Extended Mathematics

Topic: Statistics

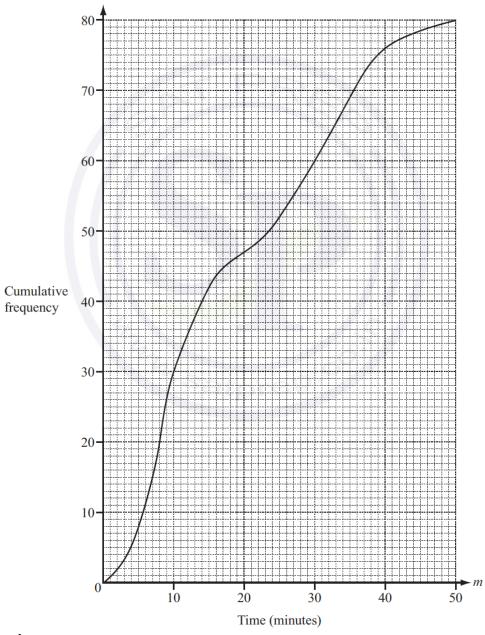
Year :May 2013 -May 2023

Paper -4

Questions Booklet

Question 1

Sam asked 80 people how many minutes their journey to work took on one day. The cumulative frequency diagram shows the times taken (m minutes).



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(i) the median,

Answer(a)(i)	min [1]	1
12/12//01/01/01/01/01/01/01/01/01/01		н

(ii) the lower quartile,

(iii) the inter-quartile range.

(b) One of the 80 people is chosen at random.

Find the probability that their journey to work took more than 35 minutes. Give your answer as a fraction.

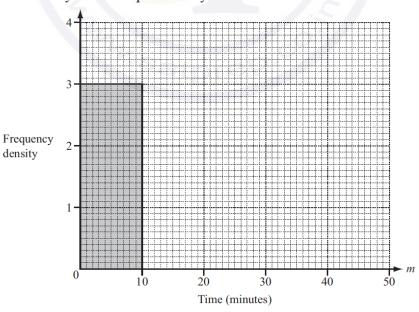
(c) Use the cumulative frequency diagram to complete this frequency table.

Time (<i>m</i> minutes)	0 < m Y 10	10 < m Y 15	15 < m Y 30	30 < m Y 40	40 < m Y 50
Frequency	30	12	18		

[2]

(d) Using mid-interval values, calculate an estimate of the mean journey time for the 80 people.

(e) Use the table in **part** (c) to complete the histogram to show the times taken by the 80 people. One column has already been completed for you.



[5]

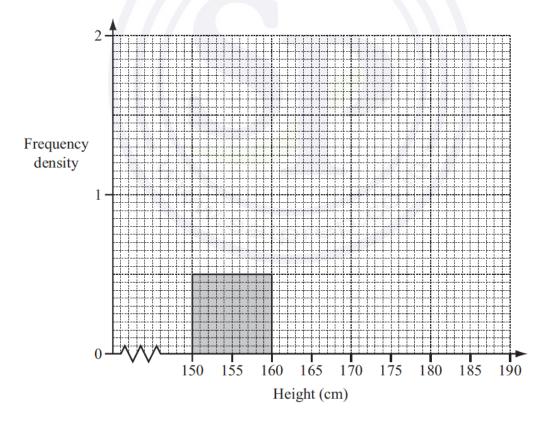
Height (h cm)	150 < h ≤ 160	160 < h ≤ 165	$165 < h \le 180$	180 < h ≤ 190
Frequency	5	9	18	10

The table shows information about the heights of a group of 42 students.

(a) Using mid-interval values, calculate an estimate of the mean height of the students. Show your working.

(b) Write down the interval which contains the lower quartile.

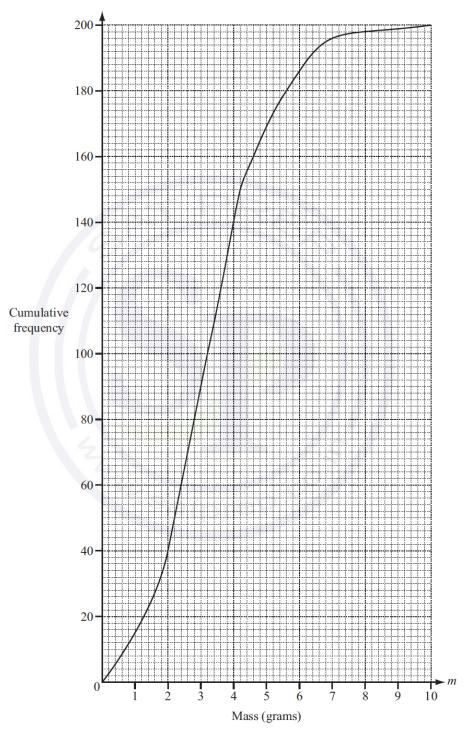
(c) Complete the histogram to show the information in the table. One column has already been drawn for you.



[4]

Question 3

200 students estimate the mass (m grams) of a coin. The cumulative frequency diagram shows the results.



artile,		Answer(a)	(i)		g [1]
		Answer(a)(ii)		g [1]
centile,					
		Answer(a)(i	ii)		g [1]
of students wh	iose estimate i	s 7 g or less.			
		Answer(a)(i	iv)		[1]
ulative freque	ncy diagram t	o complete the	frequency tal	ole.	
$0 < m \le 2$	$2 < m \le 4$	4 < m ≤ 6	6 < m ≤ 8	8 < <i>m</i> ≤ 10	
40	4.8-4	00:0	,0	2	
	dent estimates				
	centile, of students when ulative freque $0 < m \le 2$ 40 chosen at rand ity that the stu	centile, of students whose estimate in a student of students whose estimate in a student estimate in a student estimates are of M .	centile, $Answer(a)(a)$ controlled $Answer(a)(a)$ consists whose estimate is $7 g$ or less. $Answer(a)(a)$ controlled	centile, $Answer(a) \text{(iii)} \dots \dots$	centile, $Answer(a) \text{(iii)} \qquad \qquad$

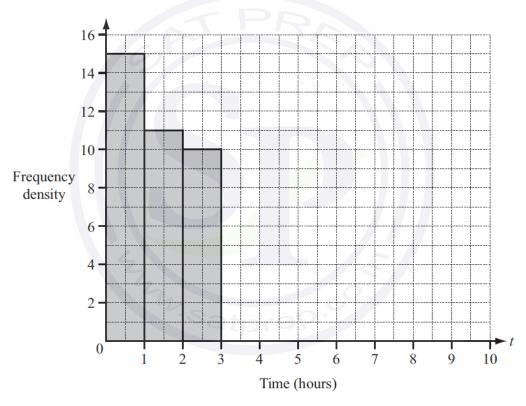
80 students were asked how much time they spent on the internet in one day. This table shows the results.

Time (t hours)	0 < t Y 1	1 < t Y 2	2 < t Y 3	3 < t Y 5	5 < t Y 7	7 < t Y 10
Number of students	15	11	10	19	13	12

(i) Calculate an estimate of the mean time spent on the internet by the 80 students.

Answer (i) hours [4]

(ii) On the grid, complete the histogram to show this information.



[4]

120 students are asked to answer a question.

The time, t seconds, taken by each student to answer the question is measured.

The frequency table shows the results.

Time	0 < t Y 10	10 < t Y 20	20 < t Y 30	30 < t Y 40	40 < t Y 50	50 < t Y 60
Frequency	6	44	40	14	10	6

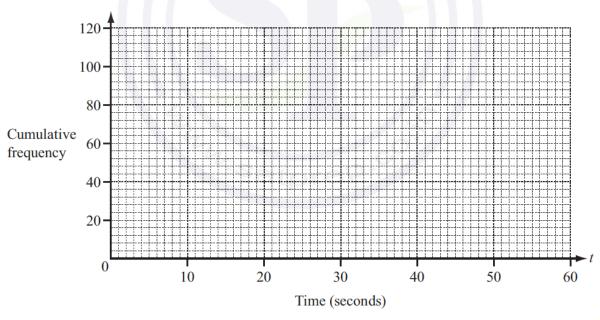
(a) Calculate an estimate of the mean time.

(b) (i) Complete the cumulative frequency table.

Time	t Y 10	t Y 20	t Y 30	t Y 40	t Y 50	t Y 60
Cumulative frequency	6			104		120

[2]

(ii) On the grid below, draw a cumulative frequency diagram to show this information.



[3]

(iii) Use your cumulative frequency diagram to find the median, the lower quartile and the 60th percentile.

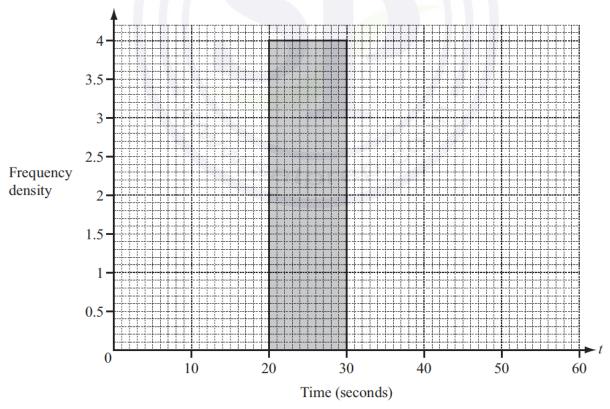
Answer(b)(iii)	Median	 S	
	Lower quartile	 S	
	60th percentile	 s [4]	

- (c) The intervals for the times taken are changed.
 - (i) Use the information in the frequency table on the opposite page to complete this new table.

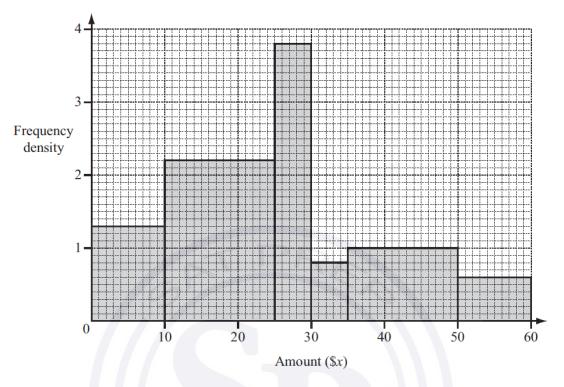
Time	0 < t Y 20	20 < t Y 30	30 < t Y 60
Frequency		40	

[2]

(ii) On the grid below, complete the histogram to show the information in the new table. One column has already been drawn for you.



[3]



A survey asked 90 people how much money they gave to charity in one month. The histogram shows the results of the survey.

(a) Complete the frequency table for the six columns in the histogram.

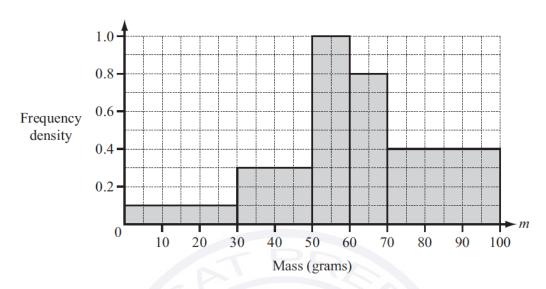
Amount (\$x)	$0 < x \le 10$	Ź	1.5	
Frequency		34	4	

[5]

(b) Use your frequency table to calculate an estimate of the mean amount these 90 people gave to charity.

Answer(b) \$[4]

(a)



The histogram shows some information about the masses (m grams) of 39 apples.

(i) Show that there are 12 apples in the interval $70 < m \le 100$.

Answer(a)(i)

[1]

(ii) Calculate an estimate of the mean mass of the 39 apples.

Continue on the next page..

Answer(a)(ii) g [5]

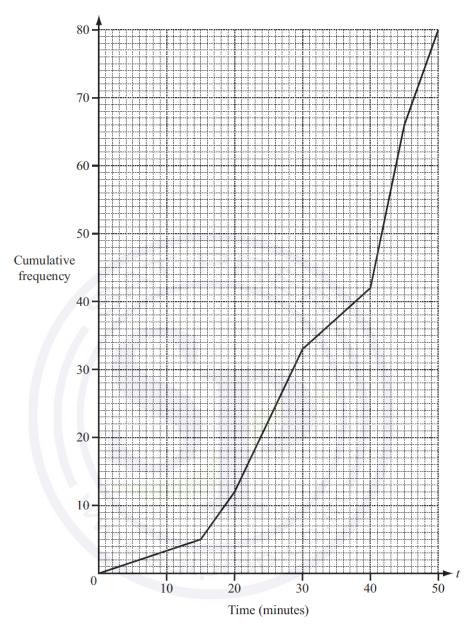
(b) The mean mass of 20 oranges is 70 g.

One orange is eaten.

The mean mass of the remaining oranges is 70.5 g.

Find the mass of the orange that was eaten.

Answer(b) g [3]



The times (t minutes) taken by 80 people to complete a charity swim were recorded
The results are shown in the cumulative frequency diagram above.

/ \	TO .	1
(a)) Fin	d

(i) the median,

Answer(a)(i) min [1]

(ii) the inter-quartile range,

Answer(a)(ii) min [2]

(iii) the 70th percentile.

Answer(a)(iii) min [2]

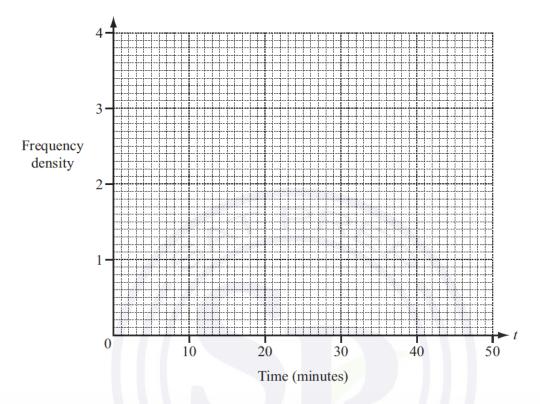
(b) The times taken by the 80 people are shown in this grouped frequency table.

Time (t minutes)	$0 < t \le 20$	$20 < t \le 30$	$30 < t \le 45$	$45 < t \le 50$
Frequency	12	21	33	14

(i) Calculate an estimate of the mean time.

Answer(b)(i) min [4]

(ii) Draw a histogram to represent the grouped frequency table.



[4]

(a) Ricardo asks some motorists how many litres of fuel they use in one day. The numbers of litres, correct to the nearest litre, are shown in the table.

Number of litres	16	17	18	19	20
Number of motorists	11	10	p	4	8

(i) For this table, the mean number of litres is 17.7.

Calculate the value of p.

$$Answer(a)(i) p = \dots [4]$$

(ii) Find the median number of litres.

Answer(a)(ii) litres [1]

Question 10

The time, t seconds, taken for each of 50 chefs to cook an omelette is recorded.

Time (t seconds)	20 < t ≤ 25	$25 < t \le 30$	$30 < t \le 35$	$35 < t \le 40$	40 < t ≤ 45	$45 < t \le 50$
Frequency	2	6	7	19	9	7

(a) Write down the modal time interval.

(b) Calculate an estimate of the mean time. Show all your working.

(c) A new frequency table is made from the results shown in the table opposite.

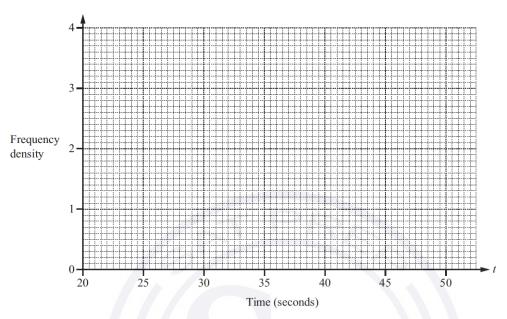
Time (t seconds)	20 < t ≤ 35	$35 < t \le 40$	40 < t ≤ 50
Frequency			

(i) Complete the table.

[1]

[3]

(ii) On the grid, draw a histogram to show the information in this new table.



Question 11

The table shows the height, $h \, \text{cm}$, of 40 children in a class.

Height (h cm)	$120 < h \le 130$	$130 < h \le 140$	$140 < h \le 144$	$144 < h \le 150$	$150 < h \le 170$
Frequency	3	14	4	6	13

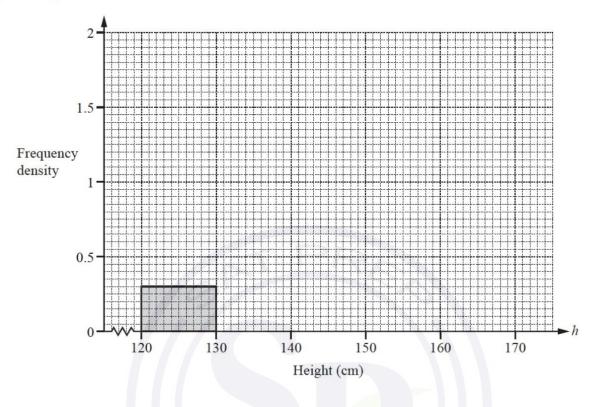
(a) Write down the class interval containing the median.

$$Answer(a) \dots < h \leq \dots$$
 [1]

(b) Calculate an estimate of the mean height.

