Extended Mathematics

Topic: Mensuration

Year: May 2013 - May 2024

Paper -2 Answers

Question 1

15.4 or 15.35 to 15.36

M1 for $\frac{120}{360} \times \pi \times 5^2$ oe

M1 for $\frac{1}{2} \times 5^2 \times \sin 120$ oe

M1 for $\frac{120}{360} \times \pi \times 5^2 - \frac{1}{2} \times 5^2 \times \sin 120$ oe

Question 2

260

M2 for $[2 \times](4 \times 10 + 18 \times 5)$ oe or M1 for a correct area statement

Question 3

420

M1 for $[CB =] \sqrt{4^2 + (9-6)^2}$ M1 for their CB from Pythagoras × 15

M1 for $[2 \times] \frac{1}{2}(6+9) \times 4$ M1 for 4×15 , 9×15 , 6×15 with intention to add

Question4

52.3 or 52.27 to 52.28 3 SC2 for 28.3 or 28.7 to 28.8 If 0, M2 for $\frac{135}{360} \times \pi \times 24 + 2 \times 12$ or M1 for $\frac{135}{360} \times \pi \times 24$

Question 5

35.4 or 35.36 to 35.37 **M2** for $1000 \div (\pi \times 0.75^2 \times 16)$ oe or M1 for $\pi \times 0.75^2 \times 16$ oe or $1000 \div (\pi \times 0.75^2)$

3 M2 for
$$\sqrt[3]{(80 \div \frac{4}{3}\pi)}$$
 oe or M1 for $80 \div \left(\frac{4}{3}\pi\right)$ oe

Question 7

4 M1 for
$$\frac{1}{2} \times 3^2 \times \pi \times \sin 120$$

M1 for $\frac{30}{360} \times \pi \times 3^2 \times 2$
M1 for area of triangle + 2 sectors

M1 for $\frac{1}{2} \times \frac{4}{3} \times \pi \times 12^3$ or better

Question 8

Question 9

Question 10

Question 11

2 M1 for
$$\frac{1}{2} \times (12 + 22) \times 10$$
 oe

FT their (a) \times 50

2 M1 for
$$2 \times \pi \times 2.5$$

1FT

M1 for
$$\frac{1}{2} \times 4\pi r^2 + \pi r^2 = 243\pi$$
 or better **A1** for $[r =]9$
M1 for $\frac{1}{2} \times \frac{4}{3} [\pi] (\text{their } r)^3$

5 M1 for
$$\frac{2}{3} \times 2\pi \times 6$$

and M2 for $(\frac{2}{3} + \frac{1}{3}) \times 2\pi \times 4$ oe
or M1 for $\frac{2}{3} \times 2\pi \times 4$ or $\frac{1}{3} \times 2\pi \times 4$
and M1 for $2 \times (2+4) + k\pi, k \neq 0$

(a) 3 (b) 303 to 304 **B3** for 3.536 to 3.54 as an answer or

M2 for
$$2000 \div \frac{1}{3} \pi \times 6^2 \times 15$$

or **M1** for
$$\frac{1}{3}\pi \times 6^2 \times 15$$

and SC1 for truncating their 3.54 to a whole number

3 M2 for $2000 - their 3 \times their$ volume or M1 for their $3 \times their$ volume

- Question 15
- 572.4 Question 16
- 912 or 912.2...

- 2 M1 for figs $(120 \times 90 \times 53)$
- 5 M4 for $4 \times 0.5 \times 20 \times \sqrt{8^2 + 10^2} + 20 \times 20$ or better or

M3 for
$$4 \times 0.5 \times 20 \times \sqrt{8^2 + 10^2}$$
 or better

or

M1 for
$$\sqrt{8^2 + 10^2}$$

and

M1 for
$$0.5 \times 20 \times \sqrt{8^2 + 10^2}$$

and

M1 for 20×20

Question 17

(a) 4.77 or 4.774 to 4.775

- 2 M1 for $30 \div [2]\pi$
- **(b)** 35.7 or 35.8 or 35.74 to 35.82
- 2 M1 for $0.5 \times \pi \times (their (\mathbf{a}))^2$ or $0.5 \times \pi \times (30 \div 2\pi)^2$

Question 20

Question 21

3 M2 for
$$5 \times 12 + \frac{1}{2} \times 12 \times (8 - 5)$$
 or $\frac{1}{2} \times 6 \times (5 + 8) \times 2$ oe or M1 for 5×12 , $\frac{1}{2} \times 12 \times (8 - 5)$, $\frac{1}{2} \times 6 \times (5 + 8)$ or $12 \times 8 - (...)$

1FT $15 \times their$ (a)

