Extended Mathematics Topic : Statistics Year :May 2013 -May 2023 Paper -2 Questions Booklet

Question 1

The heights, in metres, of 200 trees in a park are measured.

| Height (<i>h</i> m) | $2 \le h \le 6$ | $6 \le h \le 10$ | $10 \le h \le 13$ | $13 < h \le 17$ | $17 < h \le 19$ | $19 < h \le 20$ |
|----------------------|-----------------|------------------|-------------------|-----------------|-----------------|-----------------|
| Frequency | 23 | 47 | 45 | 38 | 32 | 15 |

(a) Find the interval which contains the median height.

Answer(a)[1]

(b) Calculate an estimate of the mean height.

Answer(b) m [4]

(c) Complete the cumulative frequency table for the information given in the table above.

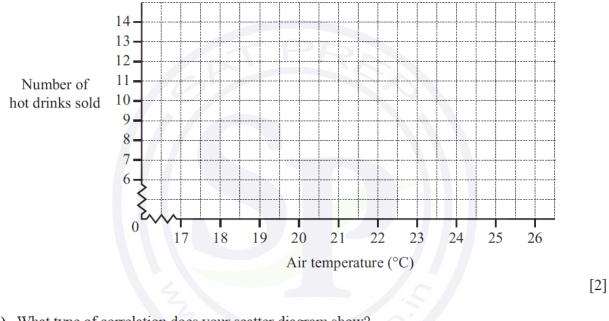
| Height (hm) | $2 < h \le 6$ | $h \leq 10$ | $h \le 13$ | $h \le 17$ | <i>h</i> ≤ 19 | $h \leq 20$ |
|----------------------|---------------|-------------|------------|------------|---------------|-------------|
| Cumulative frequency | 23 | | | | | |

[2]

The owner of a small café records the average air temperature and the number of hot drinks he sells each day for a week.

| Air temperature (°C) | 18 | 23 | 19 | 23 | 24 | 25 | 20 |
|---------------------------|----|----|----|----|----|----|----|
| Number of hot drinks sold | 12 | 8 | 13 | 10 | 9 | 7 | 12 |

(a) On the grid, draw a scatter diagram to show this information.

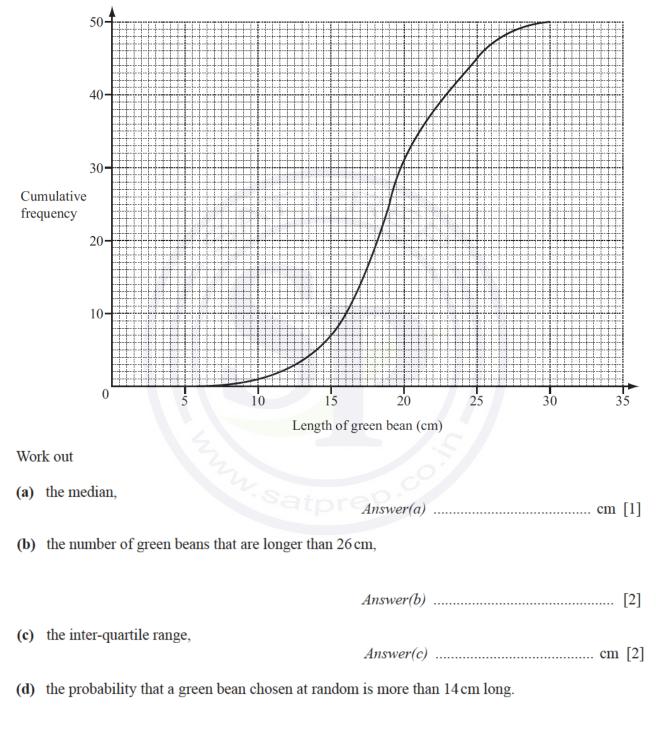


(b) What type of correlation does your scatter diagram show?

(c) Draw a line of best fit on the grid.

[1]

18 A gardener measured the lengths of 50 green beans from his garden. The results have been used to draw this cumulative frequency diagram.



Answer(d) [2]

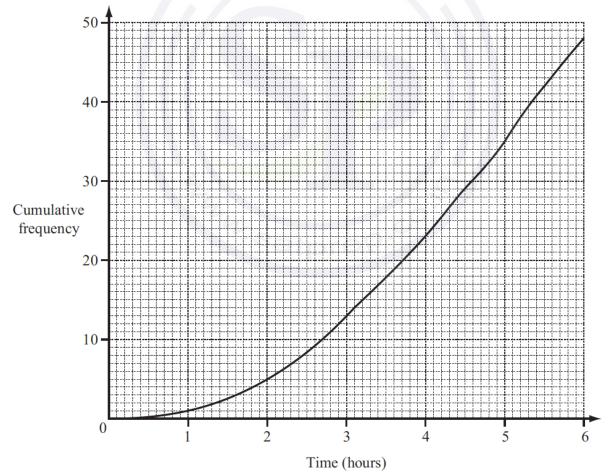
Bruce plays a game of golf. His scores for each of the 18 holes are shown below.

The information is to be shown in a pie chart.

Calculate the sector angle for the score of 4.

Question 5

During one day 48 people visited a museum. The length of time each person spent in the museum was recorded. The results are shown on the cumulative frequency diagram.



Continue on the next page.

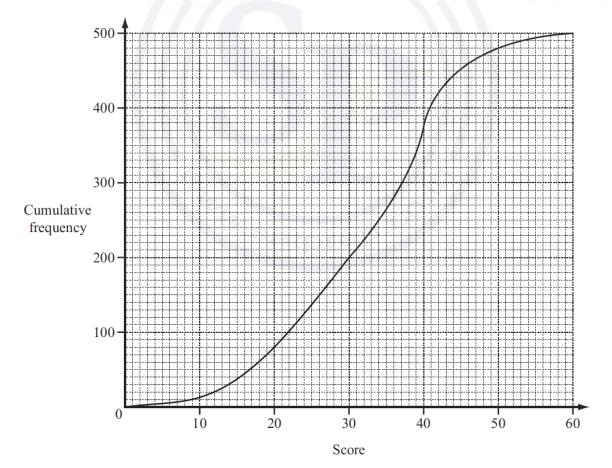
Work out

(a) the median,

| | Ansv | ver(a) | h [1] | | |
|------------|--|---------|-------|--|--|
| (b) |) the 20th percentile, | ver(h) | h [2] | | |
| | e) the inter-quartile range, | ver (b) | | | |
| (0) | , 1 0, | ver(c) | h [2] | | |
| (d) |) the probability that a person chosen at random spends 2 hours or less in the museum. | | | | |

Question 6

Jenna draws a cumulative frequency diagram to show information about the scores of 500 people in a quiz.



Continue on the next page..