Answer(b) cm [4]

(c) Complete the histogram.



Question 12

The table shows the times, t minutes, taken by 200 students to complete an IGCSE paper.

Time (t minutes)	40 < <i>t</i> ≤ 60	$60 < t \le 70$	$70 < t \le 75$	$75 < t \le 90$
Frequency	10	50	80	60

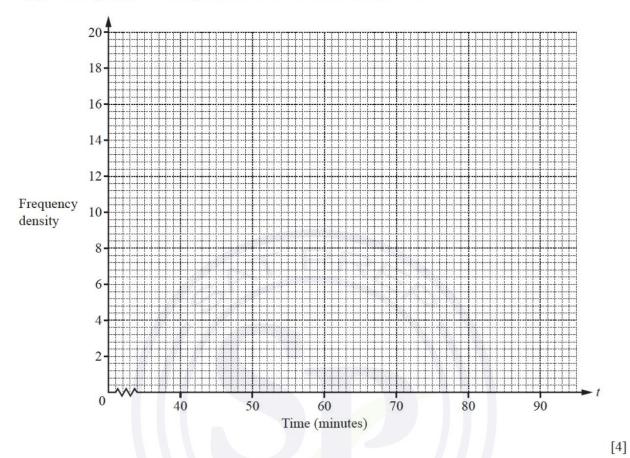
(a) By using mid-interval values, calculate an estimate of the mean time.

Answer(a) min [3]

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[4]

(b) On the grid, draw a histogram to show the information in the table.



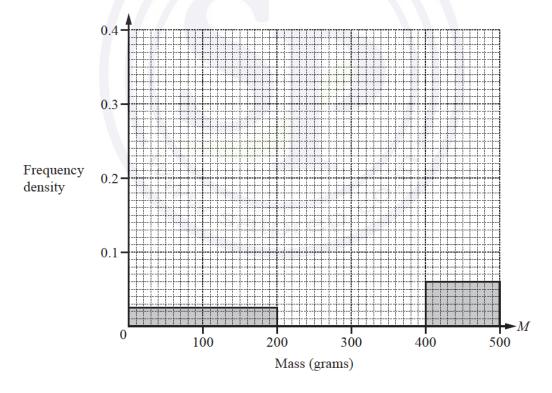
(a) A group of 50 students estimated the mass, M grams, of sweets in a jar. The results are shown in the table.

Mass (M grams)	Number of students
$0 < M \le 200$	5
$200 < M \le 300$	9
$300 < M \le 350$	18
$350 < M \le 400$	12
$400 < M \le 500$	6

(i) Calculate an estimate of the mean.

Answer(a)(i) grams [4]

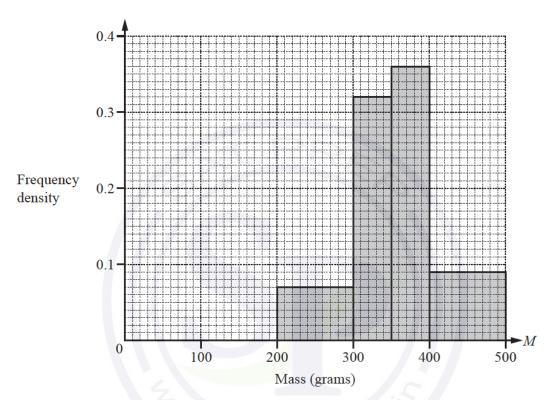
(ii) Complete this histogram to show the information in the table.



[3]

(b) A group of 50 adults also estimated the mass, M grams, of the sweets in the jar. The histogram below shows information about their estimates.

Use the histograms to make two comparisons between the distributions of the estimates of the students and the adults.



The table shows the time, t minutes, that 400 people take to complete a test.

Time taken (t mins)	0 < <i>t</i> ≤ 10	$10 < t \le 24$	24 < <i>t</i> ≤ 30	$30 < t \le 40$	$40 < t \le 60$	$60 < t \le 70$
Frequency	10	90	135	85	70	10

(a) (i) Write down the modal time interval.

Answer(a)(i) min [1]

(ii) Calculate an estimate of the mean time taken to complete the test.

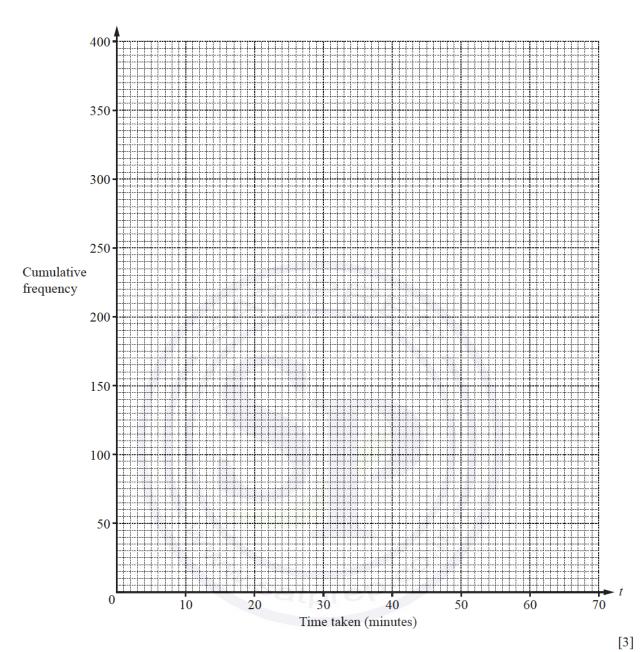
Answer(a)(ii) min [4]

(b) (i) Complete the table of cumulative frequencies.

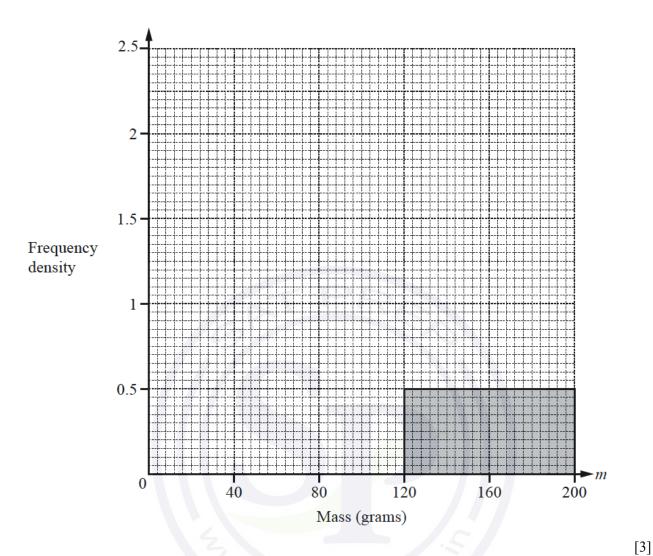
Time taken (t mins)	<i>t</i> ≤ 10	<i>t</i> ≤ 24	<i>t</i> ≤ 30	<i>t</i> ≤ 40	<i>t</i> ≤ 60	<i>t</i> ≤ 70
Cumulative frequency	10	100				400

[2]

(ii) On the grid opposite, draw a cumulative frequency diagram to show this information.



(c)	Use	your graph to es	timate				
	(i)	the median time	,	Ar	nswer(c)(i)		min [1]
	(ii)	the inter-quartile	e range,				
	(iii)	the 15th percent	tile,	An	swer(c)(ii)		min [2]
				Ans	wer(c)(iii)		min [2]
	(iv)	the number of p	eople who took m	nore than 50 minut			[2]
Quest	tion 1	15			(iv)		[2]
The	table	shows informati	on about the mass	ses, m grams, of 10	60 apples.		
		Mass (m grams)	30 < m ≤ 80	80 < m ≤ 100	100 < m ≤ 120	120 < m ≤ 200	
		Mass (m grams) Frequency	$30 < m \le 80$ 50	$80 < m \le 100$ 30	$100 < m \le 120$ 40	$120 < m \le 200$ 40	
(a)	N		50	30	40		



(c) An apple is chosen at random from the 160 apples.

Find the probability that its mass is more than 120 g.

Answer(c) [1]

(d) Two apples are chosen at random from the 160 apples, without replacement.

Find the probability that

(i) they both have a mass of more than 120 g,

Answer(d)(i) [2]

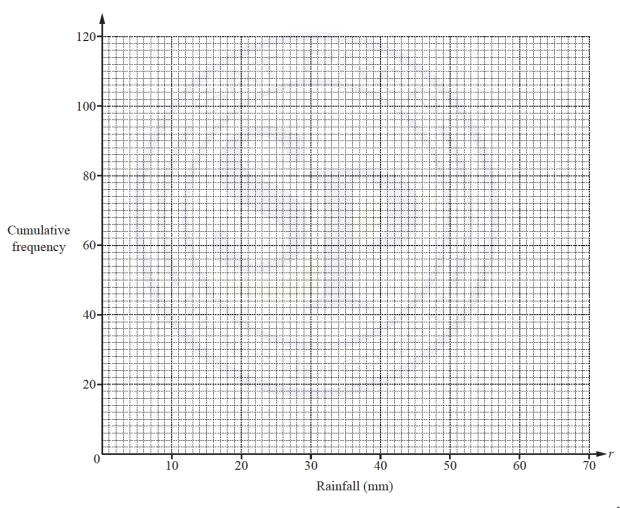
(ii) one has a mass of more than 120 g and one has a mass of 80 g or less.

Leo measured the rainfall each day, in millimetres, for 120 days.

The cumulative frequency table shows the results.

Rainfall (r mm)	r ≤ 20	r ≤ 25	r ≤ 35	r ≤ 40	r ≤ 60	<i>r</i> ≤ 70
Cumulative frequency	5	13	72	90	117	120

(a) On the grid below, draw a cumulative frequency diagram to show these results.



	a . \		· · ·	T: 1	41	11
۱	(b)) ((i)) Fina	une	median.

(ii) Use your diagram to find the number of days when the rainfall was more than 50 mm.

(c) Use the information in the cumulative frequency table to complete the frequency table below.

Rainfall (r mm)	0 < r ≤ 20	$20 < r \le 25$	$25 < r \le 35$	$35 < r \le 40$	40 < r ≤ 60	$60 < r \le 70$
Frequency	5		59			3

[2]

(d) Use your frequency table to calculate an estimate of the mean. You must show all your working.

(e) In a histogram drawn to show the information in the table in **part** (c), the frequency density for the interval $25 < r \le 35$ is 5.9.

Calculate the frequency density for the intervals $20 < r \le 25$, $40 < r \le 60$ and $60 < r \le 70$.

- 6 120 students take a mathematics examination.
 - (a) The time taken, m minutes, for each student to answer question 1 is shown in this table.

Time (<i>m</i> minutes)	0 < m ≤ 1	1 < m ≤ 2	2 < m ≤ 3	3 < <i>m</i> ≤ 4	4 < m ≤ 5	5 < <i>m</i> ≤ 6
Frequency	72	21	9	11	5	2

Calculate an estimate of the mean time taken.

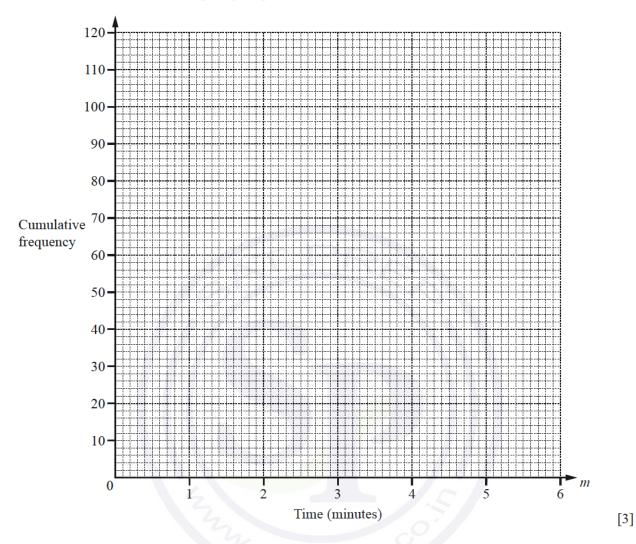
Answer(a) min [4]

(b) (i) Using the table in part (a), complete this cumulative frequency table.

Time (m minutes)	$m \leq 1$	$m \leq 2$	<i>m</i> ≤ 3	<i>m</i> ≤ 4	<i>m</i> ≤ 5	<i>m</i> ≤ 6
Cumulative frequency	72					120

[2]

(ii) Draw a cumulative frequency diagram to show the time taken.



(iii) Use your cumulative frequency diagram to find

(a) the median,

(b) the inter-quartile range,

(c) the 35th percentile.

(c) A new frequency table is made from the table shown in part (a).

Time (m minutes)	$0 < m \le 1$	1 < <i>m</i> ≤ 3	3 < <i>m</i> ≤ 6
Frequency	72		

(i) Complete the table above.

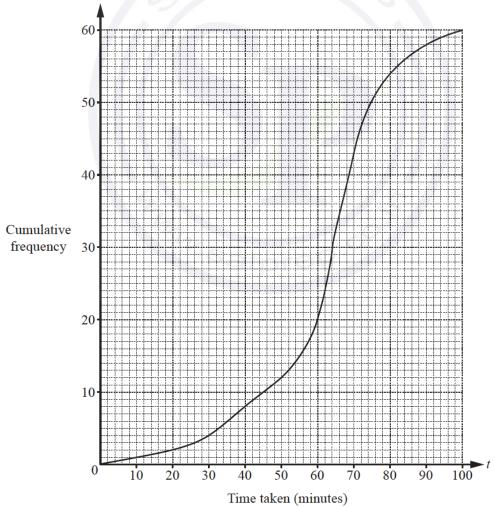
[2]

(ii) A histogram was drawn and the height of the first block representing the time $0 < m \le 1$ was 3.6 cm.

Calculate the heights of the other two blocks.

Question 18

The cumulative frequency diagram shows information about the time taken, t minutes, by 60 students to complete a test.



(a)	Find

(i)	the	med	lian.

	F 4 3
 min	Ш

(ii) the inter-quartile range,

 	min [2]	

(iii) the 40th percentile,

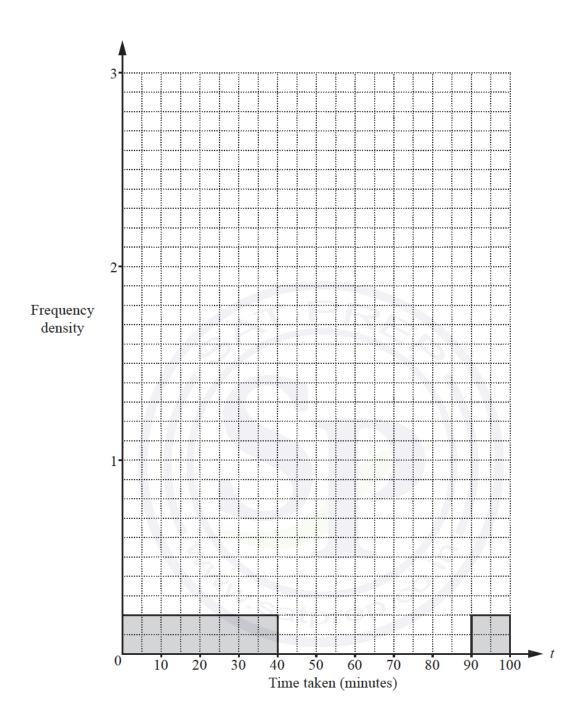
(iv) the number of students who took more than 80 minutes to complete the test.

(b) Use the cumulative frequency diagram to complete the frequency table below.

Time taken (t minutes)	$0 < t \le 40$	40 < <i>t</i> ≤ 60	60 < t ≤ 70	$70 < t \le 80$	80 < <i>t</i> ≤ 90	90 < <i>t</i> ≤ 100
Frequency	8				4	

[3]

(c) On the grid below, complete the histogram to show the information in the table in part (b).



[4]

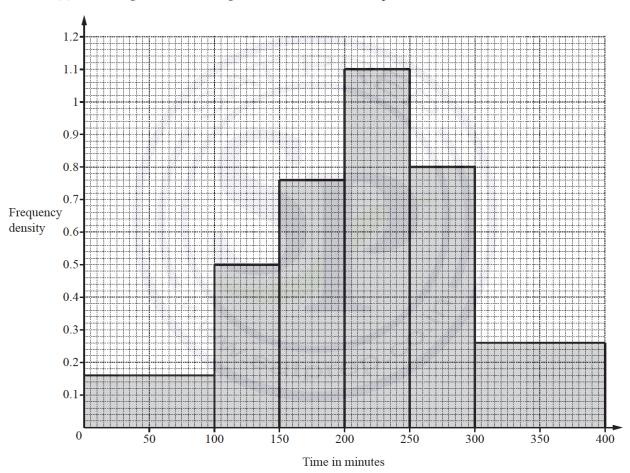
The table shows the amount of money, \$a, received for parking each day for 200 days.

