargement $-\frac{1}{2}$ (-2, -1)	3	B1 for each
(b)	Image at (-3, -5) (1, -5) (1, 3)	2	B1 for translation by $\begin{pmatrix} -5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -10 \end{pmatrix}$
(c)	Image at (2, 3) (6, 3) (6, -5)	2	B1 for reflection in $y = k$ or $x = 4$

Question 81

(a)(i)	4	1	
(a)(ii)	3	1	
(a)(iii)	13	1	FT $5 \times \text{their (a)(i)} - 7$

(b)	$\frac{x+2}{3}$ final answer	2	M1 for $y+2=3x$ or for $\frac{y}{3}=x-\frac{2}{3}$ or for $x=3y-2$
(c)	$9x^2-9x+2$ final answer	3	M1 for $(3x-2)^2+3x-2$ B1 for $(3x-2)^2=9x^2-6x-6x+4$
(d)	$2x+1$	1	
(e)(i)	81	1	
(e)(ii)	x	1	Not $y=x$

Question 82

(i)	$\begin{pmatrix} 0 \\ 2 \end{pmatrix}$	2	B1 for $\begin{pmatrix} 0 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 2 \end{pmatrix}$
(ii)	$\begin{pmatrix} -2 \\ 9 \end{pmatrix}$	2	FT their \overline{PQ} B1FT for $\begin{pmatrix} 0 \\ 6 \end{pmatrix}$

Question 83

(i)	$\frac{2}{3}\mathbf{t} + \frac{1}{3}\mathbf{u}$ or $\frac{1}{3}(2\mathbf{t} + \mathbf{u})$ final answer	2	M1 for $\overline{UY} = \frac{2}{3}(\mathbf{t}-\mathbf{u})$ oe or $\overline{TY} = \frac{1}{3}(\mathbf{u}-\mathbf{t})$ oe or correct route soi
(ii)	$\frac{2}{3}\mathbf{t}$ cao	1	

Question 84

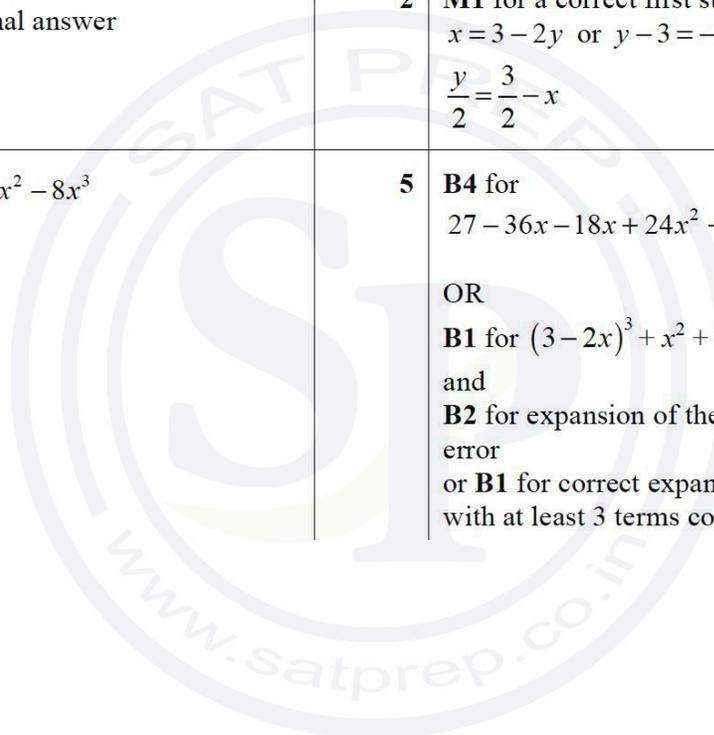
(a)(i)	Triangle at (4, 0) (4, 3) (6, 3)	2	B1 for translation by $\begin{pmatrix} 2 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -1 \end{pmatrix}$ If 0 scored SC1 for triangle at (3, 0.5) (3, 3.5) (5, 3.5)
(a)(ii)	Triangle at (1, -2) (4, -4) (4, -2)	2	B1 for rotation 90 clockwise wrong centre or for rotation 90 anticlockwise about the origin
(a)(iii)	Triangle at (-4, 4) (-4, 2.5) (-5, 2.5)	2	B1 for enlargement SF $-\frac{1}{2}$ with wrong centre or for enlargement SF $\frac{1}{2}$ with centre (-2, 3)
(b)	Reflection $y = -x$ oe	2	B1 for each

