# Extended Mathematics <br> Topic :Algebra-2 <br> Year :May 2013 -May 2023 <br> Paper - 2 <br> Answers 

Question 1
$\frac{4}{y^{2}-8}$ oe final answer

Question 2

$$
\frac{8 x}{(x-3)(x+1)}
$$

Question 3
$n<9$

Question 4
2500

3

$$
\mathbf{M 1} \text { for } m=k r^{3}
$$

A1 for $k=20$

Question 5
$\begin{array}{llll}-1 & -2 & -3 & -4\end{array}$

Question 6
0.625 oe

4
B3 for $x<-3 / 5$ and $x>-4.5$ oe or B2 for $x<-3 / 5$ or $x>-4.5$ oe or B1 for $5 x<-3$ or $-9<2 x$ oe Or mark on answer line -1 oe

M1 for $2 n<18$ or $2 n-18<0$ oe If 0 scored SC1 for 9 with incorrect inequality.

## Question 7

$$
\frac{5 x+13}{(x+3)(x+2)} \text { oe final answer }
$$

Question 8

$$
\frac{6}{7} \text { or } 0.857[1 \ldots]
$$

Question 9

$$
3 x^{4}
$$

Question 10

$$
x \geq-\frac{3}{8} \text { oe }
$$

Question 11

Question 12
1.6 oe

Question 13
$x<6.8$

Question 14
120

Question 15
$[ \pm] \sqrt{y-4}$ final answer

3 B1 for common denominator $(x+3)(x+2)$ seen
M1 for $2(x+2)+3(x+3)$ soi
$3 \quad$ M1 for $t=\frac{k}{\sqrt{u}}$ oe
A1 for $k=6$

$\mathbf{2} |$| B1 for $k x^{4}$ or $3 x^{k}$ |
| :--- | :--- |

$2 \quad$ M1 for $-3 \leq 8 x$ oe
If 0 then $\mathbf{S C 1}$ for $-\frac{3}{8}$ with incorrect inequality.
(a) $8 q^{-1}$ or $\frac{8}{q}$
(b) $1 / 5$ or 0.2
2 M1 for $5^{-2}, \frac{1}{5^{2}}$ or [0]. 04 seen oe

| 3 | $\begin{array}{l}\text { M1 for } m=k x^{3} \\ \text { A1 for } k=25\end{array}$ |
| :--- | :--- |

$4 \quad$ B3 for 6.8 with wrong inequality or equal as answer.

Or
M1 for first move completed correctly and M1 for second move completed correctly and M1 for third move completed correctly

2 M1 for first move completed correctly M1 for second move completed correctly on answer line

Question 16

$$
\frac{2 t-5}{t-1} \text { final answer }
$$

Question 17

Question 18
$[ \pm] \sqrt{c^{2}-a^{2}}$ oe final answer

Question 19
3.5

M1 for $y=k \sqrt[3]{x+3}$
A1 for $k=\frac{1}{2}$

Alternative method:
M2 for $\frac{y}{\sqrt[3]{340+3}}=\frac{1}{\sqrt[3]{5+3}}$ oe
Question 20

$$
t<-\frac{6}{7}
$$

Question 21

$$
3 x^{6} y^{4}
$$

Question 22

| (a) | $5 t^{25}$ |
| :--- | :--- |
| (b) | -2 |
| (c) | 64 |

(a) $\frac{5}{4} \mathrm{oe}$
(b) $4 y^{6}$

1

2 B1 for $k y^{6}$ or $y^{6}$ or $4 y^{k}$ or 4 as final answer

M1 for correct square M1 for correct re-arrangement M1 for correct square root

Question 23
1.6 oe

| 3 | M1 for $w=\frac{k}{\sqrt{x}}$ <br> A1 for $k=8$ <br> Alternative method: <br> M2 for $w \sqrt{25}=4 \sqrt{4}$ oe |
| :--- | :--- |

Question 24

| (a) | 35 |
| :--- | :--- |
| (b) | $\frac{3 V}{A}$ or $3 V A^{-1}$ |


| $\mathbf{1}$ | M1 for multiplying b <br> $\mathbf{2}$ |
| :--- | :--- |
| dividing by $\frac{1}{3}$ <br> or <br> M1 for dividing by $A$ |  |

Question 25
(a)
(b)

$\left.\right|^{8}$| $8 q^{\frac{3}{2}}$ |
| :--- |

B1 for $2^{12}$ or 4096
B2 for $k q^{\frac{3}{2}}$ as the answer
or
B1 for $2 q^{2}$ and B1 for $q^{\frac{1}{2}}$ oe nfww

Question 26
[0], 1, 2, 3

Question 27

$$
\frac{2}{x(x+1)}
$$

Question 28

$$
4 \pm \sqrt{y-6}
$$

Question 29

$$
\frac{16 x^{2}+18 x+9}{6 x} \text { final answer }
$$

4 M1 for moving the 5 correctly
M1 for collecting their terms
A1 for a correct inequality for $x$ eg [ $0 \leq] x<4$

3 B1 for common denominator $x(x+1)$ seen
M1 for $2(x+1)-2 x$ oe or better

3 M1 for their 6 moved correctly M1 for their $\sqrt{ }$ taken correctly M1 for their 4 moved correctly

M2 for $9[+] 4 x^{2}[+] 18 x[+] 12 x^{2}$ or better or M1 for 2 of these
and M1FT for adding their four 'numerators' together correctly
and B1 for denominator $6 x$ to a maximum of $\mathbf{3}$ marks

Question 30 4

Question 32
$\frac{x+7}{(2 x-1)(x+2)}$
Final answer

Question 33


Question 34
97.2[0]

Question 35

$$
v^{3}-p
$$



$|$| $\mathbf{3}$ | $\begin{array}{l}\text { M1 for } C=k r^{2} \\ \text { A1 for } k=30\end{array}$ |
| :--- | :--- |

or M2 for $\frac{202.8}{2.6^{2}}=\frac{c}{1.8^{2}}$ oe

$$
\begin{array}{l|l}
\mathbf{2} & \mathbf{M 1} \text { for } v^{3}=p+r
\end{array}
$$

