Subject - Math AI(Higher Level) Topic - Function Year - May 2021 - Nov 2022 Paper -2 Answers

Question 1

(a)
$$y = \frac{5}{8}x + \frac{7}{2}$$
 $(y = 0.625x + 3.5)$

Note: Award A1 for 0.625x, A1 for 3.5.

Award a maximum of A0A1 if not part of an equation.

[2 marks]

(b) (i)
$$y = -0.975x^2 + 9.56x - 16.7$$
 (M1)A1
 $(y = -0.974630x^2 + 9.55919x - 16.6569...)$

(ii) gradient of curve is positive at x = 4

Note: Accept a sensible rationale that refers to the gradient.

[3 marks]

R1

$$let y = ax^2 + bx + c$$

differentiating or using
$$x = \frac{-b}{2a}$$
 (M1)

$$8a + b = 0$$

substituting in the coordinates

$$7.5^{2}a + 7.5b + c = 0$$
 (A1)
 $4^{2}a + 4b + c = 6$ (A1)

solve to get

$$y = -\frac{24}{49}x^2 + \frac{192}{49}x - \frac{90}{49}$$
 OR $y = -0.490x^2 + 3.92x - 1.84$

Note: Use of quadratic regression with points using the symmetry of the graph is a valid method.

METHOD 2

$$y = a(x-4)^2 + 6 (M1)$$

$$0 = a(7.5 - 4)^2 + 6 (M1)$$

$$a = -\frac{24}{49}$$
 (A1)

$$y = -\frac{24}{49}(x-4)^2 + 6$$
 OR $y = -0.490(x-4)^2 + 6$ A1

[4 marks]

(d) (i)
$$\pi \int_0^4 \left(\frac{5}{8}x + 3.5\right)^2 dx + \pi \int_4^{7.5} \left(-\frac{24}{49}(x - 4)^2 + 6\right)^2 dx$$
 (M1)(M1)(M1)A1

Note: Award (M1)(M1)(M1)A0 if π is omitted but response is otherwise correct. Award (M1) for an integral that indicates volume, (M1) for their part (a) within their volume integral, (M1) for their part (b)(i) within their volume integral, A1 for their correct two integrals with all correct limits.

(ii) 501 cm³ (501.189...)

A1

[5 marks]

Total [14 marks]