Amount (\$a)	$200 < a \le 250$	$250 < a \le 300$	$300 < a \le 350$	$350 < a \le 400$	$400 < a \le 450$	450 < <i>a</i> ≤ 500
Frequency	13	19	27	56	62	23

Calculate an estimate of the mean amount of money received each day.

\$.....[4]

(d) The histogram shows the length of time that 200 cars were parked.



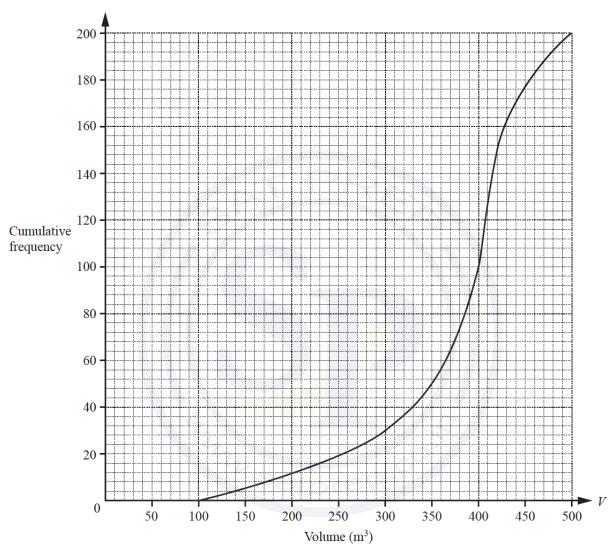
(i) Calculate the number of cars that were parked for 100 minutes or less.

.....[1]

(ii) Calculate the percentage of cars that were parked for more than 250 minutes.

.....% [2]

3 (a) 200 students estimate the volume, $V \, \text{m}^3$, of a classroom. The cumulative frequency diagram shows their results.



_			4
н	1	n	d

(i)	the	median,
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m ³ [1]

(ii) the lower quartile,

m ³	[1]
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(iii) the inter-quartile range,

(iv) the number of students who estimate that the volume is greater than $300 \,\mathrm{m}^3$.

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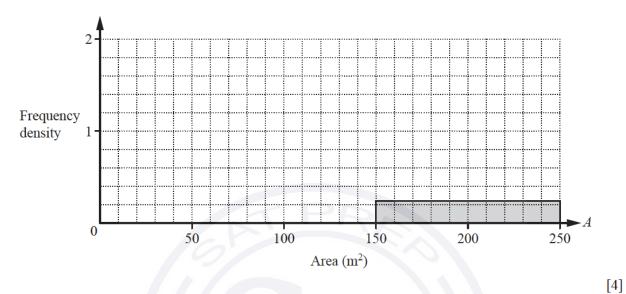
(b) The 200 students also estimate the total area, $A \,\mathrm{m}^2$, of the windows in the classroom. The results are shown in the table.

Area (A m²)	$20 < A \leqslant 60$	$60 < A \le 100$	$100 < A \leqslant 150$	$150 < A \le 250$
Frequency	32	64	80	24

(i) Calculate an estimate of the mean. Show all your working.

..... m² [4]

(ii) Complete the histogram to show the information in the table.

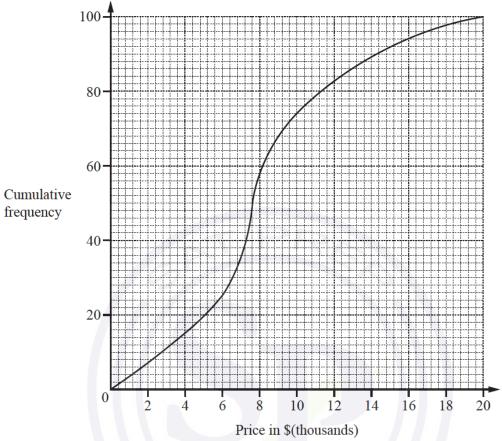


(iii) Two of the 200 students are chosen at random.

Find the probability that they both estimate that the area is greater than 100 m².







The cumulative frequency diagram shows information about the prices of 100 cars on Website A. Use the information to complete this table.

Lower quartile	Median	Upper quartile	Inter-quartile range
\$	\$7600	\$	\$

[2]

(ii) This table shows information about the prices of cars on Website B.

Lower quartile	Median	Upper quartile	Inter-quartile range
\$7600	\$10800	\$13 600	\$6000

Here are two	statements	comparing	the	distributions	of	the	prices	of	cars	on	Website	A	and
Website B.													

	(a)	The prices of cars on Website	e A are lo	wer than the price	s of cars on Website B.								
		because .											
	(b)	Website B.	A greater percentage of cars have a price more than \$13 600 on Website A compared Vebsite B. because										
(b)	The table	shows the prices of cars on W		2RA	[1]								
		Price (\$.	P)	Number of cars									
		0 < P <	6000	9									
		6000 < P <	8 000	29									
		8 000 < P \le	10000	20	-111								
		10 000 < P <	12 000	14									
		12 000 < P \le	14000	21	///								
		14 000 < P \le \	22 000	27									
	Calculate	an estimate of the mean price	of the 12	0 cars.									
		7.5			\$[4]								
(c)	Bryan pa	e of a car is \$8760. The system of 25% of this primonths, he will have paid a to			hly payments.								
	Calculat	e the cost of one monthly payr	nent.										
				9	5[3]								

200 people run 10 km.

The table shows some information about the times, t minutes, taken to run the 10 km.

Time (t minutes)	30 < <i>t</i> ≤ 40	40 < <i>t</i> ≤ 45	45 < <i>t</i> ≤ 50	50 < <i>t</i> ≤ 55	55 < <i>t</i> ≤ 60	$60 < t \le 80$
Frequency	8	22	95	55	14	6

(a) Howard takes 40 minutes to run the 10 km.

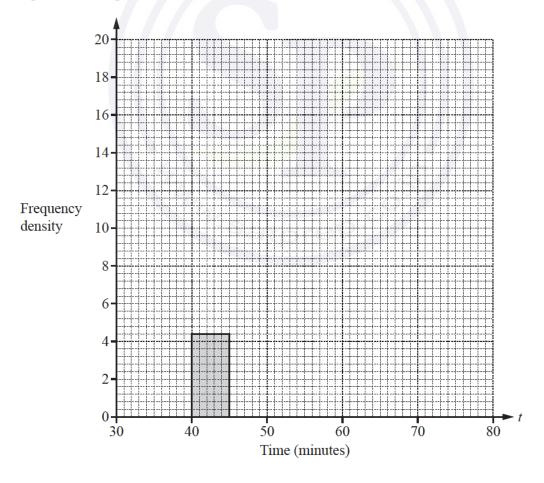
Calculate his average speed in kilometres per hour.

.....km/h [2]

(b) Calculate an estimate of the mean time.

.....min [4]

(c) Complete the histogram to show the information in the table.



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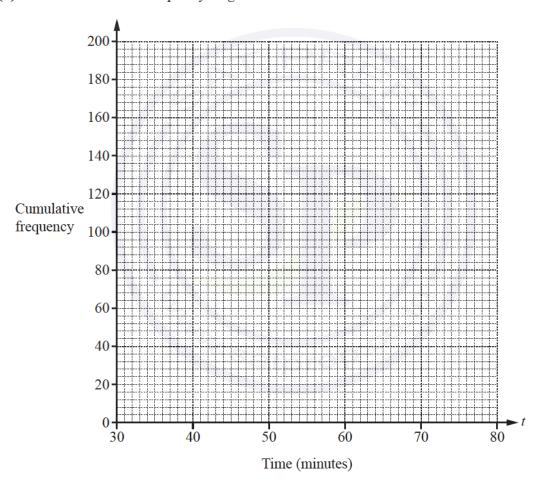
[4]

(d) (i) Use the frequency table opposite to complete the cumulative frequency table.

Time (t minutes)	<i>t</i> ≤ 40	<i>t</i> ≤ 45	<i>t</i> ≤ 50	<i>t</i> ≤ 55	<i>t</i> ≤ 60	t ≤ 80
Cumulative frequency	8	30			194	200

[1]

(ii) Draw a cumulative frequency diagram to show the information in the table above.



[3]

(iii)	Use	your	diagram	to	find	
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(a) the median,

																														1	n	1		n	Γ	1		1
	•					•	•	•	•	•	•	•	•	•	•	•	•	•	•	•	•		•	•	•	•	•	•	•	1	П	1	Ц	П	L	1	٠.	

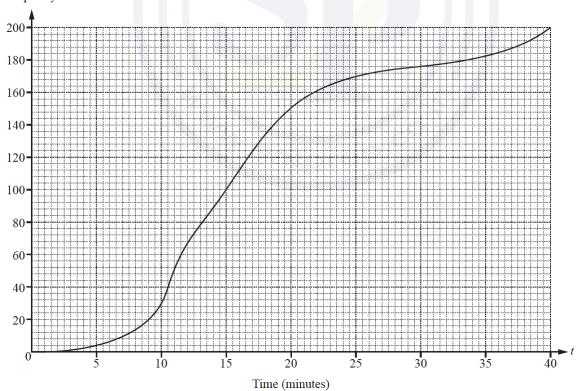
(b) the 90th percentile,

(c) the number of people who took more than 58 minutes to run the 10 km.

Question 23

(a) 200 students record the time, t minutes, for their journey from home to school. The cumulative frequency diagram shows the results.



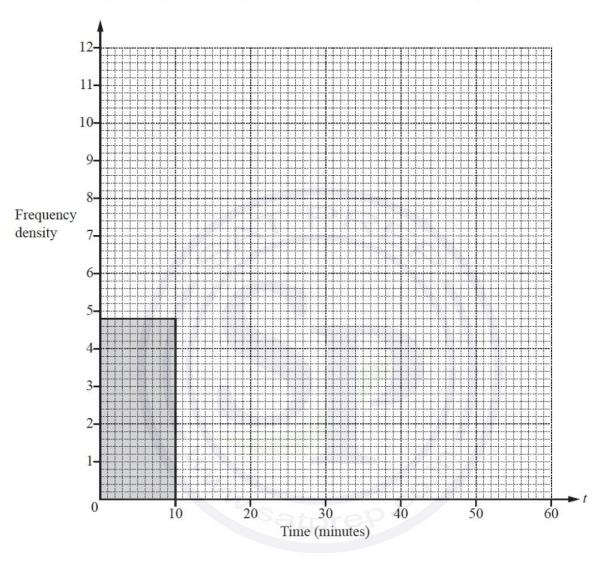


	Find	1						
	(i)	the median,						
								min [1]
						•••••		111111 [1]
	(ii)	the lower qua	ortile,					
								min [1]
	(iii)	the inter-quar	tile range,					
								min [1]
	(iv)	the 15th perc	entile					
	(11)	the 15th pere	chare,					
								min [1]
	(v)	the number o	f students whos	se journey time	was more than	30 minutes.		
								[2]
a.) T1-	- 2001		t mainread and format	1 i i	11 4- 1		[2]
(b			ole shows the re		neir journey iro	om school to ho	me.	
								ī
	Time	e (t minutes)	$0 < t \le 10$	$10 < t \le 15$	$15 < t \le 20$	$20 < t \le 30$	$30 < t \le 60$	
	Freq	uency	48	48	60	26	18	

(i) Calculate an estimate of the mean.

	min	[4]
--	-----	-----

(ii) On the grid, complete the histogram to show the information in the frequency table.



[4]

The table shows information about the time taken by 400 people to complete a race.

Time taken (m minutes)	45 < m ≤ 50	50 < m ≤ 60	60 < m ≤ 70	70 < m ≤ 90	90 < m ≤ 100	$100 < m \le 120$
Frequency	23	64	122	136	26	29

(a) Calculate an estimate of the mean time taken.

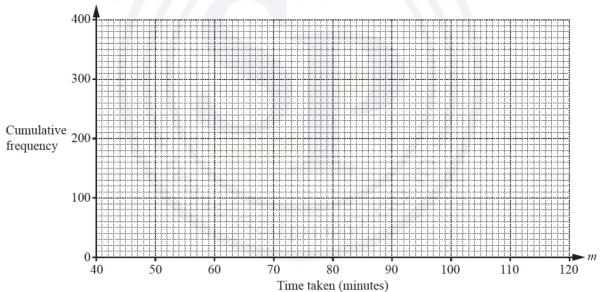
..... min [4]

(b) (i) Complete the cumulative frequency table.

Time taken (m minutes)	<i>m</i> ≤50	<i>m</i> ≤60	<i>m</i> ≤70	<i>m</i> ≤90	<i>m</i> ≤100	<i>m</i> ≤120
Cumulative frequency	23		TP	RAIN		400

[2]

(ii) On the grid, draw a cumulative frequency diagram to show this information.



- (iii) Use your diagram to estimate
- (a) the median,

..... min [1]

(b) the inter-quartile range,

..... min [2]

(c) the 60th percentile.

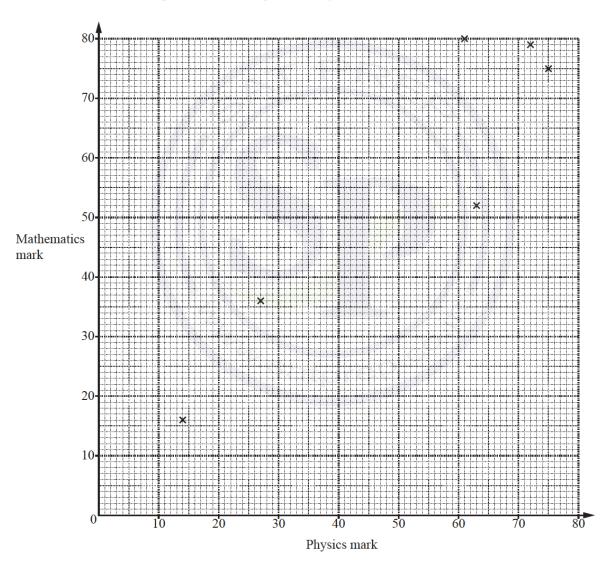
..... min [2]

(a) The table shows the marks gained by 10 students in their physics test and their mathematics test.

Physics mark	63	61	14	27	72	75	44	40	28	50
Mathematics mark	52	80	16	36	79	75	51	35	24	63

(i) Complete the scatter diagram below.

The first six points have been plotted for you.



	(22)	What type	of samulati	ion ia ab	arren in tha	anotton die	
l	(iii)) what type	of correlati	ion is sno	own m me	scatter dia	12141117

Г1	п.	
- 11		
1	- 1	

(b) The marks of 30 students in a spelling test are shown in the table below.

Mark	0	1	2	3	4	5
Frequency	2	4	5	5	6	8

Find the mean, median, mode and range of these marks.

Mean =	
1edian =	
Mode =	

(c) The table shows the marks gained by some students in their English test.

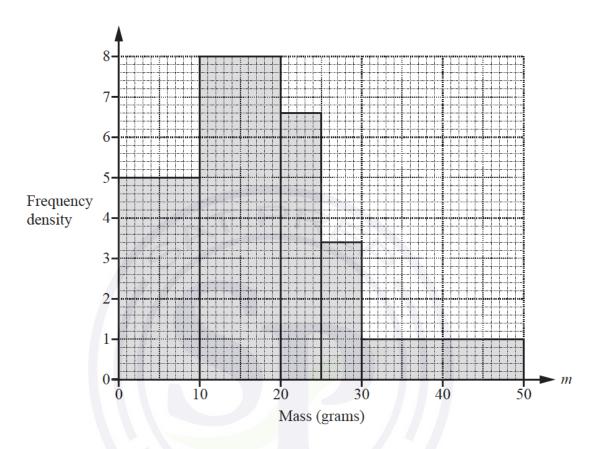
Mark	52	75	91
Number of students	x	45	11

The mean mark for these students is 70.3.

Find the value of x.

(a) Haroon has 200 letters to post.

The histogram shows information about the masses, *m* grams, of the letters.



(i) Complete the frequency table for the 200 letters.

Mass (m grams)	0 < <i>m</i> ≤ 10	$10 < m \le 20$	$20 < m \le 25$	$25 < m \le 30$	30 < m ≤ 50
Frequency	50			17	

[3]

(ii) Calculate an estimate of the mean mass.

	g	[4]	
--	---	-----	--

(b) Haroon has 15 parcels to post.

The table shows information about the sizes of these parcels.

Size	Small	Large
Frequency	9	6

Two parcels are selected at random.

Find the probability that

(i) both parcels are large,

.....[2]

(ii) one parcel is small and the other is large.

.....[3]

(c) The probability that a parcel arrives late is $\frac{3}{80}$.
4000 parcels are posted.

Calculate an estimate of the number of parcels expected to arrive late.