## Question 36

(a) (i) 1

| (ii) | $m^{7}$ |
| :--- | :--- |
| (iii) | $2 p^{2}$ |

(b)

| $\mathbf{1}$ |  |  |  |
| :--- | :--- | :--- | :--- |
| $\mathbf{1}$ |  |  |  |
| $\mathbf{2}$ | $\mathbf{S C} 1$ for $2 p^{k}$ | or $k p^{2}$ | $k \neq 0$ |
| $\mathbf{2}$ | B1 for $3^{5}$ | or $3^{5 x}$ | or $243^{\frac{1}{5}}$ |
| or $243^{\frac{2}{5}}$ seen |  |  |  |

Question 37
12

3
A1 for $k=3$
or M2 for $\frac{6}{\sqrt[3]{8}}=\frac{x}{\sqrt[3]{64}}$ oe

Question 38

| (a) | $4 x^{9}$ final answer |
| :--- | :--- |
| (b) | $2 y^{32}$ final answer |

Question 39
$\frac{2 x-23}{(x+2)(2 x-5)}$ final answer

Question 40
$\frac{1}{4}$ or 0.25
$3 \left\lvert\, \begin{aligned} & \mathbf{B 1} \text { for a common denominator of } \\ & (x+2)(2 x-5)\end{aligned}\right.$
B1 for $3(2 x-5)-4(x+2)$ or better or SC2 for final answer $\frac{2 x-7}{(x+2)(2 x-5)}$ or SC1 for numerator of $2 x-7$ in final answer

1

Question 41
$y<8$
$y \geqslant 6-x$ oe and $y \geqslant x+2$ oe

B2 for either $y \geqslant 6-x$ oe or $y \geqslant x+2$ oe or
SC2 for $y=6-x$ oe and $y=x+2$ oe or SC1 for $y>6-x$ or $y=6-x$ or $y>x+2$ or $y=x+2$

Question 42
18

3

M2 for $2(2+4)^{2}=p(-2+4)^{2}$ oe M1 for $p=\frac{k}{(q+4)^{2}}$
A1 for $k=72$

Question 43
$\frac{18}{(x+2)^{2}}$ oe

Question 44
$\frac{x^{16}}{2 y^{4}}$ final answer

Question 45
$\frac{2(s-u t)}{t^{2}}$ oe final answer

Question 46
(a) $\frac{3 x}{2}$ oe final answer
(b) $\frac{x^{2}+2}{x}$ oe final answer

Question 47

## 175

2 M1 for $y=\frac{k}{(x+2)^{2}}$ or better
If zero scored
SC1 for final answer of $y=\frac{k}{(x+2)^{2}}$
where $k \neq 0$ or 18

B2 for fraction as final answer with two of $x^{16}, 2, y^{4}$ correct and in correct position
or B1 for fraction as final answer with one of $x^{16}, 2, y^{4}$ correct and in correct position

3 M1 for correctly isolating term in $a$
M1 for correctly multiplying by 2 (or -2 )
M1 for correctly dividing by $t^{2} \quad\left(\right.$ or $\left.-t^{2}\right)$

3 | M1 for $y=k(x-1)^{2}$ | oe |
| :--- | :--- |
| A1 for $k=7$ |  |

or M2 for $\frac{63}{(4-1)^{2}}=\frac{y}{(6-1)^{2}}$ oe
Question 48
$[ \pm] \sqrt{\frac{y-b}{a}}$ oe final answer

M1 for correctly subtracting to isolate term in $x^{2}$
M1 for correct division
M1 for the final stage of correctly finding the square root

Question 49

81
M1 for $V=k(r+1)^{3}$
and A1 for $k=3$
or
M2 for $\frac{V}{24}=\frac{3^{3}}{2^{3}}$ oe

Question 50
$y<2$ oe and $x \geqslant-2$ oe
$y \geqslant \frac{1}{2} x+1$ oe and $y \leqslant-x+3$ oe
2 B1 for either correct
B2 for either $y \geqslant \frac{1}{2} x+1$ oe or $y \leqslant-x+3$ oe or $\mathbf{S C} 2$ for $y=\frac{1}{2} x+1$ oe and $y=-x+3$ oe or SC1 for $y=\frac{1}{2} x+1$ oe or $y=-x+3$ oe
or SC4 for $y \leqslant 2$ oe, $x>-2$ oe, $y>\frac{1}{2} x+1$ oe and $y<-x+3$ oe

Question 51

| (a) | $x^{8} y^{7}$ final answer |
| :--- | :--- |
| (b) | $27 p^{6} m^{15}$ final answer |

Question 52
$n<1.5$ oe final answer

2 B1 for 1.5 oe in answer
or M1 for $3>8 n-6 n$ oe

Question 53

$$
\begin{aligned}
& y<4 \\
& y \geqslant 3 \\
& x \geqslant 2 \\
& y>x
\end{aligned}
$$

B1 for each correct answer to a maximum of 3 marks.
First two may be combined as a single inequality e.g. $3 \leqslant y<4$ for $\mathbf{B} 2$

After 0 scored SC1 for use of = signs or incorrect inequality signs in all four equations

Question 54

90

Question 55
$8 x^{6}$ final answer

M1 for $y=k(x+2)^{2}$
A1 for $k=2.5$
or M2 for $\frac{(8+2)^{2}}{250}=\frac{(4+2)^{2}}{y}$ oe

Question 56
Correct shading with three ruled accurate solid boundary lines


Question 57
$p=\frac{8 r-5}{r-3}$ oe final answer

5
B2 for $3 x+4 y=12$ line through $(0,3)$ and $(4,0)$ or B1 for a diagonal line through one of these points
B1 for $y=2 x$ line through $(0,0)$ and $(1,2)$ or through $(1,2)$ and $(3,6)$
B1 for $x=3$ line

3 M1 for correctly collecting terms in $p$ on one side and terms not in $p$ on the other side
M1 for correct factorising
M1 for correct division dependent on $p$ appearing only once in a factorised expression Maximum M2 for an incorrect final answer

Question 58

$$
x>-9
$$

$2 |$| M1 | for $\frac{x}{3}>2-5$ oe or $\left(\frac{x}{3}+5\right) \times 3>2 \times 3$ oe |
| :--- | :--- |