1

2FT FT
$$30-2 \times their$$
 (a)

or M1 for $4 \times 7 = 2(x-1) + FG$ oe

or $4(x-4) = 2(x-1) + FG$ oe

or $2 \times 7 + 2(x-4) = 2(x-1) + FG$ oe

Allow x to be their (a) in each

4 M1 for
$$\frac{1}{3} \times \pi \times 4^2 \times 9$$
, 48π
M1 for $\frac{1}{2} \times \frac{4}{3} \times \pi \times 4^3$, $\frac{128\pi}{3}$
A1 for 284.8 to 284.9, $\frac{272\pi}{3}$

If A0 then B1 for their final answer rounded correctly to nearest whole number from their more accurate answer dependent on at least M1

2 M1 for $\frac{1}{2} \times \frac{4}{3} \pi \times 5^3$ If zero scored SC1 for final answer 524 or 523.5 to 523.7

Question 23

Parallelogram

1

Question 24

3 M2 for
$$\left[\frac{2}{2}\times\right]6.1\times\pi+2\times6.1$$
 oe

01

B2 for 19.16 to 19.17 or 19.2

or

M1 for $6.1 \times \pi$ or for $12.2 \times \pi$

Question 25

3 M2 for
$$7^3 - \frac{1}{2} \times \frac{4}{3} \times \pi \times \left(\frac{5}{2}\right)^3$$

or M1 for $\frac{1}{2} \times \frac{4}{3} \times \pi \times \left(\frac{5}{2}\right)^3$
or SC1 for $7^3 - \frac{4}{3} \times \pi \times \left(\frac{5}{2}\right)^3$ soi

Question 26

2 M1 for 5x = 51.5 oe

Question 27

4 M2 for height =
$$\sqrt{8^2 - 4^2}$$

or M1 for $4^2 + h^2 = 8^2$ oe

and M1 for $\frac{1}{2}(8+12) \times their$ perp height oe

Question 30

58

Question 31

68.6 or 68.62 to 68.64

Question 32

62

Question 33

628 or 628.3 to 628.4

cm³

Question 34

81.7 or 81.71 to 81.72...

Question 35

900

Question 36

917 or 918 or 917.4 to 917.6

2 M1 for
$$\left[\frac{1}{2} \times \right] \frac{4}{3} \times \pi \times \left(\frac{5}{2}\right)^3$$

2 M1 for
$$\frac{(13+16)\times 4}{2}$$
 or $4\times 13 + \frac{1}{2}\times 4\times 3$ oe

M1 for
$$\frac{1}{2} \times \frac{4}{3} \pi \times 3.2^3$$

If zero scored, SC1 for final answer 137 or 137.2 to 137.3

3 M1 for [height =]
$$21 \div 7$$

M1 for $2(1 \times their3 + their3 \times 7 + 1 \times 7)$ oe

3 B2 for 628 or 628.3 to 628.4 or M1 for
$$5^2 \times 8 \times \pi$$
B1 for cm³

2 M1 for
$$\pi \times 5.1^2$$

3 M2 for
$$\frac{150 \times 100 \times 60}{1000}$$
 oe
or M1 for $150 \times 100 \times 60$ or $1.5[\times 1] \times 0.6$
or B1 for figs 9

3 M2 for
$$\pi \times 2.6^2 \times 12 \times 60 \times 60 \div 1000$$

or M1 for $\pi \times 2.6^2$ isw or $12 \times 60 \times 60 \div 1000$
isw
If 0 scored SC1 for figs 917 to 918

3 M2 for
$$\sqrt{\frac{275 \times 3}{14.8 \times \pi}}$$
 oe
or M1 for $275 = \frac{1}{3} \times \pi \times r^2 \times 14.8$ oe

Question 38

3 M2 for
$$2(12 \times 5 + 12 \times 7.5 + 5 \times 7.5)$$
 oe or M1 for 12×5 or 12×7.5 or 5×7.5

Question 39

2 M1 for
$$180 \div 6^2$$
 oe

5 **M4** for

$$\left(\pi \times 5^2 \times 12 - \frac{1}{3} \times \pi \times 5^2 \times 4.8\right) \div \left(\pi \times 5^2\right)$$
or **M3** for $\pi \times 5^2 \times 12 - \frac{1}{3} \times \pi \times 5^2 \times 4.8$

or

M1 for
$$\pi \times 5^2 \times 12$$

M1 for
$$\frac{1}{3} \times \pi \times 5^2 \times 4.8$$

Question 41

3 M2 for $[2 \times]$ (5 × 7 + 5 × 9.5 + 7 × 9.5) oe or M1 for one correct area, 5 × 7 or 5 × 9.5 or 7 × 9.5

4 M3 for
$$1.2 \times 100 \times 60 \times 60 \times 6 \div 1000$$
 oe or M2 for $1.2 \times 60 \times 60 \times 6$ oe or M1 for figs $12 \times$ figs 6 or 60×60 or correct conversion e.g. their value in cm³ ÷ 1000 their value in m³ × 1000 1.2×100 $6 \div 1000$