.....[1]

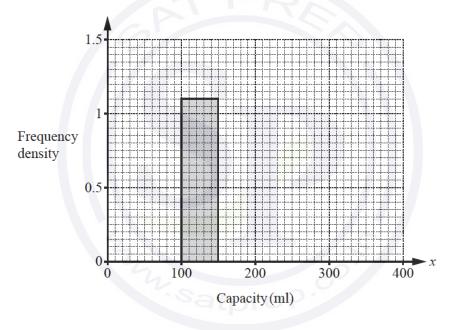
(a) 200 students estimate the capacity, *x* millilitres, of a cup. The results are shown in the frequency table.

Capacity (xml)	$0 < x \le 100$	$100 < x \le 150$	$150 < x \le 200$	$200 < x \le 250$	$250 < x \le 400$
Frequency	20	55	66	35	24

(i) Calculate an estimate of the mean.

..... ml [4]

(ii) Complete the histogram.



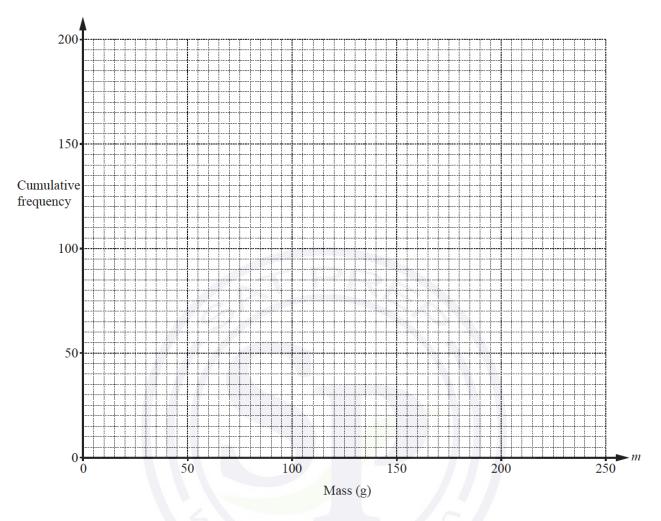
(b) The 200 students also estimate the mass, m grams, of a small rock. The results are shown in the cumulative frequency table.

Mass (m grams)	<i>m</i> ≤ 50	<i>m</i> ≤ 100	<i>m</i> ≤ 150	<i>m</i> ≤ 200	<i>m</i> ≤ 250
Cumulative frequency	28	64	104	168	200

(i) On the grid, draw a cumulative frequency diagram.

Continue on the next page..

[4]



- (ii) Find
 - (a) the 65th percentile,

..... g [1]

(b) the number of students who estimated more than $75\,\mathrm{g}$.

.....[2]

The time taken for each of 90 cars to complete one lap of a race track is shown in the table.

Time (t seconds)	$70 < t \leqslant 71$	$71 < t \le 72$	72 < <i>t</i> ≤ 73	$73 < t \le 74$	74 < <i>t</i> ≤ 75
Frequency	17	24	21	18	10

(a) Write down the modal time interval.

.....
$$< t \le$$
[1]

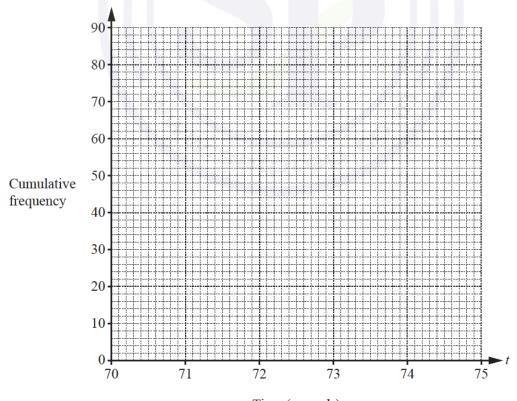
(b) Calculate an estimate of the mean time.

(c) (i) Complete the cumulative frequency table.

Time (t seconds)	<i>t</i> ≤ 71	<i>t</i> ≤ 72	<i>t</i> ≤ 73	<i>t</i> ≤ 74	<i>t</i> ≤ 75
Cumulative frequency	17				

[2]

(ii) On the grid, draw a cumulative frequency diagram to show this information.



Time (seconds)

(iii) Find the me	dian time.				
					s [1]
(iv) Find the inte	er-quartile range.				
					s [2]
	ace track measure I the lap in 75 seco	· ·			
_	oper bound for the er in kilometres p		f this car.		
					km/h [4]
Question 29					
The table shows in	nformation about t	he time, t minutes	s, taken for each	of 150 girls to cor	nplete an essay.
Time (t minutes)	60 < <i>t</i> ≤ 65	65 < <i>t</i> ≤ 70	$70 < t \le 80$	80 < <i>t</i> ≤ 100	$100 < t \le 150$
Frequency	10	26	34	58	22
(a) Write down to	he interval that co	ntains the mediar	ı time.		
				<	<i>t</i> ≤[1]
(b) Calculate an	estimate of the m	ean time			
(b) Calculate an	estimate of the in	Satn			min [4]
(c) Rafay looks	at the frequency	table			min [4]
			t the series of the	timas	
	s that it is not pos		t the range of the	times.	
Explair	n why he is correc	et.			
				•••••	
					[1]
Continue on the next	t page				

(ii)	He draws a pie chart to show this information.
	Calculate the sector angle for the interval $65 < t \le 70$ minutes.

ſο	,
 4	

(d) A girl is chosen at random.

Work out the probability that she took more than 100 minutes to complete the essay.

.....[1]

(e) Two girls are chosen at random.

Work out the probability that, to complete the essay,

(i) they both took 65 minutes or less,

.....[2]

(ii) one took 65 minutes or less and the other took more than 100 minutes.

.....[3]

(f) The information in the frequency table is shown in a histogram.

The height of the block for the $60 < t \le 65$ interval is 5 cm.

Complete the table.

Time (t minutes)	60 < <i>t</i> ≤ 65	65 < <i>t</i> ≤ 70	70 < <i>t</i> ≤ 80	80 < <i>t</i> ≤ 100	$100 < t \le 150$
Height of block (cm)	5 2			.5	

[3]

(a) There are 100 students in group *A*. The teacher records the distance, *d* metres, each student runs in one minute. The results are shown in the cumulative frequency diagram.



Find

(i) the median,

..... m [1]

(ii) the upper quartile,

..... m [1]

(iii) the inter-quartile range,

..... m [1]

(iv) the number of students who run more than 350 m.

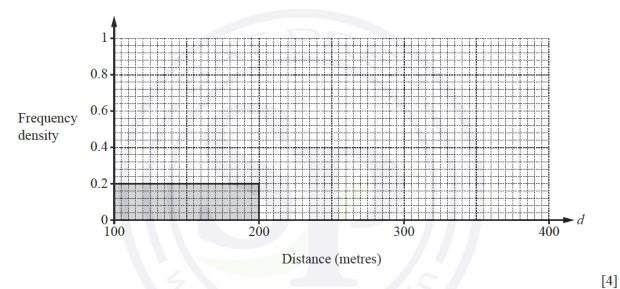
.....[2]

(b) There are 100 students in group *B*.

The teacher records the distance, *d* metres, each of these students runs in one minute. The results are shown in the frequency table.

Distance (d metres)	$100 < d \leqslant 200$	$200 < d \leqslant 250$	$250 < d \leqslant 280$	280 < <i>d</i> ≤ 320	320 < <i>d</i> ≤ 400
Number of students	20	22	30	16	12

- (i) Calculate an estimate of the mean distance for group B.
- (ii) Complete the histogram to show the information in the frequency table.



(c) For the 100 students in group B, the median is 258 m.

Complete the statement.

On average, the students in group A run than the students in group B. [1]

7 The frequency table shows information about the time, m minutes, that each of 160 people spend in a library.

Time (m minutes)	0 < m ≤ 10	10 < m ≤ 40	40 < m ≤ 60	60 < m ≤ 90	90 < m ≤ 100	100 < m ≤ 120
Frequency	3	39	43	55	11	9

(a)	(i)	Find the probability that one of these people, chosen at random, spends more than 100 minutes in
		the library.

Г	1	1
	1	ı

(ii) Calculate an estimate of the mean time spent in the library.

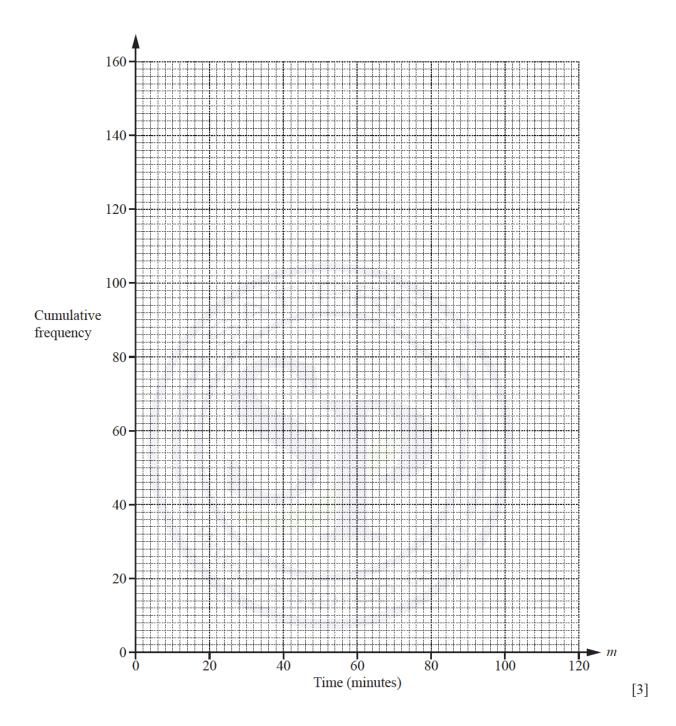
 min	[4]
 111111	

(b) Complete the cumulative frequency table below.

Time (m minutes)	<i>m</i> ≤ 10	<i>m</i> ≤ 40	<i>m</i> ≤ 60	<i>m</i> ≤ 90	<i>m</i> ≤ 100	<i>m</i> ≤ 120
Cumulative frequency	3	42				

[2]

(c) On the grid opposite, draw the cumulative frequency diagram.



(d) Us	se your cumulative frequer	cy diagram to find			
(i)	the median,				min [1]
(ii)	the interquartile range,				min [2]
(iii)	the 90th percentile,				
(iv)	the number of people w	ho spend more than	30 minutes in the	e library.	
Question	132				[2]
	ne scatter diagram shows th	ne physics mark and	the chemistry ma	ark for each of 12 stu	idents.
	7- 6- 5- Chemistry mark 3- 2- 1- 0- 0	1 2 3 4 Phys	* * * * * * * * * * * * * * * * * * *	* * * * * * * * * * * * * * * * * * *	
(i)	What type of correlation	ı is shown in the sca	itter diagram?		[1]
(ii)	On the scatter diagram,	draw a line of best f	ĭt.		[1]
(iii)	Find an estimate of the	hemistry mark for a	nother student wl	ho has a physics man	547

Continue on the next page..

56

(b) A teacher records the number of days each of the 24 students in her class are absent. The frequency table shows the results.

Number of days	0	1	2	3	4	5
Frequency	10	8	3	2	0	1

Find the mode, the median and the mean.

Mode =	

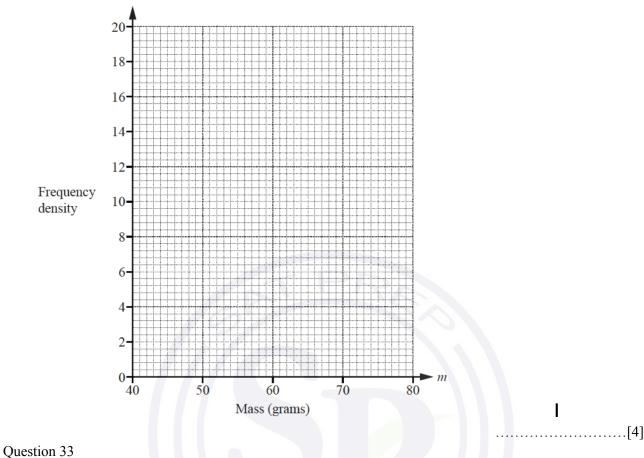
(c) Three sizes of eggs are sold in a shop.

The table shows the number of eggs of each size sold in one day.

Size	Small	Medium	Large
Mass (m grams)	46 < m ≤ 52	52 < m ≤ 62	62 < m ≤ 80
Number of eggs sold	78	180	162

(i)	Calculate an	estimate	of the	mean	mass

(ii) On the grid, draw a histogram to show the information in the table.



The time taken for each of 120 students to complete a cooking challenge is shown in the table.

Time (t minutes)	20 < t ≤ 25	25 < t ≤ 30	30 < t ≤ 35	35 < <i>t</i> ≤ 40	40 < <i>t</i> ≤ 45
Frequency	44	32	28	12	4

/ \	(*)	TT 7 14	1	41	1 1	· \		1
(a)	(i)	write	aown	the	modai	time	interval	L.

.....
$$< t \le$$
 [1]

(ii) Write down the interval containing the median time.

(iii) Calculate an estimate of the mean time.

 min	[4]

(iv) A student is chosen at random.

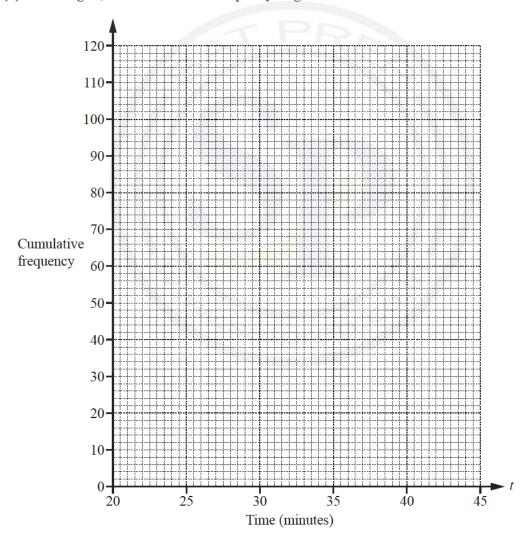
Find the probability that this student takes more than 40 minutes.

(b) (i) Complete the cumulative frequency table.

Time (t minutes)	<i>t</i> ≤ 20	<i>t</i> ≤ 25	<i>t</i> ≤ 30	<i>t</i> ≤ 35	<i>t</i> ≤ 40	<i>t</i> ≤ 45
Cumulative frequency	0	44				

[2]

(ii) On the grid, draw a cumulative frequency diagram to show this information.

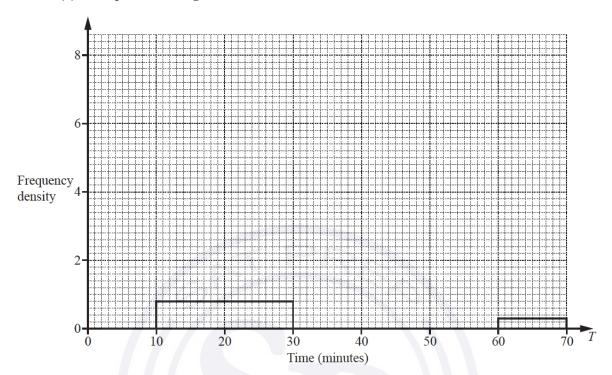


[3]

(iii)	Find the median time	e.		
(iv)	Find the interquartile	e range.		min [1]
				min [2]
(v)	Find the number of s	students who took mor	e than 37 minutes to	complete the cooking challenge.
			1.0	[2]
Questi	on 34			
(a) T	The table shows the an	nount of time, T minute	es, 120 people each sp	end in a supermarket one Saturday.
		Time (<i>T</i> minutes)	Number of people	
		10 < T ≤ 30	16	
		30 < <i>T</i> ≤ 40	18	7 /
		$40 < T \leqslant 45$	22	-
		$45 < T \leqslant 50$	40	
		50 < T ≤ 60	re 21	
		60 < T < 70	3	

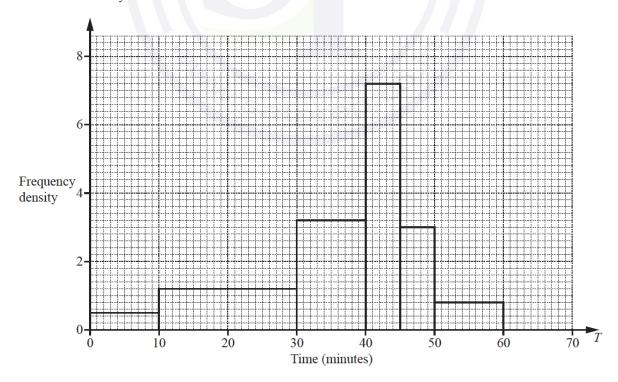
(i) Use the mid-points of the intervals to calculate an estimate of the mean.

(ii) Complete this histogram to show the information in the table.



