

Extended Mathematics
Topic : Probability
Year : May 2013 - May 2024

Paper -2

Answers

Question 1

| | | | |
|-----|-------------------|---|---|
| (a) | $\frac{5}{25}$ oe | 2 | B1 for answer $\frac{5}{k}$ or $\frac{k}{25}$ |
| (b) | $\frac{4}{25}$ oe | 2 | B1 for answer $\frac{4}{k}$ or $\frac{k}{25}$ |

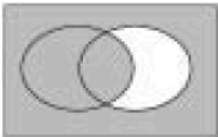
Question 2

| | | |
|---------------------|---|--|
| $\frac{30}{300}$ oe | 2 | M1 for 30 seen or $\frac{k}{300}$ seen |
|---------------------|---|--|

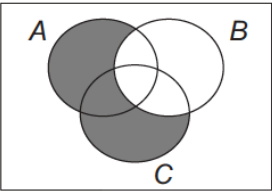
Question 3

| | | |
|----------------------|-----|--|
| (a) $\frac{2}{6}$ oe | 1 | |
| (b) 200 | 1FT | FT $600 \times \text{their (a)}$ providing <i>their (a)</i> is a probability |

Question 4

| | | |
|---|---|---|
| (a) (i) $\frac{5}{50}$ oe | 1 | |
| (ii) $\frac{11}{50}$ oe | 1 | |
| (b) $\frac{11}{16}$ oe | 1 | |
| (c) $\frac{380}{2450}$ oe | 2 | M1 for $\frac{20}{50} \times \frac{19}{49}$ |
| (d)  | 1 | |

Question 5

| | | |
|---------|---|---|
| (a) (i) | 4 | 1 |
| (ii) | {3, 9} | 1 |
| (iii) | fewer than 6 numbers from {1, 3, 5, 7, 9, 11} or \emptyset | 1 |
| (b) | ξ  | 1 |

Question 6

| | | |
|--------|---|----------------------------------|
| 0.2 oe | 2 | M1 for $1 - (0.15 + 0.3 + 0.35)$ |
|--------|---|----------------------------------|

Question 7

| | | |
|--|---|---|
| Sammy and correct reason with 25.7% oe shown | 2 | B1 for 25.7% or 0.257... seen or conversion of 26% to fraction and common denominator |
|--|---|---|

Question 8

| | | |
|---------|---|---|
| 0.96 oe | 3 | M2 for $1 - 0.2 \times 0.2$ or $0.8 + 0.2 \times 0.8$ or $0.8 \times 0.8 + 0.8 \times 0.2 + 0.2 \times 0.8$ or B1 for one of 0.2×0.2 , 0.8×0.8 , 0.8×0.2 , 0.2×0.8 seen |
|---------|---|---|

Question 9

| | |
|---|---|
| 6 | 1 |
|---|---|

Question 10

| | | |
|---------|-----------------------------------|---|
| (a) | $\frac{8}{14}$ and $\frac{5}{13}$ | 1 |
| | $\frac{6}{13}$ and $\frac{7}{13}$ | 1 |
| (b) (i) | $\frac{30}{182}$ oe | 2 M1FT for $\frac{6}{14} \times \text{their } \frac{5}{13}$ |

| | | | |
|------|----------------------|---|---|
| (ii) | $\frac{126}{182}$ oe | 3 | M2FT for $1 - \frac{8}{14} \times \frac{7}{13}$ or $\frac{6}{14} \times \frac{5}{13} + \frac{6}{14} \times \frac{8}{13} + \frac{8}{14} \times \frac{6}{13}$ or $\frac{6}{14} + \frac{8}{14} \times \frac{6}{13}$ oe or M1FT for sum of any two of $\frac{6}{14} \times \frac{5}{13}$ or $\frac{6}{14} \times \frac{8}{13}$ or $\frac{8}{14} \times \frac{6}{13}$ |
|------|----------------------|---|---|

Question 11

| | | | |
|-----|---------|---|---|
| (a) | 0.16 oe | 2 | M1 for 0.4×0.4 If zero scored SC1 for fully correct evaluated method involving a without replacement method |
| (b) | 0.58 oe | 4 | M3 for $1 - (0.4^2 + 0.5^2 + 0.1^2)$ oe or M2 for $0.4^2 + 0.5^2 + 0.1^2$ |

