Extended Mathematics

Topic: Mensuration

Year: May 2013 - May 2023

Paper -2

Answers

Question 1

15.4 or 15.35 to 15.36	4	M1 for $\frac{120}{360} \times \pi \times 5^2$ oe
		M1 for $\frac{1}{2} \times 5^2 \times \sin 120$ oe
		M1 for $\frac{120}{360} \times \pi \times 5^2 - \frac{1}{2} \times 5^2 \times \sin 120$ oe
Question 2		Rei

Question 3

420

M1 for
$$[CB =] \sqrt{4^2 + (9-6)^2}$$

M1 for their CB from Pythagoras × 15

M1 for $[2 \times] \frac{1}{2}(6+9) \times 4$

M1 for 4×15 , 9×15 , 6×15 with intention to add

Question4

52.3 or 52.27 to 52.28

3 SC2 for 28.3 or 28.7 to 28.8

If 0, M2 for
$$\frac{135}{360} \times \pi \times 24 + 2 \times 12$$

or M1 for $\frac{135}{360} \times \pi \times 24$

35.4 or 35.36 to 35.37
M2 for
$$1000 \div (\pi \times 0.75^2 \times 16)$$
 oe or **M1** for $\pi \times 0.75^2 \times 16$ oe or $1000 \div (\pi \times 0.75^2)$

3 M2 for
$$\sqrt[3]{(80 \div \frac{4}{3}\pi)}$$
 oe or M1 for $80 \div \left(\frac{4}{3}\pi\right)$ oe

1FT

Question 7

4 M1 for
$$\frac{1}{2} \times 3^2 \times \pi \times \sin 120$$

M1 for $\frac{30}{360} \times \pi \times 3^2 \times 2$
M1 for area of triangle + 2 sectors

M1 for $\frac{1}{2} \times \frac{4}{3} \times \pi \times 12^3$ or better

M1 for $\frac{1}{2} \times (12 + 22) \times 10$ oe

FT their (a) \times 50

Question 8

Question 9

Question 11

2 | M1 for
$$2 \times \pi \times 2.5$$

| M1 for $\frac{1}{2} \times 4\pi r^2 + \pi r^2 = 243\pi$ or better

A1 for
$$[r =] 9$$

M1 for $\frac{1}{2} \times \frac{4}{3} [\pi] (\text{their } r)^3$

Question 12 150

5 M1 for
$$\frac{2}{3} \times 2\pi \times 6$$

and M2 for $(\frac{2}{3} + \frac{1}{3}) \times 2\pi \times 4$ oe
or M1 for $\frac{2}{3} \times 2\pi \times 4$ or $\frac{1}{3} \times 2\pi \times 4$
and M1 for $2 \times (2+4) + k\pi, k \neq 0$

(a) 3 303 to 304 **(b)**

B3 for 3.536 to 3.54 as an answer

M2 for
$$2000 \div \frac{1}{3} \pi \times 6^2 \times 15$$

or **M1** for
$$\frac{1}{3}\pi \times 6^2 \times 15$$

and SC1 for truncating their 3.54 to a whole number

M2 for $2000 - their 3 \times their$ volume 3 or **M1** for *their* $3 \times their$ volume

- Question 15
- 572.4 Question 16
- 912 or 912.2...

- M1 for figs $(120 \times 90 \times 53)$
- **M4** for $4 \times 0.5 \times 20 \times \sqrt{8^2 + 10^2} + 20 \times 20$ 5 or better or

M3 for $4 \times 0.5 \times 20 \times \sqrt{8^2 + 10^2}$ or better

or

M1 for $\sqrt{8^2 + 10^2}$

and

M1 for $0.5 \times 20 \times \sqrt{8^2 + 10^2}$

M1 for 20×20

2 M1 for
$$30 \div [2]\pi$$

2 M1 for
$$0.5 \times \pi \times (their (\mathbf{a}))^2$$

or $0.5 \times \pi \times (30 \div 2\pi)^2$

Question 19

684

Question 20

(b) 8

Question 21

285 cao

3 M2 for
$$5 \times 12 + \frac{1}{2} \times 12 \times (8 - 5)$$
 or $\frac{1}{2} \times 6 \times (5 + 8) \times 2$ oe or M1 for 5×12 , $\frac{1}{2} \times 12 \times (8 - 5)$, $\frac{1}{2} \times 6 \times (5 + 8)$ or $12 \times 8 - (...)$