Question 59
$\frac{1}{8} x^{2}$ or $0.125 x^{2}$ final answer

$2 |$| B1 for answer $\frac{1}{8} x^{k}$ or $n x^{2}$ |
| :--- | :--- |

Question 60

2

Question 61
$2 p^{4}$ final answer
Question 62
$n>3.75$
Question 63

$$
\frac{p y}{q} \text { final answer }
$$

Question 64
$y \leqslant-\frac{3}{5} x+6$ oe
$x \geqslant 2$ oe
$y>x$ oe
final answers

3 M1 for $y=k \sqrt{x}$
A1 for $k=4$
or M2 for $\frac{\sqrt{9}}{12}=\frac{\sqrt{1 / 4}}{y} \mathrm{oe}$

2 $\mid$ B1 for $k p^{4}$ or $2 p^{k}$ as answer

$2 |$| M1 for $7+8<5 n-n$ oe |
| :--- | :--- |



5 SC4 for $y<-\frac{3}{5} x+6, x>2, y \geqslant x$ oe
or
B3 for $y \leqslant-\frac{3}{5} x+6$ oe
or $\mathbf{B 2}$ for $y=-\frac{3}{5} x+6$ oe
or $\mathbf{B 1}$ for gradient $=-\frac{3}{5}$ oe soi
and
B2 for $x \geqslant 2$ and $y>x$ oe
or B1 for either $x \geqslant 2$ or $y>x$ oe
or for $x=2$ and $y=x$ with incorrect inequalities

Question 65
1.25

3 M1 for $d=\frac{k}{(w+1)^{2}}$ or better
M1 for $[d=] \frac{\text { theirk }}{(7+1)^{2}}$
or
M2 for $3.2(4+1)^{2}=d(7+1)^{2}$ oe

Question 66
$n^{7}$ final answer

Question 67
$1,2,3$

Question 68
$9 y^{3}$ final answer
Question 69

$$
\begin{aligned}
& y \geqslant 0 \text { and } x \geqslant 1 \text { oe } \\
& \text { and } \\
& x+y \leqslant 4 \text { oe }
\end{aligned}
$$

$3 \quad$ B2 for $t<4$
or
M1 for $2+6>3 t-t$ oe or better
If zero scored, SC1 for answer $0,1,2,3$ or $1,2,3,4$
$2 \quad$ B1 for $9 y^{k}, 9 \times y^{3}$ or $k y^{3}(k \neq 0)$ as final answer
$4 \quad$ SC3 for $y>0, x>1$ and $x+y<4$ oe
or
B1 for $y \geqslant 0$
B1 for $x \geqslant 1$ oe
and
B2 for $x+y \leqslant 4$ oe
or M1 for grad $=-1$ soi
If B0 scored for first two $\mathbf{B}$ marks, $\mathbf{S C} 1$ for $y=0$ and $x=1$ or with incorrect inequality sign
Question 70

| (a) | 4 |
| :--- | :--- |
| (b) | $\sqrt{y-q r}$ oe final answer |

Question 71
$6 \frac{2}{3}$ oe
3 M1 for $y=k \sqrt{x+2}$ oe or better
e.g. $2=k \sqrt{7+2}$

M1 for $[y=]$ their $k \times \sqrt{98+2}$
or
M2 for $\frac{y}{2}=\frac{\sqrt{98+2}}{\sqrt{7+2}}$

Question 72
$\frac{p t-2 t-3 p}{p t}$ final answer
2 B1 for $p t-2 t-3 p$ or $1-\frac{2 t+3 p}{p t}$
Question 73
$6 x^{8}$ final answer
Question 74

| (a) | $t^{20}$ final answer |
| :--- | :--- |
| (b) | $x^{10}$ final answer |
| (c) | $27 m^{6}$ final answer |


$2 |$| B1 for |
| :--- | :--- |
| $6 x^{k}$ |, $6 \times x^{8}$ or $k x^{8}(k \neq 0)$ as final answer

Question 75
4

3 M1 for $y=\frac{k}{x^{2}}$
M1 for $y=\frac{\text { their } k}{10^{2}}$
or
M2 for $5^{2} \times 16=10^{2} \times y$ oe

Question 76
(a)
(b)
(c)


Question 77

| i(a) | $x \leqslant 3$ final answer | $\mathbf{2}$ | M1 for $13-7 \geqslant 3 x-x$ oe |
| :--- | :--- | ---: | :--- |
| i(b) | $1,2,3$ | 1FT | correct answer or $\mathbf{F T}$ their answer to (a) |

Question 78
Correct region


SC1 for $R$ not marked and reverse shading
Question 79
$\frac{32}{x^{2}}$ or $32 x^{-2}$ final answer
2 M1 for $y=\frac{k}{x^{2}}$ oe
or $[k=] 32$
Question 80
$\frac{2}{a^{4}}$ or $2 a^{-4}$ final answer
$2 \mid$ B1 for $\frac{2}{a^{k}}$ oe or $\frac{k}{a^{4}}$ oe $(k \neq 0)$ final answer

## Question 81

$(x-y)^{2}$ oe final answer

## Question 82

| (a) | $8 x^{12}$ final answer | $\mathbf{2}$ | B1 for $8 x^{k}$ or $k x^{12}$ in final answer $k \neq 0$ |
| :--- | :--- | :--- | :--- |
| (b) | 9 | $\mathbf{2}$ | M1 for $27^{\frac{2}{3}}$ or $3^{k}$ or $p^{\frac{1}{2}}=3$ or $p^{3}=729$ |

Question 83
1.5 or $\frac{3}{2}$ or $1 \frac{1}{2}$

M1 for $\frac{k}{\sqrt{1+x}}$
M1 for $y=\frac{\text { their } k}{\sqrt{1+15}}$
or M2 for $\frac{2}{\sqrt{1+15}}=\frac{y}{\sqrt{1+8}}$