Use the diagram to find

(a) the median score,

(b) the inter-quartile range,

(c) the 40th percentile,

(d) the number of people who scored 30 or less but more than 20.

Answer(d) [1]

Question 7

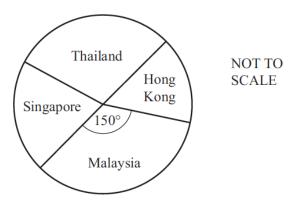
Michelle sells ice cream.

The table shows how many of the different flavours she sells in one hour.

| Flavour | Vanilla | Strawberry | Chocolate | Mango |
|-------------|---------|------------|-----------|-------|
| Number sold | 26 | 8 | 9 | 7 |

Michelle wants to show this information in a pie chart.

Calculate the sector angle for mango.



A travel brochure has 72 holidays in four different countries. The pie chart shows this information.

(a) There are 24 holidays in Thailand.

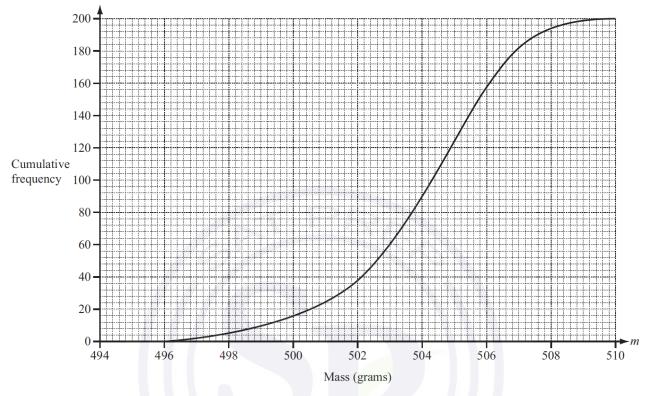
Show that the sector angle for Thailand is 120°.

Answer(a)

(b) The sector angle for Malaysia is 150°. The sector angle for Singapore is twice the sector angle for Hong Kong.

Calculate the number of holidays in Hong Kong.

17 The mass, *m* grams, of cornflakes in each of 200 boxes is recorded. The cumulative frequency diagram shows the results.



(a) Use the diagram to estimate the inter-quartile range.

(b) Find the probability that a box chosen at random has a mass of 500 grams or less.

(c)

| Mass (<i>m</i> grams) | $496 < m \le 500$ | $500 < m \le 504$ | $504 < m \leq 508$ | $508 < m \leq 510$ |
|------------------------|-------------------|-------------------|--------------------|--------------------|
| Frequency | 16 | 74 | 104 | 6 |

The data in this frequency table is to be shown in a histogram.

Complete the frequency density table below.

| Mass (<i>m</i> grams) | $496 < m \le 500$ | $500 < m \le 504$ | $504 < m \leq 508$ | $508 < m \leq 510$ |
|------------------------|-------------------|-------------------|--------------------|--------------------|
| Frequency density | 4 | | | |

[2]

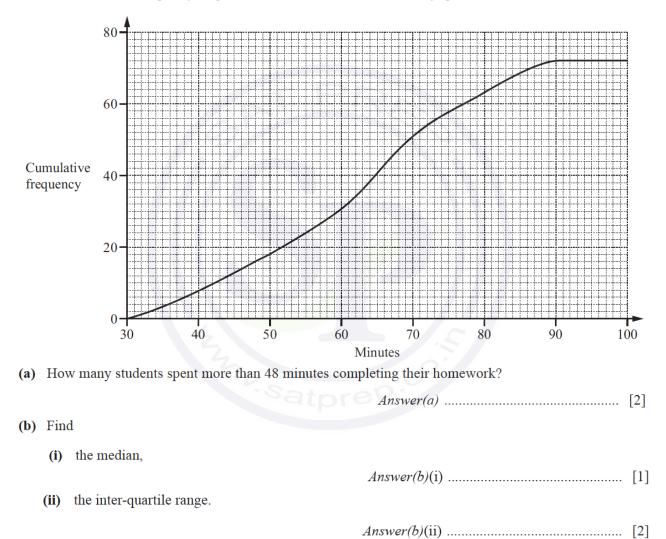
The four sector angles in a pie chart are $2x^{\circ}$, $3x^{\circ}$, $4x^{\circ}$ and 90° .

Find the value of x.

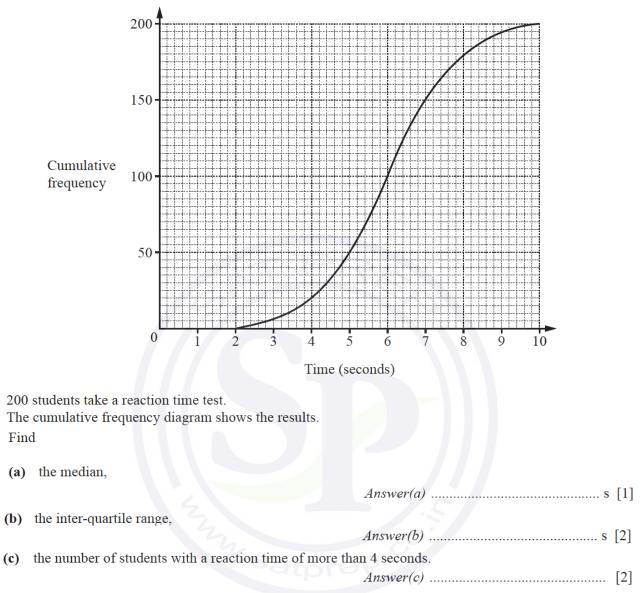
Answer x = [2]

Question 11

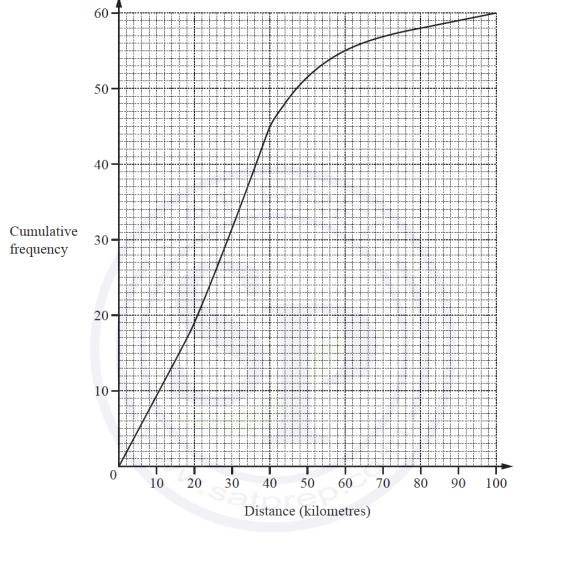
18 72 students are given homework one evening.They are told to spend no more than 100 minutes completing their homework.The cumulative frequency diagram shows the number of minutes they spend.