1FT $15 \times their$ (a)

1

2FT FT
$$30-2 \times their$$
 (a)

or M1 for $4 \times 7 = 2(x-1) + FG$ oe

or $4(x-4) = 2(x-1) + FG$ oe

or $2 \times 7 + 2(x-4) = 2(x-1) + FG$ oe

Allow x to be their (a) in each

4 M1 for
$$\frac{1}{3} \times \pi \times 4^2 \times 9$$
, 48π
M1 for $\frac{1}{2} \times \frac{4}{3} \times \pi \times 4^3$, $\frac{128\pi}{3}$
A1 for 284.8 to 284.9, $\frac{272\pi}{3}$

If **A0** then **B1** for *their* final answer rounded correctly to nearest whole number from their more accurate answer dependent on at least **M1**

2 M1 for $\frac{1}{2} \times \frac{4}{3} \pi \times 5^3$ If zero scored SC1 for final answer 524 or

Question 23

Parallelogram

1

Question 24

3 M2 for
$$\left[\frac{2}{2}\times\right]6.1\times\pi+2\times6.1$$
 oe

523.5 to 523.7

01

B2 for 19.16 to 19.17 or 19.2

or

M1 for $6.1 \times \pi$ or for $12.2 \times \pi$

Question 25

3 M2 for
$$7^3 - \frac{1}{2} \times \frac{4}{3} \times \pi \times \left(\frac{5}{2}\right)^3$$

or M1 for $\frac{1}{2} \times \frac{4}{3} \times \pi \times \left(\frac{5}{2}\right)^3$
or SC1 for $7^3 - \frac{4}{3} \times \pi \times \left(\frac{5}{2}\right)^3$ soi

Question 26

10.3 oe

2 M1 for 5x = 51.5 oe

Question 27

4 M2 for height =
$$\sqrt{8^2 - 4^2}$$

or M1 for $4^2 + h^2 = 8^2$ oe

and M1 for $\frac{1}{2}(8+12) \times their$ perp height oe

2 M1 for
$$4.5 \times 5$$
 or

Question 30

58

Question 31

68.6 or 68.62 to 68.64

Question 32

62

Question 33

628 or 628.3 to 628.4

cm3

Question 34

81.7 or 81.71 to 81.72...

Question 35

900

Question 36

917 or 918 or 917.4 to 917.6

2 M1 for
$$\left[\frac{1}{2} \times \right] \frac{4}{3} \times \pi \times \left(\frac{5}{2}\right)^3$$

2 M1 for
$$\frac{(13+16)\times 4}{2}$$
 or $4\times 13 + \frac{1}{2}\times 4\times 3$ oe

M1 for
$$\frac{1}{2} \times \frac{4}{3} \pi \times 3.2^3$$

If zero scored, SC1 for final answer 137 or 137.2 to 137.3

3 M1 for [height =]
$$21 \div 7$$

M1 for $2(1 \times their3 + their3 \times 7 + 1 \times 7)$ oe

3 **B2** for 628 or 628.3 to 628.4 or **M1** for
$$5^2 \times 8 \times \pi$$
B1 for cm³

2 M1 for
$$\pi \times 5.1^2$$

3 M2 for
$$\frac{150 \times 100 \times 60}{1000}$$
 oe
or M1 for $150 \times 100 \times 60$ or $1.5[\times 1] \times 0.6$
or B1 for figs 9

3 M2 for
$$\pi \times 2.6^2 \times 12 \times 60 \times 60 \div 1000$$

or M1 for $\pi \times 2.6^2$ isw or $12 \times 60 \times 60 \div 1000$
isw
If 0 scored SC1 for figs 917 to 918

3 M2 for
$$\sqrt{\frac{275 \times 3}{14.8 \times \pi}}$$
 oe
or M1 for $275 = \frac{1}{3} \times \pi \times r^2 \times 14.8$ oe