Question 85

(a)(i)(a)	$\begin{pmatrix} 5 \\ -13 \end{pmatrix}$ final answer	1	
(a)(i)(b)	$\begin{pmatrix} -4 \\ 11 \end{pmatrix}$ final answer	2	B1 for answer $\begin{pmatrix} -4 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 11 \end{pmatrix}$ or $\begin{pmatrix} -6 \\ 16 \end{pmatrix}$ seen
(a)(i)(c)	5.39 or 5.385...	2	M1 for $2^2 + ([-]5)^2$
(a)(ii)	$[k =] 8$ $[m =] -32$	3	B2 for $k = 8$ or $m = -32$ or M1 for $-3 + 2k = 13$ oe or for $m = -5 \times \text{their } k + 8$ correctly evaluated
(b)(i)(a)	$\mathbf{p} + \mathbf{q}$ final answer	1	
(b)(i)(b)	$\frac{1}{2}\mathbf{p} - \frac{1}{2}\mathbf{q}$ or $\frac{1}{2}(\mathbf{p} - \mathbf{q})$ or $\frac{\mathbf{p} - \mathbf{q}}{2}$ final answer	2	M1 for unsimplified answer or any correct vector route for \overrightarrow{CM} , e.g. $-\mathbf{q} + \frac{1}{2}$ their (b)(i)(a)
(b)(i)(c)	$\frac{1}{2}\mathbf{p} + \frac{1}{10}\mathbf{q}$ or $\frac{5\mathbf{p} + \mathbf{q}}{10}$ final answer	2	M1 for unsimplified answer or any correct vector route for \overrightarrow{MN}

Question 86

(a)	13	1	
(b)	$4x - 3$ final answer	2	M1 for $3 - 2(3 - 2x)$
(c)	-7 5	4	M1 for $x^2 + 2x - 35 [= 0]$ or $x^2 + 2x = 35$ M2 for $(x + 7)(x - 5)$ or $x(x - 5) + 7(x - 5)$ or $x(x + 7) - 5(x + 7)$ or M1 for $(x + a)(x + b)$ where a, b are integers with $ab = -35$ or $a + b = 2$
(d)	$\frac{3-x}{2}$ oe final answer	2	M1 for a correct first step: $x = 3 - 2y$ or $y - 3 = -2x$, $2x = 3 - y$ or $\frac{y}{2} = \frac{3}{2} - x$
(e)	$32 - 54x + 37x^2 - 8x^3$ final answer	5	B4 for $27 - 36x - 18x + 24x^2 + 12x^2 - 8x^3 + x^2 + 5$ oe OR B1 for $(3 - 2x)^3 + x^2 + 5$ and B2 for expansion of the 3 brackets, allow one error or B1 for correct expansion of 2 of the brackets with at least 3 terms correct



Question 87

(a)(i)	64	1	
(a)(ii)	127	1	FT $2 \times \text{their (a)(i)} - 1$
(b)	$\pm \frac{1}{2}$ oe nfw	4	<p>M1 for $(2x-1)^2 + 2(2x-1)$</p> <p>B1 for $4x^2 - 2x - 2x + 1$ or $(2x-1)(2x-1+2)$</p> <p>B1 for $4x^2 - 1 [= 0]$ or $(2x-1)(2x+1) [= 0]$</p> <p>OR</p> <p>M1 for $x(x+2) = 0$ (solving $g(x) = 0$)</p> <p>A1 for $x = 0$ or -2</p> <p>B1 for $2x - 1 = 0$ or $2x - 1 = -2$</p>
(c)	$\frac{x+1}{2}$ oe final answer	2	<p>M1 for</p> <p>$y+1=2x$ or $\frac{y}{2}=x-\frac{1}{2}$ or $x=2y-1$</p>
(d)	$-\frac{1}{6}$ oe nfw	3	<p>B2 for $3x = -\frac{1}{2}$ oe</p> <p>OR</p> <p>M1 for $2^{2x} \times 2^x$ oe or $4^{\frac{1}{2}x} \times 4^x$ oe or 8^x oe</p> <p>M1 for $2^{\frac{1}{2}}$ or $4^{\frac{1}{4}}$ or $8^{\frac{1}{6}}$ soi</p>

Question 88

(a)	Rotation 90° clockwise oe [centre] (5, 2)	3	B1 for each
(b)(i)	Translation $\begin{pmatrix} -1 \\ 4 \end{pmatrix}$	2	B1 for each
(b)(ii)	4.12 or 4.123...	2	M1 for $(\text{their } (-1))^2 + (\text{their } 4)^2$