The cumulative frequency diagram shows information about the distances travelled, in kilometres, by 60 people.



(a) the 80th percentile,

Find

- *Answer(a)* km [2] (b) the inter-quartile range,

 - *Answer(b)* km [2]
- (c) the number of people who travelled more than 60 km.

7 9 20 3 9

(a) A number is removed from this list and the median and range do not change.

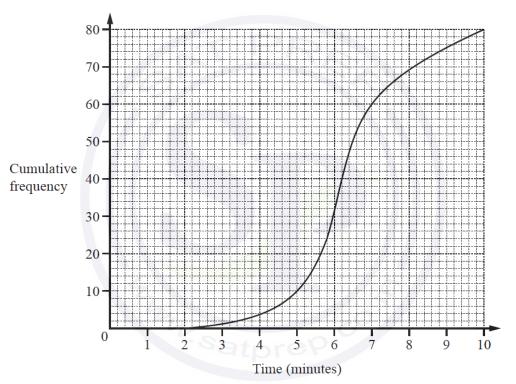
Write down this number.

(b) An extra number is included in the original list and the mode does not change.

Write down a possible value for this number.

Question 15





The cumulative frequency diagram shows information about the times, in minutes, taken by 80 students to complete a short test.

Find

- (a) the median,
- (b) the 30th percentile,

- *Answer(a)* min [1]
- (c) the number of students taking more than 5 minutes.
- Answer(b) min [2]

The table shows information about the numbers of pets owned by 24 students.

| Number of pets | 0 | 1 | 2 | 3 | 4 | 5 | 6 |
|----------------|---|---|---|---|---|---|---|
| Frequency | 1 | 2 | 3 | 5 | 7 | 3 | 3 |

(a) Calculate the mean number of pets.

(b) Jennifer joins the group of 24 students.

When the information for Jennifer is added to the table, the new mean is 3.44.

Calculate the number of pets that Jennifer has.

Question 17

Jim scores the following marks in 8 tests.

7 8 8 v 6 9 10 5

His mean mark is 7.5.

Calculate the value of y.

Question 18

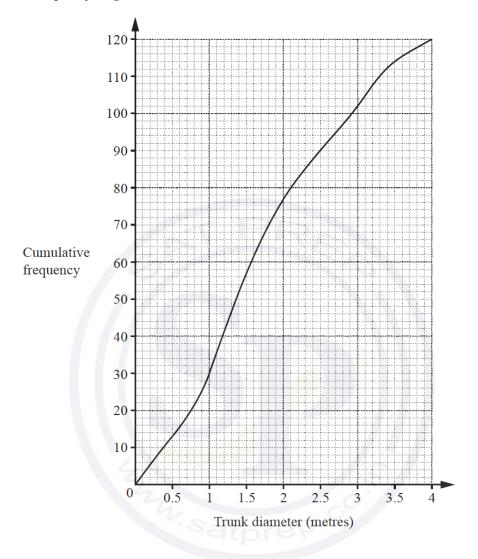
Raj measures the height, h cm, of 70 plants. The table shows the information.

| Height (<i>h</i> cm) | $10 < h \le 20$ | $20 < h \le 40$ | $40 < h \le 50$ | $50 < h \le 60$ | $60 < h \le 90$ |
|-----------------------|-----------------|-----------------|-----------------|-----------------|-----------------|
| Frequency | 7 | 15 | 27 | 13 | 8 |

Answer y

Calculate an estimate of the mean height of the plants.

The cumulative frequency diagram shows information about the trunk diameter, in metres, of 120 trees.



Find

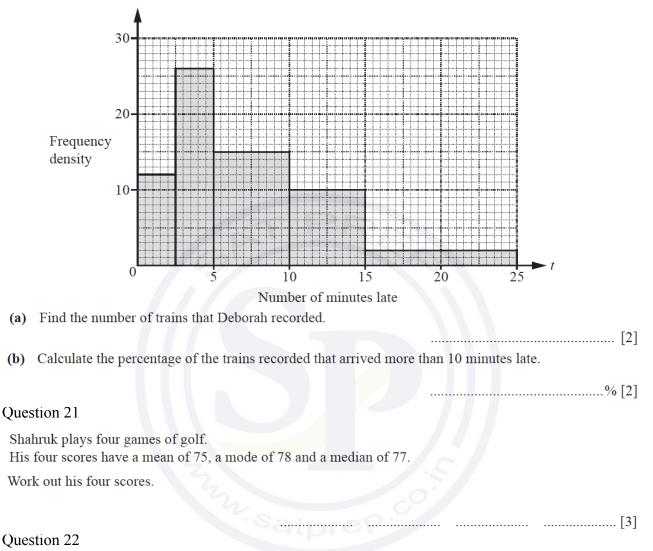
⁽a) the inter-quartile range,

| | m[2] |
|--------------------------|-------|
| (b) the 95th percentile, | m [2] |

(c) the number of trees with a trunk diameter greater than 3 metres.

.....[2]

Deborah records the number of minutes late, t, for trains arriving at a station. The histogram shows this information.



The table shows some information about the mass, m grams, of 200 bananas.

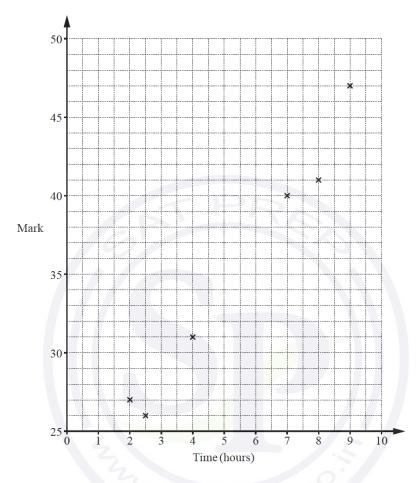
| Mass (<i>m</i> grams) | $90 < m \le 110$ | $110 < m \le 120$ | $120 < m \le 125$ | $125 < m \le 140$ |
|---------------------------------------|------------------|-------------------|-------------------|-------------------|
| Frequency | 40 | 70 | 60 | 30 |
| Height of column in histogram (cm) | | | 6 | |

Complete the table.

[4]

Six students revise for a test.

The scatter diagram shows the time, in hours, each student spent revising and their mark in the test.