Question 38

3 M2 for
$$2(12 \times 5 + 12 \times 7.5 + 5 \times 7.5)$$
 oe or M1 for 12×5 or 12×7.5 or 5×7.5

Question 39

2 **M1** for
$$180 \div 6^2$$
 oe

$$\left(\pi \times 5^2 \times 12 - \frac{1}{3} \times \pi \times 5^2 \times 4.8\right) \div \left(\pi \times 5^2\right)$$
or **M3** for $\pi \times 5^2 \times 12 - \frac{1}{3} \times \pi \times 5^2 \times 4.8$

or

M1 for
$$\pi \times 5^2 \times 12$$

M1 for
$$\frac{1}{3} \times \pi \times 5^2 \times 4.8$$

Question 41

3 M2 for $[2 \times]$ (5 × 7 + 5 × 9.5 + 7 × 9.5) oe or M1 for one correct area, 5 × 7 or 5 × 9.5 or 7 × 9.5

4 M3 for
$$1.2 \times 100 \times 60 \times 60 \times 6 \div 1000$$
 oe or M2 for $1.2 \times 60 \times 60 \times 6$ oe or M1 for figs $12 \times$ figs 6 or 60×60 or correct conversion e.g. their value in cm³ ÷ 1000 their value in m³ × 1000 1.2×100 $6 \div 1000$

141 or 141.3 to 141.4

4 M1 for $[2 \times] \pi \times 3^2$ M2 for $2 \times \pi \times 3 \times 4.5$ or M1 for $2 \times \pi \times 3 \times 4.5$

Question 44

208

1

Question 45

45

2 M1 for $\frac{11+7}{2} \times 5$ oe

Question 46

142 or 142.2 to 142.3

3 M2 for $\frac{1}{2} \times 7.4 \times 7.4 \times \sin 60 \times 6$ or $\tan 60 \times \frac{7.4}{2} \times \frac{7.4}{2} \times 6$ or M1 for $\frac{1}{2} \times 7.4 \times 7.4 \times \sin 60$ or $\tan 60 \times \frac{7.4}{2}$

Question 47

86

M1 for correct method to find the perimeter e.g. $(8+3) \times 2 \times 5 - 3 \times 8$ If 0 scored, SC1 for answer 98

Question 48

205.8

M2 for
$$38.4 \times \left(\frac{7}{4}\right)^3$$
 oe

or M1 for $\left(\frac{7}{4}\right)^3$ or $\left(\frac{4}{7}\right)^3$ oe or

 $\frac{7}{4} = \sqrt[3]{\frac{v}{38.4}}$ oe

60

3 M2 for
$$4 \times \sqrt[3]{\frac{40500}{12}}$$
 oe
or M1 for $\left(\frac{4}{l}\right)^3 = \frac{12}{40500}$ oe
or $\sqrt[3]{\frac{40500}{12}}$ oe or $\sqrt[3]{\frac{12}{40500}}$ oe

Question 50

60

3 M2 for
$$12 \times \sqrt{13^2 - 12^2}$$

or M1 for $13^2 - 12^2$
or for $12 \times their$ 5 from Pythagoras or trig

Question 51

9

$$\begin{array}{c|c} \mathbf{2} & \mathbf{M1} \text{ for } \frac{1}{2} \times 6 \times h = 27 \text{ oe} \end{array}$$

Question 52

990 or 989.58 to 989.73

4 M1 for
$$4 \times \pi \times 7^2$$
 [÷2]
M1 for $\pi \times 7^2$
M1 for $\pi \times 7 \times 2 \times 12$

Question 53

34.6 or 34.63 to 34.64

M2 for
$$\frac{1}{4} \times \pi \times 5^2 + \frac{1}{2} \times 5 \times 6$$
 oe
or M1 for $\frac{1}{4} \times \pi \times 5^2$ oe or $\frac{1}{2} \times 5 \times 6$ oe

Question 54

(a)	2

(b) 2 correct lines

2 M1 for
$$2 \times \pi \times 4.7$$
 oe

166

Question 57

90.2 or 90.18...

3 M2 for
$$[2 \times] (7 \times 4 + 4 \times 5 + 5 \times 7)$$

or M1 for 7×4 or 4×5 or 5×7

OR

M3 for
$$[100 \times] \left(k^2 - \frac{45}{360} \times \pi \times \left(\frac{k}{2} \right)^2 \right) \div k^2$$

oe

or **M2** for
$$[100 \times] \frac{45}{360} \times \pi \times \left(\frac{k}{2}\right)^2 \div k^2$$
 oe

or
$$k^2 - \frac{45}{360} \times \pi \times \left(\frac{k}{2}\right)^2$$

or
$$100 \times (k^2 - m\pi k^2) \div k^2$$

or **M1** for
$$\frac{c}{360} \times \pi \times \left(\frac{k}{2}\right)^2$$
 oe

or for
$$(k^2 - m\pi k^2) \div k^2$$

or for $100 \times (k^2 - mk^2) \div k^2$

Question 58

18.4 or 18.40...