Question 84

$$
\frac{2 x^{2}+x-7}{3(x+1)} \text { or } \frac{2 x^{2}+x-7}{3 x+3}
$$

final answer
Question 85
$[ \pm] \sqrt{\frac{p}{2}}$ oe

3 M1 for $(2 x-1)(x+1)-2 \times 3$ oe with an attempt to expand the brackets

B1 for $3(x+1)$ or $3 x+3$ for denominator
2
M1 for $\frac{p}{2}=q^{2} \quad$ or $\quad \sqrt{p}=\sqrt{2} q$
or $[q=] \sqrt{\text { their } \frac{p}{2}} \quad$ or $\quad[q=] \frac{\sqrt{p}}{\text { their } \sqrt{2}}$

Question 86

| (a) | 25 | $\mathbf{1}$ |  |
| :--- | :--- | :--- | :--- |
| (b) | 9 | $\mathbf{1}$ |  |

Question 87
$n<3.5$ oe final answer
$2 \mid \mathbf{M 1}$ for $18-11>5 n-3 n$ oe
Question 88

| (a) | $\frac{x}{x+3}$ final answer | $\mathbf{B} 1$ for $x(x-3)$ <br> B1 for $(x-3)(x+3)$ |  |
| :--- | :--- | :--- | :--- |
| (b) | $\frac{8 x+7}{(x-4)(2 x+5)}$ final answer | $\mathbf{3}$ | B1 for common denominator of $(x-4)(2 x+5)$ <br> oe |
| M1 for $3(2 x+5)+2(x-4)$ oe with an attempt |  |  |  |
| to expand the brackets |  |  |  |

Question 89

Correct region identified


3


SC1 for


Question 90
7.65

Question 91
(a)

| (a) | -4 | $\mathbf{1}$ |  |
| :--- | :--- | ---: | :--- |
| (b) | $\frac{1}{5}$ or 0.2 | $\mathbf{1}$ |  |


$\left\lvert\,$| 3 |
| :--- | | M1 for $h=k \sqrt{p}$ oe |
| :--- |
| M1 for $h=$ their $k \sqrt{p}$ |
| or M2 for $\frac{5.4}{\sqrt{1.44}}=\frac{h}{\sqrt{2.89}}$ oe |\right.

Question 92
$x^{2}$ final answer
1
Question 93
$\frac{y^{2}}{2}$ or $0.5 y^{2}$ final answer
2
M1 for $\left(\frac{y^{6}}{8}\right)^{\frac{1}{3}}$ or $\left(\frac{2}{y^{2}}\right)^{-1}$ or better
or $\mathbf{S C} \mathbf{1}$ for answer $\frac{y^{2}}{c}$ or $\frac{y^{k}}{2}$ or $\frac{2}{y^{2}}$
Question 94
$[ \pm] \sqrt{y^{2}-1}$ final answer

Question 95
$\frac{y+x}{x y}$ final answer

Question 96
$-1,0,1,2,3$

3 M1 for correct squaring
M1 for correct rearranging for $x$ or $x^{2}$ term M1 for correct square root

3 B1 for $y(x+1)-x(y-1)$
B1 for common denominator $x y$ or SC2 for $\frac{y-x}{x y}$ final answer

B2 for $-2<n \leqslant 3$ or list with one error or omission
or M1 for $-5+1<2 n$ or $2 n \leqslant 5+1$ or a list with 3 correct and no more than 1 incorrect or if zero scored, $\mathbf{S C 1}$ for $5,3,1,-1,-3$

Question 97
\(\left.$$
\begin{array}{l|l|r|l}\text { (a) } & \begin{array}{l}x+y \leqslant 16 \text { oe } \\
x \geqslant 4 \text { oe }\end{array} & \mathbf{2} & \begin{array}{l}\text { B1 for each mark final answers } \\
\text { If zero scored, } \mathbf{S C 1} \text { for } x+y<16 \text { and } x>4\end{array} \\
\hline \text { (b) } & \text { Correct shading } & \mathbf{3} & \begin{array}{l}\text { M2 for lines at } x=4 \text { and } x+y=16 \\
\text { or for correct shading of } x<4 \\
\text { or } x+y>16\end{array}
$$ <br>
or M1 for line at x=4 or their x=4 <br>

or for line at x+y=16 or their x+y=16\end{array}\right]\)| M1 for $(8,8)$ selected |
| :--- |
| or for $10 \times x+8 \times y$ for any numerical point |
| which is inside or on the boundary of their |
| unshaded region |

## Question 98

$\frac{x^{2}+20 x+31}{2(x-3)(x+7)}$ final answer

Question 99

| '(a) | $(y=) \frac{72}{(x+1)^{2}}$ oe | $\mathbf{2}$ | M1 for $y=\frac{k}{(x+1)^{2}}$ |
| :--- | :--- | ---: | :--- |
| '(b) | 32 | 1FT | FT correct evaluation from their equation in (a) <br> using 0.5 |

Question 100
(a)
(b)

| $m^{10}$ final answer | $\mathbf{1}$ |  |
| :--- | :--- | :--- |
| $20 x^{5} y^{2}$ final answer | $\mathbf{2}$ | $\mathbf{1}$ |

B1 for 2 out of 3 elements correct in final answer or correct answer spoiled

Question 101

12

Question 102
-12
Question 103
$\frac{1}{y(y-1)}$ or $\frac{1}{y^{2}-y}$ final
answer
Question 104
150

$$
3 \left\lvert\, \begin{aligned}
& \text { M2 for } 9 \times 8=6 y \text { oe } \\
& \text { OR } \\
& \text { M1 for } y=\frac{k}{x} \text { oe } \\
& \text { M1 for }[y=] \text { their } \frac{k}{6}
\end{aligned}\right.
$$

$2 \mid \mathbf{B 1}$ for $2^{3}, 2^{-3}, 2^{12}$ or $2^{-12}$

B1 for common denominator of $y(y-1)$ or $y^{2}-y$ B1 for $y-(y-1)$ or $y-y+1$
$3 \left\lvert\, \begin{aligned} & \text { M1 for } y=k(x-1)^{2} \\ & \text { M1 for }[y=] \text { their } k \times(6-1)^{2} \text { oe }\end{aligned}\right.$
OR
M2 for $\frac{y}{24}=\frac{(6-1)^{2}}{(3-1)^{2}}$