141 or 141.3 to 141.4

4 M1 for $[2 \times] \pi \times 3^2$ M2 for $2 \times \pi \times 3 \times 4.5$ or M1 for $2 \times \pi \times 3 \times 4.5$

Question 44

208

1

Question 45

45

2 | **M1** for $\frac{11+7}{2} \times 5$ oe

Question 46

142 or 142.2 to 142.3

3 M2 for $\frac{1}{2} \times 7.4 \times 7.4 \times \sin 60 \times 6$ or $\tan 60 \times \frac{7.4}{2} \times \frac{7.4}{2} \times 6$ or M1 for $\frac{1}{2} \times 7.4 \times 7.4 \times \sin 60$ or $\tan 60 \times \frac{7.4}{2}$

Question 47

86

2 M1 for correct method to find the perimeter e.g. $(8+3) \times 2 \times 5 - 3 \times 8$ If 0 scored, SC1 for answer 98

Question 48

205.8

M2 for
$$38.4 \times \left(\frac{7}{4}\right)^3$$
 oe
or M1 for $\left(\frac{7}{4}\right)^3$ or $\left(\frac{4}{7}\right)^3$ oe or $\frac{7}{4} = \sqrt[3]{\frac{v}{38.4}}$ oe

60

3 M2 for
$$4 \times \sqrt[3]{\frac{40500}{12}}$$
 oe
or M1 for $\left(\frac{4}{l}\right)^3 = \frac{12}{40500}$ oe
or $\sqrt[3]{\frac{40500}{12}}$ oe or $\sqrt[3]{\frac{12}{40500}}$ oe

Question 50

60

3 M2 for
$$12 \times \sqrt{13^2 - 12^2}$$

or M1 for $13^2 - 12^2$
or for $12 \times their$ 5 from Pythagoras or trig

Question 51

9

$$\begin{array}{c|c} \mathbf{2} & \mathbf{M1} \text{ for } \frac{1}{2} \times 6 \times h = 27 \text{ oe} \end{array}$$

Question 52

990 or 989.58 to 989.73

4 M1 for
$$4 \times \pi \times 7^2$$
 [÷2]
M1 for $\pi \times 7^2$
M1 for $\pi \times 7 \times 2 \times 12$

Question 53

34.6 or 34.63 to 34.64

M2 for $\frac{1}{4} \times \pi \times 5^2 + \frac{1}{2} \times 5 \times 6$ oe or M1 for $\frac{1}{4} \times \pi \times 5^2$ oe or $\frac{1}{2} \times 5 \times 6$ oe

Question 54

(2)	2
(a)	2

(b) 2 correct lines

2 B1 for each

Question 55

29.5 or 29.53...

2 M1 for
$$2 \times \pi \times 4.7$$
 oe

166

Question 57

90.2 or 90.18...

3 M2 for
$$[2 \times] (7 \times 4 + 4 \times 5 + 5 \times 7)$$

or M1 for 7×4 or 4×5 or 5×7

OR

M3 for
$$[100 \times] \left(k^2 - \frac{45}{360} \times \pi \times \left(\frac{k}{2} \right)^2 \right) \div k^2$$

oe

or **M2** for
$$[100 \times] \frac{45}{360} \times \pi \times \left(\frac{k}{2}\right)^2 \div k^2$$
 oe

or
$$k^2 - \frac{45}{360} \times \pi \times \left(\frac{k}{2}\right)^2$$

or
$$100 \times (k^2 - m\pi k^2) \div k^2$$

or M1 for
$$\frac{c}{360} \times \pi \times \left(\frac{k}{2}\right)^2$$
 oe

or for
$$(k^2 - m\pi k^2) \div k^2$$

or for $100 \times (k^2 - mk^2) \div k^2$

Question 58

18.4 or 18.40...