Question 12

| | | | |
|---------|--|---|--|
| (a) | $\frac{2}{3}$ oe | 1 | |
| (b) | their $\frac{2}{3}$, $\frac{7}{8}$, $\frac{5}{8}$ oe | 2 | B1 for either $\frac{7}{8}$ or $\frac{5}{8}$ |
| (c) (i) | $\frac{1}{24}$ oe | 2 | M1 for $\frac{1}{3} \times \frac{1}{8}$ seen |
| (ii) | $\frac{17}{24}$ oe | 3 | M2FT for $\frac{1}{3} \times \frac{7}{8} + \frac{2}{3} \times \frac{5}{8}$ or M1FT for $\frac{1}{3} \times \frac{7}{8}$ or $\frac{2}{3} \times \frac{5}{8}$ |

Question 13

| | | | |
|-----|------------------------|---|---|
| (a) | 0.6 oe | 1 | |
| (b) | 20 0.3 oe 0.3 oe | 2 | B1 for 20 B1 for 0.3 oe and 0.3 oe |

Question 14

$$\frac{5}{6} \text{ oe}$$

3

M2 for $1 - \frac{2}{3} \times \frac{1}{4}$ or $\frac{1}{3} + \frac{2}{3} \times \frac{3}{4}$
 or $\frac{1}{3} \times \frac{3}{4} + \frac{1}{3} \times \frac{1}{4} + \frac{2}{3} \times \frac{3}{4}$
 or **M1** for $\frac{2}{3} \times \frac{1}{4}$ or $\frac{1}{3} \times \frac{1}{4} + \frac{2}{3} \times \frac{3}{4}$

Question 15

$$\frac{4}{25} \text{ oe}$$

2

M1 for $\frac{2}{5} \times \frac{2}{5}$ oe or denominator 5^2 oe

Question 16

[0].15 oe

1

Question 17

| | | | | | | | | | | | | | |
|---------|--|---|----|----|---|----|---|---|---|----|----|---|--|
| (a) | <table><tr><td>5</td><td>7</td><td>7</td><td>8</td><td>10</td></tr><tr><td>7</td><td>9</td><td>9</td><td>10</td><td>12</td></tr></table> | 5 | 7 | 7 | 8 | 10 | 7 | 9 | 9 | 10 | 12 | 1 | |
| 5 | 7 | 7 | 8 | 10 | | | | | | | | | |
| 7 | 9 | 9 | 10 | 12 | | | | | | | | | |
| (b) | 7 | 1 | | | | | | | | | | | |
| (c)(i) | $\frac{7}{25}$ or 0.28 or 28% | 2FT FT $\frac{\text{their } 7}{25}$ B1 for $\frac{k}{25}$ If zero scored, then SC1 for $\frac{2}{5}$ or $\frac{6}{15}$ if no values in the bottom two rows of the table. | | | | | | | | | | | |
| (c)(ii) | 0 | 1FT FT $\frac{\text{their } 0}{25}$ | | | | | | | | | | | |

Question 18

| |
|---------------------|
| rt |
| $(1 - t)r$ |
| $(1 - r)t$ oe |
| $(1 - r)(1 - t)$ oe |

3

B1 for each

Question 19

| | | | |
|---------|------------------------------------|-----------|--|
| (a) | $\frac{9}{20}$ oe | 1 | |
| (b)(i) | $\frac{6}{20} \times \frac{5}{19}$ | M1 | |
| | $\frac{30}{380}$ oe | A1 | |
| (b)(ii) | $\frac{258}{380}$ oe | 4 | <p>M3 for $1 - \frac{3}{38} - \frac{5}{20} \times \frac{4}{19} - \frac{9}{20} \times \frac{8}{19}$ oe</p> <p>or M2 for $\frac{3}{38} + \frac{5}{20} \times \frac{4}{19} + \frac{9}{20} \times \frac{8}{19}$ oe</p> <p>or $\frac{5}{20} \times \frac{9}{19} + \frac{6}{20} \times \frac{9}{19} + \frac{6}{20} \times \frac{5}{19}$ oe</p> <p>or M1 for one correct product other than $\frac{6}{20} \times \frac{5}{19}$</p> |

Question 20

| | | | |
|-----|-------------------|----------|--|
| (a) | $\frac{4}{5}$ oe | 2 | M1 for $\frac{2}{3} \times p = \frac{8}{15}$ or better |
| (b) | $\frac{1}{15}$ oe | 3 | <p>3FT $(1 - \text{their } \frac{4}{5}) \times \frac{1}{3}$ correctly evaluated</p> <p>M2 for $(1 - \text{their } \frac{4}{5}) \times (1 - \frac{2}{3})$ oe</p> <p>or M1 for $1 - \text{their } \frac{4}{5}$ or $1 - \frac{2}{3}$</p> |