(a) The data for two more students is shown in the table.

| Time (hours) | 4.5 | 6.5 |
|--------------|-----|-----|
| Mark | 33 | 35 |

| | Plot these two points on the scatter diagram. | [1] |
|------------|---|-----|
| (b) | What type of correlation is shown on the scatter diagram? | |

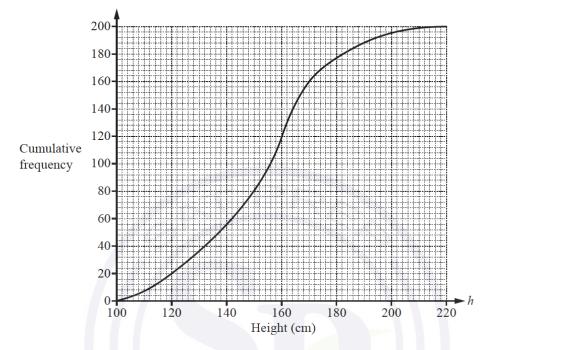
- (c) Draw a line of best fit on the scatter diagram.
- (d) Another student spent 5.5 hours revising.

Estimate a mark for this student.

[1]

.....[1]

Simon records the heights, h cm, of 200 sunflowers in his garden. The cumulative frequency diagram shows this information.



(a) Find the number of these sunflowers that have a height of more than 160 cm.



(b) Sue records the heights, h cm, of 200 sunflowers in her garden. The cumulative frequency table shows this information.

| Cumulative frequency |
|----------------------|
| atoreo |
| 20 |
| 48 |
| 100 |
| 140 |
| 172 |
| 188 |
| 200 |
| |

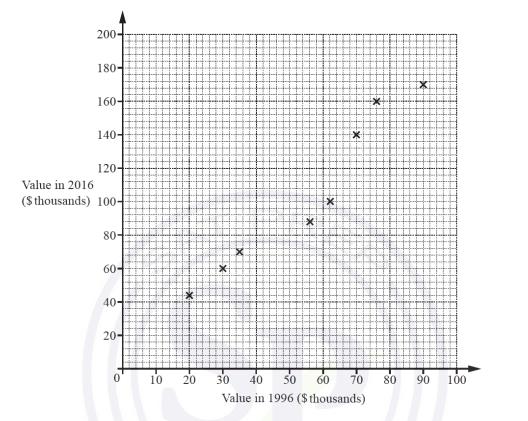
On the grid above, draw another cumulative frequency diagram to show this information. [3]

(c) Work out the difference between the median heights of Simon's sunflowers and Sue's sunflowers.

..... cm [2]

Question 25

The scatter diagram shows the value, in thousands of dollars, of eight houses in 1996 and the value of the same houses in 2016.



(a) One of these eight houses had a value of \$70000 in 1996.

Write down the value of this house in 2016.

\$[1]

(b) The values of two more houses are shown in the table.

| Value in 1996 (\$ thousands) | 40 | 80 |
|------------------------------|----|-----|
| Value in 2016 (\$ thousands) | 80 | 150 |

On the scatter diagram, plot these values.

- (c) On the scatter diagram, draw a line of best fit.
- (d) Another house had a value of \$50000 in 1996.

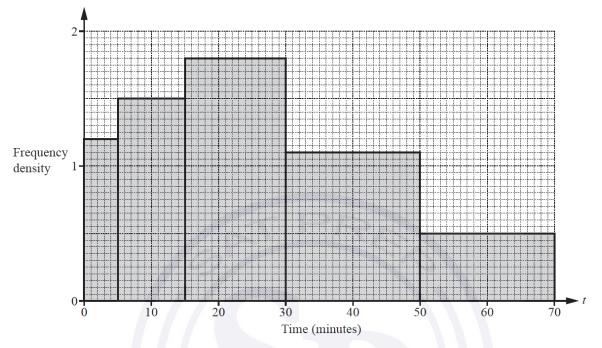
Find an estimate of the value of this house in 2016.

\$[1]

[1]

[1]

The histogram shows information about the time, *t* minutes, spent in a shop by each of 80 people.



Complete the frequency table.

| Time (<i>t</i> minutes) | $0 < t \le 5$ | $5 < t \le 15$ | $15 < t \le 30$ | $30 < t \le 50$ | $50 < t \le 70$ | |
|--------------------------|---------------|----------------|-----------------|-----------------|-----------------|-----|
| Number of people | 6 | | 27 | | 10 | |
| O | | | | | | [2] |

Question 27

40 people were asked how many times they visited the cinema in one month. The table shows the results.

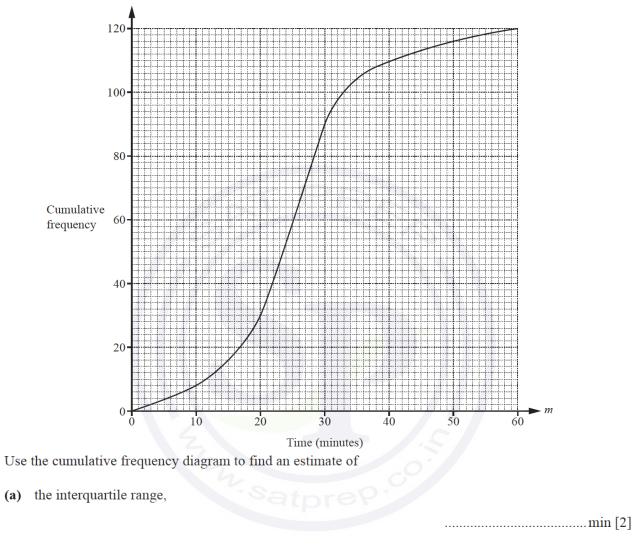
| | | | - | | | | | | |
|---|---|---|---|---|---|---|---|---|-----|
| Number of cinema visits | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | |
| Frequency | 5 | 5 | 6 | 6 | 7 | 3 | 6 | 2 | |
| (a) (i) Find the mode. | | | | | | | | | |
| | | | | | | | | | [1] |
| (ii) Calculate the mean. | | | | | | | | | |
| | | | | | | | | | [3] |
| (b) Other wants to show the information from the table in a nic short | | | | | | | | | |

(b) Omar wants to show the information from the table in a pie chart.

Calculate the sector angle for the people who visited the cinema 5 times.

.....[2]

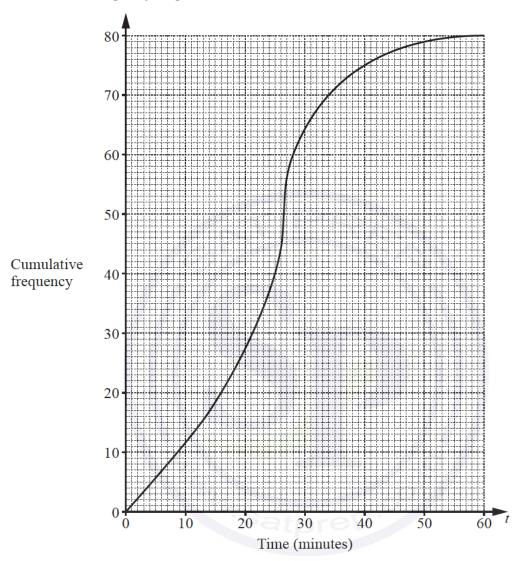
The cumulative frequency diagram shows information about the time, m minutes, taken by 120 students to complete some homework.