Question 89

(a)(i)	(3, 1)	1	
(a)(ii)	$\begin{pmatrix} -10 \\ 15 \end{pmatrix}$	1	
(a)(iii)	3.61 or 3.605 to 3.606	2	M1 for $(-2)^2 + 3^2$ oe
(b)(i)(a)	$\frac{1}{2} \mathbf{c}$	1	
(b)(i)(b)	$\mathbf{a} + \frac{1}{2} \mathbf{c}$ oe	1	FT $\mathbf{a} + \text{their (b)(i)(a)}$
(b)(ii)(a)	$\overrightarrow{OP} = \frac{1}{3}(2\mathbf{a} + \mathbf{c})$ oe and $\overrightarrow{OQ} = \frac{1}{2}(2\mathbf{a} + \mathbf{c})$ oe OR $\overrightarrow{OP} = \frac{2}{3}(\mathbf{a} + \frac{1}{2}\mathbf{c})$ OR $\overrightarrow{PQ} = \frac{1}{3}(\mathbf{a} + \frac{1}{2}\mathbf{c})$ and correct comment e.g. have the same base vector or that they are multiples of one another and they share a common point OR e.g. $\overrightarrow{OQ} = 1.5\overrightarrow{OP}$, $2\overrightarrow{PQ} = \overrightarrow{OP}$	2	B1 for \overrightarrow{OP} or \overrightarrow{PQ} factorised or for correct multiplicative statement on relationship without factorised vectors e.g. $\overrightarrow{OQ} = 1.5\overrightarrow{OP}$, $\frac{2}{3}\overrightarrow{OQ} = \overrightarrow{OP}$, $2\overrightarrow{PQ} = \overrightarrow{OP}$, $1.5\left(\frac{2}{3}\mathbf{a} + \frac{1}{3}\mathbf{c}\right) = \mathbf{a} + \frac{1}{2}\mathbf{c}$
(b)(ii)(b)	1.5 oe	1	

Question 90

(a)(i)	Image at $(-5, 6)$ $(-5, 8)$ $(-6, 7)$	2	B1 for translation by $\begin{pmatrix} -4 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 5 \end{pmatrix}$
(a)(ii)	Image at $(3, 1)$ $(3, 3)$ $(4, 2)$	2	B1 for reflection in $y = 1$ or $x = k$
(a)(iii)	Image at $(3, 4)$ $(3, 8)$ $(1, 6)$	2	B1 for enlargement, sf 2, in wrong position
(b)	Rotation 90° [anticlockwise] oe $(-3, 0)$	3	B1 for each

Question 91

(i)	1.6 oe	2	M1 for $3 - 5x = -5$
(ii)	$\frac{3-x}{5}$ oe final answer	2	M1 for $x = 3 - 5y$ or $\frac{y}{5} = \frac{3}{5} - x$ or better, or $y - 3 = -5x$ oe

Question 92

(a)(i)(a)	Shape at $(-2, 1)$ $(-4, 1)$ $(-4, 7)$ $(0, 7)$	2	B1 for 3 correct points or for enlargement SF2 from any centre
(a)(i)(b)	Shape at $(2, -2)$ $(2, -3)$ $(5, -1)$ $(5, -3)$	3	B2 for correct orientation but wrong position or for 3 correct points or B1 for $y = x - 1$ drawn
(a)(ii)	Rotation 90 [anticlockwise] oe $(0, 0)$ oe	3	B1 for each
(b)	$\frac{3}{4}\mathbf{p} + \frac{1}{2}\mathbf{q}$ or $\frac{1}{4}(3\mathbf{p} + 2\mathbf{q})$ or $\frac{3\mathbf{p} + 2\mathbf{q}}{4}$ final answer	3	M2 for $AM = \overline{AM} = \frac{1}{2}\left(-\mathbf{p} + \mathbf{q} + \frac{1}{2}\mathbf{p}\right)$ oe or M1 for correct route for \overline{AB} oe soi by $-\frac{1}{2}\mathbf{p} + \mathbf{q}$ or for \overline{OM} soi

Question 93

(a)(i)	169	2	M1 for $g(13)$ or $(1+4x)^2$ or better
(a)(ii)	$1+4x^2$ final answer	1	
(a)(iii)	x	1	
(b)	3.5 or $\frac{7}{2}$	2	M1 for $1+4x=15$

Question 94

(a)(i)	Triangle drawn at $(2, -1)$, $(2, -4)$, $(3, -4)$	2	B1 for two correct points If 0 scored, SC1 for reflection of triangle T in $y = -x$
(a)(ii)	Triangle drawn at $(-5, 6)$, $(-2, 5)$, $(-5, 5)$	2	B1 for translation by $\begin{pmatrix} -1 \\ k \end{pmatrix}$ or by $\begin{pmatrix} k \\ 3 \end{pmatrix}$ If 0 scored SC1 for triangle drawn at $(-4.5, 3.5)$, $(-4.5, 4.5)$ and $(-1.5, 3.5)$
(a)(iii)	Enlargement [SF] -1.5 oe [centre] $(0, 3)$	3	B1 for each
(b)	28.8 , $28\frac{8}{10}$, $28\frac{4}{5}$	2	M1 for 1.2^2 oe