Question 21

| | | | |
|-----|----------------------|----------|--|
| (a) | $\frac{8}{15}$ oe | 1 | |
| (b) | $\frac{168}{210}$ oe | 3 | <p>M2 for $1 - \frac{7}{15} \times \frac{6}{14}$ oe or $3(\frac{7 \times 8}{15 \times 14})$ oe</p> <p>or M1 for $\frac{7}{15} \times \frac{6}{14}$ or $\frac{7}{15} \times \frac{8}{14}$ or $\frac{8}{15} \times \frac{7}{14}$ oe</p> |

Question 22

| | | | |
|-----|---------------------|---|---|
| (a) | $\frac{94}{200}$ oe | 2 | M1 for $\frac{46}{200} + \frac{48}{200}$ oe |
| (b) | 14.1 or 14.07... | 3 | M2 for $2\left(\frac{50}{200} \times \frac{56}{199}\right)$ oe or M1 for $\frac{50}{200} \times \frac{56}{199}$ oe |

Question 23

| | | |
|----|---|--|
| 70 | 2 | M1 for $25\,000 \times 0.0028$ oe |
|----|---|--|

Question 24

| | | |
|-------------------|---|---|
| $\frac{2}{20}$ oe | 2 | M1 for $\frac{2}{5} \times \frac{1}{4}$ oe |
|-------------------|---|---|

Question 25

| | | | |
|-----|----------|---|---|
| (a) | 0.3 oe | 2 | M1 for 0.4×0.75 |
| (b) | 0.975 oe | 2 | M1 for $1 - 0.4 \times 0.25 \times 0.25$ oe or $0.6 + 0.4 \times 0.75 + 0.4 \times 0.25 \times 0.75$ or $0.6 + \textit{their (a)} + 0.4 \times 0.25 \times 0.75$ |

Question 26

| | | |
|----------------------|---|--|
| $\frac{147}{160}$ oe | 3 | M2 for $\frac{1}{10} \times \frac{3}{4} + \frac{9}{10} \times \frac{15}{16}$ or M1 for $\frac{1}{10} \times \frac{3}{4}$ or $\frac{9}{10} \times \frac{15}{16}$ |
|----------------------|---|--|

Question 27

| | | |
|----|---|--|
| 42 | 2 | M1 for $\frac{7}{15} [\times 90]$ |
|----|---|--|

Question 28

| | | | |
|-----|---------|---|---|
| (a) | 0.22 oe | 2 | M1 for $0.15 + 0.2 + ? + 0.43 = 1$ or better |
| (b) | 40 | 1 | |

Question 29

| | | | |
|-----|----|---|---|
| (a) | 50 | 2 | M1 for $\frac{5}{7+5+2} [\times 140]$ or $\frac{140}{7+5+2} [\times 5]$ |
| (b) | 26 | 2 | M1 for $\frac{5+9}{n} = \frac{2}{7}$ oe or $\frac{5+9}{p+7+5+2+9} = \frac{2}{7}$ oe |

Question 30

0.845 oe

3 **M2** for $0.7 \times 0.95 + (1 - 0.7) \times 0.6$ oe
or **M1** for one of these products

Question 31

| | | | |
|-----|-------------------|---|--|
| (a) | $\frac{3}{10}$ oe | 1 | |
| (b) | 35 | 1 | |

Question 32

$\frac{19}{60}$ oe

3 **M2** for $\frac{8}{16} \times \frac{7}{15} + \frac{5}{16} \times \frac{4}{15}$
or **M1** for $\frac{8}{16} \times \frac{7}{15}$ or $\frac{5}{16} \times \frac{4}{15}$
If 0 scored **SC1** for $\frac{89}{256}$ oe