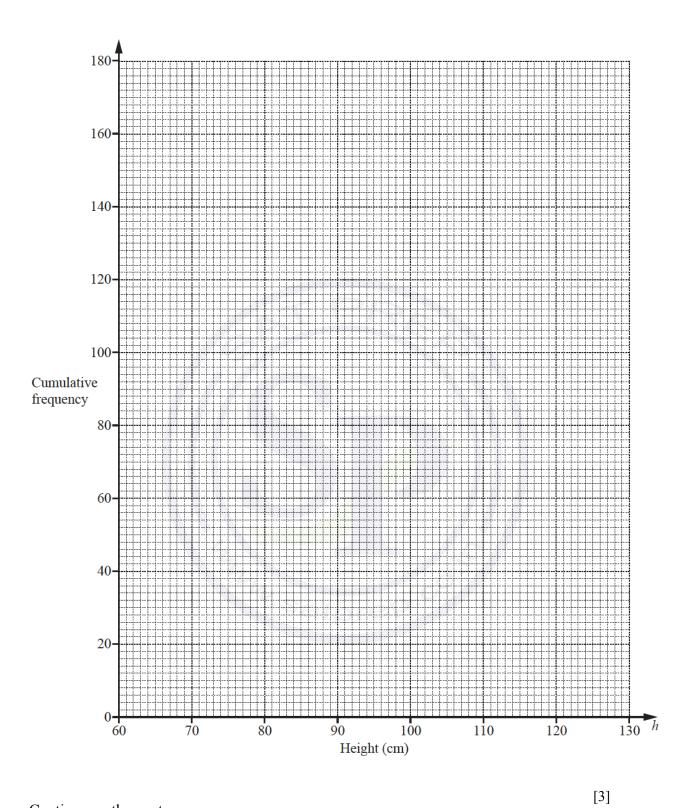
[4]

(b) This histogram shows the amount of time, *T* minutes, 120 people each spend in the supermarket one Wednesday.



Make a c	omment comp	aring the distri	butions of the t	imes for the two	days.	
						[1]
Question 35						
	urse records the hows the infor		of each of 180	children.		
Height (h cm)	$60 < h \leqslant 70$	70 < h ≤ 90	$90 < h \le 100$	$100 < h \leqslant 110$	$110 < h \leqslant 115$	$115 < h \le 125$
Frequency	8	26	35	67	28	16
			ach of the follow			
				$115 < h \le 125$		cm
				$110 < h \le 115$		cm
				$70 < h \le 90$		cm [3]
(c) Com	plete the cumul					
Height (h cm)	<i>h</i> ≤ 70	<i>h</i> ≤ 90	<i>h</i> ≤ 100	<i>h</i> ≤ 110	<i>h</i> ≤ 115	<i>h</i> ≤ 125
Cumulative frequency						180
						[2]

(d) On the grid opposite, draw a cumulative frequency diagram.



(e) Use y	our cumulative freq	uency diagram to	find an estimate of		
(i) t	he interquartile rang	ge,			cm [2]
(ii) t	he 70th percentile,				cm [2]
(iii) t	he number of childs	ren with height gre	ater than 106 cm.		[2]
Question 36					
(a) 20 stude	ents each record the le below shows the		of their pencil case		
Mass (p grams)	0 < p ≤ 50	50 < p ≤ 100	100	125	150 < p ≤ 200
Frequency	2	5	4	6	3
	se the frequency tal	ble above to compl	lete the cumulative	e frequency table.	g [4]
Mass (p grams)	<i>p</i> ≤ 50	<i>p</i> ≤ 100	<i>p</i> ≤ 125	<i>p</i> ≤ 150	<i>p</i> ≤ 200
Cumulative frequency	14			1.5	20
(iii) A	student is chosen a		s a pencil case wit		[2] nan 150 g[1]
Continue on t	he next page				

(b) Some students each record the mass, $m \log$, of their school bag. Adil wants to draw a histogram to show this information.

Complete the table below.

Mass (mkg)	$0 < m \le 4$	4 < m ≤ 6	6 < <i>m</i> ≤ 7	7 < m ≤ 10
Frequency	32			42
Height of bar on histogram (cm)	1.6	2	1.2	2.8

[2]

(c) The frequency table below shows information about the number of books read by some students in a reading marathon.

Number of books read	1	2	3	4	5	6	7	8
Frequency	2	2	16	10	9	4	x	2

(i)	The mean	number	of	books	read	is	4.28	
------------	----------	--------	----	-------	------	----	------	--

Find the value of x.

$$x =$$
 [3]

(ii) Write down the mode.

 	 																		[]	ľ	1	

(iii) Write down the median.

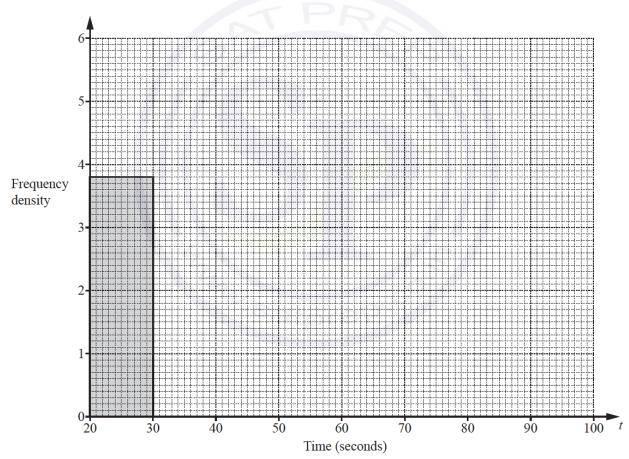
The table shows the time, *t* seconds, taken by each of 120 boys to solve a puzzle.

Time (t seconds)	20 < t ≤ 30	30 < <i>t</i> ≤ 35	35 < <i>t</i> ≤ 40	$40 < t \le 60$	$60 < t \le 100$
Frequency	38	27	21	16	18

(a) Calculate an estimate of the mean time.

.....s [4]

(b) On the grid, complete the histogram to show the information in the frequency table.



[4]

100 students were each asked how much money, m, they spent in one week.

The frequency table shows the results.

Amount (\$m)	0 < m ≤ 5	5 < m ≤ 10	10 < m ≤ 20	20 < m ≤ 30	30 < m ≤ 50
Frequency	16	38	30	9	7

(a) Calculate an estimate of the mean.

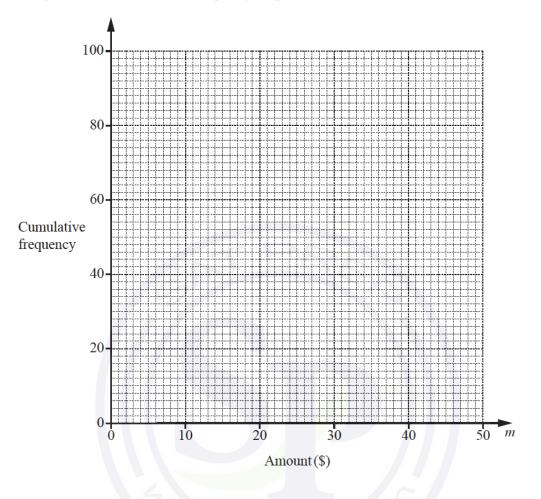
Φ	1	1
Φ	 4	ı

(b) Complete the cumulative frequency table below.

Amount $(\$m)$	<i>m</i> ≤ 5	<i>m</i> ≤ 10	<i>m</i> ≤ 20	<i>m</i> ≤ 30	<i>m</i> ≤ 50
runount (\$\psi m)	$m \leqslant 3$	<i>m</i> < 10	<i>m</i> ≤ 20	m ≤ 30	m ≤ 50
Cumulative frequency	16				100

[2]

(c) On the grid, draw the cumulative frequency diagram.



[3]

(d) Use your cumulative frequency diagram to find an estimate for

(i) the median,

\$[1]

(ii) the interquartile range,

\$ [2]

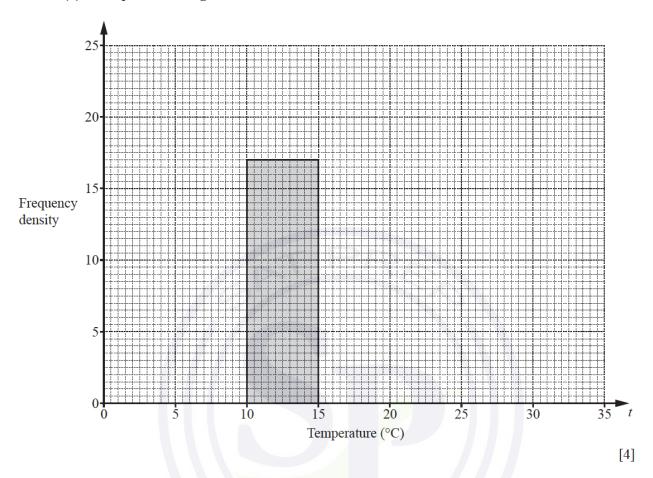
(iii) the number of students who spent more than \$25.

.....[2]

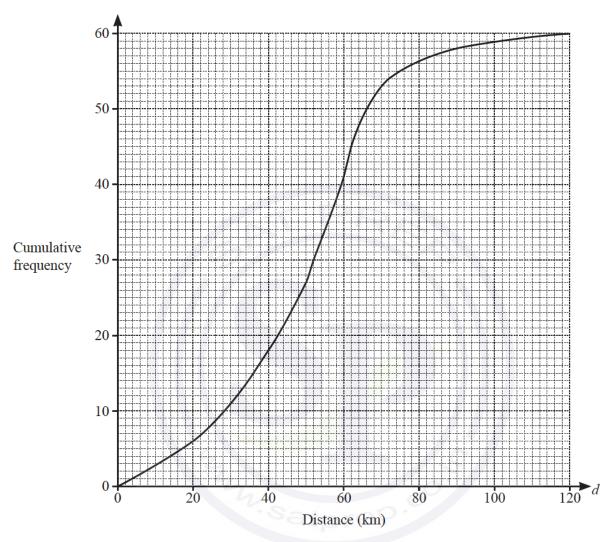
Ouestion	39
Oucsuon	ט ע

(a)	The	test score	es of 14	students	s are shov	vn belo	W.							
	21	21	23	26	25	21	22	20	21	23	23	27	24	21
	(i)	Find the	range, r	node, n	nedian and	d mean	of the t	est scor	es.					
								Range	=					
								Mode	=					
								Media	n =					
								Mean	=					[6]
(ii)	A student	is chose	en at rai	ndom.									
		Find the p	orobabili	ity that	this stude	ent has	a test so	ore of i	more th	nan 24				
(b)	Petr	a records	the scor	re in eac	h test she	takes						•••••		.[1]
(6)						uncs.								
		mean of				(x + 1).								
	Fine	d the <i>n</i> th s	score in t	terms o	f n and x .									
	Giv	e your ans	swer in i	ts simp	lest form.									
														.[3]
(c)	Dur	ing one y	ear the n	nidday	temperati	ires t ^o (C in Ze	dford w	ere rec	orded				
(0)		table sho		•	temperati	1105, 1	c, m 2c	aioia w	cre rec	oraca.	•			
	Te	mperature	e (t°C)	0 <	< t ≤ 10	10 <	< <i>t</i> ≤ 15	15 ·	$< t \le 2$	20 2	$20 < t \le 2$	25 2	5 < <i>t</i> ≤	35
	Νι	ımber of o	days		50		85		100		120		10	
	(i)	Calculat	e an esti	imate of	f the mear	n.								
	()												°C	[4]
Con	tinue	on the n	ext pag	e										

(ii) Complete the histogram to show the information in the table.



The cumulative frequency diagram shows information about the distance, $d \, \mathrm{km}$, travelled by each of 60 male cyclists in one weekend.



- (a) Use the cumulative frequency diagram to find an estimate of
 - (i) the median,

..... km [1]

(ii) the lower quartile,

..... km [1]

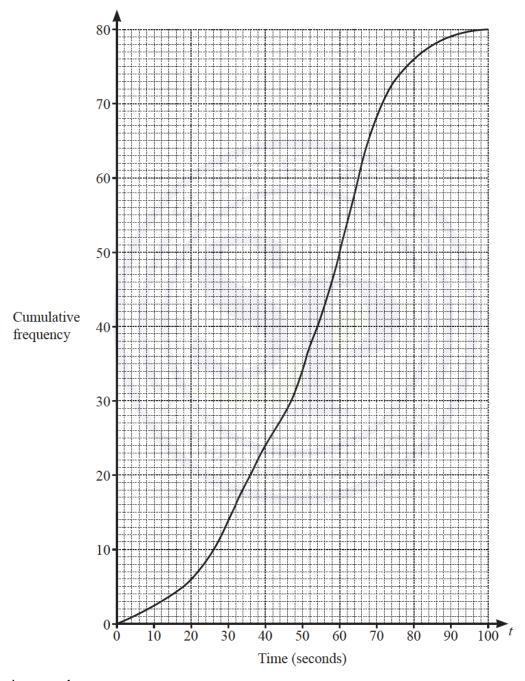
(iii) the interquartile range.

......km [1]

(b)	For the same we is 40 km.	ekend, the interquartile ra	ange for the distances travelled	d by a group of female cyclists
		nent comparing the distribute distances travelled by the	ution of the distances travelle he females.	d by the males with the
				[1]
(c)	A male cyclist is	chosen at random.		
	Find the probabi	lity that he travelled more	e than 50 km.	
				[2]
(d)	(i) Use the cur	nulative frequency diagra	m to complete this frequency	table.
		Distance (dkm)	Number of male cyclists	
		$0 < d \leq 40$	18	7
		40 < <i>d</i> ≤ 50	9	
		50 < d ≤ 60		
		$60 < d \le 70$		
		$70 < d \leqslant 90$		7/
		90 < <i>d</i> ≤ 120	2	
		4		[2]
	(ii) Calculate a	n actimate of the magn di	estance travalled	
	(ii) Calculate a	n estimate of the mean dis	stance travened.	
				km [4]

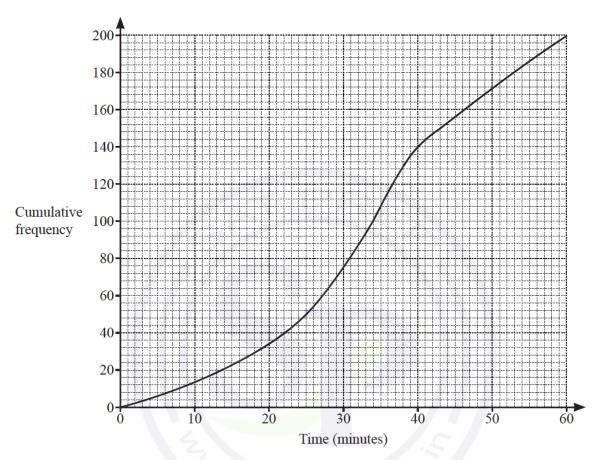
Question 41

The cumulative frequency diagram shows information about the time taken, t seconds, for a group of girls to each solve a maths problem.



(a) Use the cumulation	ve frequency dia	gram to find an	estimate for			
(i) the median,						
						.s [1]
(ii) the interquar	rtile range					.s [2]
(iii) the 20th per	rcentile,					
						. s [1]
(iv) the number	of girls who too	ok more than 66	seconds to solve	e the problem.		
(b) (i) Use the c	umulative freque	ency diagram to	complete the fre			[2]
Time (t seconds)	0 < <i>t</i> ≤ 20	20 < <i>t</i> ≤ 40	40 < <i>t</i> ≤ 60	$60 < t \le 80$	80 < <i>t</i> ≤ 100	
Frequency	6				4	
(c) A group of boy	an estimate of the same a median time of	ne problem.	lower quartile o	of 46 seconds an	nd an upper quan	
(i) Write dov	vn the percentag	e of boys with a	time of 66 secon			
(ii) Howard s		imes vary mor	e than the gir			% [1]
						[2]

(a) The cumulative frequency diagram shows information about the times taken by 200 students to solve a problem.



Use the cumulative frequency diagram to find an estimate for

- (i) the median, min [1
- (ii) the interquartile range,

..... min [2]

(iii) the number of students who took more than 40 minutes.

.....[2]

(b) Roberto records the value of each of the coins he has at home. The table shows the results.

Value (cents)	1	2	5	10	20	50
Frequency	3	1	3	2	4	2

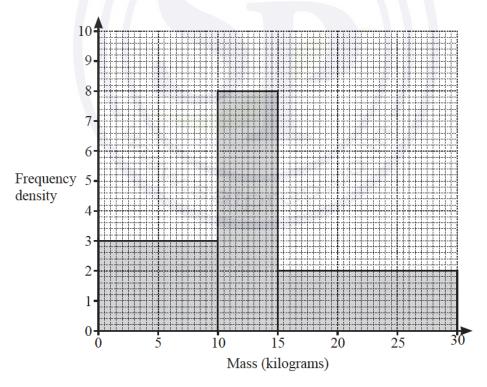
- (i) Find the range. cents [1]
- (ii) Find the mode. cents [1]
- (iii) Find the median. cents [1]
- (iv) Work out the total value of Roberto's coins.