(b) the number of students who took more than 50 minutes to complete the homework.

.....[2]

The time, *t* minutes, 80 students each spend completing their homework is recorded. The cumulative frequency diagram shows the results.



Use the cumulative frequency diagram to find an estimate of

(a) the median,

..... min [1]

(b) the interquartile range,

..... min [2]

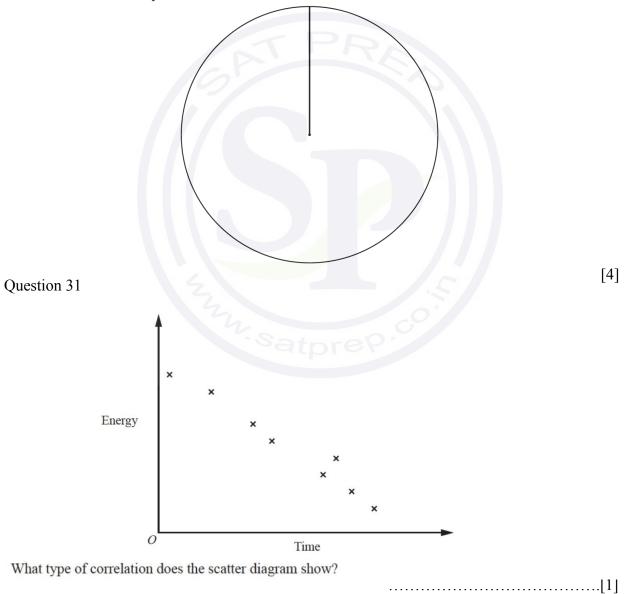
(c) the number of students who spend more than 40 minutes completing their homework.

......[2]

120 students choose what they want to do when they leave school. Their choices are shown in the table.

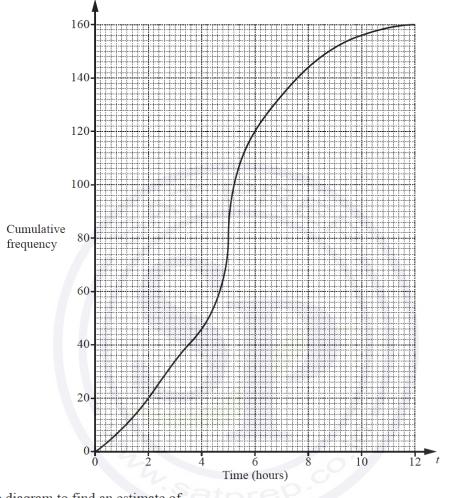
| Choice | Number of students |
|------------|--------------------|
| University | 57 |
| Training | 45 |
| Work | 18 |

Complete the pie chart to show this information. Label each sector clearly.



22

160 students record the amount of time, *t* hours, they each spend playing computer games in a week. This information is shown in the cumulative frequency diagram.



(a) Use the diagram to find an estimate of

(i) the median,

..... hours [1]

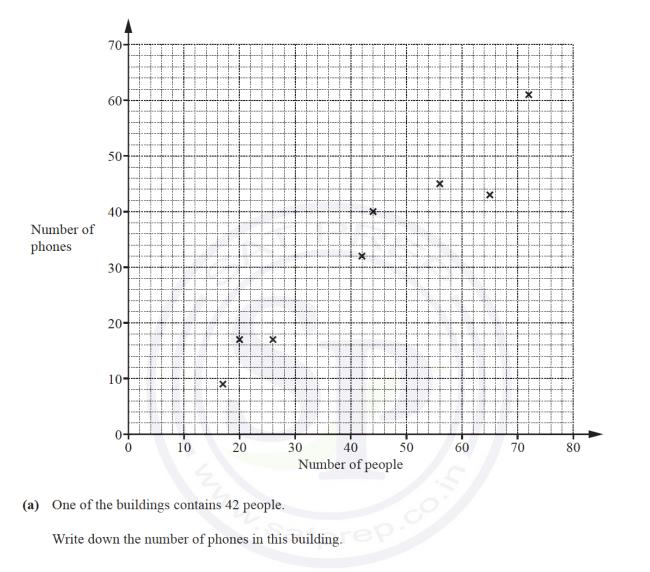
..... hours [2]

- (ii) the interquartile range.
- (b) Use the diagram to complete this frequency table.

| Time (t hours) | $0 < t \le 2$ | $2 < t \le 4$ | $4 < t \le 6$ | $6 < t \le 8$ | $8 < t \le 10$ | $10 < t \le 12$ |
|----------------|---------------|---------------|---------------|---------------|----------------|-----------------|
| Frequency | 20 | | | 24 | 12 | 4 |

[2]

The scatter diagram shows the number of people and the number of phones in each of 8 buildings.



(b) What type of correlation is shown in the scatter diagram?

| Method of travel | Frequency |
|------------------|-----------|
| Car | 10 |
| Walk | 5 |
| Bike | 3 |
| Bus | 2 |

The table shows the different methods of travel for 20 people going to work.

Which type of average, mean, median or mode, can be used for this information?

Question 35

The table shows the number of people in different age groups at a cinema.

| Age (y years) | $15 < y \le 25$ | $25 < y \leq 30$ | $30 < y \le 50$ | $50 < y \le 80$ |
|------------------|-----------------|------------------|-----------------|-----------------|
| Number of people | 35 | 32 | 44 | 12 |

Dexter draws a histogram to show this information.

The height of the bar he draws for the group $15 < y \le 25$ is 7 cm.

Calculate the height of each of the remaining bars.

| $25 < y \le 30$ | cm | |
|------------------|----|-----|
| $30 < y \leq 50$ | cm | |
| $50 < y \le 80$ | cm | [3] |

Question 36

The time, *t* minutes, it takes each of 50 students to travel to school is recorded. The table shows the results.

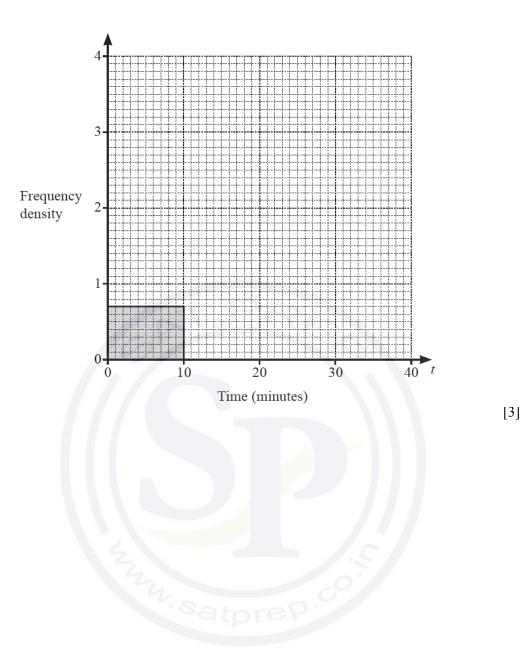
| Time (<i>t</i> minutes) | $0 < t \le 10$ | $10 < t \le 15$ | $15 < t \le 20$ | $20 < t \le 40$ |
|--------------------------|----------------|-----------------|-----------------|-----------------|
| Frequency | 7 | 19 | 16 | 8 |

(a) Write down the modal class.