Question 33

0.85 oe

1

Question 34

| | | | | | | | | | | | | | | | | | | | | | | | |
|-----|---|----|----------------|--|--|---|---|---|---|---|---|---|----|---|---|---|----|---|---|----|----|---|--|
| (a) | <div>Prime numbers</div> <table><tr><td></td><td colspan="3">Multiples of 3</td></tr><tr><td>+</td><td>3</td><td>6</td><td>9</td></tr><tr><td>2</td><td>5</td><td>8</td><td>11</td></tr><tr><td>3</td><td>6</td><td>9</td><td>12</td></tr><tr><td>5</td><td>8</td><td>11</td><td>14</td></tr></table> | | Multiples of 3 | | | + | 3 | 6 | 9 | 2 | 5 | 8 | 11 | 3 | 6 | 9 | 12 | 5 | 8 | 11 | 14 | 2 | B1 for at least 4 correct entries |
| | Multiples of 3 | | | | | | | | | | | | | | | | | | | | | | |
| + | 3 | 6 | 9 | | | | | | | | | | | | | | | | | | | | |
| 2 | 5 | 8 | 11 | | | | | | | | | | | | | | | | | | | | |
| 3 | 6 | 9 | 12 | | | | | | | | | | | | | | | | | | | | |
| 5 | 8 | 11 | 14 | | | | | | | | | | | | | | | | | | | | |

| | | | |
|-----|------------------|---|--|
| (b) | $\frac{2}{5}$ oe | 2 | B2FT for $\frac{their\ 2}{their\ 5}$ or B1FT for $\frac{their\ 2}{k}$ k is any integer in the range $1 \leq k \leq 7$ or $\frac{c}{their\ 5}$ c is 0, 1 or 2 |
|-----|------------------|---|--|

| | | | |
|-----|------------------|---|--|
| (b) | $\frac{2}{5}$ oe | 2 | B2FT for $\frac{\text{their } 2}{\text{their } 5}$ or B1FT for $\frac{\text{their } 2}{k}$ k is any integer in the range $1 \leq k \leq 7$ or $\frac{c}{\text{their } 5}$ c is 0, 1 or 2 |
|-----|------------------|---|--|

Question 35

| | | |
|--------------------|---|--|
| $\frac{37}{60}$ oe | 4 | B3 for $x = 18$ or 37 [yellow] or SC2 for answer $\frac{5}{12}$ or M2 for $\frac{1}{12} = \frac{5}{5+x+2x+1}$ oe or M1 for $5 + x + 2x + 1$ oe or [total number of flowers =] 60 |
|--------------------|---|--|

Question 36

| | | |
|---------|---|--|
| 0.95 oe | 1 | |
|---------|---|--|

Question 37

| | | | |
|-----|----------------------|---|---|
| (a) | $(M \cup G) \cap P'$ | 1 | |
| (b) | 22 | 1 | |
| (c) | $\frac{8}{23}$ oe | 2 | M1 for $\frac{k}{23}$ or $\frac{k}{3+9+5+6}$ or $\frac{8}{c}$ or $\frac{3+5}{c}$ $c \neq 1$ or for 8 and 23 identified |

Question 38

| | | |
|---------|---|-------------------------------------|
| 0.48 oe | 2 | M1 for $1 - (0.2 + 0.32)$ oe |
|---------|---|-------------------------------------|

Question 39

| | | | |
|-----|----------------------------------|---|---|
| (a) | $\frac{7}{20}$ oe or 0.35 or 35% | 2 | M1 for $1 - \left(\frac{2}{5} + \frac{1}{4}\right)$ oe |
| (b) | 48 | 1 | |

Question 40

| | | |
|------------------|---|--|
| $\frac{3}{7}$ oe | 3 | M1 for clearly identifying the 7 even outcomes 2 6, 3 5, 3 7, 3 9, 5 5, 5 7, 5 9 M1 for clearly identifying the 3 even outcomes with just one five 3 5, 5 7 and 5 9 If 0 scored SC1 for answer $\frac{1}{4}$ oe |
|------------------|---|--|

Question 41

| | | | |
|---------|------------------|---|--|
| (a)(i) | $\frac{3}{4}$ oe | 1 | |
| (a)(ii) | 45 | 1 | FT $60 \times$ <i>their</i> (a)(i) correctly evaluated |

| | | | |
|-----|--------------------|---|--|
| (b) | $\frac{47}{66}$ oe | 4 | M3 for $1 - \left(\frac{5}{12} \times \frac{4}{11} + \frac{4}{12} \times \frac{3}{11} + \frac{3}{12} \times \frac{2}{11} \right)$ oe or M2 for $\left(\frac{5}{12} \times \frac{4}{11} + \frac{4}{12} \times \frac{3}{11} + \frac{3}{12} \times \frac{2}{11} \right)$ oe or $\left(\frac{5}{12} \times \frac{4}{11} + \frac{5}{12} \times \frac{3}{11} + \frac{4}{12} \times \frac{3}{11} \right)$ oe or M1 for $\frac{5}{12} \times \frac{4}{11}$ or $\frac{5}{12} \times \frac{3}{11}$ or $\frac{4}{12} \times \frac{3}{11}$ or $\frac{3}{12} \times \frac{2}{11}$ oe If 0 scored, SC1 for $\frac{47}{72}$ oe |
| (c) | 5 | 2 | M1 for correct trial to at least two balls one of which is not green |