Question 95

(a)	Correct lines drawn	2	B1 for one correct with no incorrect lines
(b)(i)(a)	Translation or translate $\begin{pmatrix} -1 \\ 4 \end{pmatrix}$ oe	2	B1 for each
(b)(i)(b)	Rotation or rotate 90 [anticlockwise] oe [centre] $(2, 1)$	3	B1 for each
(b)(ii)(a)	Triangle at $(-5, 6)$ $(-2, 6)$ $(-2, 5)$	2	B1 for reflection in $y = k$
(b)(ii)(b)	Triangle at $(1, 5)$ $(1, 7)$ $(7, 7)$	2	B1 for correct size and orientation, wrong position

Question 96

(a)(i)	3	1
(a)(ii)	7	1 FT <i>their</i> (i) 3× <i>their</i> (i)−2
(b)	$\frac{x+2}{3}$ oe final answer	2 M1 for $y+2=3x$ or $\frac{y}{3}=x-\frac{2}{3}$ or $x=3y-2$
(c)	25	2 M1 for $\frac{1}{x}=5^{-2}$ oe
(d)	$\frac{2x^2-x-1}{x}$ final answer	2 M1 for $2x-1-\frac{1}{x}$
(e)	2.98×10^{17} or $2.980... \times 10^{17}$	1
(f)	625	2 M1 for $x=j(4)$

Question 97

(a)	Triangle drawn at (1, − 5), (1, − 7), (5, − 5)	2 B1 for reflection in any horizontal line If 0 scored, SC1 for reflection in $x = -2$
(b)	Triangle drawn at (− 2, 0), (− 2, − 1), (0, − 1)	2 B1 for correct size and orientation but wrong position
(c)	Rotation 90 [anticlockwise] oe [centre] (− 1, 0)	3 B1 for each

Question 98

(a)(i)	2a drawn correctly with direction arrow	1
(a)(ii)	a − b drawn correctly with direction arrow	2 B1 for $\begin{pmatrix} 4 \\ -3 \end{pmatrix}$ seen or implied or M1 for correctly drawing <i>their</i> a − b with an arrow
(b)(i)(a)	$\mathbf{q} + \frac{3}{4} \mathbf{p}$ final answer	1
(b)(i)(b)	$\mathbf{q} - \frac{1}{4} \mathbf{p}$ final answer	2 M1 for a correct route
(b)(i)(c)	$\frac{13}{24} \mathbf{p} - \frac{2}{3} \mathbf{q}$ final answer	3 M2 for $\frac{3}{8} \mathbf{p} - \frac{2}{3}$ (<i>their</i> (b)(i)(b)) oe or for $-\frac{3}{8} \mathbf{p} - \mathbf{q} + \mathbf{p} + \frac{1}{3}$ (<i>their</i> (b)(i)(b)) oe or M1 for a correct route or for $\overrightarrow{[BN]} = -\frac{2}{3}$ (<i>their</i> (b)(i)(b)) or $\overrightarrow{[AN]} = \frac{1}{3}$ (<i>their</i> (b)(i)(b)) or final answer $k\mathbf{p} - \frac{2}{3} \mathbf{q}$ oe or $\frac{13}{24} \mathbf{p} - k\mathbf{q}$ oe
(b)(ii)	$\frac{19}{16} \mathbf{p}$ oe final answer	2 M1 for $\overrightarrow{AG} = \frac{3}{8} \mathbf{p} + 2$ soi or for answer $k\mathbf{p}$ oe

Question 99

(a)	2.5 and -2.5 oe	3	M2 for $1681m^2 = \frac{42025}{4}$ oe or M1 for $(9m)^2 + (40m)^2$ oe
(b)(i)(a)	$\mathbf{c} - \mathbf{a}$ final answer	1	
(b)(i)(b)	$\frac{3}{4}\mathbf{a}$ final answer	1	
(b)(i)(c)	$\mathbf{c} + \frac{3}{4}\mathbf{a}$ final answer	1	FT $\mathbf{c} + \text{their (b)(i)(b)}$, must be a vector in terms of \mathbf{a} and/or \mathbf{c} in its simplest form
1(b)(ii)	$\mathbf{a} + \frac{4}{3}\mathbf{c}$ oe	2	B1 for $[\overline{BQ}] = \frac{1}{3}\mathbf{c}$ or $[\overline{AQ}] = \frac{4}{3}\mathbf{c}$ or M1 for a correct route or for answer $\mathbf{a} + k\mathbf{c}$ oe, where $k > 1$

Question 100

(a)(i)	Translation $\begin{pmatrix} 7 \\ -8 \end{pmatrix}$ oe	2	B1 for each
(a)(ii)	Rotation 90° [anticlockwise] oe (0, 8)	3	B1 for each
a)(iii)	Enlargement [sf] $\frac{1}{2}$ oe [centre] $(-1, -4)$	3	B1 for each
(b)	Image at $(-4, 4) (-3, 4) (-2, 5) (-2, 3) (-4, 3)$	2	B1 for the line $y = x + 8$ drawn so long enough to be fit for purpose or correct size and orientation but wrong position