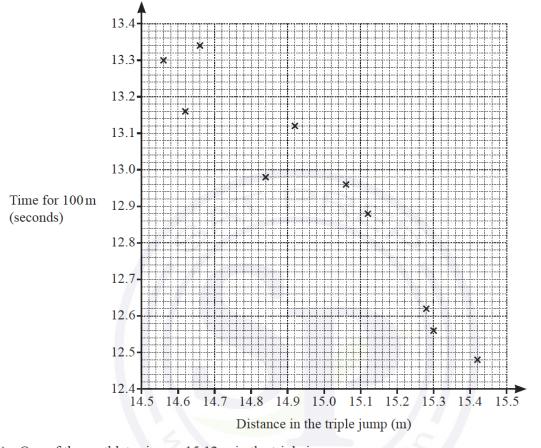
 $\dots < t \leq \dots \min [1]$

(b) On the grid, complete the histogram to show the information in the table.

Continue on the next page...



Ten athletes compete in both the 100 metre race and the triple jump. Their results are shown in the scatter diagram.



(a) One of these athletes jumps 15.12 m in the triple jump.

Write down his time for the 100 metre race.

(b) The values for two other athletes are shown in the table.

| Distance in the triple jump (m) | 14.74 | 15.2 |
|------------------------------------|-------|-------|
| Time for 100 m (seconds) | 13.2 | 12.76 |

On the scatter diagram, plot these points. [1]

(c) On the scatter diagram, draw a line of best fit.

27

[1] [1]

.....s [1]

The table shows how children in Ivan's class travel to school.

| Travel to school | Number of children |
|------------------|--------------------|
| Walk | 12 |
| Car | 7 |
| Bicycle | 9 |
| Bus | 4 |

Ivan wants to draw a pie chart to show this information.

Find the sector angle for children who walk to school.

Question 39

The mass, correct to the nearest kilogram, of each of 11 parcels is shown below.

24 23 23 26 25 27 18 96 16 17 32

(a) Find the mode.

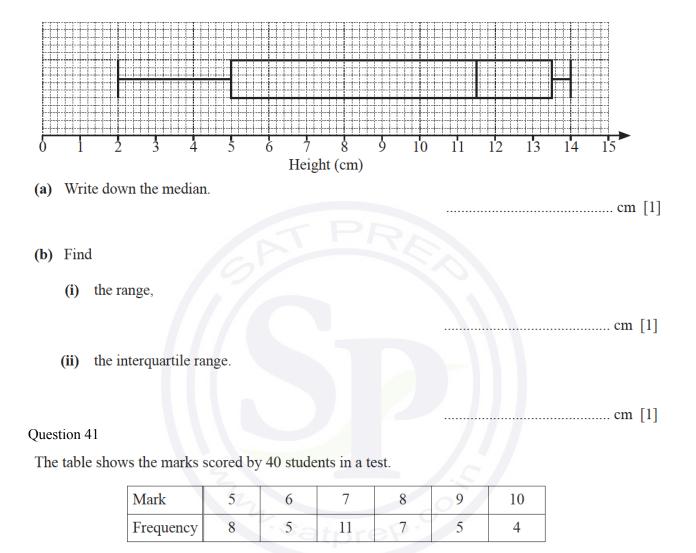
.....

(b) Give a reason why the mean would be an unsuitable average to use.

..... kg [1]

[1]

The box-and-whisker plot gives information about the heights, in centimetres, of some plants.



Calculate the mean mark.

.....[3]

The number of people swimming in a pool is recorded each day for 12 days.

| 24 | 28 | 13 | 38 | 15 | 26 |
|----|----|----|----|----|----|
| 45 | 21 | 48 | 36 | 18 | 38 |

(a) Complete the stem-and-leaf diagram.



(b) Find the median number of swimmers.

......[1]

Question 43

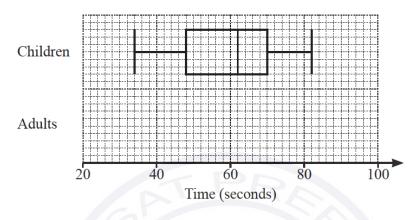
The table shows the amount of money, x, given to a charity by each of 60 people.

| Amount $(\$x)$ | $0 < x \le 20$ | $20 < x \le 25$ | $25 < x \le 35$ | $35 < x \le 50$ | $50 < x \le 100$ |
|----------------|----------------|-----------------|-----------------|-----------------|------------------|
| Frequency | 21 | 16 | 6 | 10 | 7 |

Calculate an estimate of the mean.

Gemma records the times, in seconds, taken for a group of children and a group of adults to complete a puzzle.

The box-and-whisker plot shows information about the times taken for the children to complete the puzzle.



(a) Find the interquartile range of the times taken for the children to complete the puzzle.

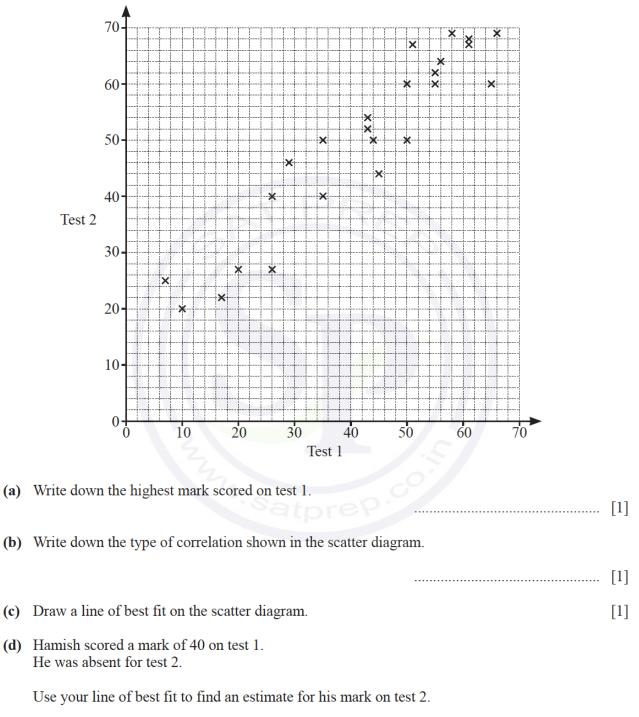
(b) The table shows some information about the times, in seconds, taken for the adults to complete the puzzle.

| Minimum | Lower quartile | Median | Upper quartile | Maximum |
|---------|----------------|--------|----------------|---------|
| 28 | 42 | 58 | 70 | 75 |

On the grid above, draw the box-and-whisker plot for the adults.