Question 105

| (a) | 27 | $\mathbf{1}$ |  |
| :--- | :--- | :--- | :--- |
| (b) | $3 t^{9}$ final answer | $\mathbf{2}$ | $\mathbf{B 1}$ for $k t^{9}$ or for $3 t^{k}(k \neq 0)$ |

Question 106
$[ \pm] \sqrt{\frac{A}{2 \pi+y}}$ final answer

2 M1 for $\frac{A}{2 \pi+y}=x^{2}$
M1 for correctly square rooting their expression in $x^{2}$ If zero scored $\mathbf{S C} \mathbf{1}$ for $\frac{[ \pm] \sqrt{A}}{2 \pi+y}$

Question 107
$y>2$ oe final answer $y \geqslant 3-x$ oe final answer

3 B1 for $y>2$ oe final answer
B2 for $y \geqslant 3-x$ oe final answer or B1 for $y=3-x$ oe soi
or SC2 for $y \geqslant 2$ oe and $y>3-x$ oe final answer

Question 108

$$
\begin{aligned}
& y \geqslant 1.5 \mathrm{oe} \\
& y \geqslant \frac{3}{4} x \mathrm{oe} \\
& y<-\frac{1}{2} x+3 \text { oe }
\end{aligned}
$$

Question 109
9

3
M1 for $y=k(x-1)^{2}$
M1 for $[y=]$ their $k(7-1)^{2}$
OR
M2 for $\frac{4}{(5-1)^{2}}=\frac{y}{(7-1)^{2}}$ oe

Question 110

$$
n<-4.4 \text { or } n<-4 \frac{2}{5}
$$

final answer
Question 111 $-7$

Question 112

$$
\frac{1}{x(x+1)} \text { oe final answer nfww }
$$

B1 for common denominator $x(x+1)$ oe M1 for $x+1-x$

## Question 113

10
3 M1 for $y=k \sqrt{x}$
M1 for $y=$ their $k \times \sqrt{25}$
OR
M2 for $\frac{y}{6}=\sqrt{\frac{25}{9}}$
Question 114

| i(a) | $\frac{1}{w}$ or $w^{-1}$ | $\mathbf{1}$ |  |
| :--- | :--- | ---: | :--- |
| i(b) | $27 w^{9}$ final answer | $\mathbf{2}$ | B1 for $k w^{9}$ or $27 w^{k}$ |

Question 115
$\frac{A-\pi r^{2}}{\pi r}$ or $\frac{A}{\pi r}-r$ oe final answer

Question 116
$\frac{2 x}{3+x}$ oe final answer
2 M1 for $A-\pi r^{2}=\pi r l$ or $\pi r^{2}-A=-\pi r l$ or $\frac{A}{\pi r}=l+r$

4 M1 for correctly clearing the denominator and expanding bracket

M1 for correctly collecting terms in $m$ on one side and terms not in $m$ on the other

M1 for correct factorising
M1 for correct division dependent on $m$ appearing only once in a factorised expression

Question 117

Correct region identified




Question 118
$m \geqslant 3$ final answer
Question 119

| $7(\mathrm{a})$ | 8 | $\mathbf{1}$ |  |
| :--- | :--- | ---: | ---: |
| (b)(i) | $\frac{x^{2}}{16}$ final answer | $\mathbf{1}$ |  |
| (b)(ii) | $a^{-3} b^{5}$ or $\frac{b^{5}}{a^{3}}$ final answer | $\mathbf{2}$ |  |

Question 120

$$
\frac{x^{2}-3 x+8}{3(x+2)} \text { or } \frac{x^{2}-3 x+8}{3 x+6}
$$

final answer
Question 121

$$
4,5,6
$$

Question 122
$\frac{4}{x^{3}}$ oe final answer
$3 \mid$ B2 for 1 error or 1 omission or M2 for $3.75 \leqslant n<7$ oe or M1 for $3.75 \leqslant n$ or $n<7$ or better

3 B1 for common denominator 3( $x+2$ )
M1 for $(x-5)(x+2)+3 \times 6$

Question 123

| (a) | -3 | $\mathbf{1}$ |  |
| :--- | :--- | ---: | :--- |
| (b) | $\frac{m}{4}$ or $0.25 m$ final answer | $\mathbf{2}$ | B1 for $\frac{1}{4}$ or 0.25 or $4^{-1}$ or $m$ correct in final <br> answer |

Question 124

$$
[y=] \frac{1}{4}(x-4) \text { oe final answer }|\quad \mathbf{2}| \text { M1 for } y=k(x-4)
$$

Question 125


Question 126
0.14 oe

Question 127

$$
2 m+1
$$

2
B1 for $2 m+c$ or $k m+1(k \neq 0)$

Question 128
$m=\frac{k}{P-1}$ final answer

Question 129
$\frac{3 x^{2}-4 x+9}{(x+3)(x-5)}$ final answer

## Question 130



Question 131

| (a) | $10 m^{5}$ final answer | $\mathbf{2}$ | $\mathbf{B 1}$ for $10 m^{k}$ or $\mathrm{km}^{5}$ as final answer |
| :--- | :--- | ---: | :--- |
| (b) | $x^{24}$ final answer | $\mathbf{1}$ |  |

Question 132
$\frac{x-5}{(x+2)(3 x-1)}$ final answer
Question 133

Question 134

$$
[ \pm] 0.6 \mathrm{oe}
$$

3
B1 for common denominator isw expansion M1 for $3 x-1-2(x+2)$ or better

| (a) | $27 y^{12}$ final answer | $\mathbf{2}$ | B1 for $k y^{12}$ or $27 y^{k}$ in final answer |
| :--- | :--- | ---: | :--- |
| (b) | $\frac{3}{2}$ oe | $\mathbf{1}$ |  |

3 M1 for $y=\frac{k}{\sqrt{x+1}}$
M1 for $y=\frac{\text { theirk }}{\sqrt{99+1}}$
OR
M2 for $\frac{2 \sqrt{8+1}}{\sqrt{99+1}}$
or M1 for $2 \sqrt{8+1}=y \sqrt{99+1}$