Question 101

(a)(i)	4	1	
(a)(ii)	16	1	FT 2 ^{their 4}
(b)	3	1	
(c)	$\frac{1}{4}$ oe	2	M1 for $\frac{2}{x} = 2^3$ or better
(d)	$\frac{5-x}{2}$ oe final answer	2	M1 for $x = 5 - 2y$ or $y + 2x = 5$ oe or $\frac{y}{2} = \frac{5}{2} - x$ oe
(e)	$\frac{11x - x^2 + 2}{x}$ final answer	3	B2 for $\frac{x(10-x) + 2 + x}{x}$ oe single fraction or B1 for $x(10-x) + 2 + x$ oe or M1 for $10 - x + \frac{2}{x} + 1$
(f)	[a =] 1 [b =] -21 [c =] 100	4	B3 for $x^2 - 21x + 100$ OR M1 for $(10-x)^2 - (10 - (10-x))$ oe or better B2 for $[(10-x)^2] = 100 - 10x - 10x + x^2$ or B1 for three out of four terms of $[(10-x)^2] = 100 - 10x - 10x + x^2$ correct
(g)	1024	2	M1 for [x =] h(10) oe or better

Question 102

(a)(i)	$\begin{pmatrix} -3 \\ 3 \end{pmatrix}$	1
(a)(ii)	$\begin{pmatrix} 3 \\ 2 \end{pmatrix}$	1
(a)(iii)	3.61 or 3.605 to 3.606	2 M1 for $2^2 + 3^2$ oe
(b)	(6, 1)	2 B1 for each
(c)	$\frac{2}{7}\mathbf{g} + \frac{3}{14}\mathbf{h}$	4 B3 for correct unsimplified expression for \overline{MK} or B2 for $[\overline{MK} =] \frac{2}{7}\mathbf{g} + k\mathbf{h}$ or $[\overline{MK} =] k\mathbf{g} + \frac{3}{14}\mathbf{h}$ or $\overline{HK} = \frac{2}{7}(\mathbf{g} - \mathbf{h})$ oe or $\overline{GK} = \frac{5}{7}(\mathbf{h} - \mathbf{g})$ oe or M1 for correct route for \overline{MK}

Question 103

(a)	1	1
(b)	$-\frac{1}{5}$ or -0.2	2 M1 for $2x - 1 + 3x + 2 = 0$ oe isw
(c)	$9x + 8$ final answer	2 M1 for $3(3x + 2) + 2$
(d)	$\frac{4x^2 + 5x - 3}{x(2x - 1)}$ final answer	4 M1 for $\frac{1}{2x - 1}$ and $3\left(\frac{1}{x}\right) + 2$ oe B1 for $x + 3(2x - 1) + 2x(2x - 1)$ oe or better isw B1 for common denominator = $x(2x - 1)$ isw If 0 scored, SC1 for answer $\frac{4x^2 + 9x + 3}{x(2x + 1)}$
(e)	h(x) indicated	1

Question 104

(a)(i)	Triangle at (3, -1), (9, -1), (9, 2)	2	B1 for correct shape, size and orientation or for correct plots but no triangle
(a)(ii)(a)	Triangle at (3, 3), (4, 3), (3, 5)	2	B1 for correct shape size and orientation or for rotation about (4, 2) 90° anticlockwise or for correct plots but no triangle
(a)(ii)(b)	Triangle at (4, 3), (5, 3), (5, 5)	3	B2 for correct shape size and orientation or for correct plots but no triangle or M1 for $x + y = 6$ drawn
(a)(ii)(c)	Reflection $x = 4$	2	B1 for each
(b)	$\frac{5}{7}\mathbf{a} + \frac{2}{7}\mathbf{b}$ final answer	3	B2 for correct unsimplified answer OR M2 for $\overline{HZ} = \frac{2}{7}(\mathbf{b} - \mathbf{a})$ or $\overline{KZ} = \frac{5}{7}(\mathbf{a} - \mathbf{b})$ oe or M1 for $\overline{HK} = -\mathbf{a} + \mathbf{b}$ or $\overline{KH} = -\mathbf{b} + \mathbf{a}$ or for a correct route

Question 105

(a)(i)	-7	1	
(a)(ii)	$\frac{x-5}{2}$ oe final answer	2	M1 for correct first step e.g. $x = 2y + 5$ or $2x = y - 5$ or $\frac{y}{2} = x + \frac{5}{2}$
(a)(iii)	$2x^3 - 11x^2 - 8x + 80$ final answer	4	M1 for $(x-4)(2x+5)(x-4)$ oe B2 for $2x^3 - 8x^2 - 8x^2 + 5x^2 - 20x - 20x + 32x + 80$ or for simplified 4 term expression of the correct form with 3 terms correct in final answer or B1 for 3 terms correct out of 4 from $x^2 - 4x - 4x + 16$ or $2x^2 - 8x + 5x - 20$
(b)	0	2	M1 for $g(-2)$ or $2(x-4) + 5$ oe or $3^x = 1$ or $g(f(2)) = 1$