[2]

Mrs Salaman gives her class two mathematics tests. The scatter diagram shows information about the marks each student scored.



.....[1]

The table shows information about the times, *t* seconds, taken by each of 100 students to solve a puzzle.

| Time (t seconds) | $0 < t \le 10$ | $10 < t \le 15$ | $15 < t \le 20$ | $20 < t \le 40$ | $40 < t \le 75$ |
|------------------|----------------|-----------------|-----------------|-----------------|-----------------|
| Frequency | 9 | 18 | 22 | 30 | 21 |

(a) Calculate an estimate of the mean time.

.....s [4]

(b) Emmanuel draws a histogram to show this information. The table shows the heights, in cm, of some of the bars for this histogram.

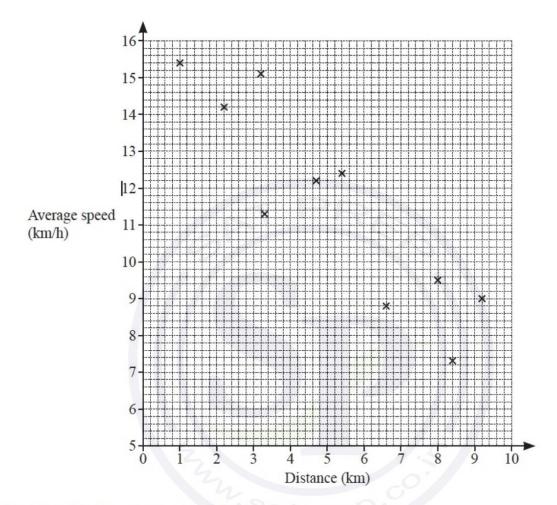
Complete the table.

| Time (<i>t</i> seconds) | $0 < t \le 10$ | $10 < t \le 15$ | $15 < t \le 20$ | $20 < t \le 40$ | $40 < t \le 75$ |
|--------------------------|----------------|-----------------|-----------------|-----------------|-----------------|
| Height of bar (cm) | 3.6 | 14.4 | 17.6 | | |

[3]



Aisha records the distance she runs and her average speed. The results are shown in the scatter diagram.



(a) The table shows the results of four more runs.

| Distance (km) | 4.2 | 5.7 | 7.1 | 8.8 |
|----------------------|------|------|-----|-----|
| Average speed (km/h) | 13.4 | 11.8 | 9.8 | 8.3 |

On the scatter diagram, plot these points.

- (b) What type of correlation is shown in the scatter diagram?
- .. [1] On the scatter diagram, draw a line of best fit. (C) [1]
- (d) Use your line of best fit to estimate her average speed when she runs a distance of 6 km.
 - km/h [1]

.

34

[2]

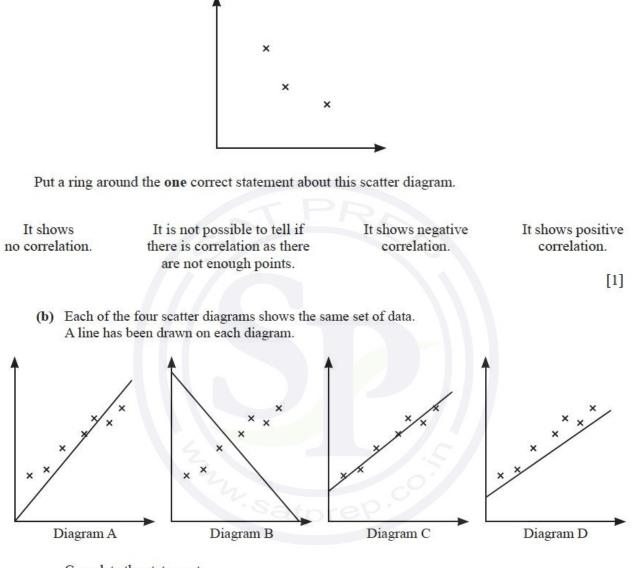
Some students were asked how many books they each had in their school bags. The table shows some of this information.

| Number of books | 5 | 6 | 7 | 8 | 9 | 10 | |
|---------------------------|-------------------------|--------------------------|-------------------------------|--------------|------------------------|----------|---|
| Frequency | 4 | 5 | x | 11 | 7 | 5 | - |
| The mean number of | books is 7.6 | õ. | | | 1 | | _ |
| Calculate the value of | f <i>x</i> . | | | | | | |
| | | | | x = | | | |
| Question 49 | | | | | | | |
| The number of bowls | s of hot soup | p sold decr | eases when | the temperat | ture rises. | | |
| What type of correlat | tion does the | is statemer | t describe? | | | | |
| 51 | | | | | | | |
| | | | | | | | |
| Question 50 | | | | | | | |
| Question 50 | of passange | are on a hus | is recorded | each day for | • 14 days | | |
| Question 50 The number | | | | | | | |
| - | of passenge 15 19 | ers on a bus 18 19 | is recorded 22 17 24 25 | 35 | : 14 days. 38 36 | 24 29 | |
| The number | 15 19 | 18 19 | 22 17 24 25 | 35 | 38 | | |
| The number | 15 | 18 19 | 22 17 24 25 | 35 | 38 | | |
| The number (a) Comple | 15 19 | 18 19 | 22 17 24 25 | 35 | 38 | | |
| The number | 15 19 | 18 19 | 22 17 24 25 | 35 | 38 | | |
| The number (a) Comple | 15 19 | 18 19 | 22 17 24 25 | 35 | 38 | | |

[2]

(b) Find the median.

(a) Henrik draws this scatter diagram.



Complete the statement.

The line in Diagram is the most appropriate line of best fit. [1]

Emma has 15 mathematics questions to complete.

The stem-and-leaf diagram shows the time, in minutes, it takes her to complete each question.

| 0 | 3 | 5 | 6 | 7 | 7 | 8 | 8 |
|---|---|---|---|---|---|---|---|
| 1 | 1 | 2 | 2 | 3 | 6 | 6 | 6 |
| 2 | 0 | | | | | | |

Key: $2 \mid 0 = 20$ minutes

Complete the table.

| Mode | min |
|--------|-----|
| Median | min |
| Range | min |

[3]

Question 53

The stem-and-leaf diagram shows the number of hours that each of 16 students studied last week.

| | - | _ | _ | | _ |
|---|---|---|---|----|----|
| 1 | 2 | 5 | 6 | 8 | |
| 2 | 0 | 1 | 1 | 7 | 9 |
| 3 | 2 | 3 | 4 | 5 | |
| 4 | 4 | 5 | 7 | re | 99 |
| | | | | | |

Find

(a) the median,

.....h [1]

(b) the mode,

(c) the range.