..... cents [2]

(v) Work out the mean

...... Cents [1]

(c) The histogram shows information about the masses of 100 boxes.

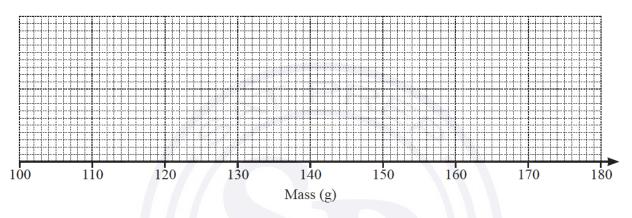


Calculate an estimate of the mean.

..... kg [6]

- (a) Here is some information about the masses of potatoes in a sack:
 - The largest potato has a mass of 174 g.
 - The range is 69 g.
 - The median is 148 g.
 - The lower quartile is 121 g.
 - The interquartile range is 38 g.

On the grid below, draw a box-and-whisker plot to show this information.



[4]

(b) The table shows the marks scored by some students in a test.

Mark	5	6	7	8	9	10
Frequency	8	2	12	2	0	1

Calculate the mean mark.

.....[3]

Question 43

The speed, v km/h, of each of 200 cars passing a building is measured.

The table shows the results.

Speed (vkm/h)	$0 < v \le 20$	$20 < v \leqslant 40$	$40 < v \leqslant 45$	$45 < v \leqslant 50$	$50 < v \le 60$	$60 < v \le 80$
Frequency	16	34	62	58	26	4

(a) Calculate an estimate of the mean.

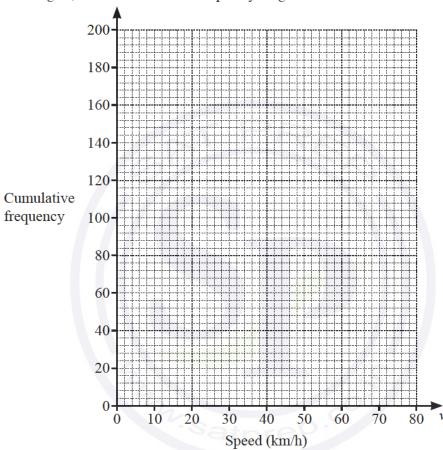
..... km/h [4]

(b) (i) Use the frequency table to complete the cumulative frequency table.

Speed (v km/h)	v ≤ 20	v ≤ 40	v ≤ 45	<i>v</i> ≤ 50	v ≤ 60	v ≤ 80
Cumulative frequency	16	50			196	200

[1]

(ii) On the grid, draw a cumulative frequency diagram.



[3]

(iii) Use your diagram to find an estimate of

(a) the upper quartile,

..... km/h [1]

(b) the number of cars with a speed greater than 35 km/h.

[ː	2	2))))																																																																																																																																							
----	---	---	---	---	--	--	--	--	--	---	---	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--

(c) Two of the 200 cars are chosen at random.

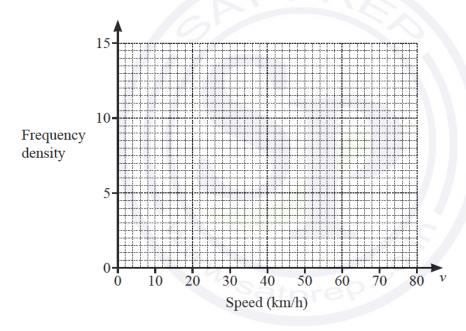
Find the probability that they both have a speed greater than $50\,\mathrm{km/h}$.

.....[2]

(d) A new frequency table is made by combining intervals.

Speed (vkm/h)	$0 < v \leqslant 40$	$40 < v \leqslant 50$	$50 < v \leqslant 80$
Frequency	50	120	30

On the grid, draw a histogram to show the information in this table.



[3]

The heights, *h* metres, of the 120 boys in an athletics club are recorded. The table shows information about the heights of the boys.

Height (h metres)	$1.3 < h \leqslant 1.4$	$1.4 < h \leqslant 1.5$	$1.5 < h \leqslant 1.6$	$1.6 < h \leqslant 1.7$	$1.7 < h \leqslant 1.8$	$1.8 < h \leqslant 1.9$
Frequency	7	18	30	24	27	14

(a)	(i)	Write down	the modal	class

..... $< h \le$ [1]

(ii) Calculate an estimate of the mean height.

..... m [4]

(b) (i) One boy is chosen at random from the club.

Find the probability that this boy has a height greater than 1.8 m.

.....[1]

(ii) Three boys are chosen at random from the club.

Calculate the probability that one of the boys has a height greater than 1.8 m and the other two boys each have a height of 1.4 m or less.

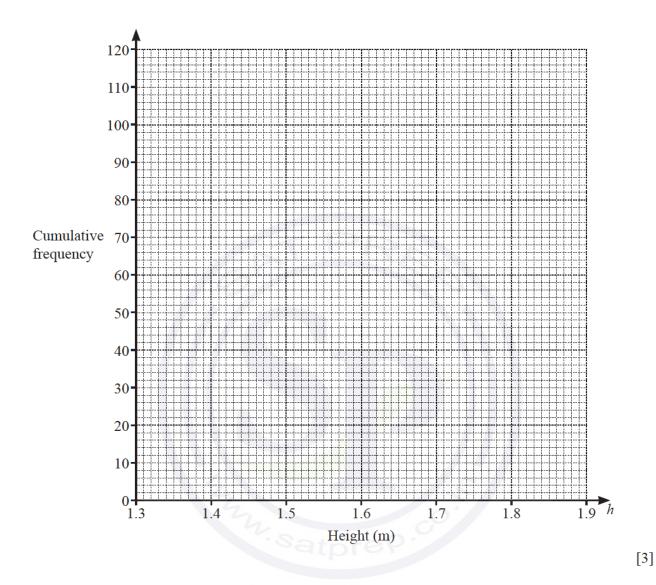
.....[4]

(c) (i) Use the frequency table on page 4 to complete the cumulative frequency table.

Height (h metres)	<i>h</i> ≤ 1.4	<i>h</i> ≤ 1.5	<i>h</i> ≤ 1.6	<i>h</i> ≤ 1.7	<i>h</i> ≤ 1.8	<i>h</i> ≤ 1.9
Cumulative frequency	7	25				

[2]

(ii) On the grid, draw a cumulative frequency diagram to show this information.



- (d) Use your diagram to find an estimate for
 - (i) the median height,

..... m [1]

(ii) the 40th percentile.

..... m [2]

The time, t minutes, taken by each of 80 people to travel to work is recorded.

The table shows information about these times.

Time (t minutes)	0 < <i>t</i> ≤ 5	5 < <i>t</i> ≤ 10	$10 < t \le 20$	20 < <i>t</i> ≤ 35	$35 < t \le 60$
Frequency	3	7	18	28	24

1	(0)	TT7 '4 1	41 1	1	containing the	1
19		WITE COM	The class	1nterval	containing the	median time
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1	(-)					

	1 +	1	Г17
• • • • • • • • • • • • • • • • • • • •	1	-	 [T]

(ii) Calculate an estimate of the mean time.

•	F 47
 mın	141
 TTTTT	

(b) (i) One of these 80 people is chosen at random.

Find the probability that this person took longer than 10 minutes to travel to work. Give your answer as a fraction in its simplest form.

(ii) Two people are chosen at random from those taking 20 minutes or less to travel to work.

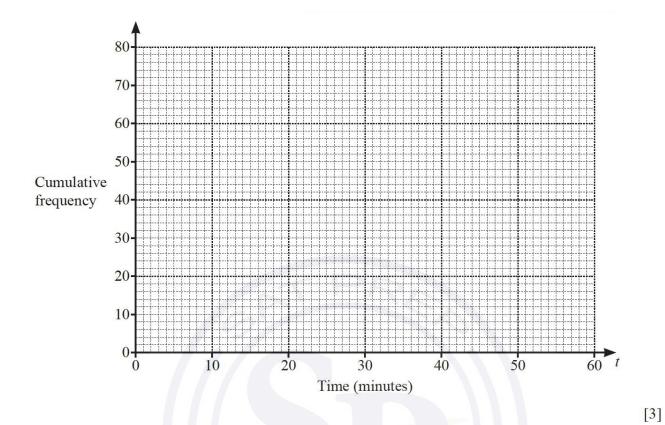
Calculate the probability that one of these people took 5 minutes or less and the other took more than 5 minutes.

(c) (i) Use the frequency table on page 8 to complete the cumulative frequency table.

Time (t minutes)	<i>t</i> ≤ 5	<i>t</i> ≤ 10	<i>t</i> ≤ 20	<i>t</i> ≤ 35	<i>t</i> ≤ 60
Cumulative frequency	3	10			80

(ii) On the grid, draw a cumulative frequency diagram to show this information.

[1]



(iii) Find an estimate for the 80th percentile.

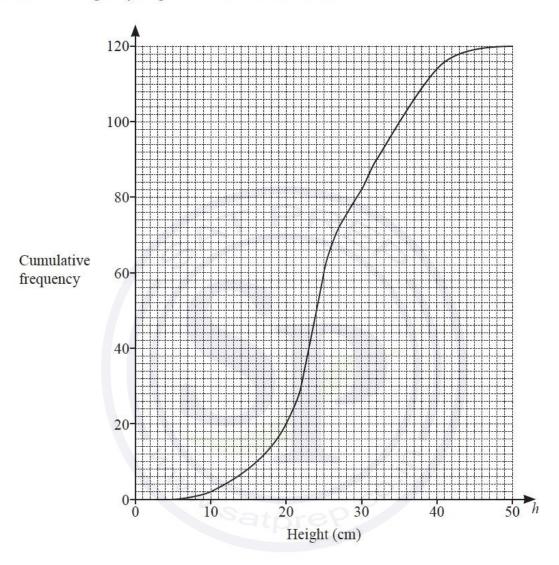
..... min [2]

(iv) Find an estimate for the percentage of people who took longer than 45 minutes to travel to work.

Show all your working.

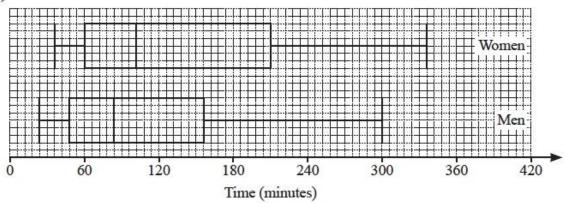
Question 46

The height, $h\,\mathrm{cm}$, of each of 120 plants is measured. The cumulative frequency diagram shows this information.



(a)	Use	the cumulative free	quency diagram	to find an estir	nate of			
	(i)	the median,						
	(ii)	the interquartile ra	nge,				cm	[1]
	(iii)	the 60th percentile					cm	[2]
					*******		cm	[1]
	(iv)	the number of plan	nts with a height	greater than 4	0 cm.			
(b)	The	information in the	cumulative freq	uency diagram	is shown in thi			[2]
		Height, h cm	0 < h ≤ 10	10 < h ≤ 20	20 < h ≤ 30	$30 < h \le 50$		
		Frequency	2	18	62	38		
	(i)	Calculate an estim	ate of the mean	height.			cm [4]
	(ii)	A histogram is dra The height of the						
		Calculate the heig	tht of the bar rep	resenting the in	nterval $30 < h$	≤ 50.		
							cm	[2]

(a)



The box-and-whisker plots show the times spent exercising in one week by a group of women and a group of men.

Below are two statements comparing these times.

For each one, write down whether you agree or disagree, giving a reason for your answer.

Statement	Agree or disagree	Reason
On average, the women spent less time exercising than the men.		
The times for the women show less variation than the times for the men.		- [.5]

[2]

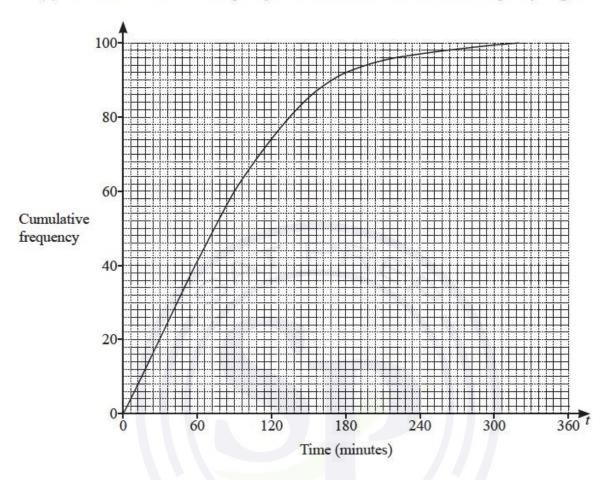
(b) The frequency table shows the times, t minutes, each of 100 children spent exercising in one week.

Time (t minutes)	0 < <i>t</i> ≤ 60	60 < <i>t</i> ≤ 100	$100 < t \le 160$	160 < <i>t</i> ≤ 220	220 < <i>t</i> ≤ 320
Frequency	41	24	23	8	4

(i) Calculate an estimate of the mean time.

	F .
 177117	14
 111111	17

(ii) The information in the frequency table is shown in this cumulative frequency diagram.



Use the cumulative frequency diagram to find an estimate of

(a) the 60th percentile,

..... min [1]

(b) the number of children who spent more than 3 hours exercising.

.....[2]

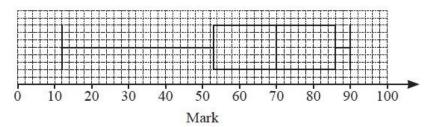
(iii) A histogram is drawn to show the information in the frequency table. The height of the bar for the interval $60 < t \le 100$ is 10.8 cm.

Calculate the height of the bar for the interval $160 < t \le 220$.

..... cm [2]

Ouestion 48

(a) The box-and-whisker plot shows information about the marks scored by some students in a test.



(i) Write down the median mark.

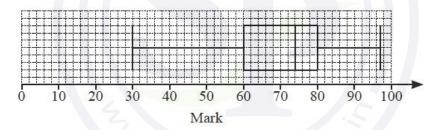


(ii) Work out the range.

(iii) Jais scored a mark in the test that was higher than the marks scored by 75% of the students.

Write down a possible mark for Jais.

- (iv) This box-and-whisker plot shows information about the marks scored by the same students in a second test.



Make one comparison between the distributions of marks in the two tests.

.....[1]

(b) The table shows information about the height, $h \, \text{cm}$, of each of 50 plants.

Height (h cm)	0 < h ≤ 20	20 < h ≤ 30	30 < h ≤ 34	34 < <i>h</i> ≤ 40	40 < h ≤ 60
Frequency	4	9	20	15	2

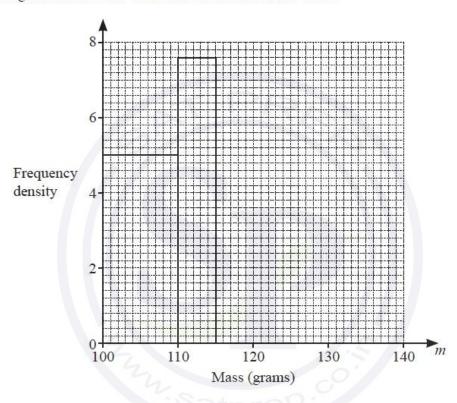
Calculate an estimate of the mean.

..... cm[4]

(c) Some apples are weighed and the mass, m grams, of each apple is recorded. The table shows the results.

Mass (m grams)	100 < m ≤ 110	110 < m ≤ 115	115 < m ≤ 125	125 < <i>m</i> ≤ 140
Frequency	50	x	44	51

The histogram shows some of the information from the table.



(i) Work out the value of x.

x = [1]

(ii) Complete the histogram.

[2]

(a) Zoe's test scores last term were 6 7 7 7 8 9 9 10 10.

Find

(i) the range,

.....[1]

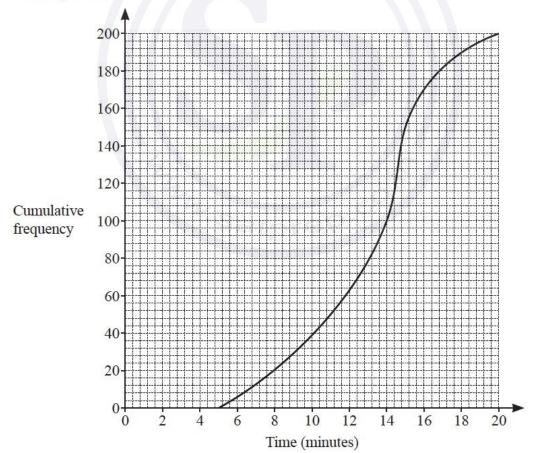
(ii) the mode,

.....[1]

(iii) the median.

.....[1]

(b) The cumulative frequency diagram shows information about the time taken by each of 200 students to solve a problem.