Question 135

| (a) | $t^{14}$ final answer | $\mathbf{1}$ |  |
| :--- | :--- | ---: | :--- |
| (b) | $u^{25}$ final answer | $\mathbf{1}$ |  |

Question 136

| (a) | $\frac{45}{(x+1)^{2}}$ final answer | $\mathbf{2}$ | M1 for $t=\frac{k}{(x+1)^{2}}$ |
| :--- | :--- | ---: | :--- |
| (b) | 4 | $\mathbf{2}$ | M1 for $1.8 \times(x+1)^{2}=$ their 45 or better |



4
B1 for $x=-2$ dashed ruled line and $x=3$ solid ruled line
B1 for $y=x+3$ solid ruled line
B2 for indication of correct region
or B1 for shading that satisfies two of the inequalities, e.g. two of $x>-2, x \leqslant 3$ and $y \leqslant x+3$

Question 138

| L(a) | 6 | $\mathbf{2}$ | B1 for $3^{4}$ or $3^{x-2}$ <br> or $\mathbf{M 1}$ for $3^{x}=81 \times 3^{2}$ or better |
| :--- | :--- | :--- | :--- |
| L(b) | 8 | $\mathbf{3}$ | M2 for $x^{\frac{5}{3}}=32$ or better <br> or M1 for $\frac{1}{x^{\frac{1}{3}}}=\frac{32}{x^{2}}$ or better |
| Question 139 |  | or $x^{\frac{1}{3}-2}=32$ or better |  |

$y=5$ ruled
$y=x+1$ ruled
Correct region indicated

Question 140
$x<-10$ final answer

Question 141
$\frac{x^{2}-3 x-8}{2(x+1)}$ or $\frac{x^{2}-3 x-8}{2 x+2}$ final answer

4 B2 for two correct lines or $\mathbf{B 1}$ for one correct line

B2 for indication of correct region or B1 for shading that satisfies two of the inequalities
$2 \mid \mathbf{M 1}$ for $-12-13>3 x-\frac{x}{2}$ oe
3 B1 for common denominator $2(x+1)$ or $2 x+2$

M1 for $x(x+1)-2(2 x+4)$ or better

Question 142
128
3 M1 for $y=\frac{k}{x^{2}}$
M1 for $y=\frac{\text { their } k}{\left(\frac{1}{2}\right)^{2}}$
OR
M2 for $\frac{2 \times 4^{2}}{\left(\frac{1}{2}\right)^{2}}$
or M1 for $2 \times 4^{2}=y \times\left(\frac{1}{2}\right)^{2}$
Question 143
$\frac{P}{2+\pi}$
Question 144 $\frac{16}{x^{4}}$ or $16 x^{-4}$

Question 145
$6 x^{5}$ final answer

2 M1 for $P=r(2+\pi)$

2 M1 for $\left(\frac{x}{2}\right)^{-4}$ or $\left(\frac{8}{x^{3}}\right)^{\frac{4}{3}}$ or $\left(\frac{x^{12}}{4096}\right)^{-\frac{1}{3}}$ or better or $\mathbf{B} 1$ for $\frac{16}{x^{k}}$ or $16 x^{k}$ or $\frac{k}{x^{4}}$ or $k x^{-4}$ final answer

Question 146

$$
[y=] 1
$$

2 B1 for $k x^{5}$ or $6 x^{k}$

3 M1 for $y=k \times \sqrt[3]{x+3}$
M1 for $y=$ their $k \times \sqrt[3]{24+3}$
OR
M2 for $\frac{y}{\sqrt[3]{24+3}}=\frac{2}{3} \times \frac{1}{\sqrt[3]{5+3}}$ oe

Question 147

| (a) | $p^{6}$ | $\mathbf{1}$ |  |
| :--- | :--- | ---: | :--- |
| (b) | $m^{10}$ | $\mathbf{1}$ |  |
| (c) | $k^{15}$ | $\mathbf{1}$ |  |

Question 148
4
$2 \mid \mathbf{M 1}$ for $y^{\frac{2}{3}}=x^{\frac{1}{6}}$ or $y^{2}=\sqrt{x}$ or $y^{4}=x$
Question 149


Question 150

3 M1 for $p=k(q+2)^{2}$
M1 for $p=($ their $k)(10+2)^{2}$
OR
M2 for $\frac{p}{(10+2)^{2}}=\frac{1}{(1+2)^{2}}$ oe

Question 151

| (a) | $125 x^{12}$ | $\mathbf{2}$ | B1 for $125 x^{k}$ or $k x^{12}$ |
| :--- | :--- | ---: | :--- |
| (b) | $8 x^{96}$ | $\mathbf{2}$ | B1 for $8 x^{k}$ or $k x^{96}$ |

Question 152

$$
2 t^{4}
$$

$$
\begin{array}{|l|l|l}
\mathbf{2} & \mathbf{B} 1 \text { for } 2 t^{n} \text { or } k t^{4}(n, k \neq 0)
\end{array}
$$

Question 153
1.8 or $1 \frac{4}{5}$

3 M2 for $m=\frac{k}{(p-1)^{2}}$
or M1 for $m=\frac{\text { theirk }}{(6-1)^{2}}$
OR
M2 for $5(4-1)^{2}=m(6-1)^{2}$ oe

Question 154

$$
y=\frac{10.5}{\sqrt{x}} \text { oe final answer }
$$

$$
\mathbf{2} \mid \mathbf{M 1} \text { for } y=\frac{k}{\sqrt{x}}
$$

Question 155

| (a) | $64 x^{3} y^{6}$ final answer | $\mathbf{2}$ | B1 for $k x^{3} y^{6}$ or $64 x^{k} y^{6}$ or $64 x^{3} y^{k}$ final <br> answer or correct answer then spoilt |
| :--- | :--- | ---: | :--- |
| (b) | $\frac{2}{3}$ | $\mathbf{1}$ |  |

Question 156
$y=\frac{10.5}{\sqrt{x}}$ oe final answer
2 M1 for $y=\frac{k}{\sqrt{x}}$
Question 157


Question 159
$10 x^{7}$ final answer
2 B1 for $k x^{7}$ or $10 x^{k}$ final answer or for correct answer then spoilt