Question 106

(a)(i)	7	1	
(a)(ii)	$\frac{1}{8}$ oe	2	M1 for $g(-0.5)$ or for $64^{5^{(x)}-3}$ or better
(b)	$\frac{2-x}{x}$ or $\frac{2}{x}-1$ final answer	3	M1 for $y(x+1) = 2$ or $x = \frac{2}{y+1}$ or better M1 for $\frac{2-y}{y}$ or $xy = 2-x$ oe
6c	$-\frac{5}{6}$ -0.833 or better	2	M1 for $[64^x =] 2^{6x}$ or $(2^6)^x$ or $6x = -5$
(d)	$\frac{7-9x}{(5x-3)(x+1)}$ or $\frac{7-9x}{5x^2+2x-3}$ or $-\frac{9x-7}{5x^2+2x-3}$ final answer	4	B1 for $\frac{1}{5x-3} - \frac{2}{x+1}$ M1 for $x+1 - 2(5x-3)$ seen isw M1 for $(5x-3)(x+1)$ seen isw

Question 107

(a)	Rotation 90° [anticlockwise] oe (2, 7)	3	B1 for each
(b)(i)	Image at $(-4, -1), (-3, -1), (-4, -4)$	2	B1 for reflection in $y = k$ or $x = 1$
(b)(ii)	Image at $(2, -4), (1, -4), (1, -1)$	2	B1 for translation by $\begin{pmatrix} 5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -7 \end{pmatrix}$
(b)(iii)	Image at $(-4, 7), (-4, 1), (-2, 1)$	2	B1 for enlargement, factor 2 with other centre

Question 108

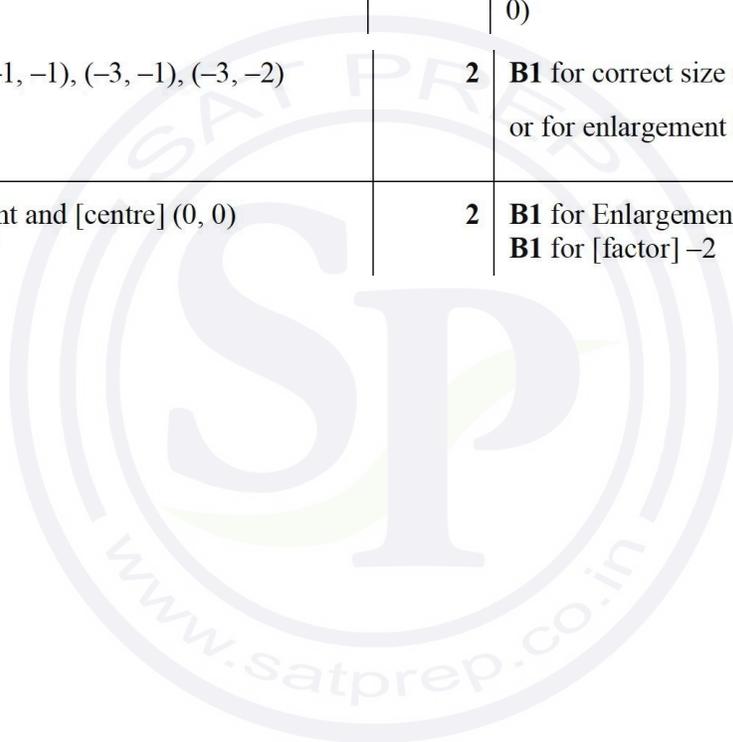
(i)	$\begin{pmatrix} 2 \\ 5 \end{pmatrix}$	1	
(ii)	$\begin{pmatrix} -6 \\ 4 \end{pmatrix}$	1	

Question 109

(a)	4	1	
(b)	$7 - 3x$ final answer	2	M1 for $1 - 3(x - 2)$
(c)	$\frac{1-x}{3}$ oe final answer	2	M1 for $x = 1 - 3y$ or $y - 1 = -3x$ or $1 - y = 3x$ or $\frac{y}{3} = \frac{1}{3} - x$
(d)	$a = 2, b = 5, c = -1$	5	<p>B4 for two correct values <u>only</u> after correct substitution seen i.e. $(1 - 3x - 1)^2 - (x - 1)^2(1 - 3x)$ or for correct unsimplified expansion or a correct simplified expansion. OR M1 for $(1 - 3x - 1)^2 - (x - 1)^2(1 - 3x)$</p> <p>B2 for correct expansion of $[-](x - 1)^2(1 - 3x)$ $[-](x^2 - x - x + 1 - 3x^3 + 3x^2 + 3x^2 - 3x)$ or better</p> <p>or B1 for expansion of one pair of brackets $[(x - 1)^2 =]x^2 - x - x + 1$ or better</p> <p>or $[(x - 1)(1 - 3x) =] - 3x^2 + x + 3x - 1$</p>
(e)	$\frac{3 - x + 3x^2}{x}$ final answer	3	<p>B1 for $3 - x(1 - 3x)$ or better B1 for common denominator x isw</p>
(f)	-7	1	