Use the diagram to find an estimate of

(i) the median,

	F17
 min	

(ii) the interquartile range.

 min	[2]
 пшп	[4]

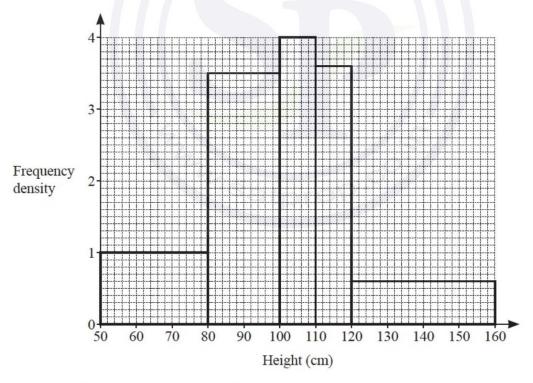
(c) The test scores of 200 students are shown in the table.

Score	5	6	7	8	9	10
Frequency	3	10	43	75	48	21

Calculate the mean.

.....[3]

(d) The height, in cm, of each of 200 plants is measured. The histogram shows the results.



Calculate an estimate of the mean height.

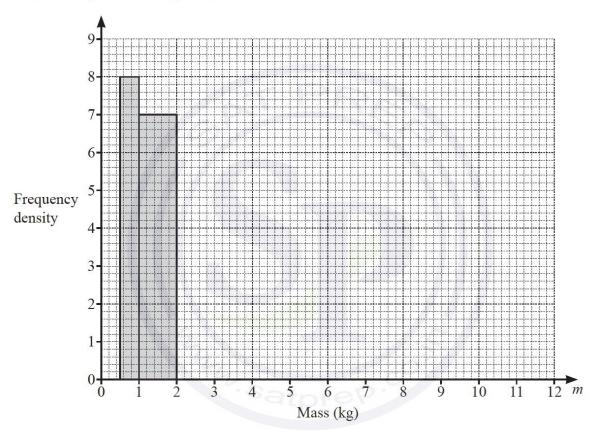
You must show all your working.

 cm	[6]

(a) The mass, m kg, of each of 40 parcels in a warehouse is recorded. The table shows information about the masses of these parcels.

Mass (m kg)	$0.5 < m \leqslant 1$	1 < m ≤ 2	2 < m ≤ 4	4 < m ≤ 7	7 < m ≤ 12
Frequency	4	7	15	10	4

(i) Complete the histogram to show this information.



[3]

(ii) Calculate an estimate of the mean mass of the parcels.

..... kg [4]

(iii) A parcel is picked at random from the 40 parcels.

Find the probability that this parcel has a mass of 2 kg or less.

.....[1]

(iv)	Two parcels are picked at random without replacement from those with a mass greater than 2 kg.
	Work out the probability that one of them has a mass greater than 7 kg and the other has a mass of 4 kg or less.
	[3]
(b)	A van delivers parcels from a different warehouse. The box-and-whisker plot shows information about the masses of the parcels in the van.
	0 1 2 3 4 5 6 7 8 9 Mass (kg)
(i)	Find the median.
(ii)	Find the interquartile range. kg [1]
	kg [1]
(iii)	Two parcels are removed from the van at the first delivery. The masses of these parcels are 2.4 kg and 5.8 kg.
	Describe the effect that removing these parcels has on the median mass of the remaining parcels. Give a reason for your answer.

.....[2]

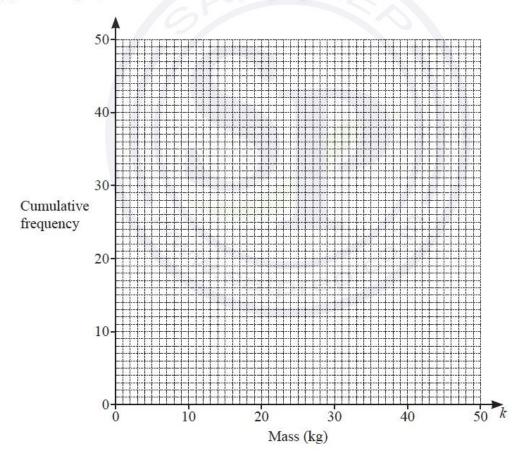
(a) The table shows information about the mass, in kilograms, of each of 50 children.

Mass (kkg)	0 < k ≤ 10	$10 < k \le 25$	$25 < k \le 35$	$35 < k \le 40$	40 < k ≤ 50
Frequency	3	19	21	5	2

(i) Complete the cumulative frequency table.

Mass (kkg)	$k \le 10$	<i>k</i> ≤ 25	<i>k</i> ≤ 35	$k \le 40$	$k \le 50$
Cumulative frequency					

(ii) On the grid, draw a cumulative frequency diagram to show this information.



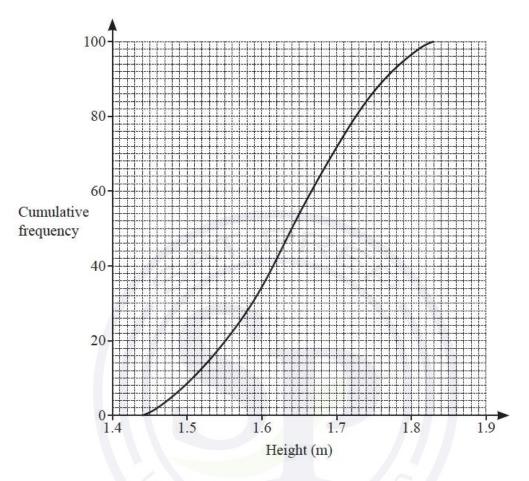
[3]

[2]

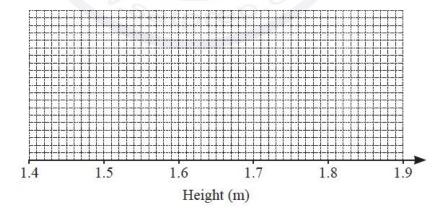
(iii) Use your diagram to find an estimate of the number of children with a mass of 32 kg or less.

 		[1]
		L.

(b) This cumulative frequency diagram shows information about the height, in metres, of each of 100 students.



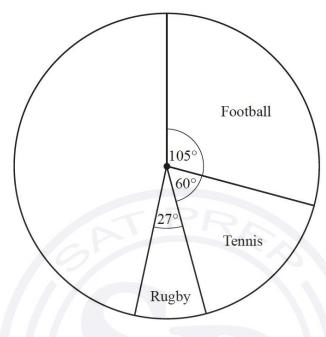
The height of the tallest student is 1.83 metres. The height of the shortest student is 1.45 metres.



On this grid, draw a box-and-whisker plot for the heights of the 100 students.

[4]

(a) Jean asks 600 people to choose their favourite sport. The pie chart shows some of this information.



- (i) Show that 100 people choose tennis.
- (ii) Work out how many people choose rugby. Continue on the next page...

[1]

(c) A dice is rolled 100 times.

The frequency table shows the results.

Score	1	2	3	4	5	6
Frequency	16	25	17	19	8	15

Find

(i) the range,

.....[1]

(ii) the mode,

.....[1]

(iii) the median.

.....[1]

(d) 50 students answer a mathematics question.

The table shows the time, t seconds, taken by each student to answer the question.

Time (t seconds)	$10 < t \le 20$	20 < <i>t</i> ≤ 25	$25 < t \le 30$	$30 < t \le 50$	$50 < t \le 80$
Frequency	2	8	12	16	12

Calculate an estimate of the mean.

.....s [4]

.....[2]

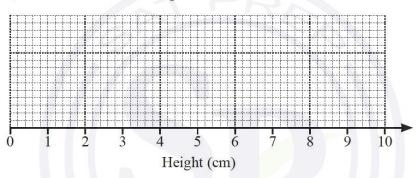
(iii) 125 people choose cricket and the rest choose swimming.

Complete the pie chart to show this information.

[2]

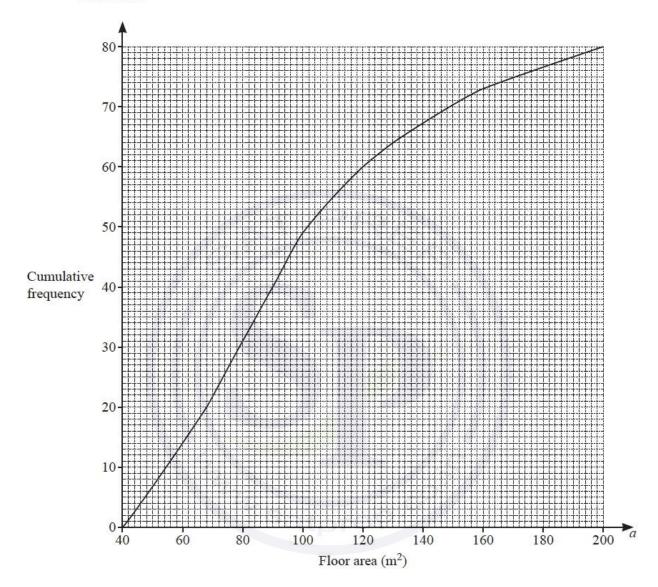
- **(b)** The heights of some plants are measured:
 - smallest height = $0.6 \,\mathrm{cm}$
 - range = $8.1 \,\mathrm{cm}$
 - median = 5.2 cm
 - lower quartile = $3.4 \,\mathrm{cm}$
 - interquartile range = 4.1 cm.

On the grid, draw a box-and-whisker plot to show this information.



[3]

2 (a) The cumulative frequency diagram shows information about the floor area, a m², of each of 80 houses.



Use the diagram to find an estimate of

-			
(i)	the	med	ian
(-/	· · · ·	TITLE	PECCET

..... m² [1]

..... m² [1]

	m^2	[1]
--	-------	-----

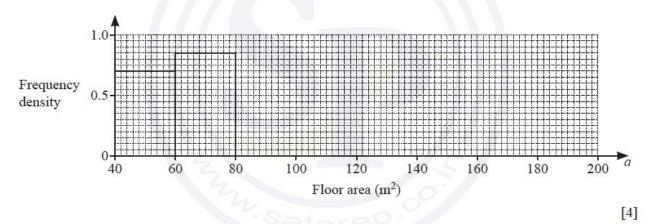
(iv) the number of houses with a floor area greater than 120 m².

(b) The information about the 80 floor areas is shown in this frequency table.

Floor area (a m²)	40 < a ≤ 60	60 < a ≤ 80	80 < <i>a</i> ≤ 100	100 < a ≤ 130	130 < a ≤ 160	160 < <i>a</i> ≤ 200
Frequency	14	17	18	15	9	7

(i) Calculate an estimate of the mean floor area.

(ii) Complete the histogram to show the information in the frequency table.

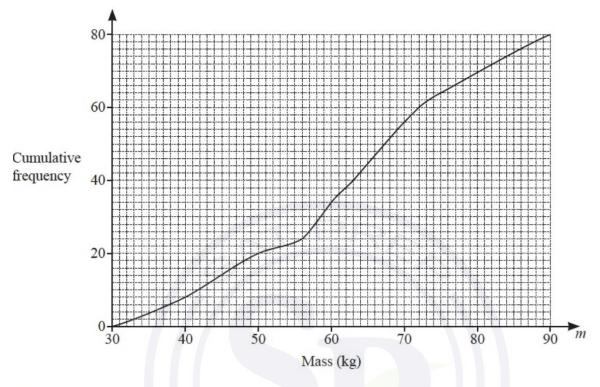


(iii) Two of the houses are picked at random.

Find the probability that one of the houses has a floor area greater than $130\,\text{m}^2$ and the other has a floor area $60\,\text{m}^2$ or less.

FO
 1 4
 0

3 The cumulative frequency diagram shows information about the mass, $m \log n$, of each of 80 boys.



(a)

30 40 50 60 70 80 90 m

Mass (kg)

On the grid, draw a box-and-whisker plot to show the information in the cumulative frequency diagram. [4]

- (b) Use the cumulative frequency diagram to find an estimate of
 - (i) the 30th percentile,
 - (ii) the number of boys with a mass greater than 75 kg.

.....[2

(c) (i) Use the cumulative frequency diagram to complete this frequency table.

Mass (mkg)	30 < m ≤ 40	40 < m ≤ 50	50 < m ≤ 60	60 < m ≤ 70	70 < m ≤ 80	80 < m ≤ 90
Frequency	8	12			14	10

(ii)	Calculate a	n estimate	of the	mean	mass	of the	boys
------	-------------	------------	--------	------	------	--------	------

 1	F47
 KQ:	14
 	F . 1

(iii) Two boys are chosen at random from those with a mass greater than 70 kg.

Find the probability that one of them has a mass greater than $80\,\mathrm{kg}$ and the other has a mass of $80\,\mathrm{kg}$ or less.



The table shows information about the mass, m grams, of each of 120 letters.

Mass (m grams)	0 < m ≤ 50	50 < m ≤ 100	$100 < m \le 200$	$200 < m \le 500$
Frequency	43	31	25	21

(a) Calculate an estimate of the mean mass.

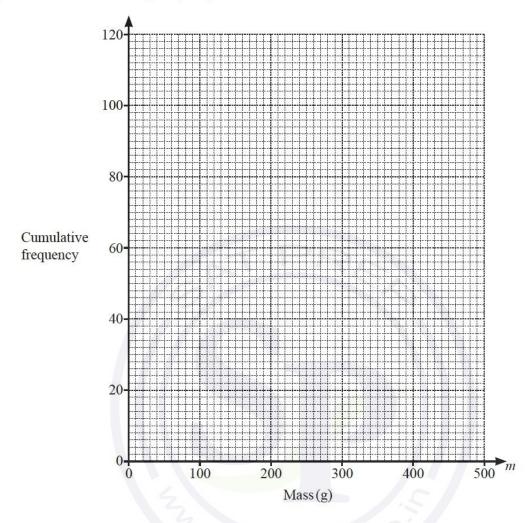
																													г		ŀ	1
																				÷	0						2	5	ŀ	4	ŀ	ı

(b) Iraj draws a histogram to show this information. He makes the height of the first bar 17.2 cm.

Calculate the height of each of the remaining bars.



(d) Draw a cumulative frequency diagram.



(e) Use the cumulative frequency diagram to find an estimate for

(i) the median,

..... g [1]

[3]

(ii) the upper quartile,

..... g [1]

(iii) the 40th percentile,

..... g [2]

(iv) the number of letters with a mass m where $250 < m \le 400$.

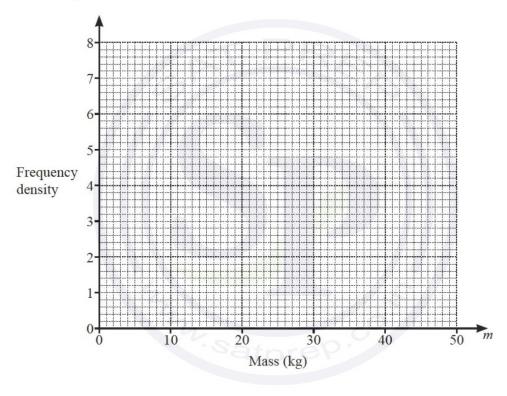
.....[2]

Information about the mass, $m \log$, of each of 150 children is recorded in the frequency table.

Mass (mkg)	$0 < m \le 10$	10 < m ≤ 20	$20 < m \leqslant 25$	$25 < m \leqslant 40$	40 < m ≤ 50
Frequency	12	38	32	50	18

(a) Calculate an estimate of the mean mass.

(b) Draw a histogram to show the information in the table.



[4]

(c) (i) Use the frequency table to complete this cumulative frequency table.

Mass (m kg)	<i>m</i> ≤ 10	<i>m</i> ≤ 20	<i>m</i> ≤ 25	$m \leq 40$	<i>m</i> ≤ 50
Cumulative frequency					

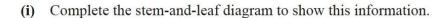
[2]

(ii) Calculate the percentage of children with a mass greater than 10 kg.

	%	[2]
--	---	-----

1	1	The list shows	15 '11 .	ACRES OF STREET STREET, ST. ST. STREET, ST.	1 /	1 1	0
ı	2	The list shows	13 midday fen	onerallites in	degrees (elsills 1	n Silntown
۱		THE HIST SHOWS	15 Illiaday tell	aperatures, m	acgices (Cisius, i	in Sumown.

17 21 21 18 23 22 25 19 21 17 19 18 21 24 23



1	7	
2		

Key: 1|7 represents 17 °C

[2]

(ii) Find the median.

.....°C [1]

(iii) Find the upper quartile.

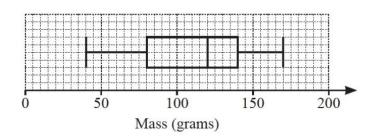
.....°C [1]

(iv) Rahul draws a pie chart to show this information.

Calculate the sector angle for the number of days the temperature is $18\,^{\circ}\text{C}$.