Question 160
$49 x^{6}$ final answer
$2 \mid$ B1 for $49 x^{k}$ or $n x^{6}$ as final answer

## Question 161

3 correct ruled lines and $R$ clearly indicated


Question 162

Question 163
$-1,0,1$ final answer

## Question 164 <br> Question 164

$12 x^{7}$ final answer

$$
\frac{81}{(y-2)^{2}} \text { final answer }
$$

5 B1 for each line
$y=1$ dashed
$y=2 x+2$ dashed
$x+y=3$ solid

B2 for correct region or $\mathbf{B} 1$ for region satisfying 2 inequalities

or $\mathbf{S C 1}$ for shading of the wanted region only
$2 \mid$ M1 for $z=\frac{k}{(y-2)^{2}}$ oe or better

2 B1 for $-1 \leqslant x<2$
or two correct answers and no extras or three correct answers and one extra/wrong

Question 165

| (a) | $[F=] \frac{108}{d^{2}}$ final answer | $\mathbf{2}$ | M1 for $F=\frac{k}{d^{2}}$ oe or better |
| :--- | :--- | ---: | :--- |
| (b) | $[n=] \frac{1}{4}$ or 0.25 | $\mathbf{1}$ |  |

Question 166

2 B1 for $12 x^{j}$ or $k x^{7}(j, k \neq 0)$ as final answer

24

3
M1 for $y=k \sqrt{x-3}$ oe
M1 for $y=$ their $k \sqrt{39-3}$ oe

Question 167

| (a) | $256 a^{4} b^{20}$ final answer | $\mathbf{2}$ | B1 for two correct elements in final <br> answer |
| :--- | :--- | ---: | :--- |
| (b) | 27 | $\mathbf{1}$ |  |
| (c) | 6 | $\mathbf{2}$ | M1 for $3^{k} \div 3^{t}=3^{2}$ or $3^{8} \div 3^{t}=3^{k}$ oe or <br> better <br> or $3^{t}=729$ oe |

Question 168
$27 y^{6}$ final answer
2 B1 for $k y^{6}$ or $27 y^{k}$ as final answer or correct answer seen and spoilt

Question 169
$8 g^{28}$ final answer
2 B1 for $\mathrm{kg}^{28}$ or $8 g^{k}$ as final answer or correct answer seen and spoilt

Question 170

| (a) | $3^{6 n+5}$ final answer | $\mathbf{2}$ | $\mathbf{B 1}$ for $3^{5}$ or $\left(3^{3}\right)^{2 n}$ or better or answer <br> $6 n+5$ |
| :--- | :--- | ---: | :--- |
| (b) | $2^{3} \times 3^{5} \times p^{6}$ final answer | $\mathbf{2}$ | B1 for two parts correct <br> or $2 \times 3 \times 2 \times 3^{2} \times p^{3} \times 2 \times 3^{2} \times p^{3}$ or <br> $1944 p^{6}$ <br> or $k^{2}=2^{2} \times 3^{4} \times p^{6}$ |

Question 171

| (a) | $x^{-2}$ or $\frac{1}{x^{2}}$ final answer | $\mathbf{1}$ |  |
| :--- | :--- | ---: | :--- |
| (b) | $\frac{2}{3}$ | $\mathbf{1}$ |  |
| (c) | 1 nfww | $\mathbf{3}$ | M1 for $3^{-2(4-3 x)}$ oe or better <br> or $9^{\frac{3 x}{2}} \times 9^{-(4-3 x)}=9^{\frac{1}{2}}$ oe or better <br> M1 for $3 x+($ their -2$) \times(4-3 x)=1$ oe or better <br> or their $\frac{3 x}{2}-(4-3 x)=$ their $\frac{1}{2}$ oe or better |

## Question 172

38
$3 \left\lvert\, \begin{aligned} & \text { M2 for } 12 \times \sqrt{4.25-2}=3 \times \sqrt{x-2} \\ & \text { OR } \\ & \text { M1 for } y=\frac{k}{\sqrt{x-2}} \text { oe } \\ & \text { M1 for } 3=\frac{\text { their } k}{\sqrt{x-2}} \text { oe }\end{aligned}\right.$
Question 173

$$
\frac{2}{3} \mathrm{oe}
$$

$3 \mid \mathbf{M 1}$ for $y=\frac{k}{\sqrt{x+4}}$
M1 for $y=\frac{\text { theirk }}{\sqrt{77+4}}$
Question 174

A correct equation leading to
41
-

3 M2 for $4 x=164$ or M1 for $x+2(x-24)+x-16=100$ oe or M1 for correctly simplifying their equation to the form $k x=c$ provided at least one part correct from $[2](x-24)$ oe or $x-16$
or B1 for answer 41 without an equation in $x$ shown

Question 175

| (a) | $h^{7}$ final answer | $\mathbf{1}$ |  |
| :--- | :--- | ---: | ---: |
| (b) | $\frac{x^{3}}{343}$ final answer | $\mathbf{1}$ |  |
| (c) | 6 |  |  |

Question 176

$$
n>-1 \text { oe }
$$

Question 177

81

3 M2 for $m^{\frac{3}{4}}=27$ or better or M1 for $\frac{1}{m^{\frac{1}{4}}}=\frac{27}{m}$ or better or $m^{-\frac{1}{4}-1}=27$

If $\mathbf{0}$ scored $\mathbf{S C} \mathbf{1}$ for answer $\frac{1}{81}$

Question 178
2.8

3
M1 for $y=\frac{k}{(x-1)^{3}}$
M1 for $y=\frac{\text { their } k}{(4-1)^{3}}$
OR
M2 for $y(4-1)^{3}=9.45(3-1)^{3}$
Question 179

| (a) | $y^{-2}$ or $\frac{1}{y^{2}}$ final answer | $\mathbf{1}$ |  |
| :--- | :--- | ---: | :--- |
| (b) | 7 | $\mathbf{1}$ |  |

Question 180

| (a) | 2.5 | $\mathbf{3}$ | M1 for $y=k \times \sqrt[3]{x+1}$ <br> M1 for $y=$ their $\times \sqrt[3]{124+1}$ |
| :--- | :--- | ---: | :--- |
| (b) | multiplied by 4 oe | $\mathbf{1}$ |  |