4 M3 for
$$\frac{600 - \frac{1}{2} \times 4 \times \pi \times 6.2^2}{6.2 \times 7}$$
 oe

or M2 for

$$\frac{1}{2} \times 4 \times \pi \times 6.2^2 + \pi \times 6.2 \times l = 600$$
 oe

or
$$\frac{600 - 4 \times \pi \times 6.2^2}{6.2 \times \pi}$$
 or better

or **M1** for
$$\left[\frac{1}{2}\right] \times 4 \times \pi \times 6.2^2$$
 or $\pi \times 6.2 \times l$

Ouestion 59 180

3 M2 for
$$[2\times](8\times6+8\times3+3\times6)$$
 oe
or M1 for 8×6 or 8×3 or 3×6

28

Question 61

3 M2 for
$$24^2 + 12^2 + 8^2$$

or M1 for $24^2 + 12^2$ or $24^2 + 8^2$ or $12^2 + 8^2$

3 M2 for isolating
$$r^3$$
, e.g. $r^3 = \frac{120}{\pi}$

or **M1** for
$$\frac{1}{2} \times \frac{4}{3} \times \pi r^3 = 80$$
 oe

If 0 scored SC1 for answer 2.67 or 2.672 to 2.673...

Question 62

16

$$\mathbf{M2} \text{ for } 12 \times \sqrt[3]{\frac{768}{324}} \text{ oe}$$
or $\mathbf{M1} \text{ for } \sqrt[3]{\frac{768}{324}} \text{ or } \sqrt[3]{\frac{324}{768}} \text{ or } \frac{h^3}{12^3} = \frac{768}{324}$
nuestion 63

Question 63

45

3 M2 for
$$\sqrt[3]{\frac{875}{56}} \times 18$$
 oe

or M1 for $\sqrt[3]{\frac{875}{56}}$ or $\sqrt[3]{\frac{56}{875}}$ oe or

 $\frac{18^3}{h^3} = \frac{56}{875}$ oe

228 or 228.3 to 228.4

4 M1 for $\frac{1}{3} \times \pi \times \left(\frac{9.2}{2}\right)^2 \times 12.5$ oe

M1 for $\frac{9.2}{12.5} = \frac{diameter}{12.5 - 5.5}$ oe or better

M1 for $\frac{1}{3} \times \pi \times \left(\frac{their 5.152}{2}\right)^2 \times (12.5 - 5.5)$ oe

OR

M2 for

 $\frac{\pi}{3} \times \left(\frac{9.2}{2}\right)^2 \times 12.5 - \frac{\pi}{3} \times r^2 \times (12.5 - 5.5)$ oe for any r < 4.6

If 0 scored SC1 for 913 or 913.3 to 913.5

Question 65

99

3 | **M2** for $44 \times \left(\frac{81}{24}\right)^{\frac{2}{3}}$ oe

or **M1** for $\left(\frac{81}{24}\right)^{\frac{1}{3}}$ oe or $\left(\frac{24}{81}\right)^{\frac{1}{3}}$ oe or $\left(\frac{44}{Area}\right)^{3} = \left(\frac{24}{81}\right)^{2}$ oe

Question 66

9.45

3 M2 for $\frac{2.7 \times 7.5}{3} + 2.7$ oe

OR

B2 for 6.75 oe

or **M1** for $\frac{3}{7.5} = \frac{2.7}{XC}$ oe

If 0 scored **SC1** for answer 7.7

3 M2 for
$$[r^2] = \frac{1970}{12.8 \times \pi}$$
 oe or better
or M1 for $1970 = \pi \times r^2 \times 12.8$ or better

Question 68

3 M2 for
$$[2](8 \times 5 + 8 \times 3 + 5 \times 3)$$

or M1 for 8×5 or 8×3 or 5×3

Question 69 57.9 or 57.90 to 57.91...

Question 70

4 M2 for
$$\frac{105}{2 \times 12.5}$$
 oe
or M1 for $2 \times \pi \times r \times 12.5 = 105\pi$ or better
M1 for $\pi \times (their \ r)^2 \times 12.5$

Question 71

4 B3 for answer figs 157[0] or 1573...

OR

M2 for
$$\frac{4}{3} \times \pi \times 3.6^3 \times 8.05$$
 oe or better

or M1 for $\frac{4}{3} \times \pi \times 3.6^3$ oe

M1 for division by 1000 of *their* mass in g and correct rounding to 3 dp

4 M3 for
$$2 \times \pi \times 5 \times 8 + 2 \times \pi \times 5^2$$
 oe

OR

M1 for $2 \times \pi \times 5 \times 8$

M1 for $[2] \times \pi \times 5^2$

Question 74
$$a = 18$$
 $b = 10$ $c = 4$ $d = 9$

2 M1 for
$$\frac{1}{2} \times (5.3 + 8.7) \times 3.8$$
 oe

4 B1 for each If 0 scored, SC1 for b or
$$c = 4$$
, 5 or 10

2 M1 for
$$10 \times 7 \times [...] = 280$$
 oe or better