.....[2

(b)



The box-and-whisker plot shows information about the masses, in grams, of some apples.

(i) Find the median.

 9	[1]
_	L 1

(ii) Find the range.

(iii) Find the interquartile range.

(c) (i) The time, t minutes, spent on homework in one week by each of 200 students is recorded. The table shows the results.

Time (t minutes)	40 < <i>t</i> ≤ 60	$60 < t \le 80$	80 < <i>t</i> ≤ 90	90 < <i>t</i> ≤ 100	$100 < t \le 150$
Frequency	6	10	70	84	30

Calculate an estimate of the mean.

(ii) A new table with different class intervals is completed.

Time (t minutes)	40 < <i>t</i> ≤ 90	90 < <i>t</i> ≤ 150	
Frequency	86	114	

On a histogram the height of the bar for the $40 < t \le 90$ interval is 17.2 cm.

Calculate the height of the bar for the $90 < t \le 150$ interval.

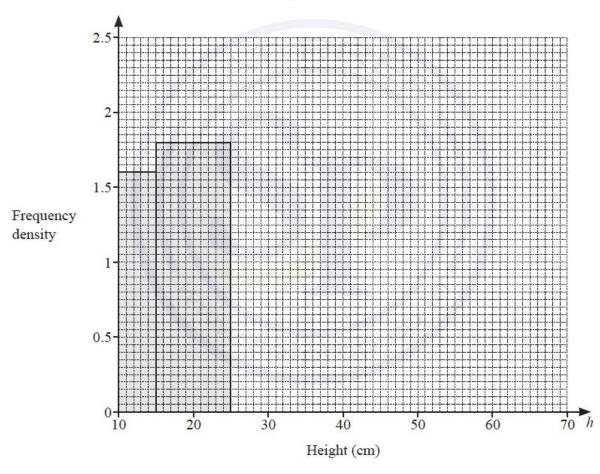
The height, $h \, \text{cm}$, of each of 100 plants is recorded.

The table shows information about the heights of these plants.

Height (h cm)	10 < h ≤ 15	15 < h ≤ 25	25 < h ≤ 40	40 < h ≤ 60	60 < h ≤ 70
Frequency	8	18	28	33	13

(a) Complete the histogram to show this information.

The first two blocks have been drawn for you.



(b) Calculate an estimate of the mean height.

..... cm [4]

[3]

3 Kai and Ann carry out a survey on the distances travelled, in kilometres, by 200 cars.

Kai completes this frequency table for the data collected.

Distance (dkm)	80 < <i>d</i> ≤ 100	100 < <i>d</i> ≤ 150	150 < <i>d</i> ≤ 200	200 < d ≤ 300	300 < <i>d</i> ≤ 400
Frequency	7	33	76	52	32

(a) (i)	Calcu	late an	estimate	of	the	mean
---------	-------	---------	----------	----	-----	------

.....km [4]

(ii) Ann uses this frequency table for the same data. There is a different interval for the final group.

Distance (dkm)	80 < <i>d</i> ≤ 100	$100 < d \le 150$	150 < <i>d</i> ≤ 200	200 < d ≤ 300	300 < <i>d</i> ≤ 360
Frequency	7	33	76	52	32

Without calculating an estimate of the mean for this data, find the difference between Ann's and Kai's estimate of the mean.

You must show all your working.

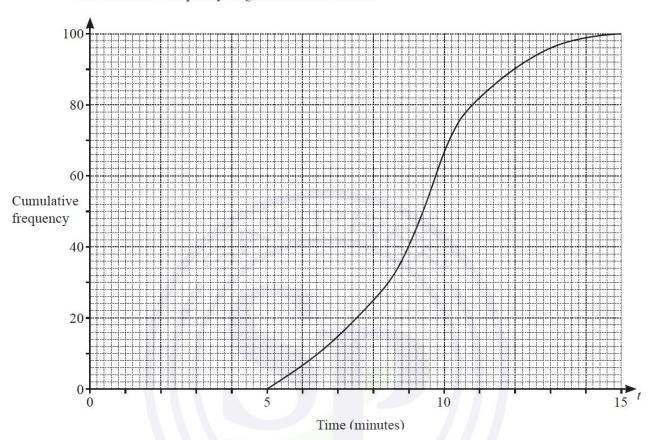
(iii) A histogram is drawn showing the information in **Kai's** frequency table. The height of the block for the interval $200 < d \le 300$ is 2.6 cm.

Calculate the height of the block for each of the following intervals.

Continue on the next page...

(b)	One car is picked at random.		
	Find the probability that the car has travelled more than 300 km	n.	
			[1]
(c)	Two of the 200 cars are picked at random.		
	Find the probability that		
	(i) both cars have travelled 150 km or less,		
			[2]
	(ii) one car has travelled more than 200 km and the other car l	nas travelled 100 km or less.	
			[3]
			[-]

5 (a) 100 students each record the time, t minutes, taken to eat a pizza. The cumulative frequency diagram shows the results.



Find an estimate of

(i) the median,

..... min [1]

(ii) the interquartile range,

..... min [2]

(iii) the number of students taking more than 11 minutes to eat a pizza.

.....[2]

Continue on the next page...

(b) 150 students each record how far they can throw a tennis ball. The table shows the results.

Distance (d metres)	0 < d ≤ 20	20 < d ≤ 30	30 < d ≤ 35	35 < d ≤ 45	45 < d ≤ 60
Frequency	4	38	40	53	15

(i) Calculate an estimate of the mean.

		m	[4]
--	--	---	-----

(ii) A histogram is drawn to show this information. The height of the bar representing $30 < d \le 35$ is $12 \, \text{cm}$.

Calculate the height of each of the other bars.

Distance (d metres)	Frequency	Height of bar (cm)
0 < d ≤ 20	4	
$20 < d \leq 30$	38	
$30 < d \le 35$	40	12
$35 < d \le 45$	53	
$45 < d \le 60$	15	

[3]

(iii) Two students are chosen at random.

Find the probability that they both threw the ball more than $45\,\mathrm{m}$.

.....[2]

(a) 100 students take part in a reaction test. The table shows the results.

Reaction time (seconds)	6	7	8	9	10	11
Number of students	3	32	19	29	11	6

1	(i)	Write	down	the	mode.
١	11	VVIIIC	UU WII	uic	mouc.

.....s [1]

(ii) Find the median.

.....s [1]

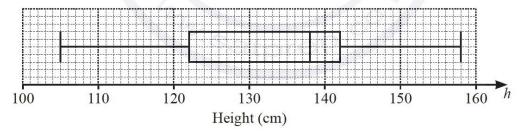
(iii) Calculate the mean.

(iv) Two students are chosen at random.

Find the probability that both their reaction times are greater than or equal to 9 seconds.

.....[2]

(b) The box-and-whisker plot shows the heights, h cm, of some students.



(i) Find the range.

 cm	[1]	

(ii) Find the interquartile range.



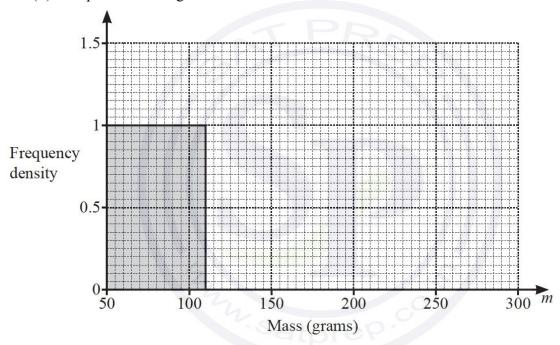
(c) The mass of each of 200 potatoes is measured. The table shows the results.

Mass (m grams)	50 < m ≤ 110	110 < m ≤ 200	$200 < m \le 300$
Frequency	60	99	41

(i) Calculate an estimate of the mean

..... g [4]

(ii) Complete the histogram to show the information in the table.

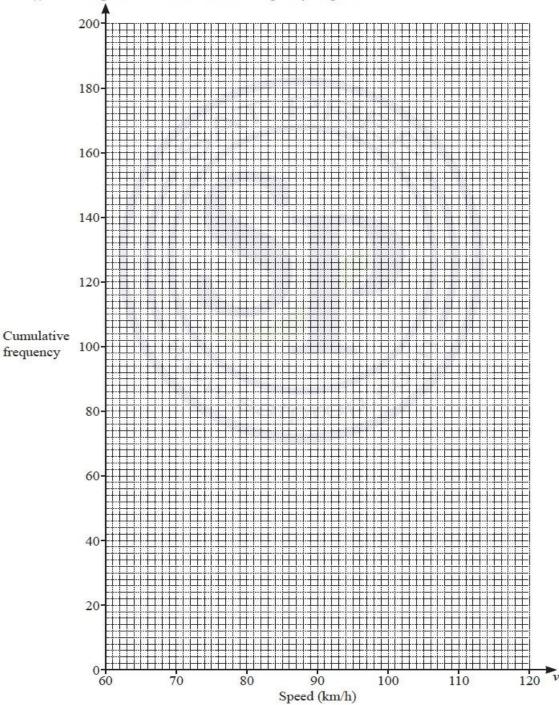


[2]

(a) The cumulative frequency table shows information about the speed of each of 200 cars as they pass a speed camera.

Speed (vkm/h)	v ≤ 70	v ≤ 80	v ≤ 90	v ≤ 95	v ≤ 100	v ≤ 120
Cumulative frequency	12	46	115	155	177	200

(i) On the grid, draw the cumulative frequency diagram.



[3]

	our cumulative frequ	ency diagram to im	direction of	
(a) ti	he median			
(b) ti	he interquartile range	e		km/
				km/
(c) ti	he number of cars wi	th a speed greater th	nan 110km/h.	
The freque	ncy table shows info	rmation about the n	nass of each of 50 tm	ucks.
Mass (mkg)	$2000 < m \leqslant 2600$	$2600 < m \le 3500$	$3500 < m \leqslant 5000$	$5000 < m \le 5700$
Frequency	12	15	16	7
(i) Caleu	late an estimate for the	he mean mass of the	e trucks.	
	late an estimate for the			kock is 6 cm.
(ii) In a h		is information, the h	neight of the first blo	
(ii) In a h	istogram showing thi	is information, the h	neight of the first blo	
(ii) In a h	istogram showing thi	is information, the h	neight of the first blo	
(ii) In a h	istogram showing thi	is information, the h	neight of the first blo	
(ii) In a h	istogram showing thi	is information, the h	neight of the first blo	

Ques	stion	63								
(a)	Anr	na records	s the num	ber of te	xt messa	ges she re	eceives f	or 14 day	S.	
			17	15	31	38	31	22	13	
			18	21	27	28	21	31	29	
	(i)	Comple	te the ster	m-and-le	af diagra	m.				
		1						- 8		
		2								
		3								
		Kev:								
										[3]
	(ii)	Find the	e median.							
										 [1]
((iii)	Find the	e mode.							
										 [1]
	(iv)	Find the	e range.							
										 [1]
(b)	In a Ann	shop, the	ere are 4 i te each pi	red and 8 ick one o	grey pho f these p	ones.	random.			

Work out the probability that they both pick a grey phone.

[2]

The table shows information about the heights of 80 children.

Height (h metres)	$1.2 < h \le 1.4$	$1.4 < h \le 1.5$	$1.5 < h \le 1.65$	$1.65 < h \le 1.8$	1.8 < h ≤ 1.9
Frequency	2	13	24	32	9

									100.4	
1	a) (i) '	Write	down	the	interval	containing	the	median

$$.... < h \le$$
 [1]

(ii) Calculate an estimate of the mean height.

(b) (i) One of these children is chosen at random.

Calculate the probability that they have a height of 1.4m or less.

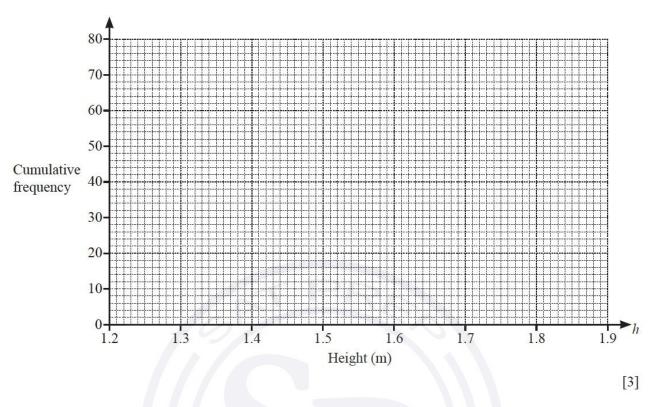
(ii) Two of these children are chosen at random. Calculate the probability that both children are taller than 1.5 m but only one of them is taller than 1.8 m.

(c) (i) Complete the cumulative frequency table for the heights.

Height (h metres)	<i>h</i> ≤ 1.4	<i>h</i> ≤ 1.5	<i>h</i> ≤ 1.65	<i>h</i> ≤ 1.8	<i>h</i> ≤ 1.9
Cumulative frequency	2	r.sat	preP.		

[2]

(ii) On the grid, draw the cumulative frequency diagram.



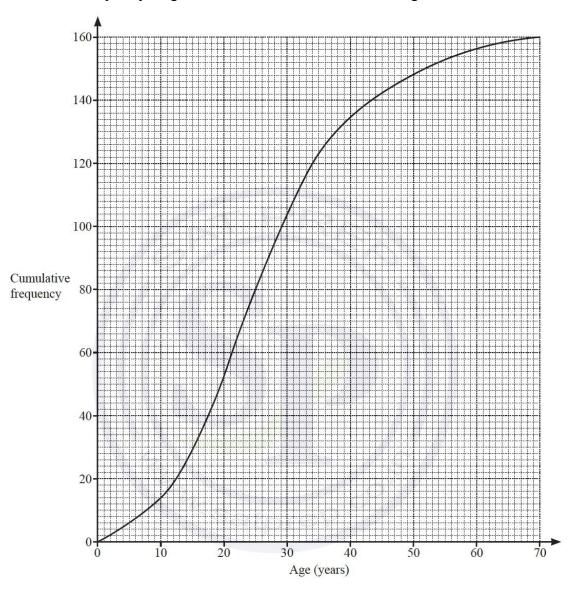
- (d) Use your diagram to find an estimate of
 - (i) the interquartile range
 - (ii) the 60th percentile.

																																						ľ	r	1		2	2	
--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	--	---	---	---	--	---	---	--

..... m [2]

(a) There are 160 people in a village.

The cumulative frequency diagram shows information about their ages.



- (i) Find an estimate for
- (a) the median age
- (b) the lower quartile
- (c) the number of people who are 50 or more years of age
- (d) the 65th percentile.

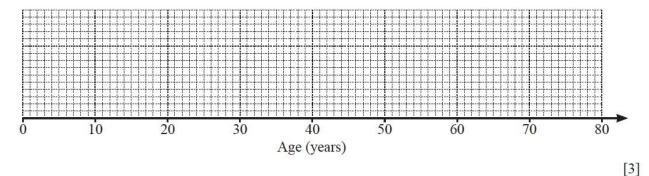
	 						•			•		 •	•		•	•		 •	•	•				•		•	•]	

 	 [1]

[2

	 [2

- (ii) The youngest person in the village is 1 year old and the oldest is 70 years old.
 - (a) Draw a box-and-whisker plot to show the distribution of ages in the village.

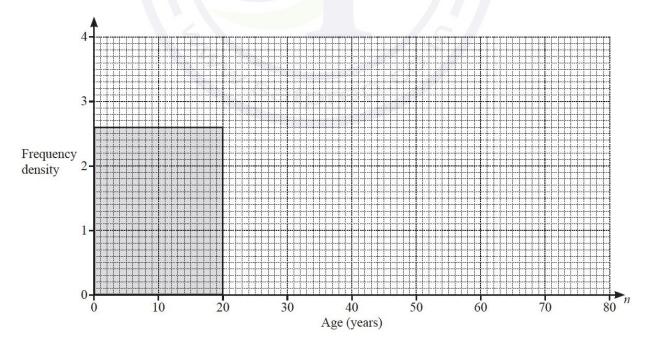


(b) Write down an estimate of the percentage of people in the village that are younger than the median age.

(b) The frequency table shows information about the age of each person in another village.

Age (n years)	$0 < n \leqslant 20$	20 < n ≤ 30	$30 < n \le 50$	50 < n ≤ 80
Frequency	52	37	24	60

On the grid, complete the histogram to show this information. The first block has been drawn for you.



[3]

(a) The table shows information about the mass of each of 1000 eggs.

Mass (m grams)	40 < m ≤ 50	50 < m ≤ 56	56 < m ≤ 64	64 < m ≤ 70
Frequency	126	520	154	200

(2)	C-11	-4	4:4-	- 5	41	
(1)	Calcul	ate an	estimate	01	tne	mean.

······ 5 [[¬] .

(ii) An egg is picked at random from the 1000 eggs.

Find the probability that this egg has a mass greater than $56\,\mathrm{g}$. Give your answer as a fraction in its simplest form.