## Question 181

## Question 182

$\frac{16}{\sqrt{x}}$ oe final answer
3 M2 for $w=\frac{k}{\sqrt{x}}$ oe
OR
M1 for $w=j \sqrt{y}$
M1 for $y=\frac{c}{x}$

Question 183

| (a) | $[p=] 4$ <br> $[q=]-6$ | 2 | B1 for one correct <br> or $(x+4)^{2}-6$ or $x^{2}+p x+p x+p^{2}[+q]$ |
| :--- | :--- | :--- | :--- |
| (b) | -10 and 2 | $\mathbf{2}$ | M1 for $(x+4)^{2}=36$ <br> or $(x+\text { their } 4)^{2}=30-$ their $(-6)$ <br> or for correct method to solve quadratic <br> e.g. $(x+10)(x-2)$ |

Question 184
$36 y^{144}$ final answer
2
B1 for $k y^{144}$ or $36 y^{k}$ final answer $k \neq 0$ or correct answer seen and spoilt

Question 185
-3
1
Question 186
$\frac{2}{x}$ final answer
4 M1 for $\left[\frac{4}{2 x-3}\right] \times \frac{2 x^{2}+11 x-21}{2 x^{2}+14 x}$ oe soi
B1 for $(x+7)(2 x-3)$ oe factorised
B1 for $2 x(x+7)$ oe factorised
Question 187
8
3

Question 188

| $[0=] 6 x^{2}-19 x+3$ | B5 | B4 for <br> $8 x-20+2 x+2=6 x^{2}+6 x-15 x-15$ or <br> better <br> OR <br> M2 for <br> $4(2 x-5)+2(x+1)=3(x+1)(2 x-5)$ oe <br> or M1 for $4(2 x-5)+2(x+1)$ or better <br> or common denominator $(x+1)(2 x-5)$ or <br> better <br> B1 for $2 x^{2}+2 x-5 x-5$ or better seen <br> M1 for correctly simplifying their <br> quadratic to the form $[0=] ~ a x^{2}+b x+c$ |
| :--- | :--- | :--- |
| Correct method to solve their three term <br> quadratic | M1 | e.g. $(6 x-1)(x-3)$ <br> $-(-19) \pm \sqrt{(-19)^{2}-4 \times 6 \times 3}$ <br> $2 \times 6$ |
| $x=3, x=\frac{1}{6}$ oe | B1 | $\frac{1}{}$ |

Question 189

| (a) | $27 x^{12}$ final answer |  |
| :--- | :--- | :--- |
| (b) | $[ \pm] y$ |  |

2 B1 for $k x^{12}$ or $27 x^{c}$ final answer or for $27 x^{12}$ then spoilt

Question 190
$\frac{144}{w}$ oe

3 M2 for $y=\frac{k}{w}$ oe
or M1 for $x=c w^{2}$ or for $y=\frac{j}{\sqrt{x}}$ oe

Question 191

$$
5 x^{625} \text { final answer }
$$

Question 192
$2 x^{9}$ final answer

2 B1 for final answer $k x^{625}$ or $5 x^{k}$ or correct answer spoiled

Question 193
$\frac{5 x-4}{x+3}$ final answer

Question 194
4.5 oe

Question 195
$5 w^{625}$ final answer

Question 196
$\frac{x+4}{2 x+3}$ final answer

4 B2 for $(5 x-4)(x-3)$
or B1 for $(5 x+a)(x+b)$
with $a b=12$ or $a+5 b=-19$
or for $5 x(x-3)-4(x-3)$
or $x(5 x-4)-3(5 x-4)$
B1 for $(x+3)(x-3)$

3 M2 for $2^{2} \times y=3^{2} \times 2$

OR
M1 for $y=\frac{k}{x^{2}}$
M1 for $y=\frac{\text { theirk }}{2^{2}}$

2 B1 for $k w^{625}$ or $5 w^{k}$ final answer or for $5 w^{625}$ then spoiled

4 B1 for $(2 x-3)(2 x+3)$

B2 for $(2 x-3)(x+4)$
or B1 for $(2 x+a)(x+b)$ where $a b=-12$ or $a+$ $2 b=5$
or $x(2 x-3)+4(2 x-3)$ or $2 x(x+4)-3(x+4)$
Question 197
8

3
M1 for $y=\frac{k}{\sqrt[3]{x+5}}$ oe
M1 for substituting their $k$ into $y=\frac{k}{\sqrt[3]{22+5}}$ oe
OR
M2 for $12 \sqrt[3]{3+5}=y \sqrt[3]{22+5}$ oe

Question 198
$m=\frac{2 k}{(2-R)}$ or $m=\frac{-2 k}{(R-2)}$
final answer

M1 for clearing fractions
M1 for expanding brackets (or $\div 2$ )
M1 for collecting terms in $m$ on one side and terms not in $m$ on the other

M1 for dividing by a bracket maximum of $\mathbf{3}$ if final answer incorrect

Question 199
$\frac{22 x+3}{(3 x+2)(2 x-1)}$ final answer

Question 200
0.16 oe

3 B1 for a common denominator $(3 x+2)(2 x-1)$ oe isw

B1 for $5(2 x-1)+4(3 x+2)$ oe isw

3
M1 for $m=\frac{k}{(t+2)^{2}}$ oe

M1 for substituting their $k$ into $m=\frac{\text { their } k}{(8+2)^{2}}$
OR
M2 for $0.64 \times(3+2)^{2}=m(8+2)^{2}$ oe

Question 201
$\frac{5 c}{2 c-3}$ oe final answer

4 M1 for correctly clearing the denominator and expanding bracket
or
correctly clearing the denominator and dividing by $c$

M1 for correctly collecting terms in $x$ on one side and terms not in $x$ on the other

M1 for correct factorising
M1 for correct division dependent on $x$ appearing only once in a factorised expression

Maximum 3 marks for an incorrect answer

Question 202
3.2 oe

3 M1 for $y=k(x+3)^{2}$ oe or better
M1 for substituting their $k$ into $y=k(1+3)^{2}$