4 M3 for
$$\frac{600 - \frac{1}{2} \times 4 \times \pi \times 6.2^2}{62}$$
 oe

or M2 for

$$\frac{1}{2} \times 4 \times \pi \times 6.2^2 + \pi \times 6.2 \times l = 600$$
 oe

or
$$\frac{600 - 4 \times \pi \times 6.2^2}{6.2 \times \pi}$$
 or better

or **M1** for
$$\left\lceil \frac{1}{2} \right\rceil \times 4 \times \pi \times 6.2^2$$
 or $\pi \times 6.2 \times l$

Ouestion 59 180

3 **M2** for
$$[2 \times](8 \times 6 + 8 \times 3 + 3 \times 6)$$
 oe

or **M1** for 8×6 or 8×3 or 3×6

28

Question 61

3.37 or 3.367 to 3.368

3 M2 for
$$24^2 + 12^2 + 8^2$$

or M1 for $24^2 + 12^2$ or $24^2 + 8^2$ or $12^2 + 8^2$

M2 for isolating r^3 , e.g. $r^3 = \frac{120}{\pi}$

or **M1** for $\frac{1}{2} \times \frac{4}{3} \times \pi r^3 = 80$ oe

If 0 scored **SC1** for answer 2.67 or 2.672 to 2.673...

Question 62

16

Question 63

45

3 M2 for
$$12 \times \sqrt[3]{\frac{768}{324}}$$
 oe

or M1 for
$$\sqrt[3]{\frac{768}{324}}$$
 or $\sqrt[3]{\frac{324}{768}}$ or $\frac{h^3}{12^3} = \frac{768}{324}$

3 M2 for
$$\sqrt[3]{\frac{875}{56}} \times 18$$
 oe

or M1 for
$$\sqrt[3]{\frac{875}{56}}$$
 or $\sqrt[3]{\frac{56}{875}}$ oe or $\frac{18^3}{h^3} = \frac{56}{875}$ oe

228 or 228.3 to 228.4

4 M1 for
$$\frac{1}{3} \times \pi \times \left(\frac{9.2}{2}\right)^2 \times 12.5$$
 oe

M1 for
$$\frac{9.2}{12.5} = \frac{diameter}{12.5 - 5.5}$$
 oe or better

M1 for
$$\frac{1}{3} \times \pi \times \left(\frac{their 5.152}{2}\right)^2 \times (12.5 - 5.5)$$
 oe

OR

$$\frac{\pi}{3} \times \left(\frac{9.2}{2}\right)^2 \times 12.5 - \frac{\pi}{3} \times r^2 \times (12.5 - 5.5)$$
 oe for any $r < 4.6$

If 0 scored **SC1** for 913 or 913.3 to 913.5

Question 65

99

3 | **M2** for
$$44 \times \left(\frac{81}{24}\right)^{\frac{2}{3}}$$
 oe

or **M1** for
$$\left(\frac{81}{24}\right)^{\frac{1}{3}}$$
 oe or $\left(\frac{24}{81}\right)^{\frac{1}{3}}$ oe or $\left(\frac{44}{Area}\right)^{3} = \left(\frac{24}{81}\right)^{2}$ oe

Question 66

9.45

3 M2 for
$$\frac{2.7 \times 7.5}{3} + 2.7$$
 oe OR

B2 for 6.75 oe

or **M1** for
$$\frac{3}{7.5} = \frac{2.7}{XC}$$
 oe

If 0 scored **SC1** for answer 7.7

7.00 or 6.998 to 7.002

3 | **M2** for $[r^2] = \frac{1970}{12.8 \times \pi}$ oe or better or **M1** for $1970 = \pi \times r^2 \times 12.8$ or better

Question 68

158

3 M2 for $[2](8\times5+8\times3+5\times3)$ or M1 for 8×5 or 8×3 or 5×3

Question 69 57.9 or 57.90 to 57.91...