Question 110

(a)(i)	Image at $(-5, 3), (-1, 3), (-1, 5)$	2	B1 for translation $\begin{pmatrix} -7 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ 1 \end{pmatrix}$
(a)(ii)	Translation $\begin{pmatrix} 7 \\ -1 \end{pmatrix}$ cao	1	
(b)	Image at $(6, 4), (6, 6), (2, 6)$	2	B1 for reflection in line $x = 4$ or for reflection in line $y = k$
(c)	Image at $(2, -2), (2, -6), (4, -6)$	2	B1 for correct size and orientation or for rotation 90° anticlockwise about $(0, 0)$
(d)(i)	Image at $(-1, -1), (-3, -1), (-3, -2)$	2	B1 for correct size and orientation or for enlargement SF $\frac{1}{2}$, centre $(0, 0)$
(d)(ii)	Enlargement and [centre] $(0, 0)$ [factor] -2	2	B1 for Enlargement and [centre] $(0, 0)$ B1 for [factor] -2



Question 111

(a)(i)	(15, 6)	2	B1 for each
(a)(ii)	$\begin{pmatrix} 3 \\ 24 \end{pmatrix}$	1	
(a)(iii)	13.6 or 13.60...	2	M1 for $(-11)^2 + 8^2$ oe
(b)(i)	$\mathbf{a} + \frac{3}{5}(\mathbf{b} - \mathbf{a})$ or $\mathbf{b} + \frac{2}{5}(\mathbf{a} - \mathbf{b})$ leading to $\frac{2}{5}\mathbf{a} + \frac{3}{5}\mathbf{b}$ with no errors	M3	M2 for $[\overline{MR} =] \frac{3}{5}(\mathbf{b} - \mathbf{a})$ oe or $[\overline{NR} =] \frac{2}{5}(\mathbf{a} - \mathbf{b})$ oe or M1 for $\overline{MN} = \mathbf{b} - \mathbf{a}$ or $\overline{NM} = \mathbf{a} - \mathbf{b}$ or a correct route for \overline{OR}
(b)(ii)(a)	$k = 5, c = 10$	4	B2 for $c = 10$ or M1 for $c(\frac{2}{5}\mathbf{a} + \frac{3}{5}\mathbf{b}) = \mathbf{b} + 4\mathbf{a} + k\mathbf{b}$ oe or for $\frac{2}{5}c = 4$ and M1 for $\frac{3}{5} \times \text{their } c = k + 1$
(b)(ii)(b)	$3\mathbf{a} + 6\mathbf{b}$ final answer	1	FT $3\mathbf{a} + (\text{their } k + 1)\mathbf{b}$

Question 112

(a)(i)	-20	1	
(a)(ii)	$\frac{x+3}{2}$ oe final answer	2	M1 for $x = 2y - 3$ or better or $y + 3 = 2x$ or better or $\frac{y}{2} = x - \frac{3}{2}$ or better
a)(iii)	125	2	M1 for $g(64)$ or $2(4^{2x-1}) - 3$
(b)	2.5 oe	2	M1 for $2(2x) - 3 = 7$ or better
(c)	$2x^2 + 4x - 11$ final answer	3	B2 for $2x^2$ and either $+4x$ or -11 in final 3 term answer or for correct answer seen then spoiled or M1 for $2x^2 - 3 + 2(2x - 3) - 3$ [+ 1]
(d)	1.5 oe	2	M1 for $4^{2x-1} = 4^2$ or better
(e)	$a = 3$ $b = 4$ $c = -59$ $d = -20$	3	B2 for 3 correct values or for correct unsimplified expanded expression or for simplified four-term expression of correct form with 3 terms correct or B1 for 2 correct values or for correct expansion of one pair of brackets with at least 3 out of 4 terms correct.

Question 113

(a)(i)	Translation $\begin{pmatrix} -7 \\ -1 \end{pmatrix}$ oe	2	B1 for each
(a)(ii)	Rotation 90° clockwise oe (5, 1)	3	B1 for each
(b)(i)	Image at (2, 6) (3, 6) (3, 8)	2	B1 for reflection in $y = k$, $k \neq 2$ or for reflection in $x = 2$
(b)(ii)	Image at (-4, 4) (-6, 4) (-6, 8)	2	B1 for an enlargement, sf -2 in the wrong position