Question 42

7

- 2 **B1** for answer 6
or **M1** for $\left(\frac{2}{3} \right)^k \left(\frac{1}{3} \right)$ shown with $k > 1$
or $\left(\frac{2}{3} \right)^{an+b} \left(\frac{1}{3} \right) = \frac{64}{2187}$ oe
or for $3^n = 2187$ soi or $2^{n-1} = 64$
or $3^{n-1} = 729$ or better

Question 43

- (a) 0.11 oe
- 2 **M1** for $1 - (0.3 + 0.16 + 0.18 + 0.25)$ oe
or **B1** for 0.89 oe

- (b) 0.46 oe

- 2 **M1** for $0.3 + 0.16$

Question 44

$\frac{1}{3}$ oe

- 3 **M1** for $\left(1 - \frac{2}{5} \right) \times p = \frac{1}{10}$ oe
M1 for $\frac{2}{5} \times (1 - \text{their } p)$ where $0 < \text{their } p < 1$

Question 45

0.4 oe

- 2 **M1** for $1 - (0.2 + 0.05 + 0.35)$ oe
or **B1** for 0.6 oe

Question 46

$$\frac{20}{39} \text{ oe}$$

3

M2 for $\frac{5}{13} \times \frac{8}{12} [\times 2]$ oe

or **M1** for $\frac{5}{13}$ or $\frac{8}{12}$ or $\frac{5}{12}$ or $\frac{8}{13}$

If 0 scored **SC1** for answer $\frac{80}{169}$ oe

Question 47

$$0.22 \text{ oe}$$

2

M1 for $1 - (0.3 + 0.35 + 0.13)$ oe

or **B1** for 0.78 oe

Question 48

(a) 0.11 oe

2

M1 for $1 - (0.4 + 0.32 + 0.17)$ oe

(b) 576

1

Question 49

$$\frac{2}{3} \text{ oe nfww}$$

4

M3 for $\frac{2}{13} \times \frac{11}{12} + \frac{5}{13} \times \frac{8}{12} + \frac{6}{13} \times \frac{7}{12}$ oe

or $1 - \left(\frac{2}{13} \times \frac{1}{12} + \frac{5}{13} \times \frac{4}{12} + \frac{6}{13} \times \frac{5}{12} \right)$ oe

or **M2** for sum of three or more correct product pairs and no incorrect pairs

or for $\frac{2}{13} \times \frac{1}{12} + \frac{5}{13} \times \frac{4}{12} + \frac{6}{13} \times \frac{5}{12}$ and no other pairs

or **M1** for $\frac{j}{13} \times \frac{k}{12}$

If 0 scored **SC1** for answer $\frac{104}{169}$ oe

Question 50

14

1

Question 51

| | | | |
|-----|--------------------|---|--|
| (a) | 54 | 2 | M1 for $\frac{3}{20}[\times 360]$ oe or $\frac{360}{20}[\times 3]$ oe |
| (b) | $\frac{17}{20}$ oe | 1 | |

Question 52

0.85 oe | 1

Question 53

93 | 2

M1 for $\frac{3}{40}[\times 1240]$ oe or $\frac{1240}{40}[\times 3]$ oe
 or $\frac{40}{3} = \frac{1240}{x}$ oe

Question 54

0.225 oe | 4

M3 for $\left(1 - \frac{0.25}{0.4}\right) \times (1 - 0.4)$ oe
 OR
M2 for $\frac{0.25}{0.4}$
 or **M1** for $0.4 \times p = 0.25$ oe
M1 for $(1 - \text{their } P(\text{Jen red})) \times (1 - 0.4)$ oe

Question 55

| | | | |
|-----|---------------|---|--|
| (a) | 0.4 oe | 1 | |
| (b) | 42 0.2 0.2 | 2 | B1 for 42 B1 for 0.2 and 0.2 If B0 scored SC1 for <i>their</i> two probabilities being half <i>their</i> (a) |