-h [1]
-h [1]

The stem-and-leaf diagram shows the age, in years, of each of 15 women.

| 3 | 1 | 5 | 8 | 9 | | | |
|---|---|---|---|---|---|---|---|
| 4 | 1 | 1 | 2 | 3 | 5 | 6 | 9 |
| 5 | 0 | 2 | 3 | 8 | | | |

Key: 3 | 1 represents 31 years

Complete these statements.

The modal age is

The median age is

The percentage of women that are older than 51 years is%.

Question 55

The table shows the relative frequency of the games won by a football team.

| Result of game | won | lost | drawn |
|--------------------|-----|------|-------|
| Relative frequency | 0.1 | | |

The number of games lost is twice the number of games drawn.

Complete the table.

Question 56

The number of items that each of 22 people buy in a supermarket is shown in the stem-and-leaf diagram.

| 1 | 1 | 3 | 6 | 6 | | | | |
|---|---|---|---|---|---|---|---|--|
| 2 | 0 | 2 | 2 | 2 | 4 | 8 | 9 | |
| 3 | 1 | 1 | 5 | 8 | 9 | 9 | | |
| 4 | 2 | 4 | 6 | 7 | 8 | | | |

Key: 1 | 1 represents 11 items

Continue on the next page..

[3]

[3]

(a) Find the mode.

(b) Find the median.

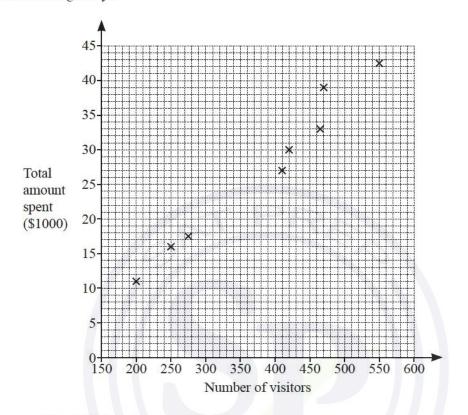
Question 57

As the temperature increases, people eat more ice cream.

What type of correlation does this statement describe?



The scatter diagram shows the number of visitors and the total amount spent, in thousands of dollars, at a zoo on each of eight days.



(a) On one of the eight days there are 410 visitors.

Find the total amount spent by visitors during this day.

(b) Information for the ninth day is shown in the table.

| Number of visitors | 175 |
|-----------------------------|-----|
| Total amount spent (\$1000) | 9 |

Plot this information on the scatter diagram.

- (c) Draw a line of best fit on the scatter diagram. [1]
- (d) On the tenth day the total amount spent is \$22000.

Estimate the number of visitors on this day.

[1]

These are the masses, in kg, of 12 parcels.

0.3 0.4 1.2 0.8 1.1 2.1 1.7 1.8 1.2 2.3 0.7 1.1

(a) Complete the stem-and-leaf diagram for the 12 parcels.

Key: 0 | 3 represents 0.3 kg

(b) Find the median.

..... kg [1]

[2]

.....[2]

Question 60

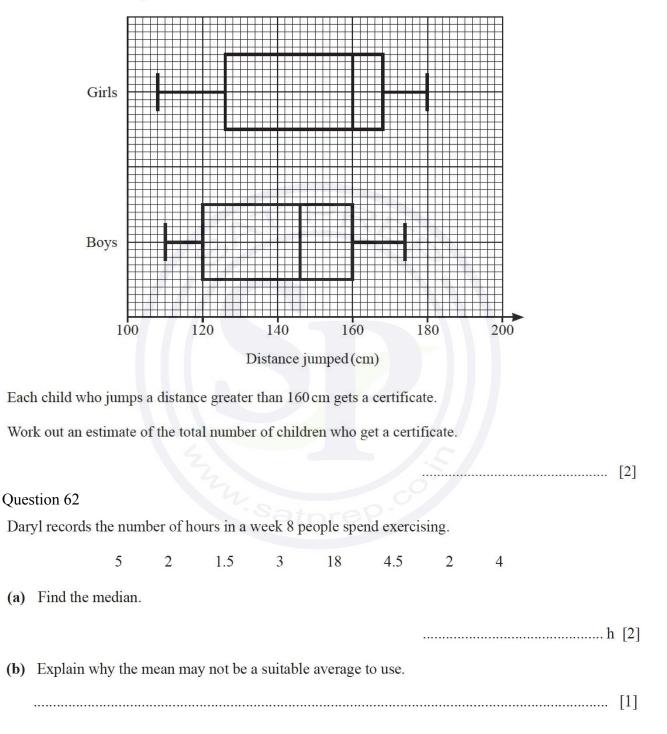
Thibault records the number of cars of each colour in a car park.

| Colour | Black | White | Silver | Red |
|----------------|-------|-------|--------|-----|
| Number of cars | 8 | 5 | 4 | 3 |

He draws a pie chart to show this information.

Calculate the sector angle for the red cars.

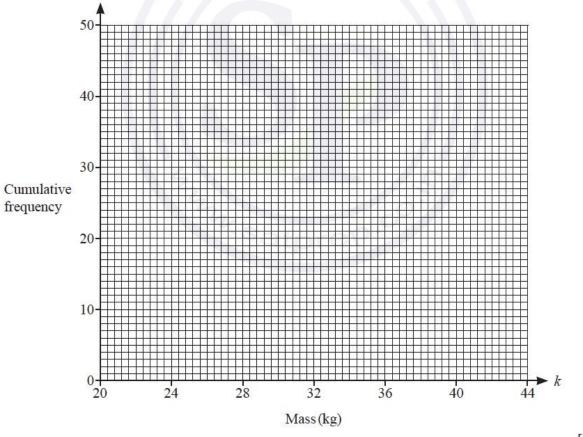
136 girls and 144 boys each measure the distance they jump in centimetres. The box-and-whisker plots show the distributions of these distances.



| The table shows information about the mass of each of 50 children. |
|--|
|--|

| Cumulative Frequency |
|-------------------------|
| 0 |
| 7 |
| 23 |
| 35 |
| 43 |
| 47 |
| 50 |
| |

(a) Draw a cumulative frequency diagram to show this information.



[3]

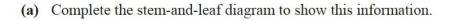
(b) Use your graph to find an estimate of the 90th percentile.



(b)

On ten days, Stefan records the number of minutes he has to wait for a train.

1 3 12 5 4 23 5 24 11 8



| 0 | 1 3 | | | |
|--------|------------|------------------|--------------|---------|
| 1 | | | | |
| 2 | | | | |
| Find t | he median. | Key: 0 1 represe | nts 1 minute | [2] |
| | | | | min [1] |