Question 114

(a)(i)	-3.5 oe	2	M1 for $g\left(\frac{1}{2}\right)$ seen or $3\left(\frac{1}{x}\right) - 5$ or better
(a)(ii)	$\frac{x+5}{3}$ oe final answer	2	M1 for correct first step $y+5=3x$, $\frac{y}{3}=x-\frac{5}{3}$ or $x=3y-5$
(b)	$3x-11$ final answer	2	M1 for $3(x-2)-5$
(c)(i)	5	2	M1 for $\frac{1}{3x-5}$ [=0.1]
(c)(ii)	4 nfw	2	M1 for $2^x - (3 \times 7 - 5) [= 0]$ or better

Question 115

(a)(i)	$\begin{pmatrix} -12 \\ 15 \end{pmatrix}$	1	
(a)(ii)(a)	$\begin{pmatrix} 12 \\ -10 \end{pmatrix}$	1	
(a)(ii)(b)	15.6 or 15.62...	2	M1dep for $their 12^2 + (their [-]10)^2$ oe, dep $their 12 \neq 0$ and $their -10 \neq 0$
(b)	$\frac{3}{8}a + \frac{5}{8}b$ final answer	3	B2 for an unsimplified correct answer or $MS = \frac{5}{8}(b-a)$ soi or $NS = \frac{3}{8}(-b+a)$ soi or B1 for correct route for \overline{OS} or for $MN = \mathbf{b} - \mathbf{a}$ or $NM = \mathbf{a} - \mathbf{b}$

Question 116

(i)	$\frac{1}{15}$ oe	1	
(ii)	19 683	2	B1 for $g(9)$, 3^9 or 3^{3^x} seen
(iii)	-3	2	M1 for $3^k = \frac{1}{27}$ or $3^k = 3^{-3}$ or answer $g(-3)$

Question 117

(a)(i)	13	1	
(a)(ii)	-20	1	FT $6 - 2(\text{their (a)(i)})$
(b)	$\frac{6-x}{2}$ oe final answer	2	M1 for correct first step $x = 6 - 2y, y - 6 = -2x, \frac{y}{2} = 3 - x$
(c)	2.375 oe	4	B1 for $6 - 2(2x - 7)$ oe B1 for $4x + 1 = 6 - 4x + 14$ M1 for $8x = 19$ FT <i>their</i> linear equation rearranged correctly from $ax + b = cx + d$ to form $ex = f$
(d)	$\frac{1}{3}$ or 0.333...	2	M1 for $h(1)$ or $3^{(3^{x-2} - 2)}$ or $3^{(3^{2-2} - 2)}$ or better
(e)	6561	2	M1 for 3^{10-2} or $x = h(10)$

Question 118

(a)(i)	$\begin{pmatrix} 4 \\ -12 \end{pmatrix}$	2	B1 for each
(a)(ii)	$1^2 + 7^2$	M1	
	$5^2 + ([-]5)^2$	M1	
	Both $\sqrt{50}$ oe	A1	With no errors seen If M0M0A0 scored SC1 for $\sqrt{50}$ oe for each
(a)(iii)	44.4 or 44.42[8...] to 44.435	2	FT <i>their</i> (a)(ii) correct to 3sf or better M1 for $2 \times \pi \times$ <i>their</i> $\sqrt{50}$ oe
(a)(iv)	(3, 1)	2	B1 for each
(a)(v)	$[y =] \frac{1}{3}x$	4	B3 for a correct equation in the wrong form as final answer Or B2 for 1/3 stated or used as perpendicular gradient OR M1 for $[\text{grad } PQ] = \frac{7 - -5}{1 - 5}$ oe M1 for $\frac{-1}{\text{their grad } PQ}$ M1dep for substituting <i>their</i> (a)(iv) or (0,0) into $y = \text{their } mx + c$ oe dep on the 2nd M1 or B2

(b)	$\frac{3}{5}\mathbf{a} + \frac{2}{5}\mathbf{b}$ final answer	4	<p>B3 for an unsimplified correct answer</p> <p>or B2 for $AM = \frac{2}{5}(\mathbf{b} - \mathbf{a})$ soi</p> <p>or $BM = \frac{3}{5}(\mathbf{a} - \mathbf{b})$ soi</p> <p>or B1 for $AB = \mathbf{b} - \mathbf{a}$ or $BA = \mathbf{a} - \mathbf{b}$</p> <p>or for a correct route for OM</p> <p>or for correct diagram</p>
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Question 119

(a)(i)	Triangle at (2, 1) (1, 3) (5, 3)	1	
(a)(ii)	Triangle at (-4, -5) (-3, -3) (0, -5)	2	B1 for translation by $\begin{pmatrix} -5 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -2 \end{pmatrix}$
(a)(iii)	Triangle at (-2.5, 2) (-4, 3) (-2, 3)	2	B1 for enlargement by sf $-\frac{1}{2}$ with any centre
(b)	14.4	3	<p>M2 for $[10 \times] 3^2 \times \left(\frac{2}{5}\right)^2$ oe</p> <p>or M1 for 3^2 or $\left(\frac{2}{5}\right)^2$ soi</p>